



Photo: R. Ketler, UBC

10 Soil thermal properties

Learning objectives

- Provide examples of why processes in the ground are of interest to climatologists.
- Know what are the key properties that describe the thermal behaviour of the soil / substrate in the climate system.
- Explain how the key properties relate to the process of heat conduction in soils.



Photo: J. Verfaillie

Why might climatologists be interested in studying soil thermal properties and subsurface processes?





Permafrost thawing on Ellesmere Island / Photo: A. Cassidy, UBC Geography

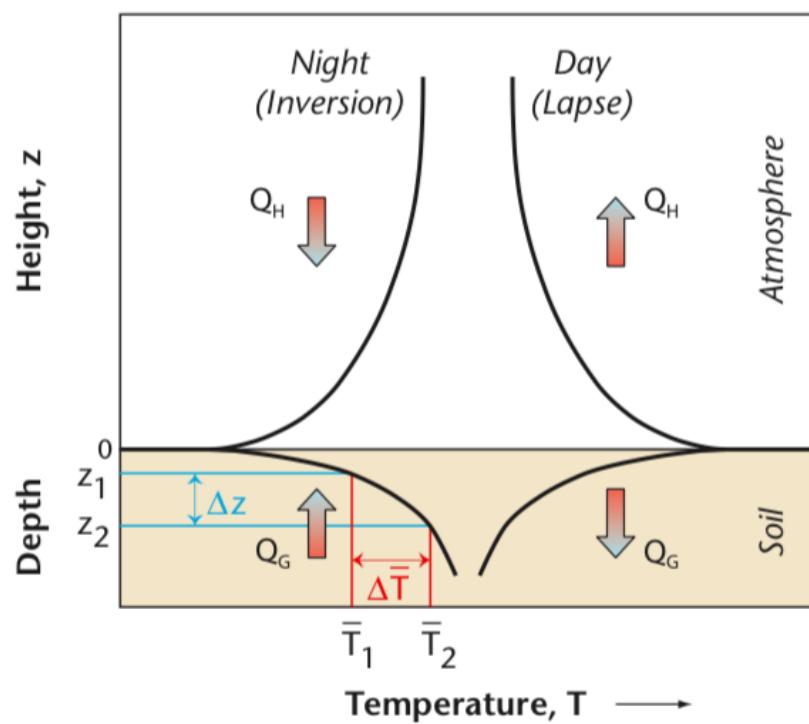


Graduate student in Geography / Photo: T. Lenkovich



Tonzi Ranch, California. Photo: J. Verfaillie

The role of the soil in the climate system



The influence of the **active surface** extends down into a relatively shallow layer of the substrate.

Nevertheless the properties of the shallow substrate layer make it a **significant volume of storage ΔQ_s** of sensible heat and water over diurnal and annual scales.

Soils act as ‘batteries’ of energy forms and mass relevant in the atmosphere.

Heat capacity and specific heat

Heat capacity **C** is the quantity of heat required to raise the temperature of a **unit volume** of a material through 1 K.



$$\text{J K}^{-1} \text{ m}^{-3}$$

Specific heat **c** is the quantity of heat required to raise the temperature of a **unit mass** of a material through 1 K.



$$\text{J K}^{-1} \text{ kg}^{-1}$$

Heat capacity and specific heat of soil materials

Material	Heat capacity C (MJ m ⁻³ K ⁻¹)	Specific heat c (kJ kg ⁻¹ K ⁻¹)	Density ρ (Mg m ⁻³)
Air	0.0012	1.01	0.0012
Water (liquid)	4.18	4.18	1
Ice	1.9	2.1	0.9
Soil mineral	2.1	0.8	2.65
Soil organic matter	2.5	1.9	1.3
Rock	2	0.8	2.7

