



Photo: R. Ketler, UBC

10 Soil thermal properties

Learning objectives

- Provide examples of why processes in the ground are of interest to climatologists.
- Know what are the key properties that describe the thermal behaviour of the soil / substrate in the climate system.
- Explain how the key properties relate to the process of heat conduction in soils.



Why might climatologists be interested in studying soil thermal properties and subsurface processes?





Permafrost thawing on Ellesmere Island / Photo: A. Cassidy, UBC Geography

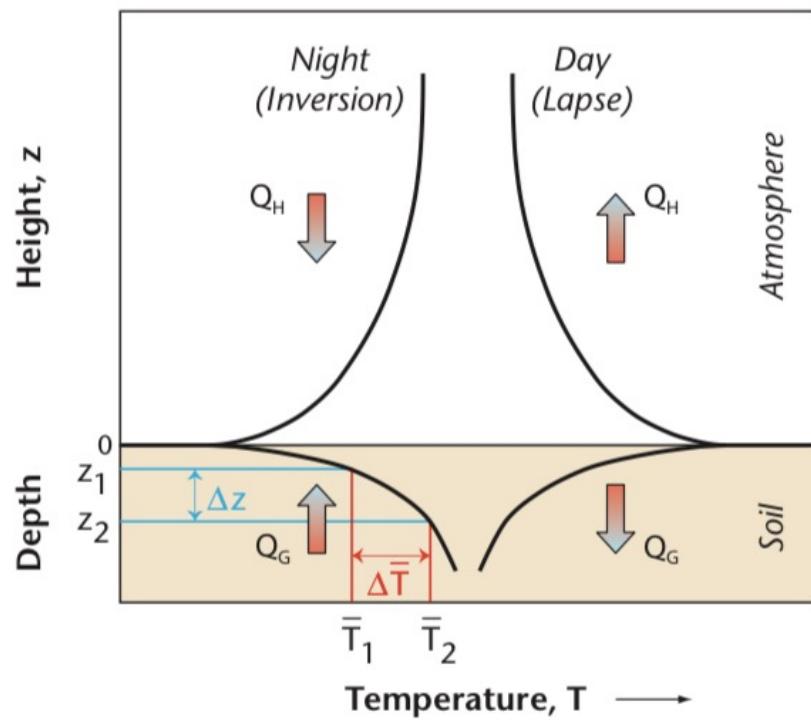


Graduate student in Geography / Photo: T. Lenkovich



Tonzi Ranch, California. Photo: J. Verfaillie

The role of the soil in the climate system



The influence of the **active surface** extends down into a relatively shallow layer of the substrate.

Nevertheless the properties of the shallow substrate layer make it a **significant volume of storage ΔQs** of sensible heat and water over diurnal and annual scales.

Soils act as ‘batteries’ of energy forms and mass relevant in the atmosphere.

Heat capacity and specific heat

Heat capacity C is the quantity of heat required to raise the temperature of a **unit volume** of a material through 1 K.



$$\text{J K}^{-1} \text{ m}^{-3}$$

Specific heat c is the quantity of heat required to raise the temperature of a **unit mass** of a material through 1 K.



$$\text{J K}^{-1} \text{ kg}^{-1}$$

Heat capacity and specific heat of soil materials

Material	Heat capacity C (MJ m ⁻³ K ⁻¹)	Specific heat c (kJ kg ⁻¹ K ⁻¹)	Density ρ (Mg m ⁻³)
Air	0.0012	1.01	0.0012
Water (liquid)	4.18	4.18	1
Ice	1.9	2.1	0.9
Soil mineral	2.1	0.8	2.65
Soil organic matter	2.5	1.9	1.3
Rock	2	0.8	2.7

