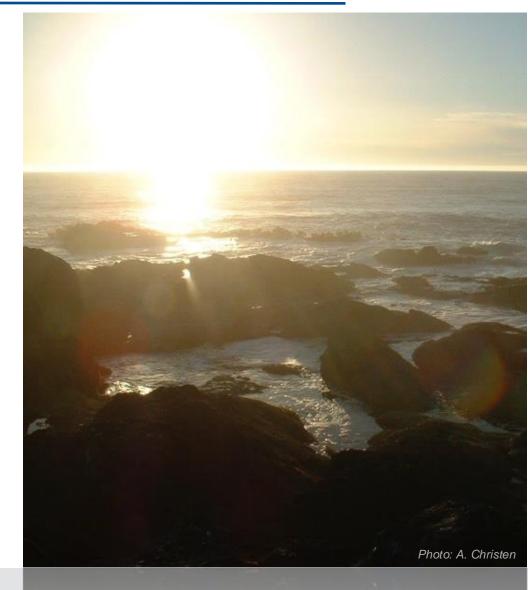


Photo: A. Christen

Learning objectives

- Be able to predict the relative position of the solar disk.
- Use this to calculate the irradiance reaching our planet 'at the top of the atmosphere' (in absence of atmospheric effects).



Input energy into Earth's climate system

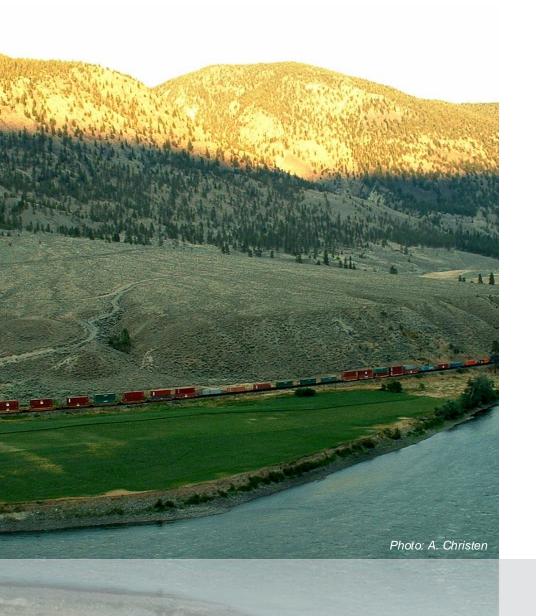
Average heat flux density from external sources at Earth's surface:

Surface Average Energy Flux

Solar electromagnetic radiation	241.5 W m ⁻²
Energetic particles (sun and space)	0.001 W m ⁻²
Geothermal	0.06 W m ⁻²
Anthropogenic (fossil fuels, nuclear energy)	0.02 W m ⁻²

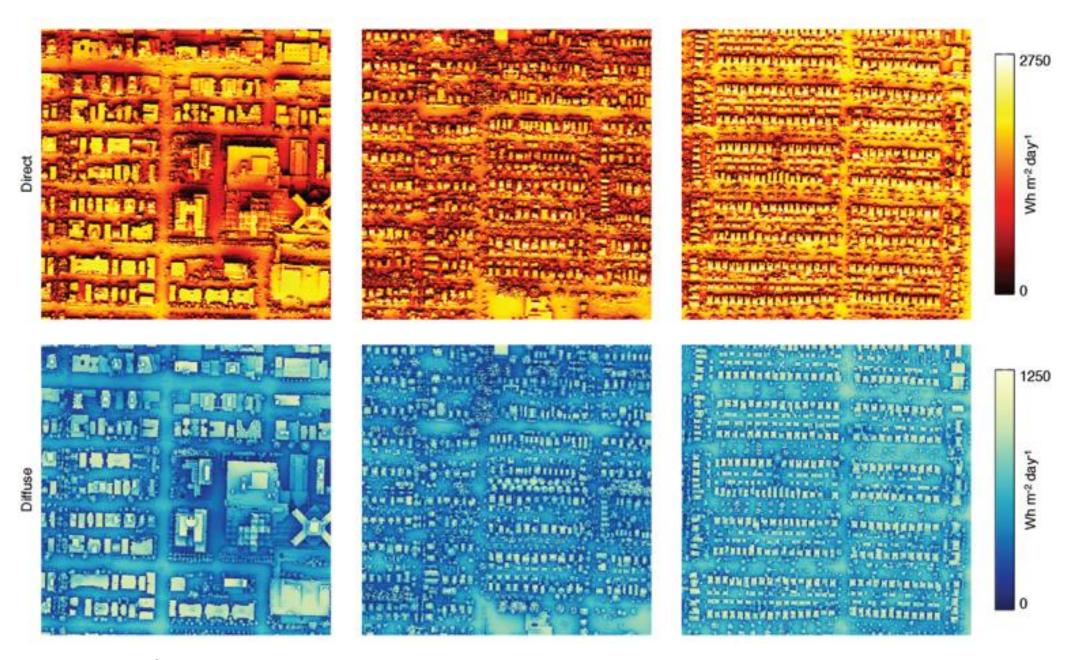
We see: Virtually all external input of energy into Earth's climate system is solar radiation (99.97%). Let us understand the solar input in more detail.

