# Model-based and model-free characterization of epidemic outbreaks — Technical notes on Dehning et al., Science, 2020

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In this technical note, we provide additional background on our Bayesian inference for change-point detection in COVID-19 case numbers (Dehning et al., Science, 2020). In particular, we explore basic properties of model-based and model-free estimates of the reproduction number, discuss what conclusions can be drawn from Bayesian analyses, further develop our model and apply it to newly available data, and discuss potential issues with changes in testing policies.

This technical note presents work in progress and should be considered like an internal draft. It is not ready for submission yet, and is being frequently updated.

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24 25 26 27	estimates that are difficult to interpret  3. R estimates depend on the assumed generation time.  4. Model-free methods may return erroneous	6	55 56	VII.	Supplementary Information: Figures  I. INTRODUCTION	17
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41 42 43	IV. Model evolution  A. Model updates based on time of symptom onset and comparison to previous results	9	70 71 72 73		Remarks on apparent discrepancies between t values for the reproductive number R as report by the Robert Koch Institute (RKI) and the c responding spreading rate resulting from our pu	ed or-

based on time of reporting

lished analysis. We will explain below how this

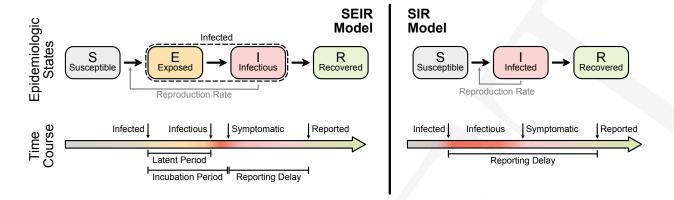


FIG. 1. Illustration of two basic compartmental models in epidemiology. The SEIR model (left) captures the basic steps that infections passes through: A healthy person becomes infected (leaves S, enters E) but not infectious; after some time ('latent period') the person becomes infectious (leaves E, enters I) but symptoms only show after some incubation period; after some time the person is no longer infectious (leaves I, enters R), which can have several reasons including isolation, conventional recovery, or death. The SIR model (right) is the most basic compartmental model and does not distinguish between infectious and infected: A healthy person becomes infected (leaves S, enters I) and by this begins to infect other persons, but only shows symptoms with some delay; after some time the person "recovers" (leaves I, enters R), which again includes isolation, recovery, or death.

apparent discrepancy arises from the comparison 108 of model-free estimates to those from a differential- 109 equation based modeling of disease dynamics. We 110 show how the model-free approach may substan- 111 tially underestimate the reproductive number R 112 immediately after a sudden drop in R has occurred. 113 From the comments we received it seems that this 114 very important fact related to estimating R is largely 115 unknown, and also counterintutive to most readers. 116 This effect, however, fully explains the apparent discrepancies between the RKI reports and our study. 117 here.

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- tion. As we will explain below, our approach selects 127 question of testing. the most plausible of multiple causal explanations of the observed data, but does not establish strict interventional causality.
- 3. New data have been released in the time since our analyses were completed. Most prominently, data on the exact times of symptom onsets (epi curve) are now available and supersede the case report data as the best data source for modeling the outbreak. 131

of performed tests, test capacity, and on delays between symptom onset, test and case report, we reanalyze in great detail the disease and testing dynamics, especially with respect to the timing of the peak in new symptom onsets. We conclude that all symptom onsets that are relevant for the main conclusions of our previous publication have been tested at a time when testing had sufficient capacity and was sufficiently constant.

We will in the following address the issues revolving We therefore derive and demonstrate it in detail 118 around the reproductive number R first, also introducing the basic terminology of disease spreading and the 120 fundamental difference between model-free and model-2. Questions revolving around the philosophy and inter- 121 based estimation of epidemiological parameters. Next, we pretation of our modeling approach that combines a 122 will discuss philosophy and interpretation of model-based differential equation model of the disease outbreak, 123 estimation in the Bayesian framework and the causality Bayesian parameter inference and Bayesian model 124 question. We then show how our original analyses can be comparison. Most frequently we were asked if and 125 evolved to incorporate new data, in particular on sympin what sense our results have a causal interpreta- 126 tom onset (epi curve). Last we turn to the important

## ESTIMATING THE REPRODUCTIVE NUMBER

# Basic SIR dynamics

Before we define the reproductive number R, we briefly As we will show below, our conclusions remain un- 132 recapitulate the basic SIR dynamics that we consider changed when updating our model to the new data. 133 (Fig. 1). In principle, the course on an infection can be 134 described as follows: A susceptible person (not infected Questions on how changes in testing capacity may 135 and not immune) becomes infected but is initially not have influenced our results. Given the data that 136 infectious; after some time, the person starts to be inhave become available on the weekly (daily) number 137 fectious but symptoms only show after the incubation

138 period; eventually, the person is no longer infectious be-139 cause it is either isolated, it recovers, or it dies. The idea 140 of compartmental models is to group the population into 141 compartments; in the most simple but established SIR 142 model these are susceptible (S), infected (I), and recov-143 ered (R). Assuming a well-mixed population (a mean-field approximation of everybody interacting with everybody), one can formulate differential equations that describe the 146 time development of these compartments:

$$\frac{dS}{dt} = -\lambda \frac{SI}{N} \tag{1}$$

$$\frac{dS}{dt} = -\lambda \frac{SI}{N} \tag{1}$$

$$\frac{dI}{dt} = \lambda \frac{SI}{N} - \mu I \tag{2}$$

$$\frac{dR}{dt} = \mu I \tag{3}$$

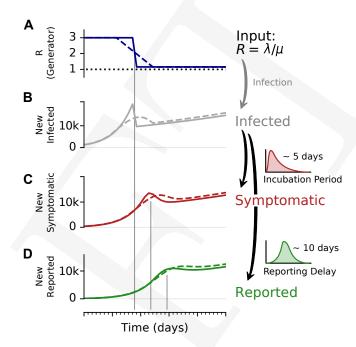
$$\frac{dR}{dt} = \mu I \tag{3}$$

This assumes a spreading rate  $\lambda$  for infected people to 148 infect susceptible people (who they meet randomly) and 149 a recovery rate  $\mu$  for infected people to recover. These differential equations can be extended to include various different compartments, in order to better resolve the 152 temporal course of the disease, but typically keep the 153 mean-field assumption of a well-mixed population unless evaluated on some (typically unknown) network. In this case, additional compartments reflect spatial information.