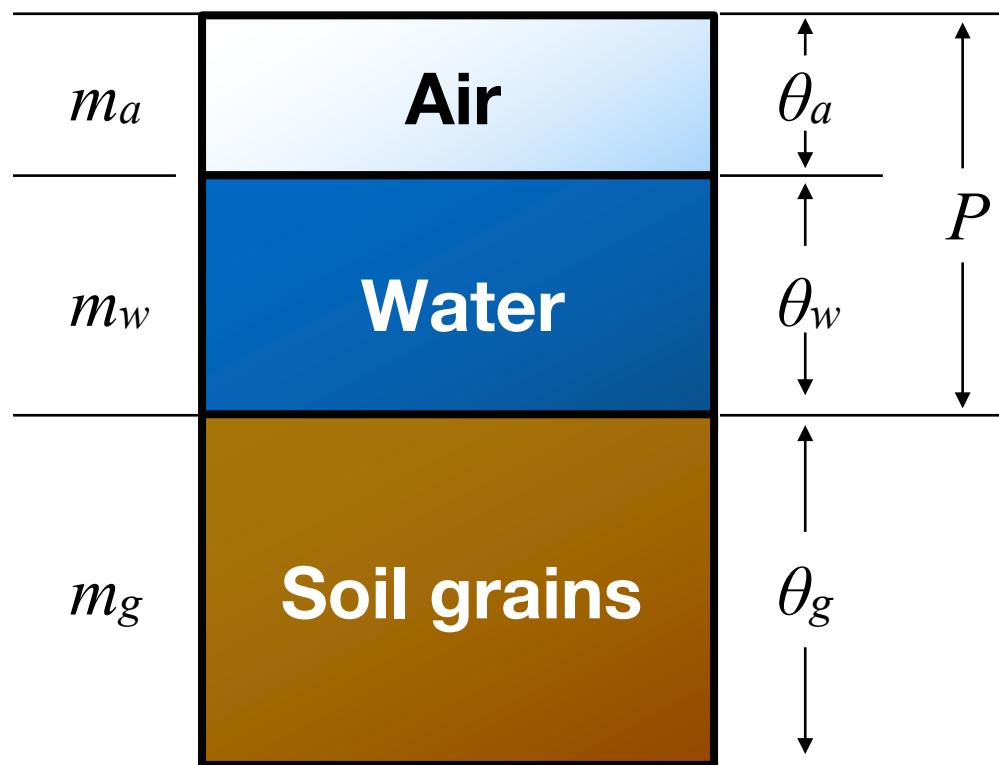
Porosity, volume fractions and mass

Mass

Expressed in mass
(kg) of a sample

$$m_a + m_w + m_g = m_s$$

m_s = total mass of soil



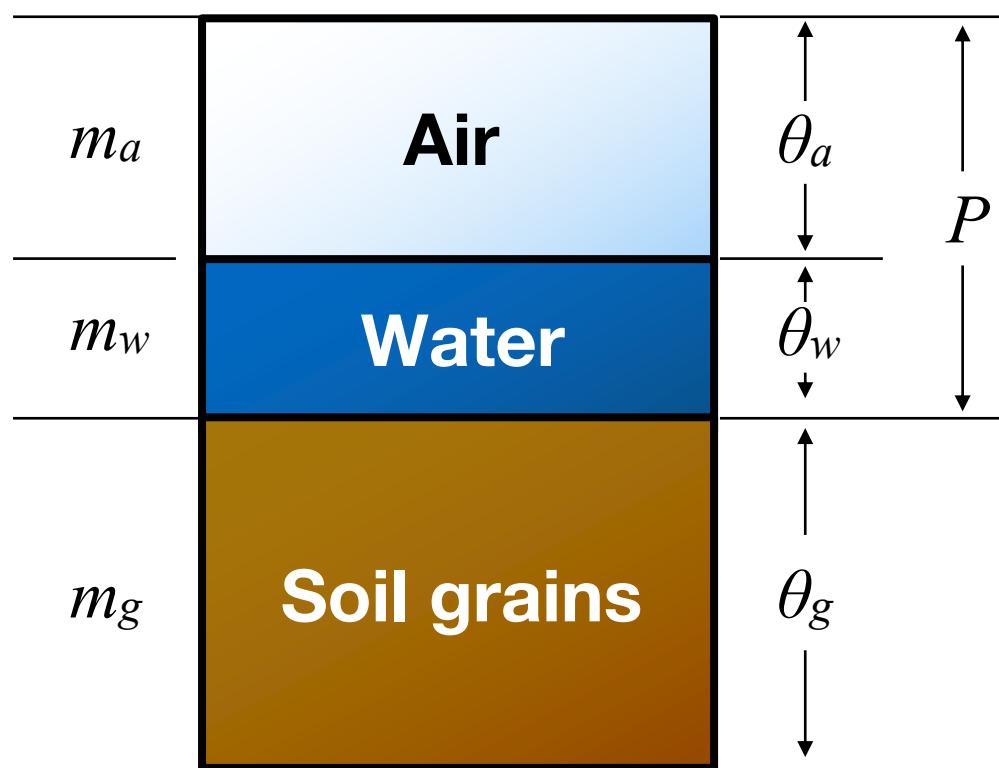
Volume

Expressed as
volume fractions
($\text{m}^3 \text{ m}^{-3}$)

$$\theta_a + \theta_w + \theta_g = 1 - \theta_g$$

$$\theta_a + \theta_w + \theta_g = 1$$

Porosity, volume fractions and mass



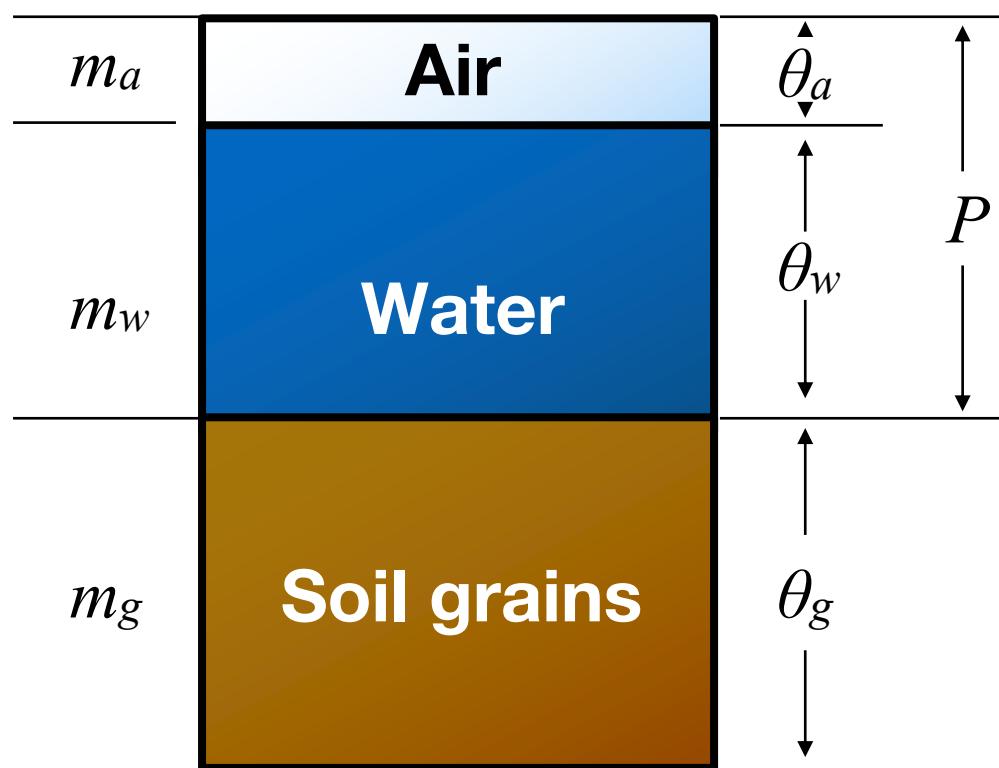
Volume

Expressed as
volume fractions
($\text{m}^3 \text{ m}^{-3}$)