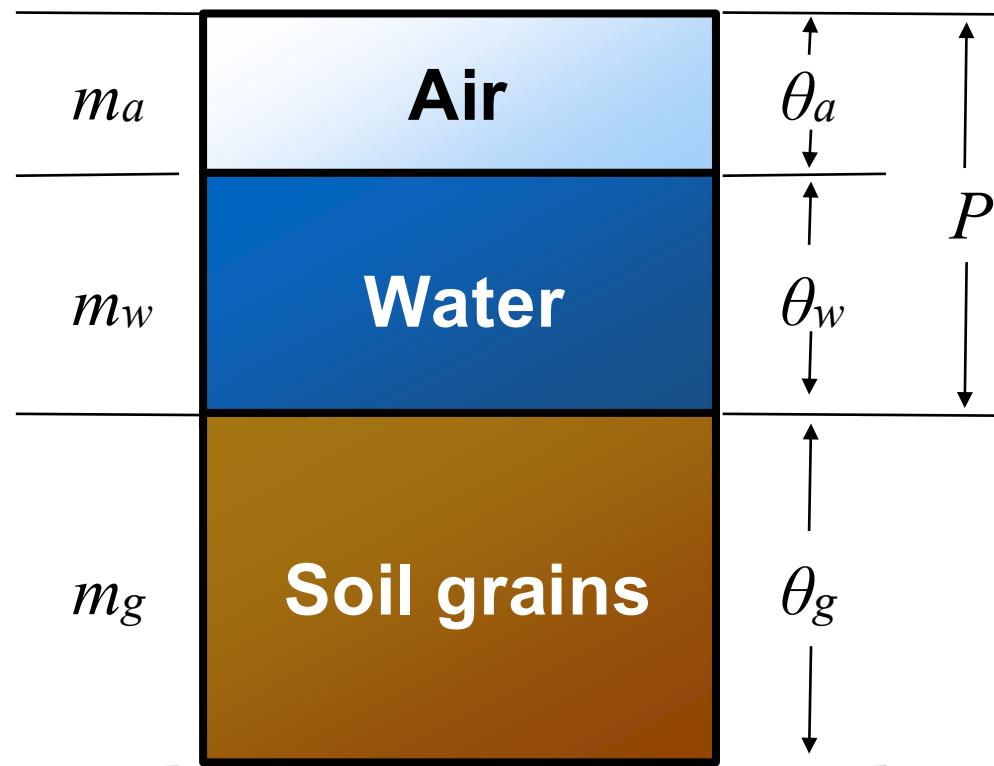
Porosity, volume fractions and mass

Mass

Expressed in mass
(kg) of a sample

$$m_a + m_w + m_g = m_s$$

m_s = total mass of soil



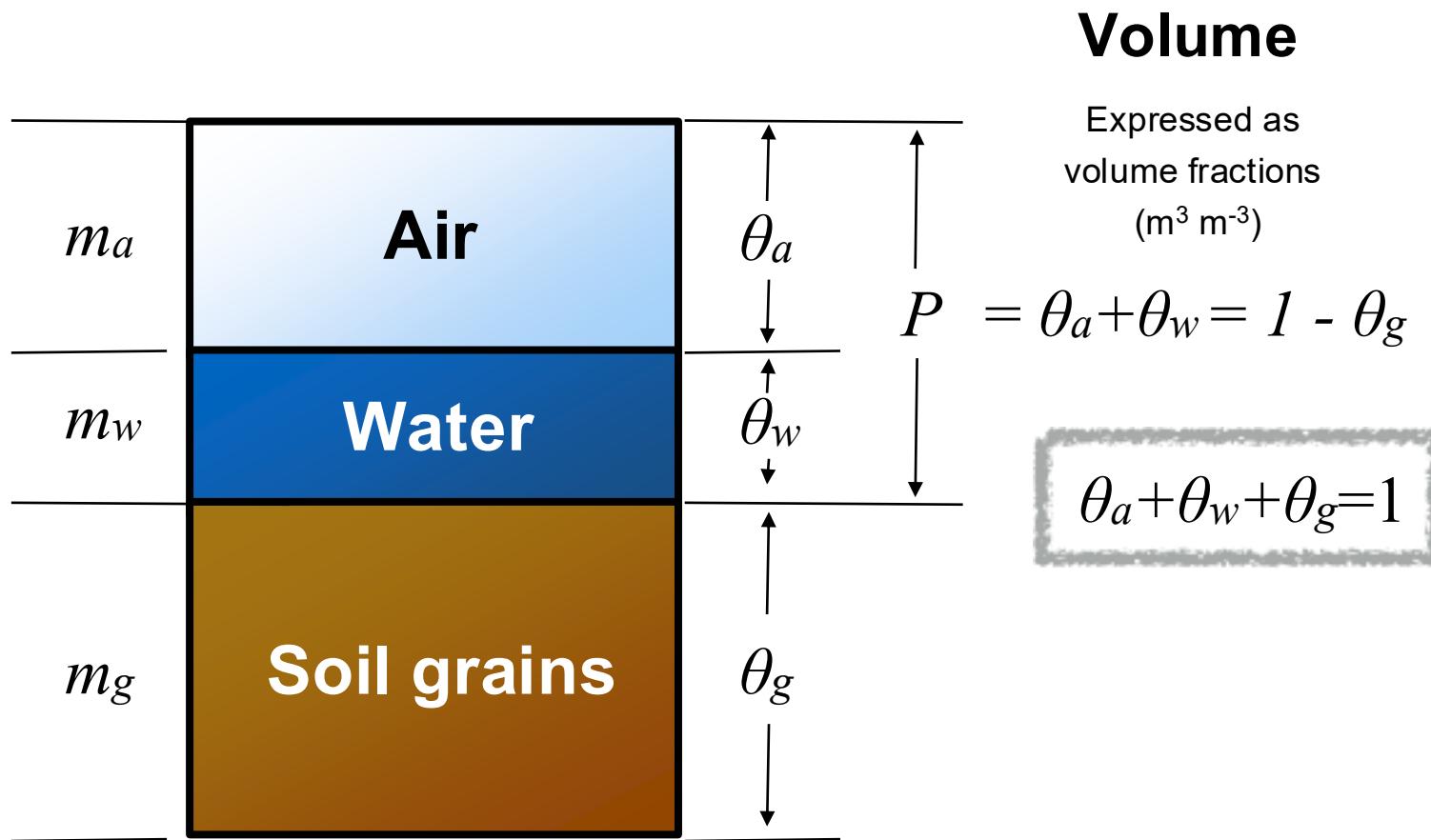
Volume

Expressed as
volume fractions
($\text{m}^3 \text{ m}^{-3}$)