Observed case numbers are always delayed from the true infection date (Fig. 2). In general, when a person becomes infected, the onset of symptoms is delayed by the incubation period. Upon symptom onset, it typically takes a few days until the person undergoes a test and the case is reported (although some people are tested before symptom onset, e.g. if contacts are traced or tests are performed at random "Stichprobe"). However, for the modeling, one is usually interested in the actual time when a person becomes infected — but this information is not directly available in real-world data. One either works with the reporting date or with the dates of the symptom onset (epi curve) that can be reconstruced e.g. via nowcasting. Note that these are 170 still delayed with respect to the true infection dates due to the incubation period. For the example models in the following, we synthetically generate observed cases symptomatic or reported — by convolving the infected 174 cases with a distribution of incubation periods or reporting 175 delays, respectively (Fig. 2).

# Model-free estimation of reproduction number

**Definition of R.** The reproductive number R quanti-179 fies how many susceptible persons are on average infected by one infected person. If one person infects on average more than one (R > 1), then case numbers are growing 194 that they are applied to the epi curve. 182 exponentially. If in contrast one person infects less than 195 <sub>183</sub> one (R < 1), then case numbers are declining. Therefore, <sub>196</sub> number assumes a reproductive process with offspring  $_{184}$  R=1 marks the critical stransition between growth and  $_{197}$  generation, such as a branching process [2]. For this, one



A change-point in R can lead to a transient decay in case numbers. To illustrate the effect of a change point, and the delays in observing symptomatic and reported cases, we consider an SIR model with a fast or slow decay of R, and generate synthetic case numbers. A The reproductive number R exhibits a change point from R=3 to R=1.15, with a duration of either 1 day (solid) or 9 days (dashed). B The number of new infections can show a transient decrease caused by the change point in R, even though the underlying dynamics are always in the exponentially growing regime of R > 1. Such a decrease can be misinterpreted as R < 1. The number of C new symptomatic cases, and D reported cases is generated by convolving the new infected with a log-normal incubation period (median = [XX] days) or reporting delay (median [xx] days), respectively. Note that the convolution shifts and smooths the curve of the new infected. Nonetheless, the counter-intuitive effects of a transient decrease in case numbers caused by a change points, is still very well visible (See Fig. ?? for the challenges of estimate R in around the change point.)

185 decline of case numbers. Estimating the reproductive 186 number R in principle can be done in two manners, either 187 by inferring it from observed case numbers, or by follow-188 ing infection chains step by step. If one infers it from 189 observed case numbers, there are a number of possible 190 approaches. Some approaches are summarized in Fig. 4 191 and detailed below. All these approaches are applied to the observed case numbers (day of symptom onset, i.e., 193 epi curve, or day of reporting). In the following we assume

The most straight-forward definition of the reproductive

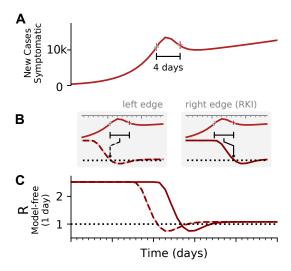


FIG. 3. Two different conventions to define the reproductive number R: Infections in the future or infections from the past. A Synthetic data for new symptomatic cases. The marked interval indicates an assumed generation time of 4 days. B The basic reproductive number can be defined either on the left edge of the generation interval (left, dashed line), describing the average number of future infections that are cause at time t, or on the right edge of the interval (right, solid line), describing the average number of infections at time t that were caused by the past ones. C Depending on the convention, the resulting curve of R is shifted by the generation time q. Note that in both cases the R is estimated erroneously to fall below R = 1, although in the underlying model it was was R > 1 all the time. This is an effect of the SIR dynamics together with a change point in the underlying R. (See Fig. 4 for model details.

assumes a generation time g in which an infectious person 199 can generate offspring infections. In the simplest case, one 200 could consider that offspring infections occur exactly after  $_{201}$  one generation time g. This allows to infer the effective  $_{202}$  spreading rate R precisely:

$$\hat{R}_t = \frac{\text{number of newly infected at time } t + g}{\text{number of newly infected at time } t}$$
 (4)

$$=\frac{C_{t+g}}{C_t}. (5)$$

In reality, these newly infected case numbers  $C_t$  have to 204 be approximated, e.g., by using new symptomatic cases or new reported cases. Moreover, the generation times g of each infection are widely distributed, so that using the average value q (or an estimate of it) is a further approximation. For its simplicity, this inference of R is widely applied and has proven quite useful.

When go into detail, there are two different conventions 211 for the timing of the estimated reproductive number with 212 respect to the case numbers (Fig. 3). Above, we consider 214 are caused by infections at time t (left-edge convention).

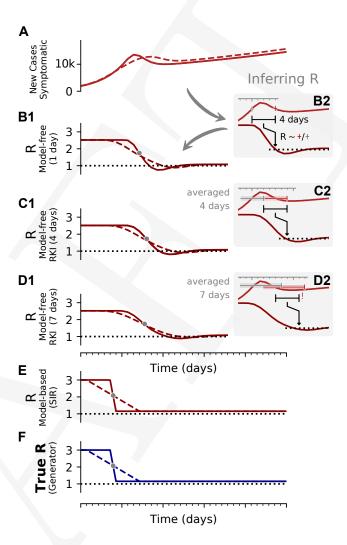
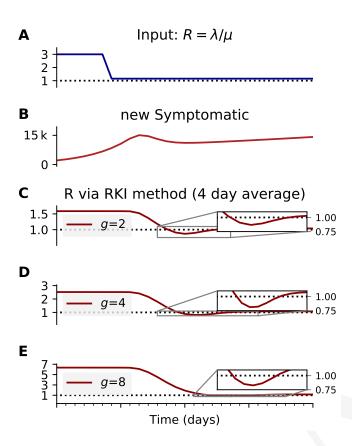