$$= \theta_a + \theta_w = 1 - \theta_g$$

$$\theta_a + \theta_w + \theta_g = 1$$

Porosity, volume fractions and mass



Volume

Expressed as
volume fractions
($\text{m}^3 \text{ m}^{-3}$)

$$P = \theta_a + \theta_w = 1 - \theta_g$$

$$\theta_a + \theta_w + \theta_g = 1$$

Heat capacity of compound substances

The **heat capacity of a mixture** of substances such as soil can be calculated if the heat capacity and volume fraction of each component are known. In the case of soil, C_s is calculated using:

$$C_s = C_m \theta_m + C_o \theta_o + C_w \theta_w + C_a \theta_a \quad *$$

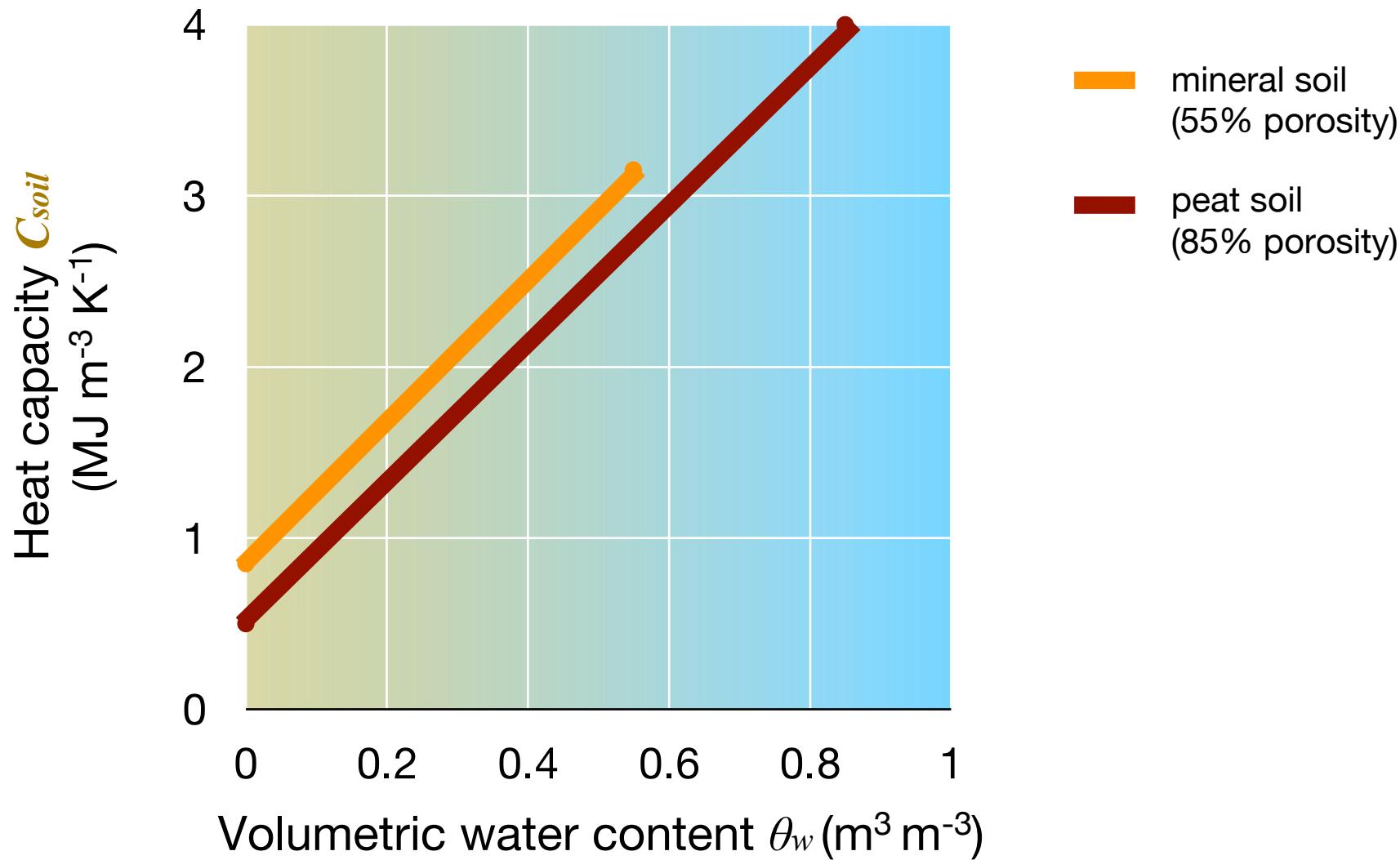
where θ is the volume fraction occupied by mineral (m), organic matter (o), water (w) and air (a).

C_a is very small relative to the other values of C , so it can be neglected.