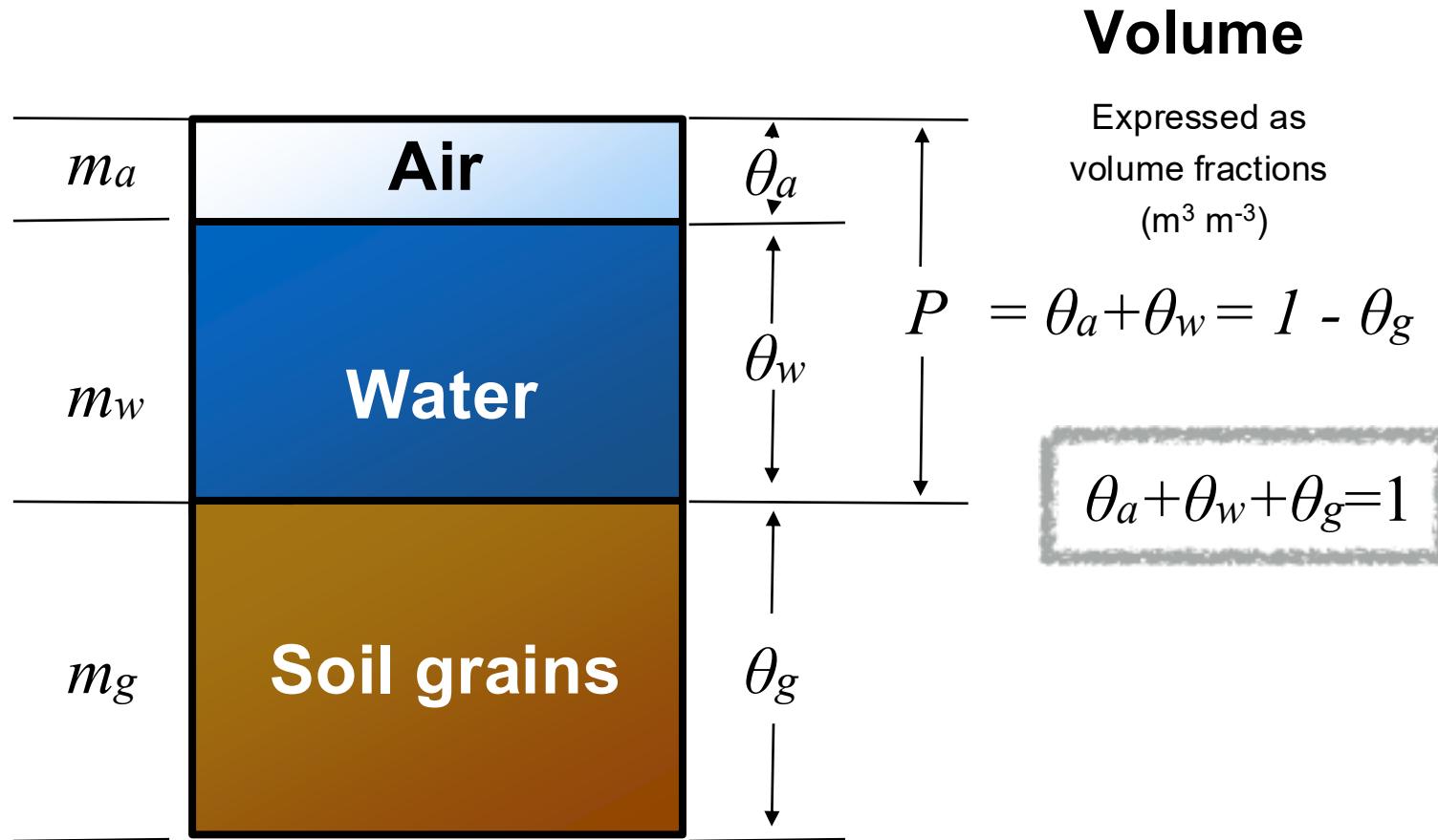
$$\theta_a + \theta_w = 1 - \theta_g$$

$$\theta_a + \theta_w + \theta_g = 1$$

Porosity, volume fractions and mass



Porosity, volume fractions and mass



Heat capacity of compound substances

The **heat capacity of a mixture** of substances such as soil can be calculated if the heat capacity and volume fraction of each component are known. In the case of soil, C_s is calculated using:

$$C_s = C_m \theta_m + C_o \theta_o + C_w \theta_w + C_a \theta_a \quad *$$

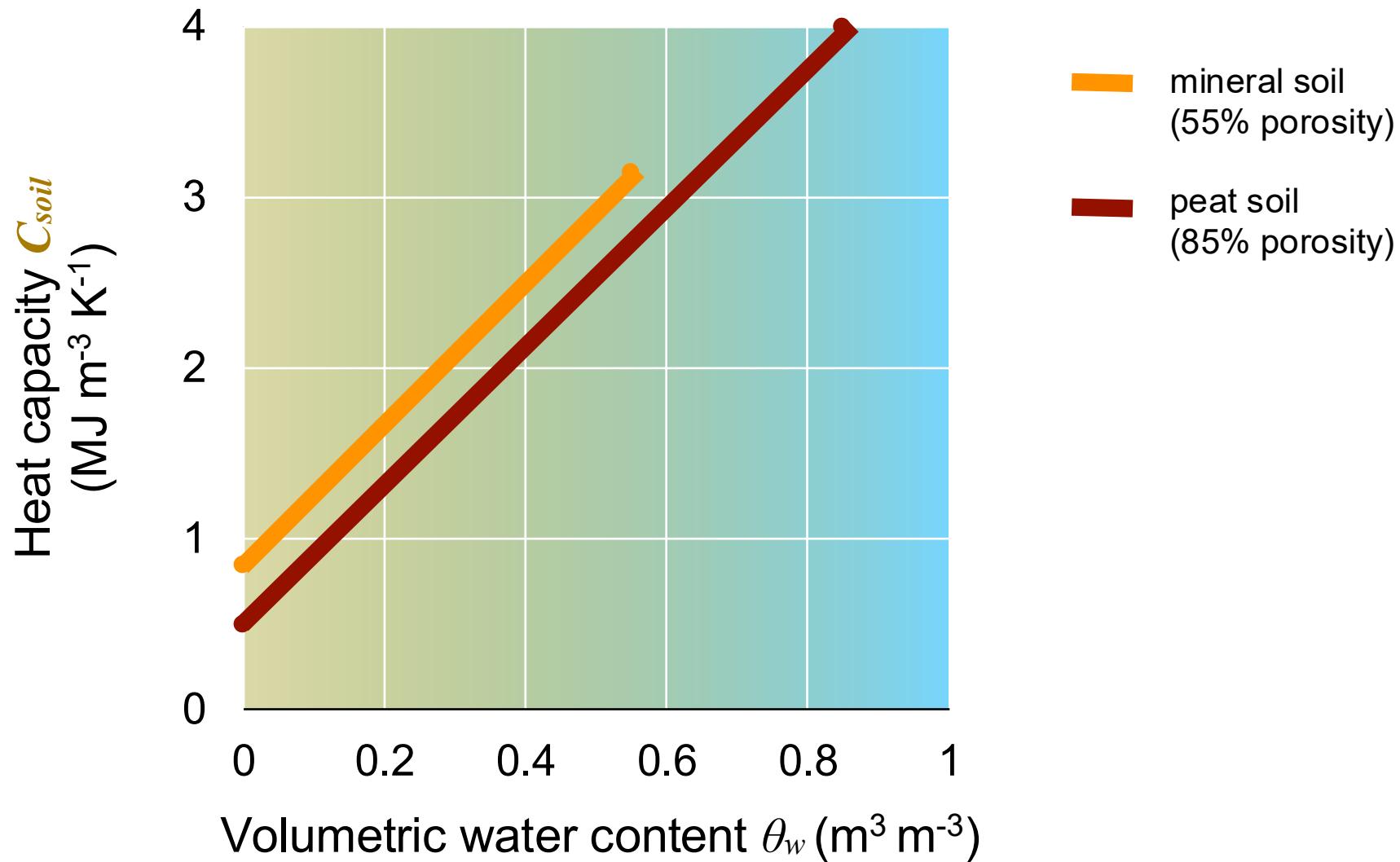
where θ is the volume fraction occupied by mineral (m), organic matter (o), water (w) and air (a).