FIG. 4. The inferred reproductive number R depends on the inference method. A Synthetic data for new symptomatic cases generated with SIR dynamics from an underlying R with one change point (see **F**) of duration 1 day (solid) or 9 days (dashed). (See Fig. 2 for details). B Model-free inference of R based on the ratio of case numbers at time t and time t-d, marked by a red and gray cross (inset), respectively ('right-edge convention', cf. Fig. 3). C Model-free inference of R following the Robert Koch Insitut convention, i.e. using the definition of **B** but with averaging over a window of the past 4 days (inset, red and gray bars). D Same as C but averaging over 7 days. Note the overlap of intervals. - All the model-free methods (B-D) can show an erroneous estimate of R < 1 transiently, due to the change point in the underlying true R (depicted in  $\mathbf{F}$ ).  $\mathbf{E}$  The inferred R using change-point detection with an underlying dynamic model (SIR) does not show a transient erroneous R < 1 period. If the underlying dynamic model corresponds well enough to the true disease dynamics, then this approach reproduces the true  $R(\mathbf{F})$  that was used to generate the data  $(\mathbf{A})$ .

 $_{213}$   $R_t$  to characterize the number of future infections that  $_{215}$  Alternatively, one can consider  $R_t$  to characterize the



Inferred reproductive number depends on the assumed generation time g. We generate synthetic data using SIR dynamics with time-dependent R including a 1-day change point (A, cf. Fig. 4) that yields new symptomatic cases with transient decrease (B) despite all R > 1. Using the RKI convention to infer R (4 day average, right-edge convention), we demonstrate how generation times (g) result in different Rcurves (C-E). In particular, we find different initial levels of R(left plateau), differently long crossover duration (time from left plateau to right plateau), and differently deep transients of R < 1 (see insets).

 $_{216}$  number of infections at time t that were caused by the past pool of infected (right-edge convention), defined as

$$\hat{R}_t = \frac{\text{number of newly infected at time } t}{\text{number of newly infected at time } t - g} = \frac{C_t}{C_{t-g}}$$
(6)

The results for R are exactly equivalent, apart from a 218 shift in time by exactly q.

R as calculated by the RKI. Real-world data are 221 often noisy, and therefore averaging over a certain time window can help to smooth the estimate. This procedure is used in two variants by the RKI, smoothing over four days or over seven days[3]. In both cases, they assume a constant serial interval (generation time) of q=4 days 226 (Fig. 4). The four-day smoothing has the advantage that 227 it reacts a bit faster, the seven-day smoothing has the ad-228 vantage that it smooths out weekend-related modulations 229 of test numbers.

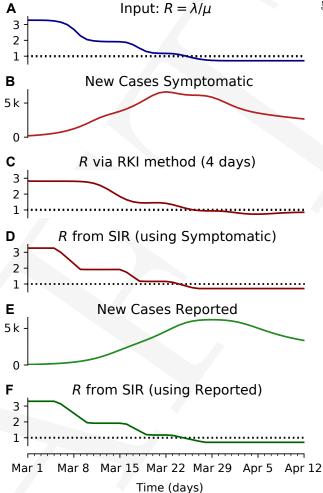


FIG. 6. The change-point detection methodology yields consistent results irrespective of whether it is applied to the new reported cases or the new symptomatic cases (e.g. obtained by nowcasting). A Time-dependent reproductive number as inferred from case numbers in Germany [1]. B Synthetic data for new symptomatic cases generated with SIR dynamics from the underlying time-dependent R (see A). C Inferred R from new symptomatic cases using RKI method (4 days generation time, right-edge convention) would reproduce step-like behavior (no noise present) but prematurely drops below R=1(dashed line).  $\mathbf{D}$  Inferred R from new symptomatic cases using change-point detection with dynamic model (SIR) correctly reproduces the input (A). E Synthetic data for new reported cases generate with SIR dynamics as in B (cf. Fig. 2). F Inferred R from new reported cases (**E**) using change-point detection with dynamic model (SIR) also correctly reproduces the input (A). Note that both **D** and **F** show sharper steps because of the assumed piece-wise linear change points in the model, and that they perform so well because they employ the true dynamic model that is used for the synthetic data. Both are model assumptions that need to be justified in our approach.

The general equation then reads as follows:

$$R_t = \frac{\sum_{j=t-w}^{t} C_j}{\sum_{k=t-q-w}^{t-g} C_k}$$

231 w is the window. The Robert Koch Institute chooses a 280 the different methods, we focus on the time point where window of 4 or 7 days [REF].

## Model-free methods versus model-based methods to infer reproductive number.

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 $_{244}$  estimates when R is changing rapidly. More precisely, in  $_{296}$  similar average delay of 5-6 days in total with respect to the following we show that these methods (1.) smooth  $^{297}$  the true R. out fast changes in R, (2.) produce some delay compared <sup>298</sup> useful for a fast estimate of R when R is not changing 303 effect cannot perfectly be disentangled or compensated. too quickly, they may lead to wrong estimates otherwise. 304

#### Model-free methods may smooth out fast changes.

In Fig. 4, the  $\hat{R}$  that is inferred by model-free methods undergoes a smoother change than the true R. The smoothing has two origins: First, when using the slidingwindow of four or seven days (RKI methods), multiple days are combined to obtain an R value for one day. Second, R has to be calculated from the daily new symptomatic or reported cases (Fig. 2 C, D), because the dates of infection (Fig. 2 B) are not directly accessible in realworld data. As discussed before, symptom onset and reporting date are delayed from the infection date. Because the delays vary from case-to-case, these two curves are smoothed out compared to the infection curve (In other words, the smoothing originates from the variance 318 269 explicitly incorporated in the inference of R, fast changes 321 270 appear slower than they truly are, and successive fast 322 changes may appear as a long transient.

# Model-free methods produce delayed estimates that are difficult to interpret

In our example in Fig. 4, we estimated  $\hat{R}$  based on the 329  $\hat{R} = R^{g_{\rm assumed}/g_{\rm true}}$ . number of new symptomatic cases as produces by our 330 in time compared to the true R (Fig. 4F).