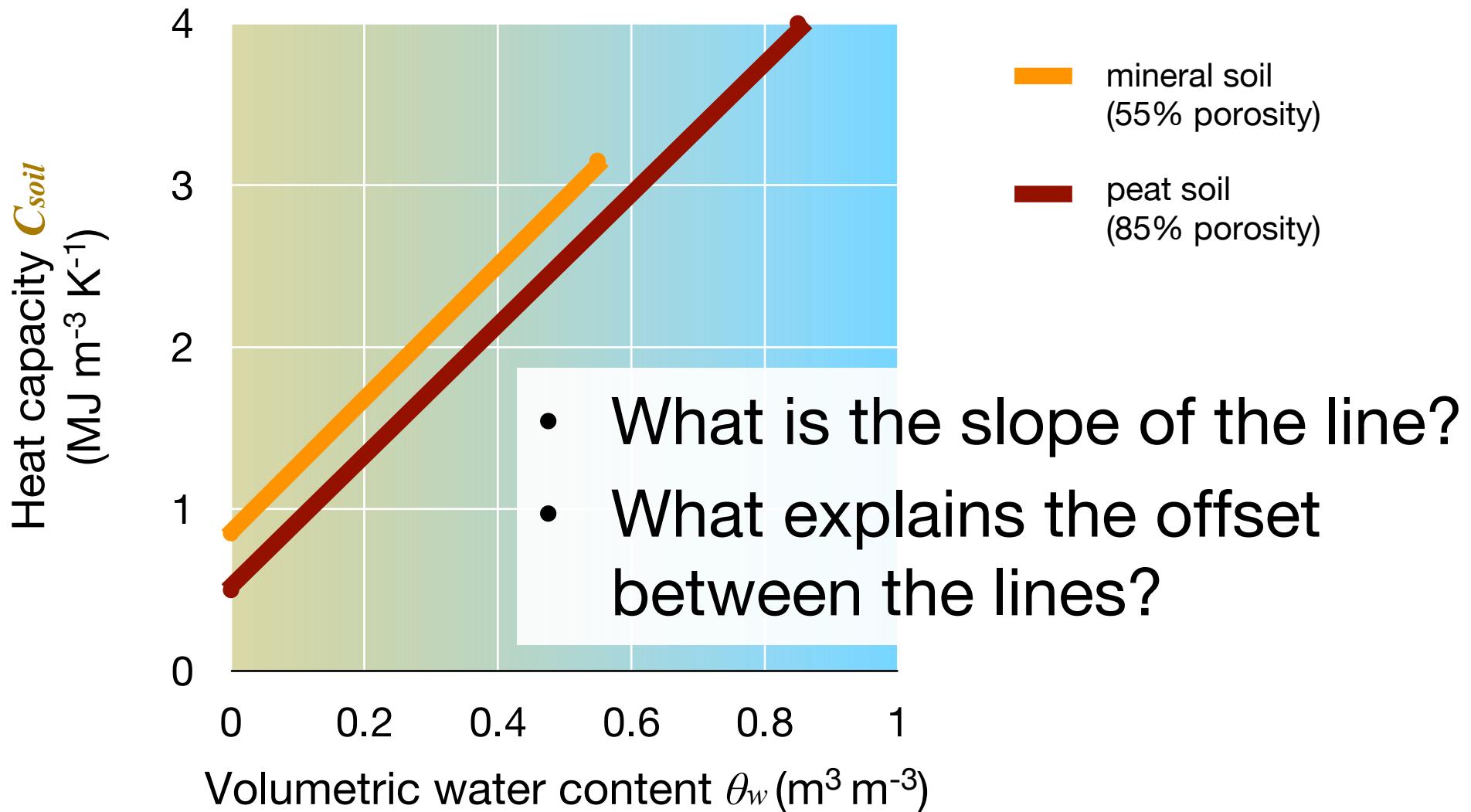


Photo: R. Ketler

Heat capacity and soil water content



Heat capacity and soil water content (Slido)



Warming / cooling of a soil

Relating the **change of soil heat flux with depth** (the divergence of Q_G , i.e. $\partial Q_G / \partial z$) to the **rate of temperature change** ($\partial T / \partial t$) due to the **heat capacity** of the layer:

$$\frac{\partial Q_G}{\partial z} = C_s \frac{\partial T}{\partial t} \quad (\text{Eq 1})$$

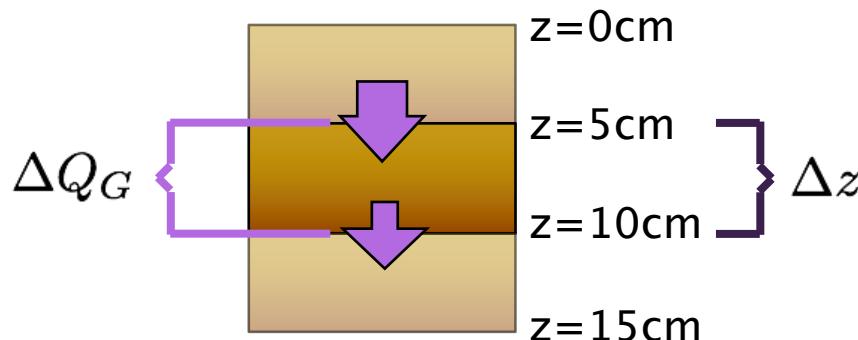
Heat capacity
in $\text{J m}^{-3} \text{K}^{-1}$

Heat flux divergence
with depth
in $\text{W m}^{-2} \text{m}^{-1} = \text{W m}^{-3}$