C_a is very small relative to the other values of C , so it can be neglected.

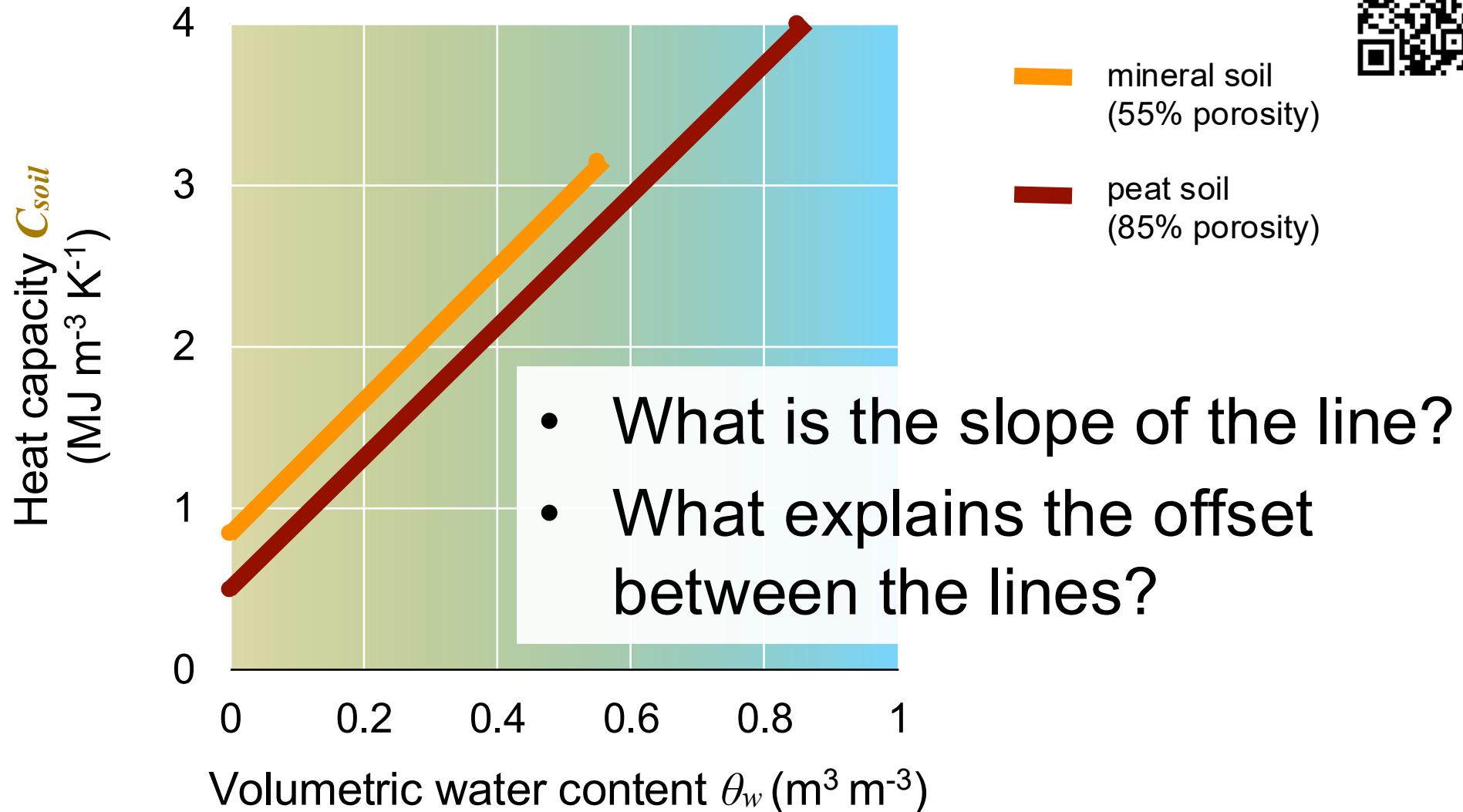


Photo: R. Ketler

Heat capacity and soil water content



Heat capacity and soil water content



Warming / cooling of a soil

Relating the **change of soil heat flux with depth** (the divergence of Q_G , i.e. $\partial Q_G / \partial z$) to the **rate of temperature change** ($\partial T / \partial t$) due to the **heat capacity** of the layer:

$$\frac{\partial Q_G}{\partial z} = C_s \frac{\partial T}{\partial t} \quad (\text{Eq 1})$$