279 come from? To interpret the shift and compare between 334 a reproductive number of 1; assuming e.g. R=1.1 then

 $_{281}$  half of the steep step in R has been detected (gray dots). 282 This shift has multiple contributions. One contribution <sup>283</sup> originates from using the dates of symptom onset, which 284 is shifted on average by the incubation period (in our  $_{285}$  example  $\approx 5$  days). This generates the 4-5 day shift of 286 the one-day method (Fig. 4B). Because the incubation In order to demonstrate potential issues when inferring <sup>287</sup> period is not constant and typically is asymmetric, there the reproductive number R, we systematically compare  $^{288}$  is an additional asymmetric distortion towards either dimodel-free methods and model-based methods on syn- 289 rection, depending on the shape of the actual distribution thetic data from an SIR model (Fig. 2). With model-free 290 of incubation periods. Another source for the shift comes methods, we refer to inference methods for R, which do 291 from the time average, which explains the additional (apnot explicitly incorporate disease dynamics (SIR). The 292 proximate) 1-2 day shift in the four-day and seven-day three methods we presented above belong to this group. 293 methods employed by the RKI (Fig. 4C,D). Because of These methods to estimate R are straight forward and 294 the specific definition of the position of the 4 and 7-day easy to implement. However, they might lead to biased 295 window of the RKI, the two versions of R have a very

Both, the variable incubation time and the time averto the underlying R, (3.) the estimate depends on the 299 aging also impact the start- and end-points of the change assumed generation time, and (4.) around change points 300 in a non-trivial manner. In combination, multiple sources they may return transiently R < 1, even if the true value 301 cause shifts that can point into opposite directions. While was never smaller than 1. While these methods are very 302 the sources can be identified conceptually, the combined

> Due to multiple sources of shifts and smoothing, a  $_{305}$  simple post-hoc shift of the R-curve cannot reproduce the  $_{306}$  true R around a change point. For example, a shift of Fig. 4D by 5 days would suggest a start of the change point before it starts in reality (Fig. 4F). This fact has led to multiple prominent misunderstandings in relation to the RKI data and the effects of governmental interventions. 311 Instead of shifting curves to partially correct for one or another potential delay, an inference of R using model-313 based methods can account for this and other potential 314 biases. When using a good model, such a model-based 315 approach returns the correct R with the correct steepness 316 and time point (Fig. 4E).

# R estimates depend on the assumed generation time.

The assumed generation time g impacts the absolute in incubation period and reporting delay, see later Fig. 10 319 value of the estimated reproductive number R (Fig. 5). in the section about testing). Hence, if smoothing is not 320 We exemplify this effect using the method of the RKI (4 day average), where we vary the assumed generation time g. (Note that the same effect applies to model-based 323 inference.) In a stationary phase with constant R, the case numbers change by a factor R within one generation. Within two generations, they change by the factor  $R^2$ . 326 and so on. Hence, when assuming erroneously double (or 327 half) generation time, then one obtains the square (or 328 square root) of the true R as estimate. More generally,

In the example, we assumed three different generation model. The R of all three model-free methods is shifted 331 times (2, 4, and 8). At the onset, R = 2.56, 332 and  $\hat{R} \simeq 6.5$  for g=8, as expected from theory. In How does one interpret the shift and where does it 333 absolute terms, this dependence is less pronounced near estimating the absolute value of the reproductive number 389 Fig. S4). from observed case numbers without knowing the precise generation time may lead to misestimates.

### Model-free methods may return erroneous transient periods of R < 1 at change points.

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In our examples (Figs. 4 and 5), we consider that  $R_{393}$ 343 changes rapidly from  $R_0 = 3$  to  $R_1 = 1.15$  within one 394 we set out to model the spread of the disease as rapidly as 356

357 due to transient non-linear effects (Fig. 2) or due to a 412 in Bayesian inference. true exponential decay (R < 1). The model-free meth- 413 We also note that all statistical procedures come with 367 non-linear effects if included in the model, e.g., as change 418 granted based on the long-established used of a method 370 one infers R in a model-free manner, by computing ratios 421 the application case may seem subjective sometimes; yet, of case numbers, then the local minimum leads to an 422 similar assumptions are being made, more tacitly perhaps, 372 erroneous estimate of R < 1 (Fig. 4B,C.D).

# Well chosen model-based methods can reconstruct complex disease dynamics

When the chosen model describes the true disease dy-376 namics well, robust inference of the true underlying reproduction number (and other parameters) is possible. To demonstrate the robustness of model-based inference, we 430 generate synthetic data using an SIR-model as inferred from case numbers in Germany between March 2 and April 21 [1] (Fig. 6). The Bayesian model inference can 432 the model-free method, the recovered R is slightly biased  $^{434}$  time point T, given the knowledge available at T (causes <sub>384</sub> (Fig. 6C). Note, however, that the model has to match <sub>435</sub> and data known at T). These results represent something 385 at least approximately the disease dynamics, to allow a 436 that we should be able to agree on given the knowledge at

335 assuming double (or half) the generation time results in 387 assess the robustness of our results in Ref. [1] (SIR: Fig. 3, R = 1.21 (or R = 1.05). This small example shows that 388 SEIR-like: Fig. S3, SIR without weekend modulation:

## WHAT CONCLUSIONS CAN ONE DRAW FROM A BAYESIAN ANALYSIS?

#### A. Modeling background

When the Coronavirus-pandemic arrived in Germany day. Such a sudden change leads to a transient decrease 395 possible. Thus, our model from the start was aimed at givin new case numbers — despite R > 1 always. How 396 ing estimates with their corresponding error bounds based can there be decrease in new cases although R > 1? 397 on the data available at that time. To this end we decided The transient decrease results from the pool of infected 398 to use a Bayesian strategy as it allowed formulating wellsuddenly infecting considerably less people. This decrease 399 documented assumptions on those aspects not available in infections causes the sharp peak and a sudden drop in  $_{400}$  from data at that time. Within the Bayesian framework new infections (Fig. 2B, solid line). It then carries over to 401 these assumptions can and should be replaced by data the number of new symptomatic and new reported cases, 402 as soon as these become available, and we implement with the respective delay and smoothing (Fig. 2C,D]). 403 such an improvement below for the case of information on This transient decrease depends on the duration of the 404 symptom onset times that have become available in the change point: While it is strongest for steep changes, it  $_{405}$  meantime. Given such new data it will also be interesting also occurs for a nine-day change point (Fig. 2, dashed 406 to evaluate post-hoc the assumptions and the performance 407 of our model. This will also give some guidance as to Naively, a transient decrease might be interpreted as 408 whether to employ a model of this kind again in a new scea transient R < 1, but that is not the case here. A 409 nario (another disease outbreak or pandemic) where some model-free method cannot distinguish between different 410 relevant data will also not be available immediately. We causes for transient decreases in case numbers, being it 411 note that taking these steps is the intended development