Motivation to study radiation geometry



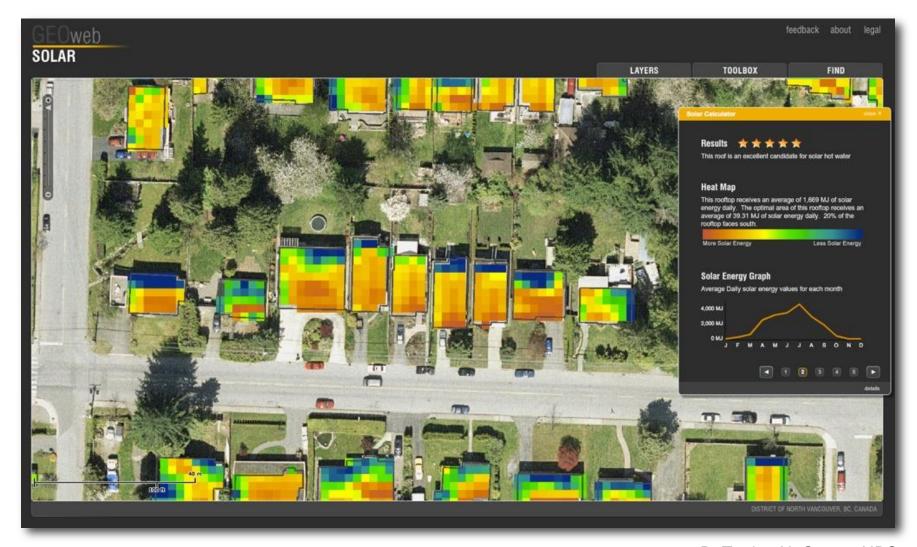
The geographic distribution of radiant energy is not equally distributed on Earth on both large scales (Earth's geometry) and small scales (topography) but rather results in strong energetic gradients.

Those differences cause many microclimates. Knowing the differences in radiant energy distribution allows you to predict weather and climates.

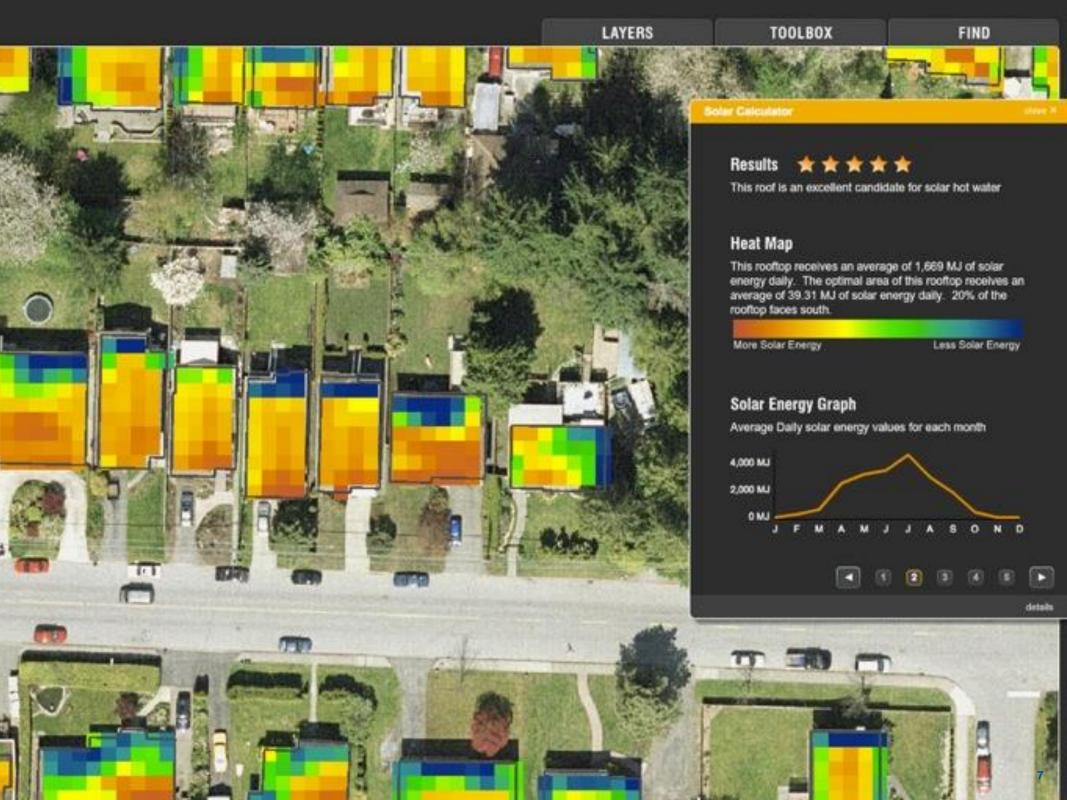


R. Tooke, UBC

District of North Vancouver Solar Calculator



R. Tooke, N. Coops, UBC



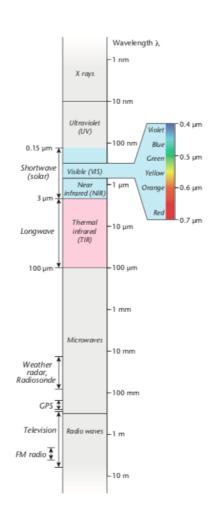
Radiation properties and laws

Properties of radiation (dual properties: wave/particle).

- Frequency v, wavelength λ and speed of light c.
- The electromagnetic spectrum.
- Energy of a photon: e = h v.