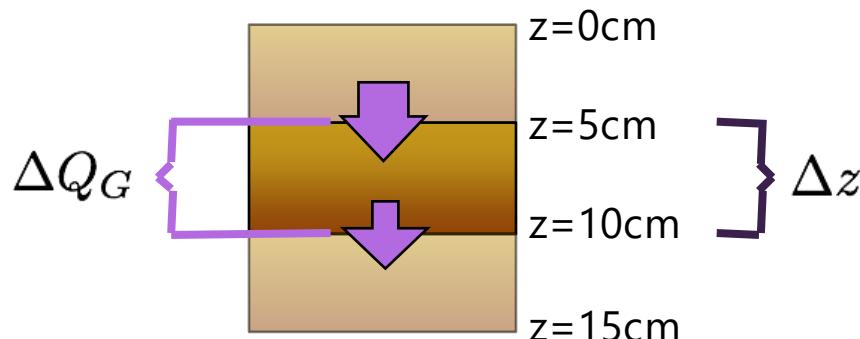
Heat capacity
in $\text{J m}^{-3} \text{K}^{-1}$

Heat flux divergence with
depth
in $\text{W m}^{-2} \text{m}^{-1} = \text{W m}^{-3}$

Temperature change
with time
in K s^{-1}

Warming / cooling of a soil

Re-arranging and writing in finite form gives the **rate of temperature change** in an actual layer of thickness Δz as:



$$\frac{\Delta T}{\Delta t} = \frac{1}{C_s} \frac{\Delta Q_G}{\Delta z}$$

★

Change of heat flux
(i.e. input - output)
in $\text{W m}^{-2} \text{m}^{-1}$

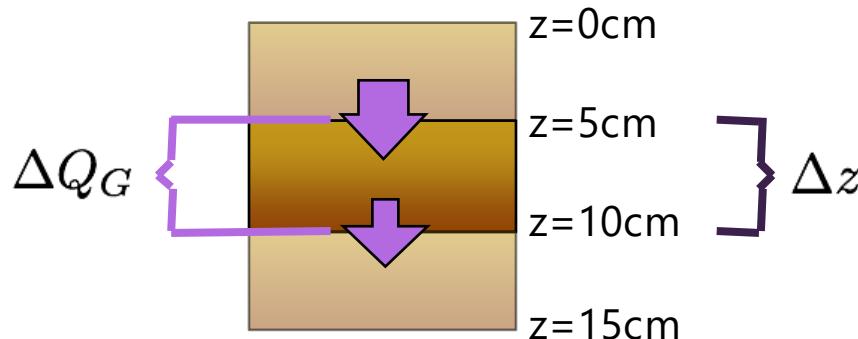
Change of
temperature over time
in layer (i.e. warming
or cooling rate) in K s^{-1}



If the soil has a high heat capacity, the rate of warming or cooling will be:

A) Higher

B) Lower



$$\frac{\Delta T}{\Delta t} = \frac{1}{C_s} \frac{\Delta Q_G}{\Delta z}$$

Change of heat flux
(i.e. input - output)
in $\text{W m}^{-2} \text{m}^{-1}$

Change of
temperature over time
in layer (i.e. warming
or cooling rate) in K s^{-1}



Fourier's law

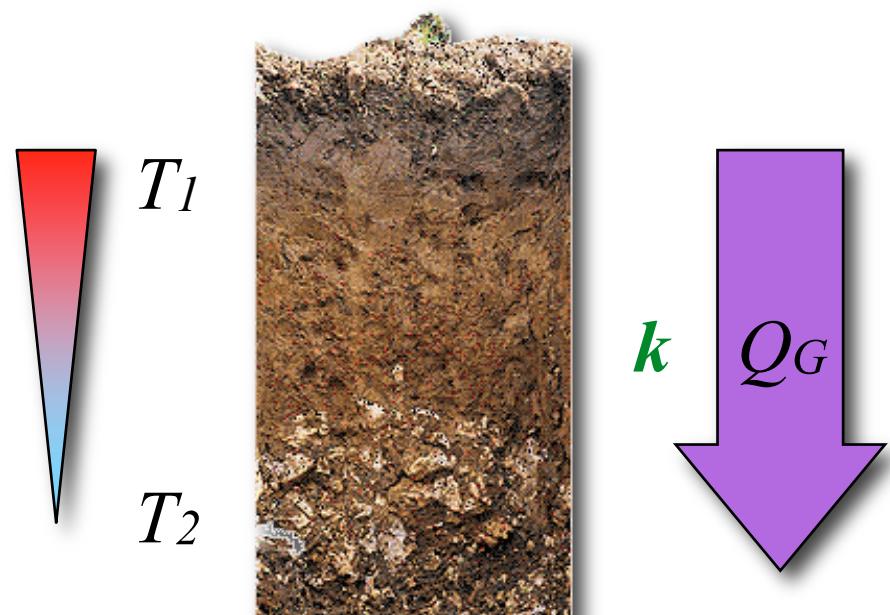
Fourier's law describes that the **flux density of heat conducted** Q_G is proportional to the **temperature gradient**:

Soil heat flux
at a given
depth
in W m^{-2}

Temperature
gradient with depth
in K m^{-1}

$$Q_G = -k \frac{\partial T}{\partial z} \quad \star \quad (\text{Eq 2})$$

Constant of
proportionality k is the
thermal conductivity (a
property of the material)
in $\text{W m}^{-1} \text{ K}^{-1}$



Thermal conductivity k of various materials

Material	k ($\text{W m}^{-1} \text{K}^{-1}$)
Air	0.025
Water (liquid)	0.59
Ice	2.1
Quartz	8.8
Clay minerals	2.9
Organic matter	0.25
Stainless steel	21
Copper	380