ods in our example (Figs. 4 and 5) correspondingly yield 414 their own assumptions, e.g. on distribution of the data, non-negligible periods of R < 1, even though the under- 415 models of measurements and random errors. Bayesian lying model dynamics have R > 1 always. Model-based 416 analysis is no exception to this rule; in our view the only approaches, on the other hand, can account for transient 417 difference is that modeling assumptions are not taken for points, and — if the model is correct — even reproduce 419 (say, a t-test) but need to be formulated anew for each the true underlying dynamics (Fig. 4E). To conclude, if 420 case. The fact that the assumptions are hand-tailored to 423 in other frameworks, as well. This said, it is neverthe-424 less important to question and discuss (our) modeling 425 assumptions and to test the sensitivity of our results to 426 the modeling assumptions. As far as space restrictions 427 allowed we have discussed our assumptions already in the 428 main manuscript [1], but we here give a much deeper and 429 broader and more educational treatment.

#### B. Bayesian inference as reasoning under uncertainty, bound to be updated

The results of a Bayesian analysis at some publication recover the reproductive rate (Fig. 6D,F), whereas with 433 time point T represent what we should believe in at that 386 good inference. This is why we used different models to 437 T (and some practical constraints, see below), but these

 $_{439}$   $T + \Delta_T$ . Changing ones mind with the availability of  $_{491}$  therefore often be integrated into noise terms that are 440 additional information is designed into Bayesian inference 492 designed accordingly (as was done with the modeling 441 as "the logic of science" (E.T. Jaynes) from the start. 493 of observation noise in our case, instead of using full 443 models are bound to be updated - just like the relativity 495 done then is to investigate the sensitivity of results with 444 theory and quantum theory in physics overrode their 496 respect to the simplifying assumptions that have been former model counterparts. The important question is 497 made. thus not whether a model is correct in absolute terms, 498 at T comprise those obtained at  $T + \Delta_T$ .

455 model can, and should, be improved accordingly. Impor-507 these credible intervals may form the basis for decisions tant data in this respect are the reliable data on putative 508 we have to take. infection dates which at present take about 7 days to 458 come in for at last 80% of the cases (Fig. 10), and which 459 where only published more recently than our internal 460 analysis cut-off. We present results obtained using these 461 data below and compare them to our published results.

# Conditions for plausible alternative models entering model comparison

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A frequent, and important misunderstanding around Bayesian model comparison is that one is allowed to formulate very many models at random and then let the data decide on the best model via the Bayesian model evidence (or the LOO-scores). This notion fails to notice that the model evidence  $p(D|M_i)$  is only one part of the decision on the preferred model. The formal equation for 471 deciding between models i and j would be:

$$\frac{p(M_i|D)}{p(M_j|D)} = \frac{p(D|M_i)}{p(D|M_j)} \frac{p(M_i)}{p(M_j)} , \qquad (7)$$

477 Rather, each model subjected to a model comparison 532 most plausible model. needs to be well justified. This is one of the reasons why we 533 Later, discussions (such as the one presented here) of 480 drifts in the effective spreading rate  $\lambda^*$  (or, equivalently 535 should then investigate and update modeling assumptions, with plausible explanations for such a behaviour (except 537 or not. perhaps arguments based on herd-immunity, which seem 538 the light of country to country comparisons, Fig. 7).

489 available data, and also computational resources. Known 544 effectiveness of governmental interventions.

438 results may change given more information at a later time 490 phenomena, that can nevertheless not be modeled must In other words, scientific inference and the associated 494 stochastic differential equations). The best that can be

It is also in order to explain in simple terms how results but whether it was possible to agree on the model (and 499 of a Bayesian analysis may be interpreted: In the Bayesian the inference provided by it) at time T, and also if the 500 framework probabilities are measures of the plausibility of inference provided at T was robust, for example in the 501 statements about the world, given our present knowledge. sense that the credible intervals for the model parameters 502 Thus, the results of Bayesian parameter inference for 503 example indicate credible (plausible) ranges in which we From this perspective it is obvious that now, more than 504 should assume the unknown parameters to be. Assuming a month after finalization of our published analyses on 505 them to be elsewhere with high probability would be April 21st, new data have become available and that the 506 inconsistent with the information we have. In this sense,

#### Models as competing causal explanations of data

Last, we note that the notion of causality resides only 512 in the construction of the models – with different models 513 incorporating different possible causal explanations (e.g. 514 in the form of differential equations for the disease dy-515 namics) of the data. Performing model comparisons then 516 selects more plausible over less plausible explanations, but 517 does not provide a proof of causality in the strict sense 518 advocated for example by Judea Pearl [4] or by Ay and <sup>519</sup> Polani [5]. Yet, fulfilling the formal criteria for causality in this strict sense would need multiple replications of 521 the pandemic process, each time with different settings of 522 the relevant variables, such as interventions. Even when 523 treating the SARS-CoV-2 outbreaks in different countries 524 around the world, with their different interventions (or 525 lack thereof), as replications establishiung formal casu-526 ality may remain an elusive goal due to multiple other 472 i.e. taking such a decision entails accounting for a-priori 527 variations from country to country. In sum, the results plausibility of different models, i.e.  $p(M_i)$  and  $p(M_i)$ . 528 of our Bayesian analysis must be seen as a search for While it is customary to assign equal a-priori plausibility 529 the most plausible causal model of the data, given the 475 to all the models being considered, this does not mean that 530 data available at the time of analysis, and as providing just any model qualifies for use in this decision procedure. 531 credible ranges of the parameter values relative to this

did not consider for example models of sustained, constant 534 the selected models and the inferred parameter ranges the reproductive number R), as we did not come up 536 and reason whether the causal model can be maintained,