Temperature change
with time
in K s^{-1}

Warming / cooling of a soil

Re-arranging and writing in finite form gives the **rate of temperature change** in an actual layer of thickness Δz as:



$$\frac{\Delta T}{\Delta t} = \frac{1}{C_s} \frac{\Delta Q_G}{\Delta z}$$

Change of heat flux
(i.e. input - output)
in $\text{W m}^{-2} \text{m}^{-1}$

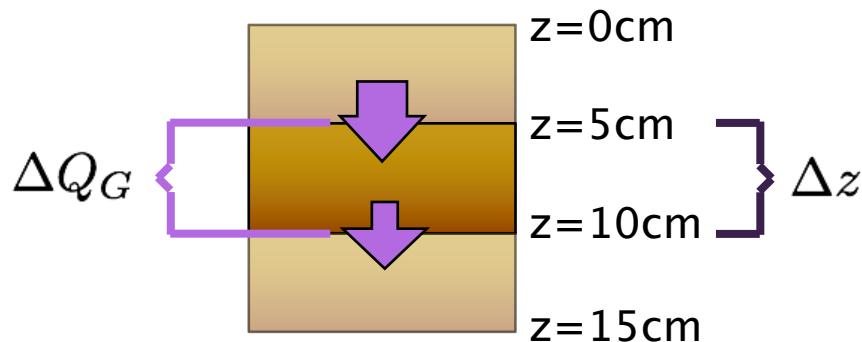
Change of
temperature over
time in layer (i.e.
warming or cooling
rate) in K s^{-1}

★

If the soil has a high heat capacity, the rate of warming or cooling will be (Slido):

A) Higher

B) Lower



$$\frac{\Delta T}{\Delta t} = \frac{1}{C_s} \frac{\Delta Q_G}{\Delta z}$$

Change of heat flux
(i.e. input - output)
in $\text{W m}^{-2} \text{m}^{-1}$

Change of
temperature over
time in layer (i.e.
warming or cooling
rate) in K s^{-1}

★

Fourier's law

Fourier's law describes that the **flux density of heat conducted** Q_G is proportional to the **temperature gradient**:

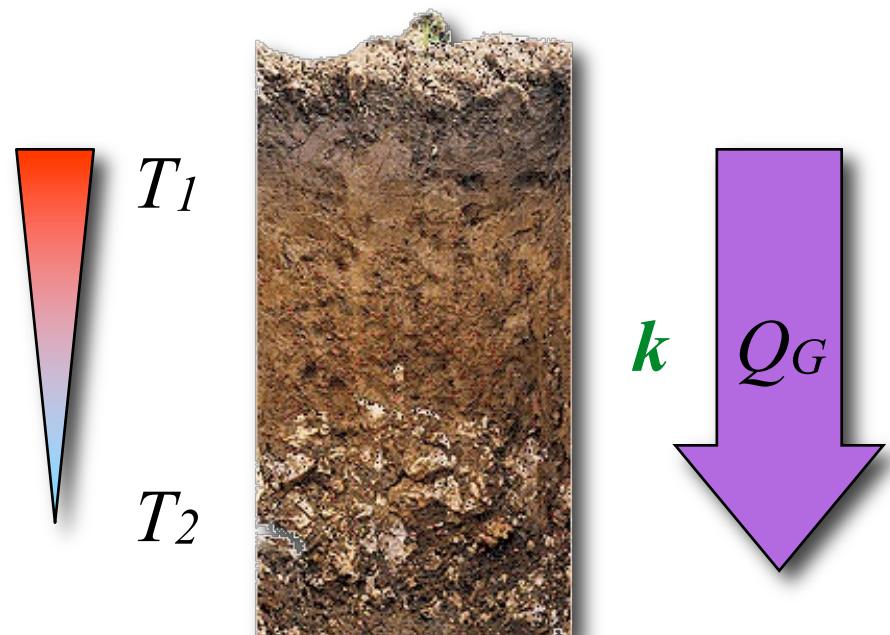
Soil heat flux
at a given
depth
in W m^{-2}

Temperature
gradient with depth
in K m^{-1}

$$Q_G = -k \frac{\partial T}{\partial z}$$

★ (Eq 2)

Constant of
proportionality k is the
thermal conductivity (a
property of the material)
in $\text{W m}^{-1} \text{K}^{-1}$



Thermal conductivity k of various materials

Material	k ($\text{W m}^{-1} \text{K}^{-1}$)
Air	0.025
Water (liquid)	0.59
Ice	2.1
Quartz	8.8
Clay minerals	2.9
Organic matter	0.25
Stainless steel	21
Copper	380