Mineral matter is a good conductor

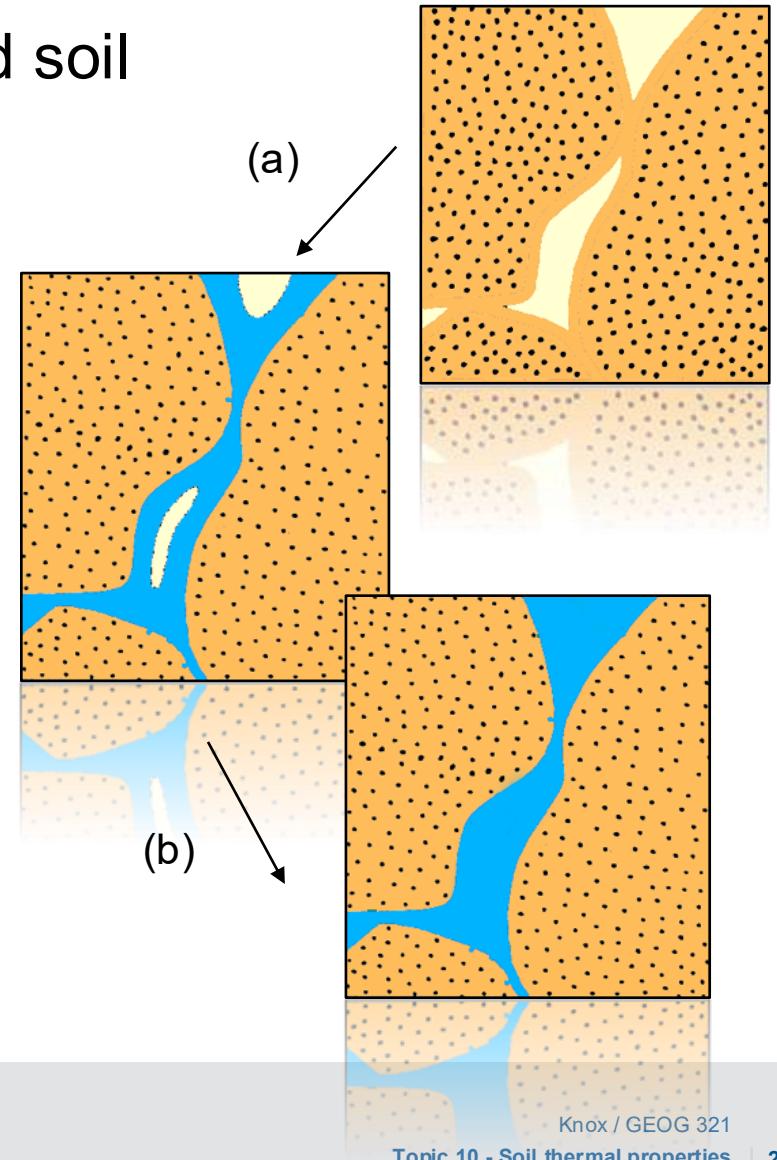
Water is intermediate

Air is very poor

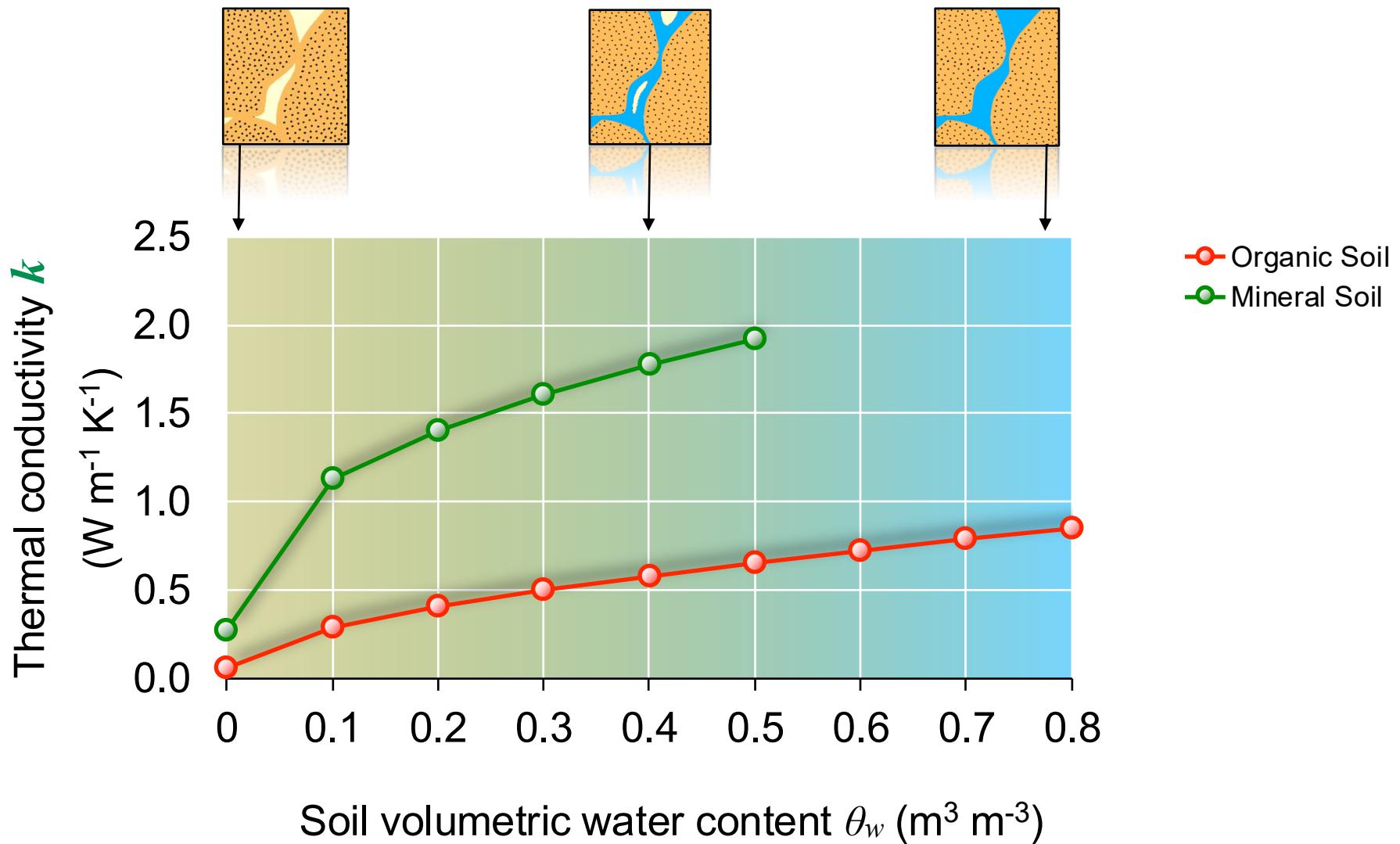
Thermal conductivity k and water content

A non-linear relation exists between k and soil water content (θ_w)

- Adding water to dry soil (a) initially causes k to increase rapidly – rapid increase in area of contacts between soil particles resulting from water film.
- As more water (b) is added, k increases less rapidly – area of contacts increases more slowly per unit of water added (i.e. diminishing returns).