When analyzing improved data that reflect the dates implausible now, in the light of second waves of infections 539 of symptom onset rather than case reports to improve and a recent rise in  $\lambda^*$  from its all-time low, and also in 540 our modeling we find that both the preference for a three 541 change point model as well as the inferred parameter On a practical note, useful modeling also has to reflect 542 ranges do not change drastically, and we maintain our certain limits on model complexity in relation to the 543 original interpretation of the pandemic process and the

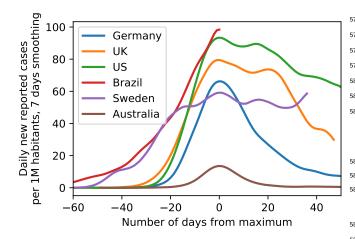


FIG. 7. Comparison of the case numbers per one million inhabitants of exemplary countries as illustration of the range of possible case numbers developments. Note how both the peak height as well as peak width of some countries are considerably larger than for Germany, providing evidence against saturation effects ('herd immunity') in Germany (Data until June 3, 2020).

Last, alternative models assuming herd immunity as a reason for the sustained observed drop in infection rates still do not seem plausible to us in the light of rapidly surging second waves or sustained high levels of new infections (such as in Sweden, see Figure 7).

# MODEL EVOLUTION

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551 folded. While these latter models are useful for a better 612 delay distribution. understanding after the fact, they cannot be applied early 613 to the later ones (here usefulness means that the early 618 are shown). models describe the epidemiological parameters and their  $_{619}$ 

576 (see Fig. 13). In particular, this means that reliable epi curve data for April  $21^{st}$ , our analysis cut-off date in [1], were not available until much later. Now that these data are available, however, we can compare models based on data organized by reporting date, modeling the reporting 581 delay and incubation period, and models based on the 582 epi curve, modeling the incubation period only.

# Model updates based on time of symptom onset and comparison to previous results based on time of reporting

Ideally modeling of an epidemic outbreak should rely 587 on data organized by infection date - yet, such data are 588 rarely available outside of the analysis of individual, wellconfined infection chains. The next best option then are data organized by date of symptom onset - the epi curve. 591 Naturally, symptom onset precedes the test and report in 592 time. Thus, the epi curve is only available after a certain 593 delay, which can be substantial. Furthermore, the time 594 of symptom onset may remain unknown for a significant 595 fraction of reported cases. If so, then reconstructing the 596 epi curve requires data imputation and further modeling 597 (e.g. nowcasting [6, 7]), which may further delay the avail-598 ability of this curve. At the initial stages of an outbreak 599 one may therefore decide to analyze data organized by 600 reporting data. For a comparison of analyses it is impor-601 tant to understand how the curve of reporting dates and 602 the epi curve are linked. Both curves originate from the 603 curve of initial infections by a convolution (see Fig. 2). 604 The epi curve is the curve of initial infections convolved 605 by the distribution of incubation periods, while the curve Modeling efforts at the beginning of an epidemic out- 606 based on reporting date is the curve of true infections break are aimed at providing a rough but timely and 607 convolved by the (less well known) distribution of delays robust description of the disease outbreak, making use 608 between infection data and reporting date. Technically, a of whichever data are available at that time. Later mod- 609 report can happen before symptom onset, albeit this may eling efforts in contrast make use of more detailed data 610 be rare. Therefore, the curve of reporting dates is not and provide deeper insights into how the outbreak un- 611 exactly a convolution of the epi curve with an additional

We have reanalyzed the initial stages of the outbreak on due to a lack of data, and often cannot inform deci- 614 until April 21st based on the epi curve that has become sions fast enough. However, a comparison of early and 615 available (see Figs. 17 and 19), using models with one, two later models can provide important insights about the 616 and three change points, based both on SIR and SEIR robustness and usefulness of the early models with respect 617 dynamics (only figures for the three change points models

These new results do not change our main conclusions uncertainties well enough to inform decisions). For the 620 presented in [1]. Specifically, model comparison still favors case of the COVD-19 outbreak in Germany, the initially 621 the three change point models over their simpler counteravailable data were sorted based on date of reporting, 622 parts (see table I), and only the third change point leads where the reporting occurred after an unknown delay  $_{623}$  to a value of the spreading rate  $\lambda^*$  that is clearly below between symptom onset and report. Only later, data 624 zero. At the quantitative level, however, we see some organized by time of symptom onset, the so-called epi 625 evidence for a larger drop introduced by the first change curve, became available. Even after their initial release, 626 point when using the epi curve data, and smaller drops these data were still updated and refined (see Fig. 8); 627 induced by the second and third change point, especially also note that data for symptom onsets still take some 628 when using an SEIR model (see Fig. 19). These quantitatime to arrive and be compiled, i.e. the delay between 629 tive changes are driven by the epi curve dropping faster 575 symptom onset and testing/reporting is still considerable 630 than the curve reflecting reporting date (see Fig. 9C).

TABLE I. Model comparison: Using leave-one-out (LOO) cross-validation, we compare the SIR and SEIR model variants using the epi curve as data (Figs. 17 and 19). Lower LOO-scores represent a better match between model and data (pLOO is the effective number of parameters).

Model	# c-pts.	LOO-score	pLOO
SIR main	0	$900 \pm 13$	6.36
SIR main	1	$774 \pm 14$	12.72
SIR main	2	$755 \pm 13$	12.17
SIR main	3	$725 \pm 15$	19.66
SEIR-like	0	$900 \pm 14$	6.65
SEIR-like	1	$749 \pm 12$	8.05
SEIR-like	2	$739 \pm 13$	10.28
$\operatorname{SEIR}$ -like	3	$726 \pm 14$	14.04

In sum, we conclude that the original model based on data organized by reporting date was useful to understand 633 disease dynamics in the absence of the epi curve and robust in the sense that its main results still hold.