Mineral matter is a good conductor

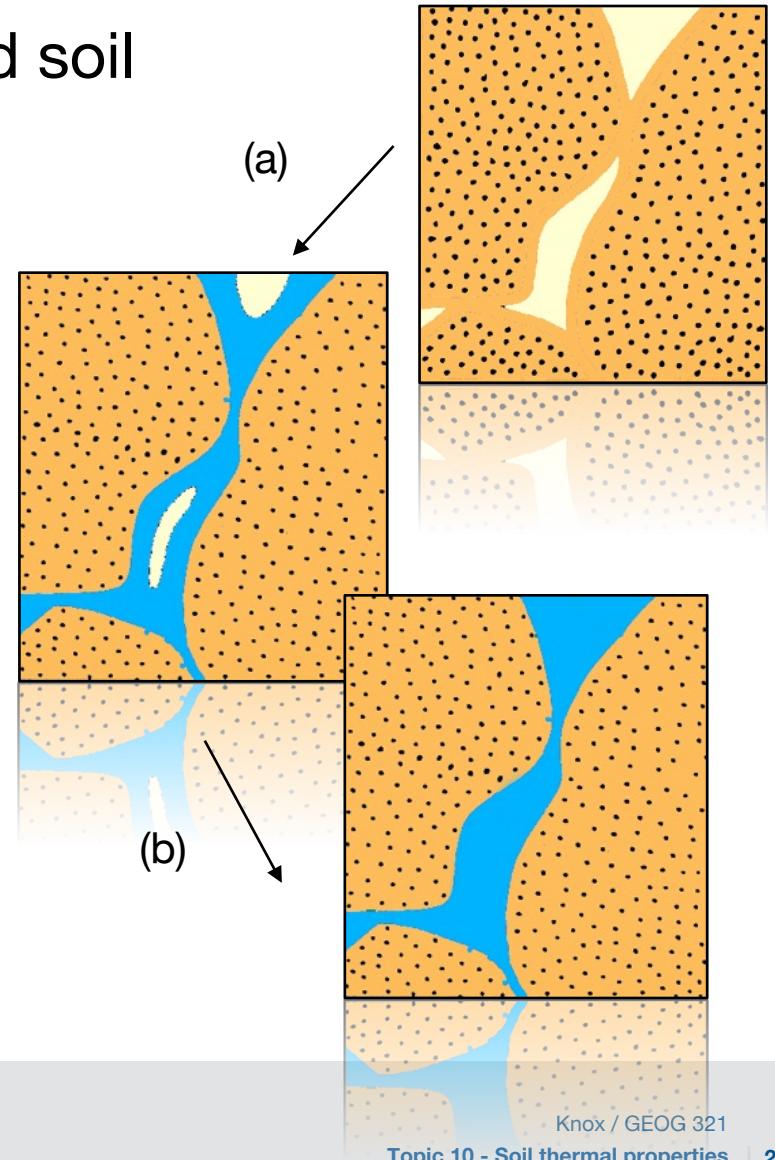
Water is intermediate

Air is very poor

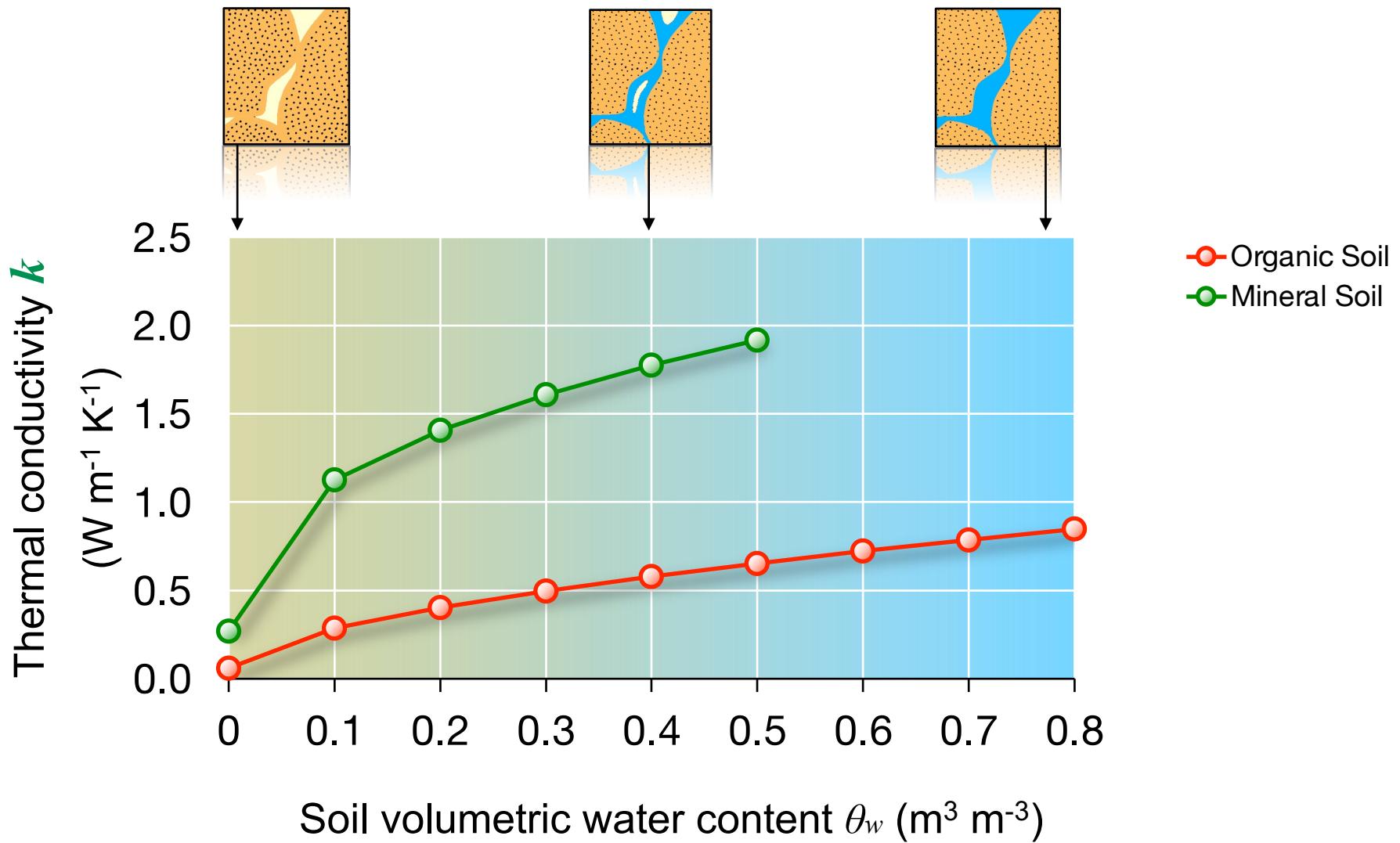
Thermal conductivity k and water content

A non-linear relation exists between k and soil water content (θ_w)

- Adding water to dry soil (a) initially causes k to increase rapidly – rapid increase in area of contacts between soil particles resulting from water film.
- As more water (b) is added, k increases less rapidly – area of contacts increases more slowly per unit of water added (i.e. diminishing returns).