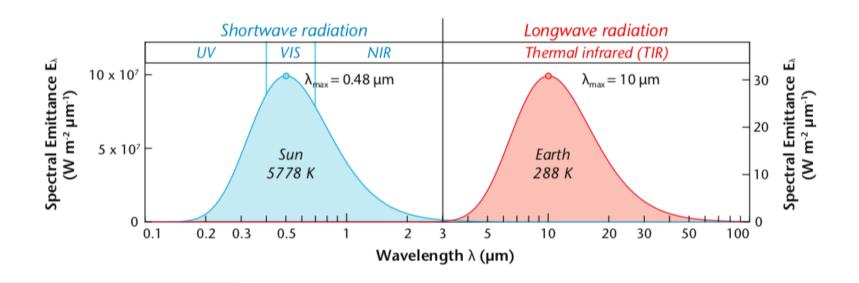


Reading package Lecture 4-5 'Radiation Basics'

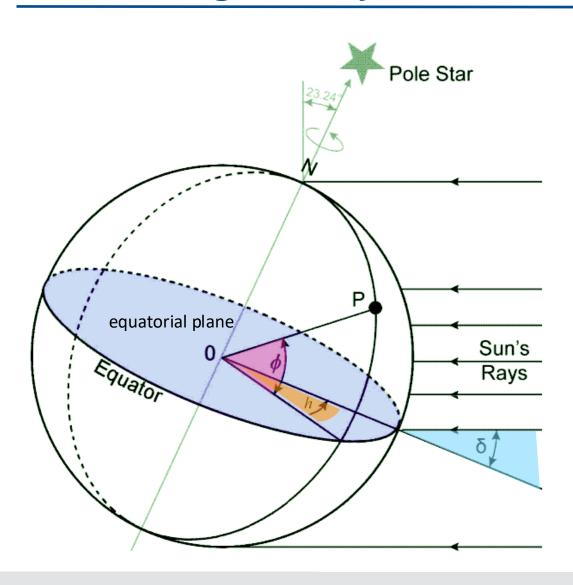


Radiation properties and laws

- Radiation laws
 - Stefan Boltzmann law $\rightarrow E = \sigma T_0^4$ (and $E = \varepsilon \sigma T_0^4$)
 - Wien's Law $\rightarrow \lambda_{\max} = \frac{b}{T}$
 - Kirchhoff's Law $\rightarrow \zeta_{\lambda} = \varepsilon_{\lambda}$



Sun-Earth geometry



Solar declination δ

Angle between Sun's rays and equatorial plane.

Latitudeφ

Angle between the equatorial plane and the site of interest (point P in the figure).

Hour angle h

Angle through which the Earth must turn to bring the meridian of the site P directly under the Sun. It is a function of the time of day.

Approximations for solar declination

 δ only depends upon day of year. As a simple approximation for δ in degrees we can use:

$$\delta \approx -23.4^{\circ} \cos \left(2\pi \frac{DOY + 10}{365}\right)$$

where DOY is the day of the year (e.g. 32 for February 1st). A more accurate approximation that takes into account the non-circular orbit of our Planet is:

$$\begin{array}{ll} \delta & \approx & 0.006918 - 0.399912\cos\gamma + 0.070257\sin\gamma \\ & -0.006758\cos(2\gamma) + 0.000907\sin(2\gamma) \\ & -0.002697\cos(3\gamma) + 0.00148\sin(3\gamma) \end{array}$$

which returns δ in <u>radians</u>. γ is the fractional year:

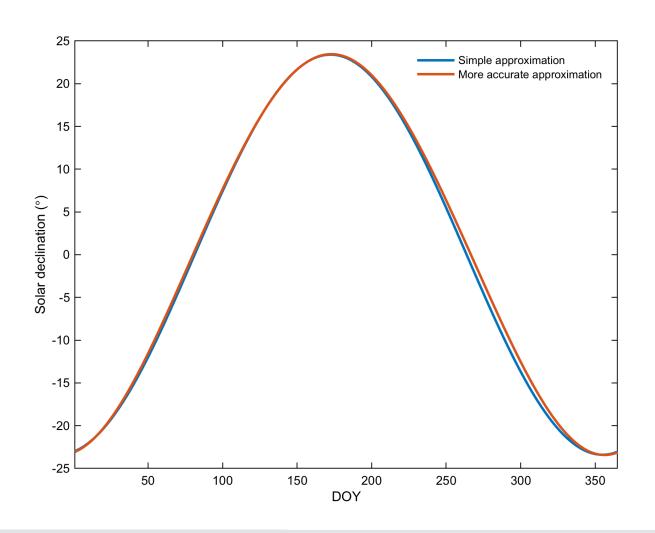
$$\gamma = \frac{2\pi}{365}(DOY - 1)$$

Quick comment on equations for declination angle

$$\delta ~pprox ~-23.4^{\circ}\cos\left(2\pirac{DOY+10}{365}
ight)$$

$$\delta \approx -23.4^{\circ} \cos \left[360(DOY + 10)/365 \right] \quad (3)$$

Approximations for solar declination



The **declination angle** (δ) varies seasonally due to the tilt of the Earth on its axis of rotation and the rotation of the Earth around the sun.

Declination is **zero** at the equinoxes (March 22 and September 22), positive during the northern hemisphere summer and negative during the northern hemisphere winter

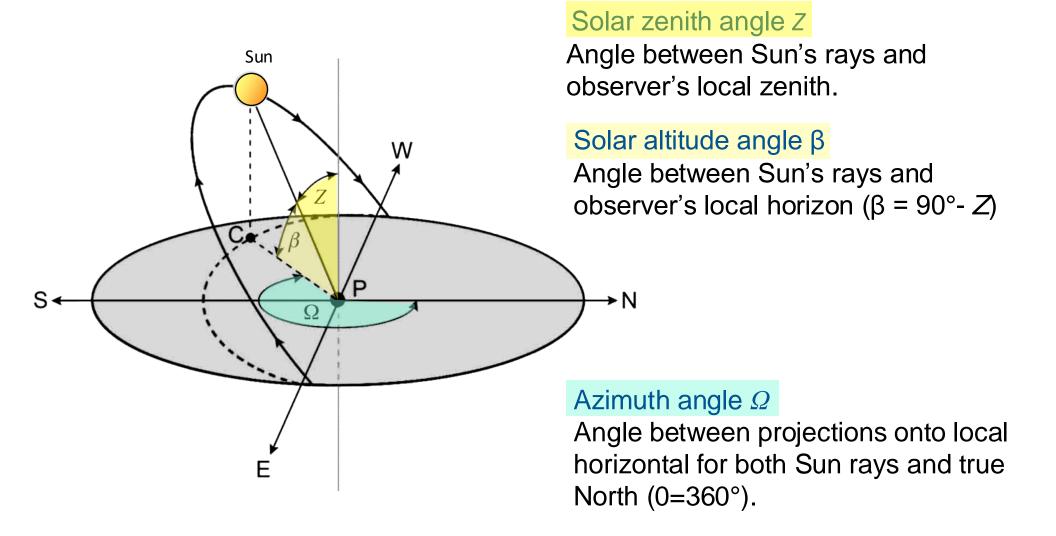
What is Earth's declination angle for:

- 1) January 1
- 2) June 21

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Observer's local geometry



Calculating the solar zenith angle

The solar zenith angle can be calculated based on:

$$\cos \frac{Z}{Z} = \sin \frac{\phi}{\delta} \sin \frac{\delta}{\delta} + \cos \frac{\phi}{\delta} \cos \frac{\delta}{\delta} \cos \frac{h}{\delta}$$
$$= \sin \frac{\beta}{\delta}$$

since 1 hour = 15° of longitude due to rotation, the hour angle is

$$h = 15^{\circ}(12 - t)$$

where t is **local apparent time (LAT)** (in hours). Next problem - how do we get t?

So many times...

- Standard time (e.g. Eastern standard time, EST) What is on your watch without daylight savings offset - same for all longitudes within a given time zone.
- Local mean solar time (LMST) Mean solar time is fixed and ensures that on average, highest solar altitude is observed at noon (but not at each day throughout the year). Changes with longitude.
- Local apparent time (LAT) A non-uniform time that is varying through the year according to the equation of time. It ensures that highest solar altitude is **always** observed at noon.

Calculating LMST

LMST = LST + 4 minutes * (LL - LSTM)

- LST (local standard time) = Clock time, adjusted for daylight savings time if necessary.
- LL = The local longitude; positive = East, and negative = West.
- LSTM = The local standard time meridian, measured in degrees, which runs through the center of each time zone. It can be calculated by multiplying the differences in hours from Greenwich Mean Time by 15 degrees per hour. Positive = East, and negative = West.

Note: The "4" in the equation is the quotient of 60 minutes of time and the 15 degrees of longitude that the earth rotates in that time (i.e., the earth rotates one degree every four minutes).

Local mean solar time (LMST) - Montreal example



EST = UTC- 5
-5 x
$$15^{\circ}$$
 = -75°

On the meridian of -75° EST = LMST

Any other longitude within time zone has an offset of 4 min per 1º between LMST and EST

Note that if the site is east of the LSTM, the (LL - LSTM) factor should be a positive number, and if it is west it should be negative. Topic 4 - Radiation geometry 20

LMST Example

Montreal's **longitude** is 73.5674°W. It is located within the Eastern Standard Time Zone (**EST**) whose standard meridian (LSTM) is at 75°W(= 5x15). The offset between EST and LMST is, in minutes:

4 minutes * (LL - LSTM) = 4 min/ $^{\circ}$ x (-73.56 – (-75)) = 5.76 min (or 5 min and 45 s)

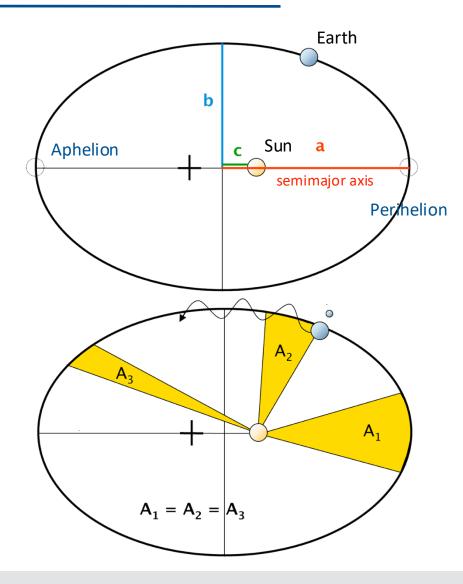
If EST is 14:00, then

LMST = EST + 4 minutes * (LL - LSTM) = 14:00 + 5.76 min = 14:05:45

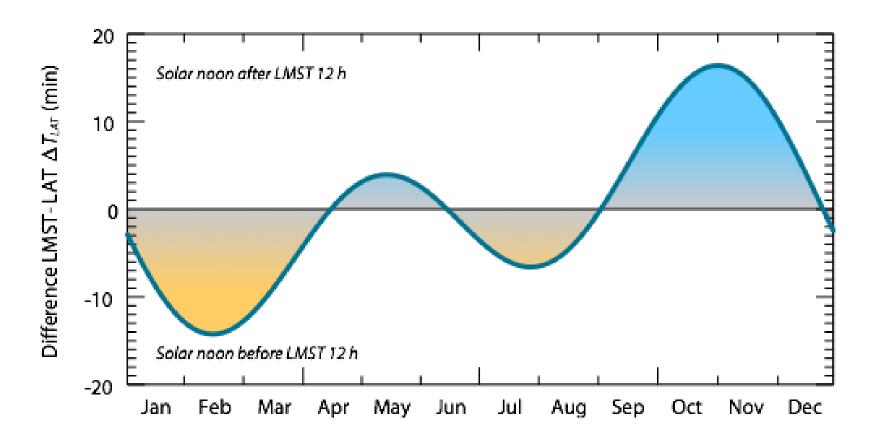
Review - planetary orbits and Kepler's laws

Kepler's first law states that planets follow an elliptical orbit, with the Sun in one focus. This implies that the Earth-Sun distance is changing during a year.

By Kepler's second law, a planet moves fastest when it is near the perihelion and slowest when it is near Aphelion.