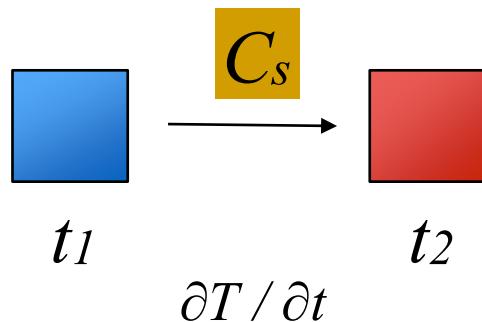


Soil water content and thermal conductivity k

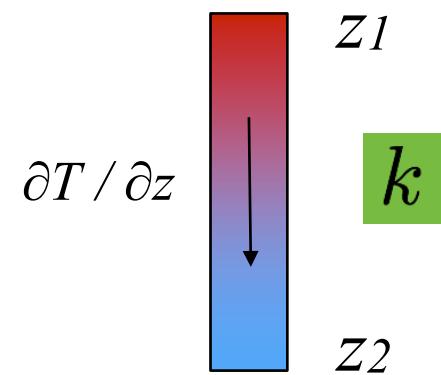


Combining thermal properties

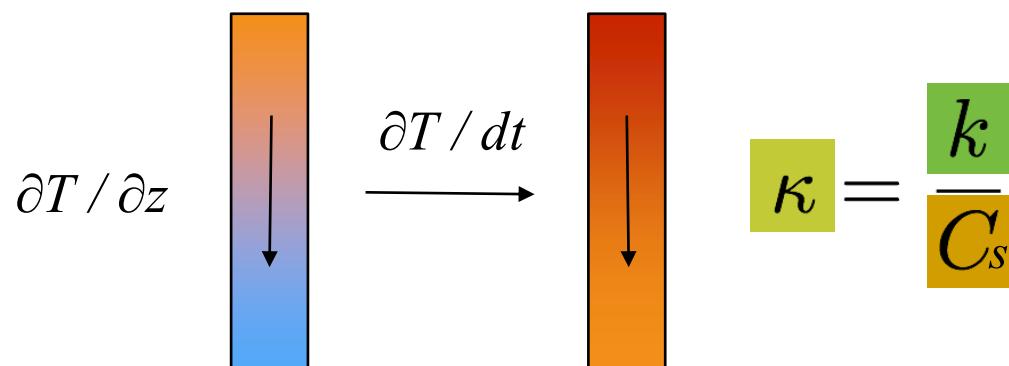
How rapidly does a volume warm when a certain amount of energy is supplied?



How well does heat conduct from one depth to another for a given temperature gradient?



How rapidly does a soil warm at depth if energy is available at the surface?



Thermal diffusivity

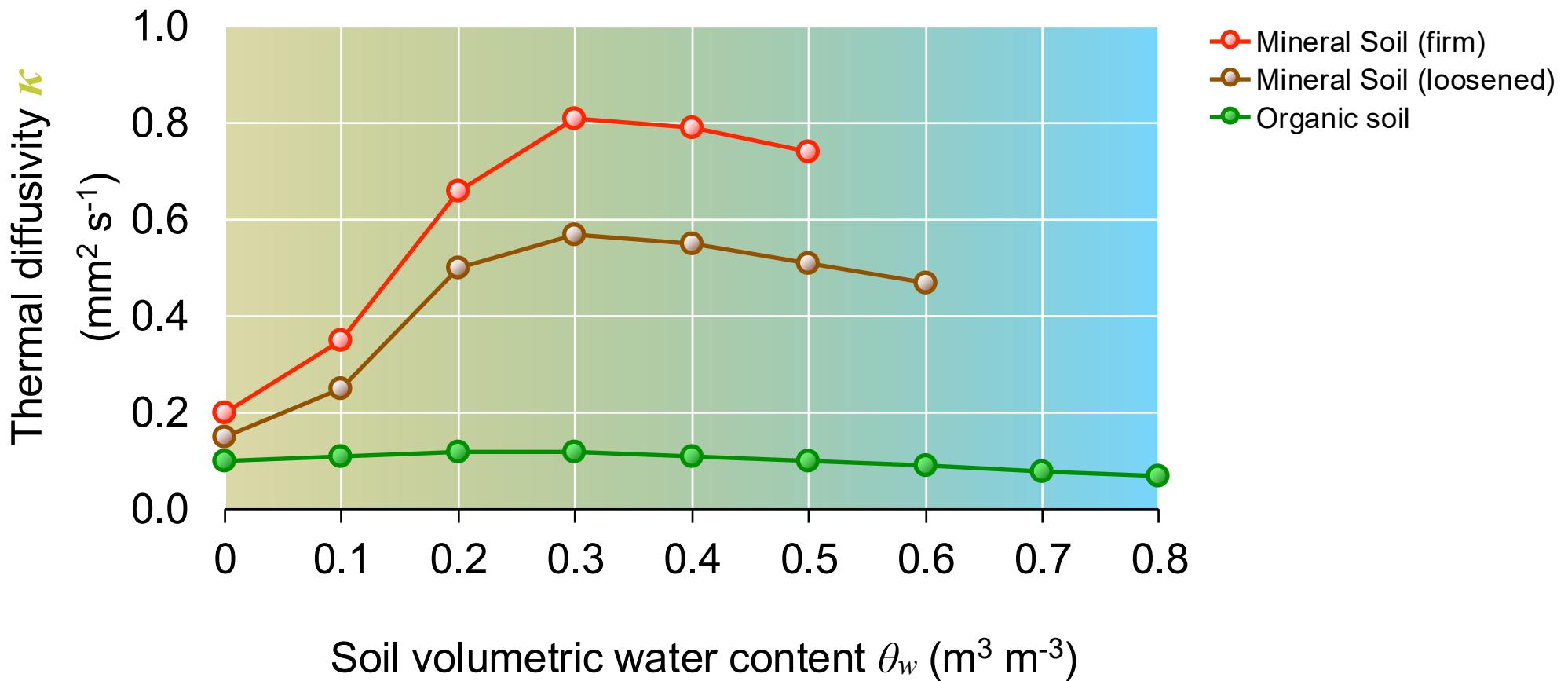
Thermal diffusivity κ (greek ‘kappa’ - not ‘K’) – indicates how quickly soil at depth will warm or cool in response to heating or cooling at the surface. It tells us how fast a temperature wave will diffuse or travel downward into a soil.