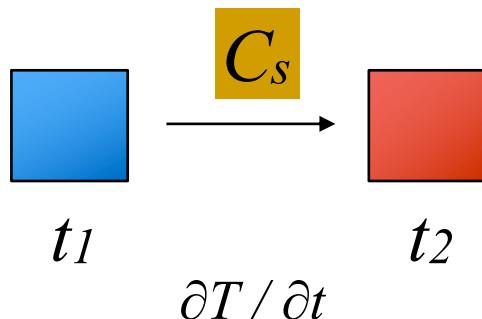


Soil water content and thermal conductivity k

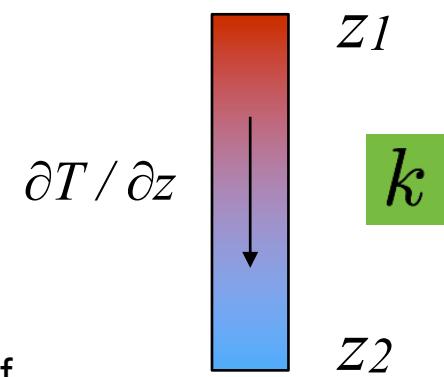


Combining thermal properties

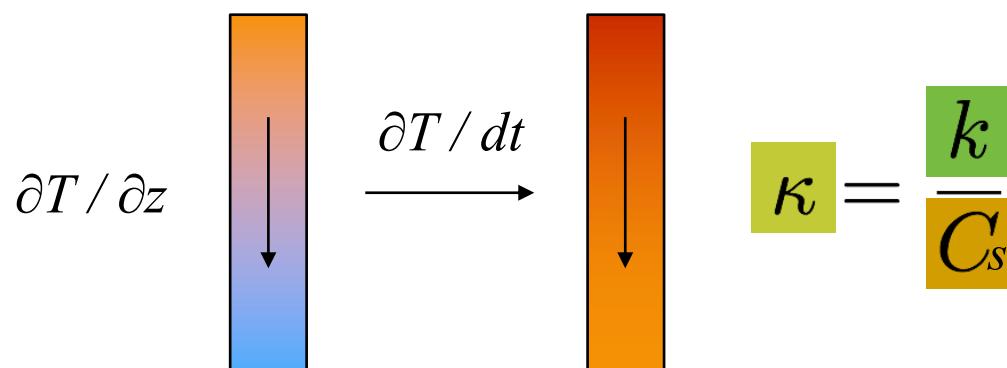
How rapidly does a volume warm when a certain amount of energy is supplied?



How well does heat conduct from one depth to another for a given temperature gradient?



How rapidly does a soil warm at depth if energy is available at the surface?



Thermal diffusivity

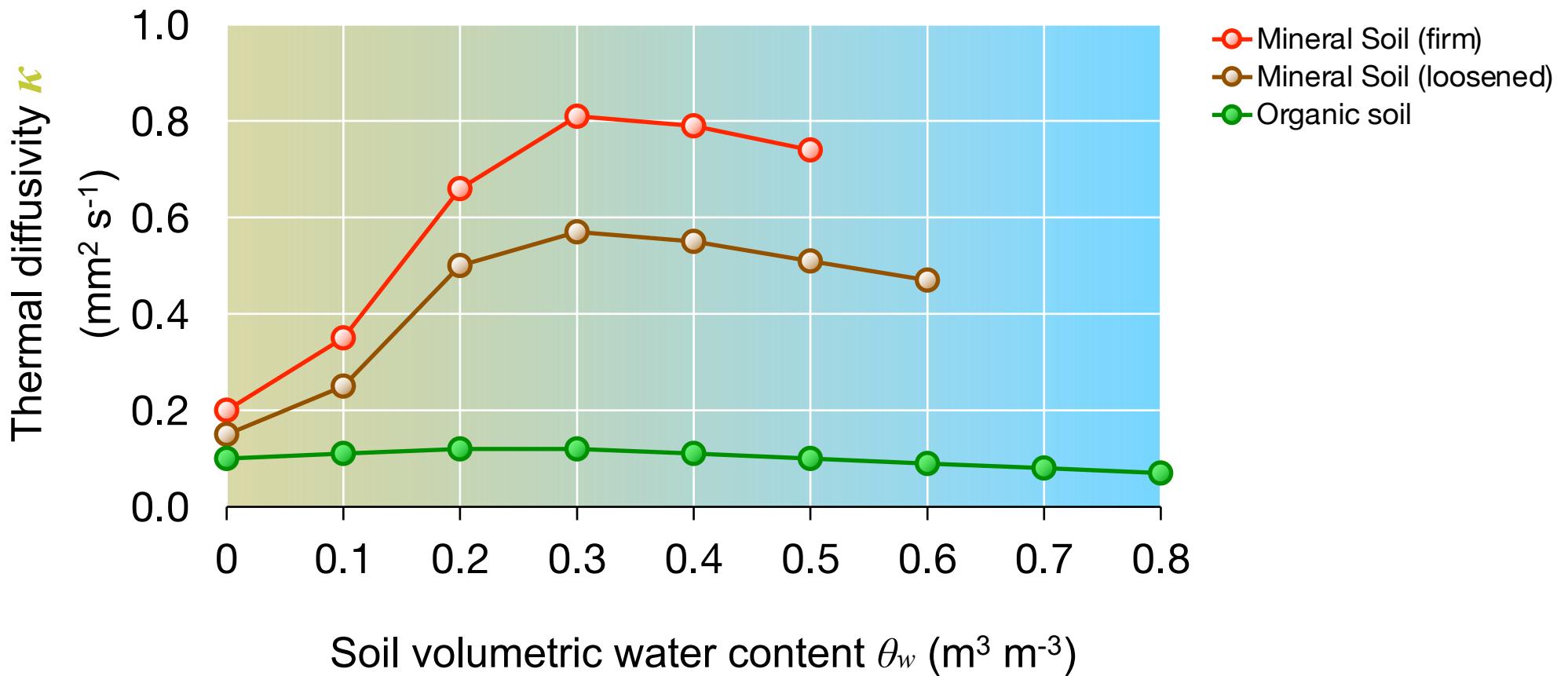
Thermal diffusivity κ (greek ‘kappa’ - not ‘K’) – indicates how quickly soil at depth will warm or cool in response to heating or cooling at the surface. It tells us how fast a temperature wave will diffuse or travel downward into a soil.