Local apparent time (LAT) - equation of time



$$\Delta T_{\mathrm{LAT}} = 229.18 \left[0.000075 + 0.001868 \cos \gamma - 0.032077 \sin \gamma - 0.014615 \cos(2\gamma) - 0.040849 (\sin 2\gamma) \right]$$

So many times...

- Standard time (e.g. Pacific standard time, PST) What is on your watch without daylight savings offset - same for all longitudes within a given time zone.
- Local mean solar time (LMST) Mean solar time is fixed and ensures that on average, highest solar altitude is observed at noon (but not at each day throughout the year). Changes with longitude.
- Local apparent time (LAT) A non-uniform time that is varying through the year according to the equation of time. It ensures that highest solar altitude is **always** observed at noon.

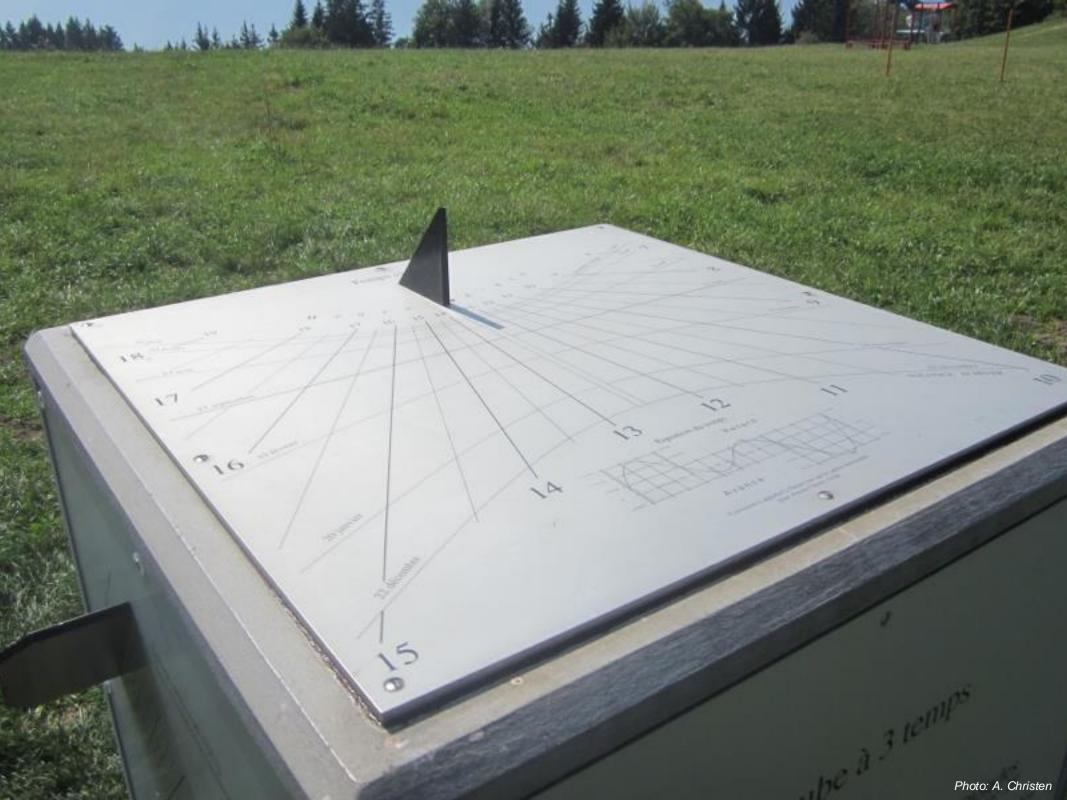
Calculating LAT

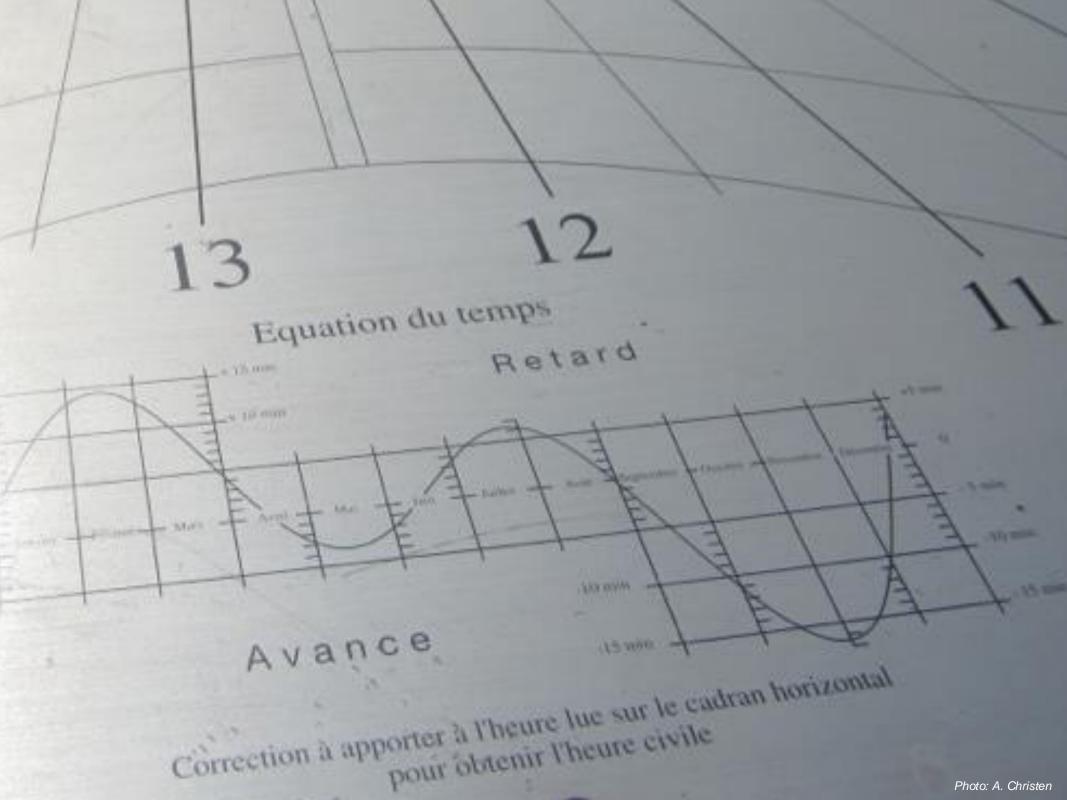
Now that we have LMST, to get LAT we use the equation:

LAT = LMST -
$$\triangle$$
LAT

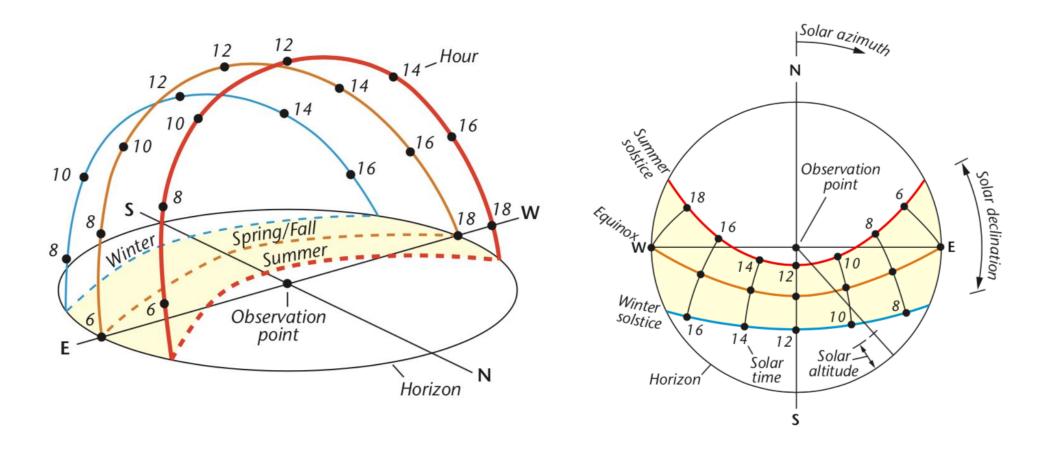
where

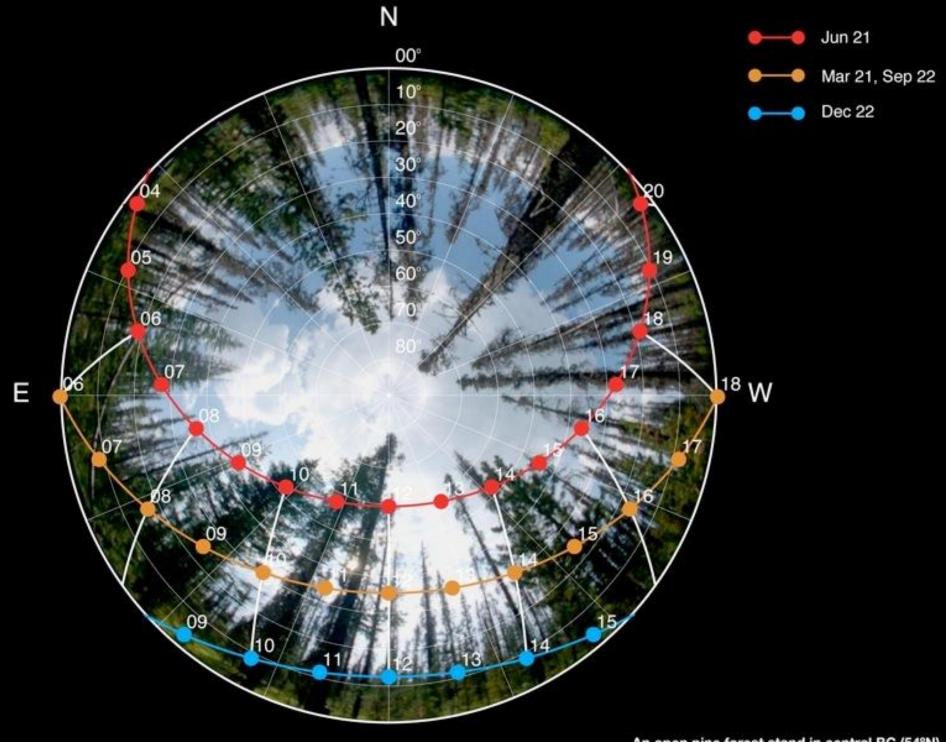
$$\Delta T_{\rm LAT} = 229.18 \left[0.000075 + 0.001868 \cos \gamma - 0.032077 \sin \gamma - 0.014615 \cos(2\gamma) - 0.040849 (\sin 2\gamma) \right]$$