#### Differences between results based on RKI versus JHU data sources

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At the beginning of the out break data were made avail-638 able on a daily basis both by John Hopkins University (JHU) and the German Robert Koch Institute (RKI). Both sources initially provided only reported cases, with the JHU resources providing data faster and with a better interface for automated analyses. The RKI resources were updated only a few days later, as information always has to be transmitted from regional agencies to the RKI, whereas the JHU data for Germany are gathered from a few reputed online media (Berliner Morgenpost, Taggesspiegel and Zeit Online [8]). However the JHU resources have been partially criticised for lacking quality control (see issues section on the Github page [9]). We therefore compared the JHU data used in [1] to the official 651 RKI count (Fig. 14) and have rerun the analysis using 652 the RKI reported cases (the "Meldedatum", Fig. 15 and 653 16). The differences are minor.

# IMPACT OF TESTING

Our modeling depends on reported case numbers, which 656 in turn depend on testing. Throughout the COVID-19 690 the number of tests is increased and we find a constant 657 spread, test availability, test requirements and known case 691 fraction of positive tests, this implies the same, an increase 658 numbers changed continuously over time, see Fig. 8. Such 692 of underlying cases. The second case only holds with decided to exclude the effects of testing in previous mod- 695 randomly, both of which were met in Germany. els, concerns about results derived from data that stem from inconsistent testing should be taken seriously. Thus, 696 we analyze possible distortions in more detail. As we 697 the number of tests as well as the fraction of positives 665 will demonstrate below, our major conclusions remain 698 increased simultaneously. This simultaneous increase in-666 unchanged.



FIG. 8. The numbers of known onsets of symptoms per day as reported at different dates in the past. As testing confirms onset of symptoms in the past with varying delay, the epi curve not only grows at its tail, but over a wide time period with each new publication. Known onsets are reproduced from the RKI's daily situation reports and the publicly available RKI-database. Unknown onsets of symptoms, which account for 40% of total number of cases, are not considered. The estimated total epi curves from the RKI (imputation and Nowcasting), as reported on a past date, are not publicly available for the month of April, hence the focus on the numbers of known onsets here.

Please also note that at the time of writing of the initial 668 manuscript, only very preliminary data and statistics on testing was available. Now, with better data, we come to the conclusion that reported case numbers, although they might derive from variable testing, are still useful to infer 672 the actual disease dynamics.

In particular, evidence for the key characteristics of the 674 first wave, i.e. strong exponential growth in new cases, 675 change in transmission dynamics over a limited time pe-676 riod and slow exponential decline, can be derived from 677 the available data, even if changes in testing are taken 678 into account.

We start our analysis by considering two central 680 quantities: i) the number of tests that are performed, say, 681 on a given day or in a given week and ii) the fraction of 682 the performed tests that are positive — a positive tests 683 translates to a confirmed case.

Let us consider two simple limiting cases, in which only one of these quantities changes, whereas the other one 686 remains constant. In the case that a constant number of 687 tests is performed day-over-day and we observe a growing 688 fraction of positive test results, this corresponds to an 689 increase of the underlying case numbers. Conversely, if an inconsistent and fluctuating data-acquisition obviously 693 additional assumptions: i) the fraction of positive tests is introduces additional sources of uncertainty. While we 694 larger than the prevalence and ii) tests are not performed

> Fig. 9 A,B shows that in Germany in early March both, 699 dicates a significant growth in new case numbers.

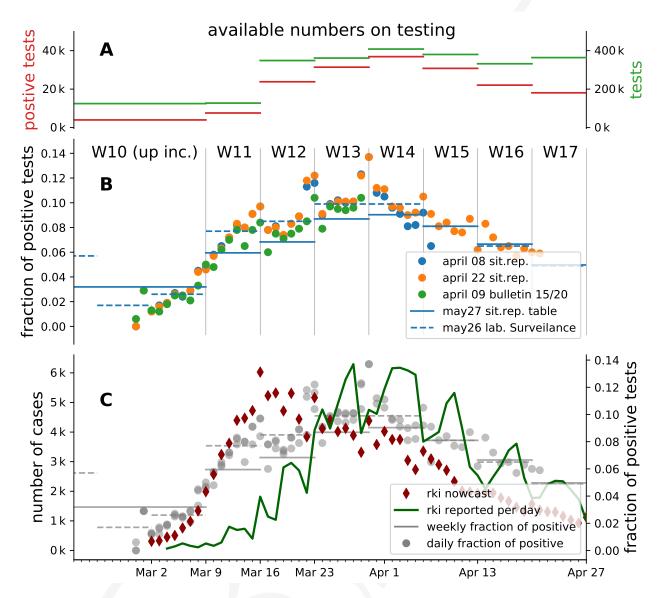


FIG. 9. The evolution of the fraction of positive tests in weeks 10 to 17. Weeks 10 to 12 strong exponential growth in in the number of new cases, which was not limited by the early testing capacity. A Comparison of number of positive test results with the number of tests performed for each week. Reproduced from Table 5 in [10]. Note: Numbers for week 10 and earlier are represented by a single data point. B Mid-term changes in the fraction of positive tests is more obvious in the daily data (points) than in the weekly (bars), especially in early March. Daily values are taken from situation reports [10-12] (full dataset) and the epi bulletin [13, 14] (ARS dataset). Weekly values, represented as horizontal lines, are taken from a situation report table and a weekly lab surveillance report (ARS dataset). Note: the latter represents a subset of all tests. Compared to the situation report, the ARS dataset lists weeks 8 to 10 individually. C Overlay of Panel 2 with the number of cases reported per day by the RKI and the estimated epi curve (imputation and Nowcasting, as described in [7]). The fraction of positive tests correlates with the number of reported cases from week 13 onward, as the total number of tests reaches a constant level.