It is defined:

$$\kappa = \frac{k}{\bar{C}} \quad *$$

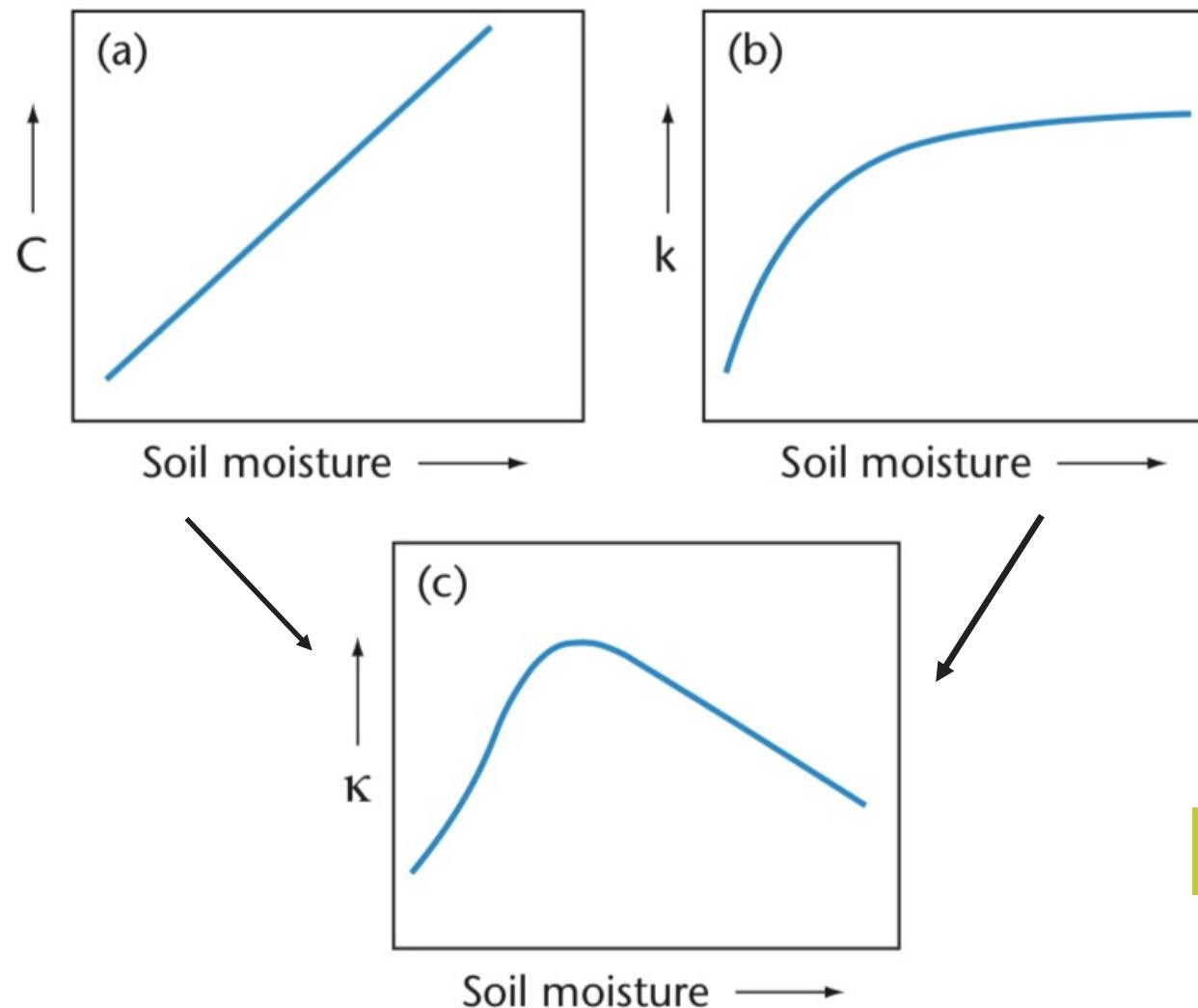
Units: $\text{m}^2 \text{ s}^{-1}$

Soil water content and thermal diffusivity



Why the curious shape?

Why the curious shape?



$$\kappa = \frac{k}{C} \quad *$$

Take home points

- Soils are important for **storage of heat and water** in the climate system.
- Two basic thermal properties regulate the exchange - **Heat capacity C_s** and **thermal conductivity k** . From those we can derive **thermal diffusivity $\kappa = k / C_s$** .
- The **water content** of the soil is significantly altering both **C** (linearly) and **k** (non-linearly).