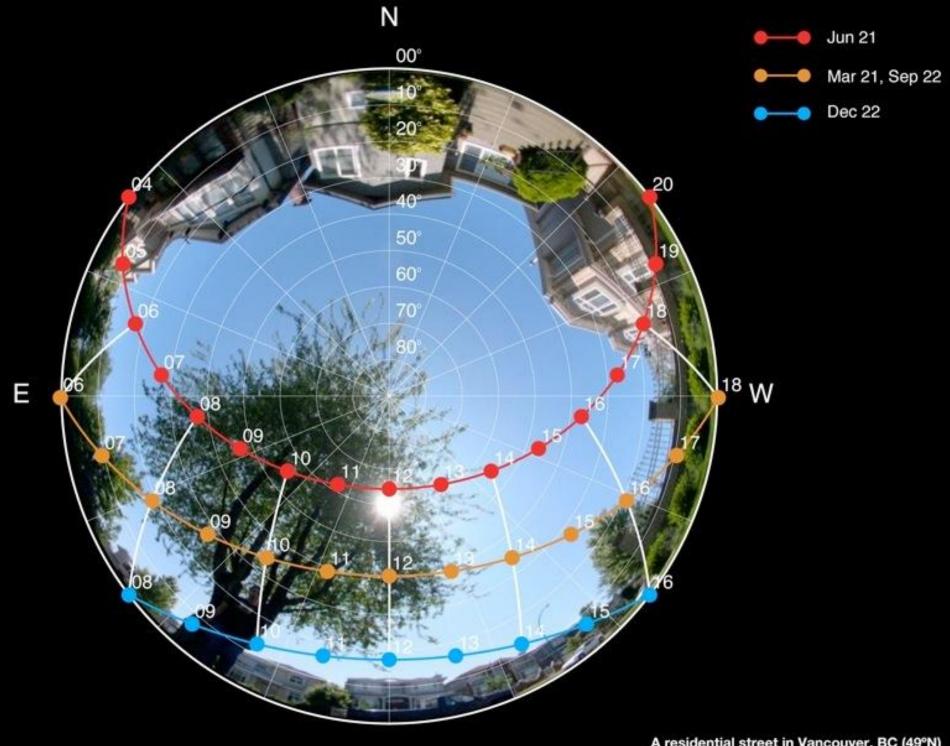


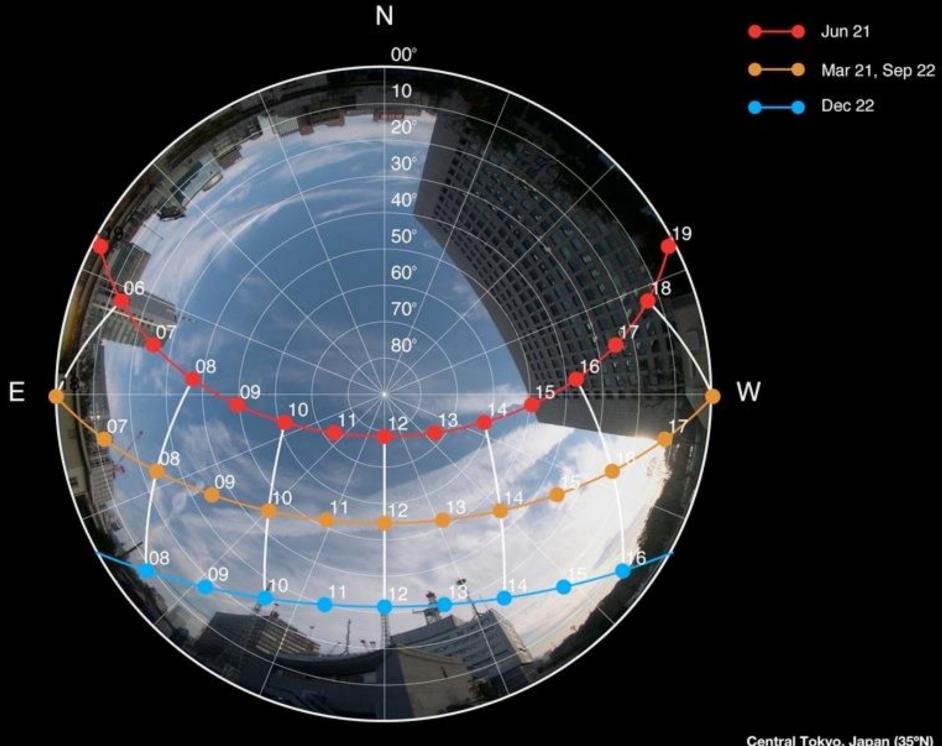
Sun path diagrams

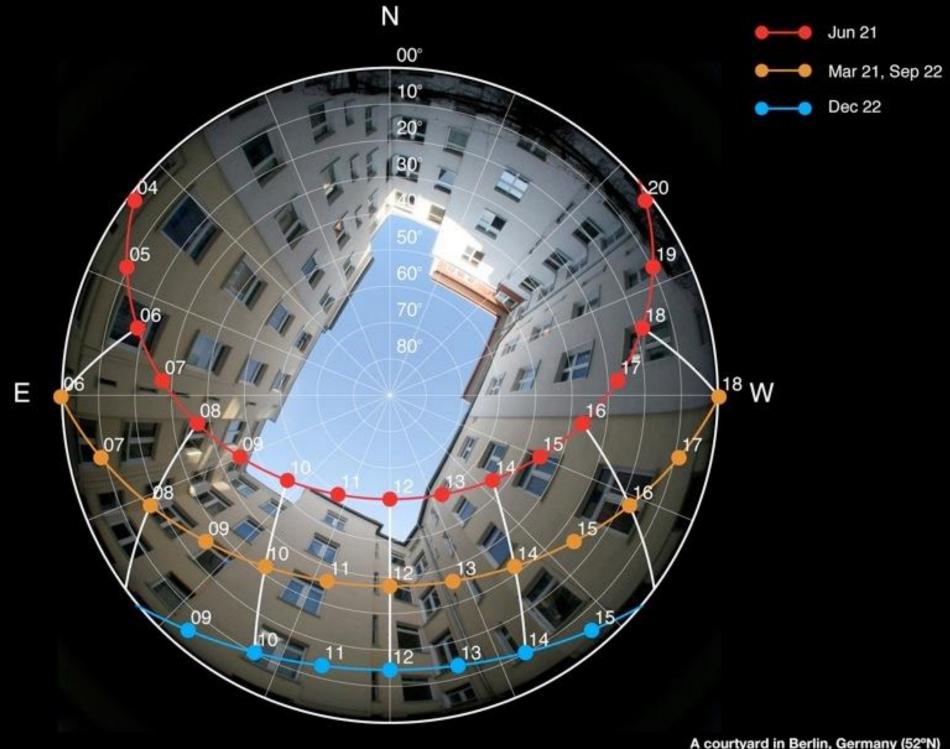


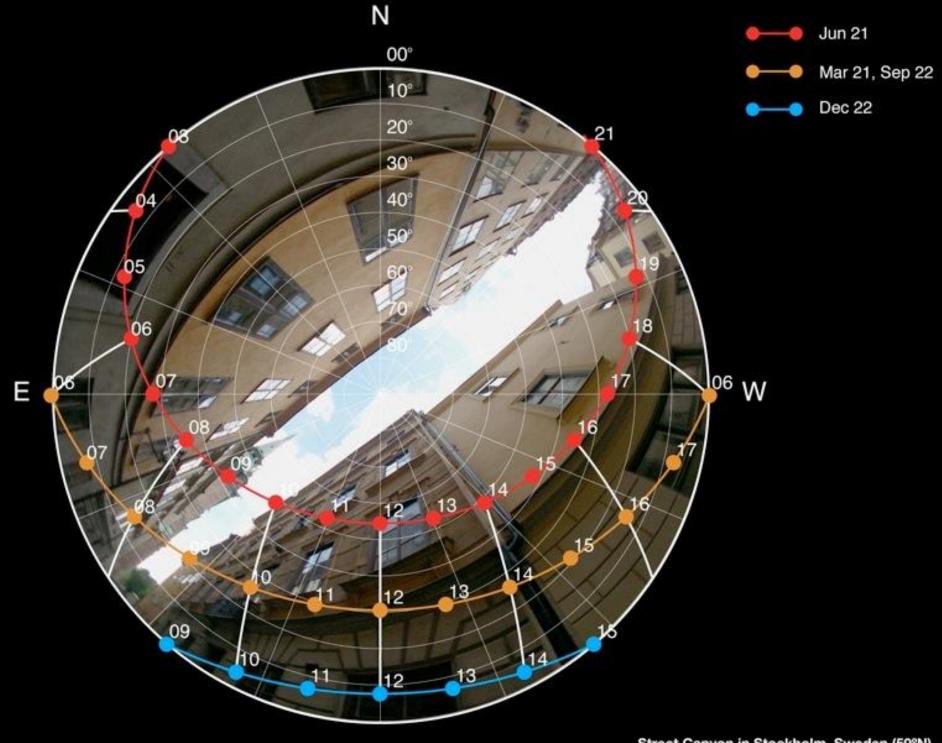


S







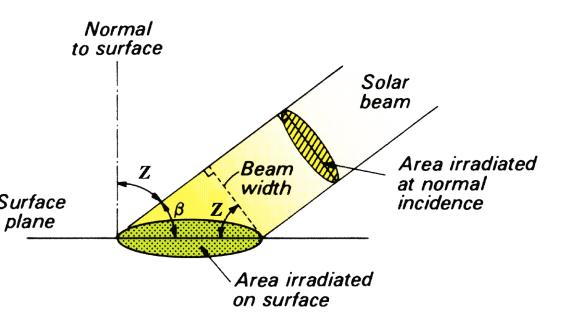


Review: Cosine-law of illumination

The radiant flux density incident on the surface (S) is given by

$$S = S_i \cos \mathbf{Z}$$

 S_i is the flux density on a surface perpendicular to the beam (i.e., Surface when $Z = 0^{\circ}$) and Z is the angle of incidence (the zenith angle, i.e., the angle between the normal to the surface and the direction of the beam).



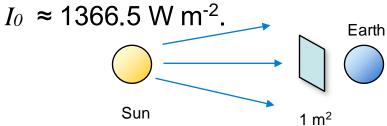
T.R. Oke (1987): 'Boundary Layer Climates' 2nd Edition.

Extraterrestrial irradiance

So the solar input at top of the atmosphere at any time and location hence is

$$K_{Ex} = I_0 \left(\frac{R_{av}}{R}\right)^2 \cos \frac{Z}{Z}$$

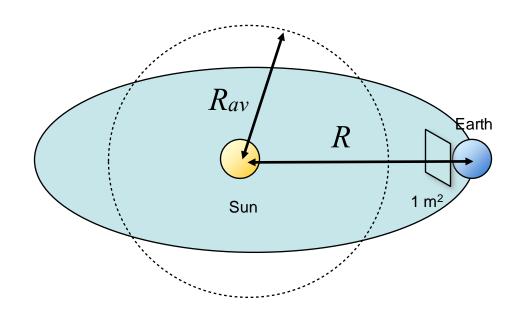
where I_0 is the Solar constant, namely the solar radiant flux density normal to the solar beam at Earth's mean distance from Sun. Present observations suggest that on the yearly average





The Nimbus satellite platforms hosted the first instruments measuring the solar constant and Earth's radiation budget directly from space (NASA).

Earth's distance to Sun



 R_{av} is the mean distance Earth-Sun over the year

R is the actual distance Earth-Sun at a given time

$$\left(\frac{R_{av}}{R}\right)^2 = 1.00011 + 0.034221\cos\gamma + 0.001280\sin\gamma + 0.000719\cos(2\gamma) + 0.000077\sin(2\gamma)$$

Take home points

- We discussed a lengthy recipe to predict the relative position of the sun with reasonable accuracy, taking geometry and astronomical parameters into account.
- We combined cosine law of illumination with the solar constant to calculate extraterrestrial irradiance at any given time and for any location.
- In the next lecture we will add the effects of the atmosphere with the goal to predict surface irradiance.