It is defined:

$$\kappa = \frac{k}{\bar{C}} \quad *$$

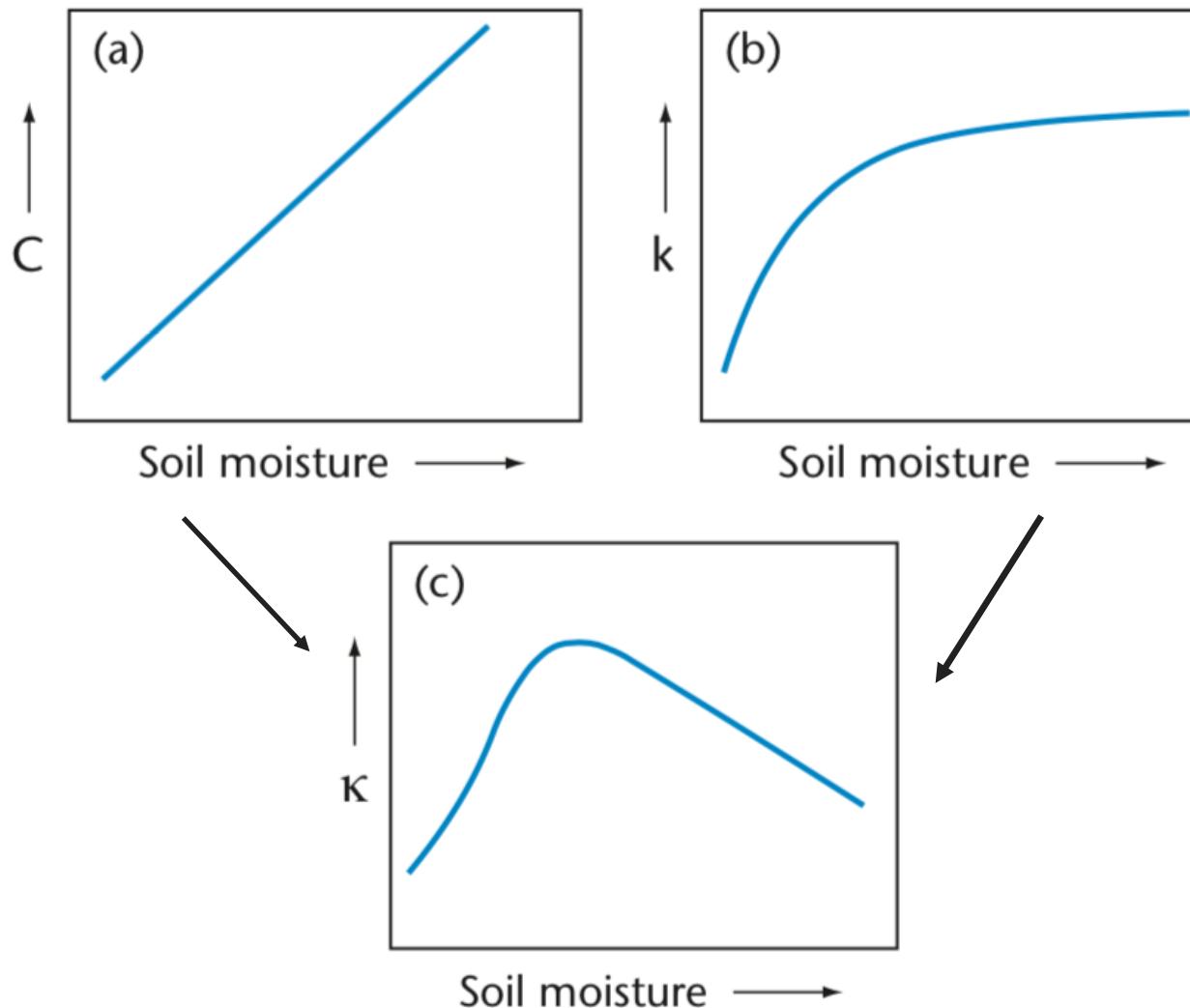
Units: $\text{m}^2 \text{ s}^{-1}$

Soil water content and thermal diffusivity



Why the curious shape?

Why the curious shape?



$$\kappa = \frac{k}{C} \star$$

Take home points

- Soils are important for **storage of heat and water** in the climate system.
- Two basic thermal properties regulate the exchange - **Heat capacity C_s** and **thermal conductivity k** . From those we can derive **thermal diffusivity $\kappa = k / C_s$** .
- The **water content** of the soil is significantly altering both **C** (linearly) and **k** (non-linearly).