#### Strong growth until week 12

706 of positive tests is apparent in the daily values, especially 715 For a better understanding of the following part of

707 as the daily number of tests can be taken as constant 708 throughout the week, see Fig. 8 in [10]. For weeks 14 709 onward, the number of performed tests stays constant Focusing on testing in weeks 10 & 11 in Fig. 9 A and B, 710 and thus, the fraction of positive tests correlates with we can clearly deduce a strong growth in daily new cases, 711 the number of reported cases, exhibiting a decline in as both the fraction of positives as well as the number 712 underlying case numbers. A similar direct comparison of performed tests rise, matching the combination of the 713 for weeks 10-12 is unfortunately not that simple, as the two scenarios described earlier. The rise in the fraction 714 number of tests changed week-to-week in that time period. 716 the analysis, we recall an important fact on exponential growth: In each doubling period the same number of new infections occurs as in all preceding periods combined. As the number of tests approximately doubles every week until week 12 and the fraction of positive tests increases to week 13, the doubling period of new infections has to be shorter than 1 week. In a time frame of less than a week, more new infections occur than in the period since the onset of the outbreak. If we assume constant testing over the span of one week, a difference in the fraction of positive tests on each day during that week should be observable, and this is indeed what we see for testing in weeks 10 and 11 and to a lesser extent from start to end of week 12 (Fig. 9 B). A more in depth analysis of Fig. 9 is attached in Sec. VD. The important questions that remain are: When did the number of new infections peak? And when did it start to decline?

Deferring the first question to Sec. VB, we answer the second: From week 14 on, there is an approximately constant high level of testing, but a decline in the number of cases reported, and an accompanying day-to-day decrease in the fraction of positive test results. These observations are consistent with an exponential decline in the number of new infections, confirming that testing can properly measure the underlying epidemiological dynamics in this period.

Summing up the above analysis so far, we have indications that during the epidemic outbreak, a growth in case numbers was indeed present, as well as a decline.

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Hypothetical Scenario: If we were to reject the 746 above simple explanation that growing case numbers reflect growing numbers of infections, there is one alternative scenario to explain the observed trend, which we, however, deem highly implausible. As this scenario has frequently occurred in the public debate on the spread of COVID-19 in Germany, we discuss it briefly. The underlying assumption in this scenario is that the few tests that were performed during the initial outbreak until week 11 missed most of the actual cases, i.e. a large pool of infected persons would have existed unobserved. Then, at the same time at which the amount of tests was increased from weeks 11 to 12, coincidentally the effectiveness of the testing could have increased, so that the unobserved pool (of constant size!) is identified and, thus, apparent case numbers rise. Given the rigorous criteria (based on symptoms and risk of exposition) that were required from patients in order to qualify for one of the early tests, we deem this scenario of an unobserved and constant pool to be quite unlikely. Especially so because the fraction of 765 positive tests stayed below 10% during the entire time.

# Locating the peak position

770 simultaneous increase in tests and fraction of positive 801 a delta-peak at three days. However, we see that most

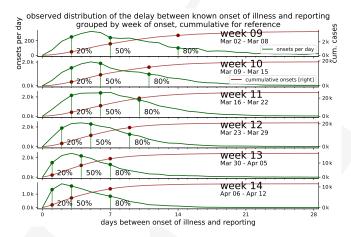


FIG. 10. The onsets of symptoms are confirmed by testing at later point in time, which accounts for most of the delay till all or the main fraction of known onset of symptoms (IstErkrankungsbeginn in RKI-database) are reported. From the RKI data, the number of cases per delay between onset of illness and reporting (i.e. RefDatum and Meldedatum) for cases with known onset of symptoms (IstErkrankungsbeginn) are counted for each week. The fraction of reported cases out of the total onsets up to a delay are highlighted for 20%, 50% and 80%. The cumulative number of cases reported up to each delay is displayed for reference.

tests to occur no earlier than week 11, as the peak would 772 indicate the end of the growth. In this section we're 773 focusing on how it can be reliably identified from the 574 stable period of testing: From week 12 and onward, the 775 number of tests remained on an almost constant, high  $_{776}$  level  $\sim 400$ k and changes in the daily new cases reported are directly reflected by the fraction of positive tests.

To understand this in more detail, we introduce the 779 following important rule of thumb here: Tests of week i780 describe well what happened in week i-1.

The key is the connection between the date of symptoms 782 onset (when symptoms first show), the testing (when the 783 symptom onset is confirmed or an asymptomatic case 784 is uncovered), and the reporting date (when a positive 785 test-result is registered).

Any reported case must inherently be preceded by 787 a test and according to the RKI, positive test results 788 are reported within 24 hours to the responsible health 789 department. The remaining task then is to reveal the 790 connection between symptom onset and reporting date, 791 i.e. the reporting delay for each individual case. The date 792 of testing is taken as the day before reporting in the rest 793 of the analysis, the testing delay is one day shorter than 794 the reporting delay.

In Fig. 10 we detail the reporting delay by plotting 796 distributions of how many days after the symptom onset 797 a case is reported. For example, if each and every infected In other words, we are interested in the peak position 798 person would receive a test result (become a reported in the curve of onsets of symptoms, see again Fig. 9, C, 799 case) exactly three days after they showed symptoms, red. The day of the peak is constrained by the initial \*\*\* then the plotted distributions would have only one entry:

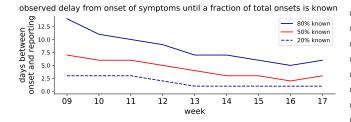


FIG. 11. Overview of the delay between onset of symptoms and the reporting of a fraction of total known onsets for a day changes with time. The 50% fraction represents the median Derived from Fig. 10

802 reports arrive 1–7 days after symptom onset, where the details of the (lognormal) distribution depend on the week of onset of symptoms. Until and including week 805 12, the distributions have heavy tails. After week 12, the distributions have lighter tails. This provides some intuition of the distributions and the meaning of the heavy tails: most of the symptom onsets are reported within the first week but *some* will be reported much later, so that shape of the distribution still keeps changing. If the test level is low, more cases will be reported later and the tails of the distribution are heavier. This is latter effect is what we see for the onsets during the first weeks until 11; due to limited testing capacities, many cases 815 are only reported weeks later — when more testing was 816 available. To rephrase based on Fig. 11: Half of the onsets of symptoms in week 11 are reported within 5 days, 80% within 9 days. The crucial example here is: Half the onsets on Wednesday get tested until Sunday, the other half in the following weeks for every following day of the week the fraction of test performed in the next week rises. Without explicitly working out the details, it's fair to declare the initial rule of thumb valid. A more thorough analysis based on actual per case testing-delays instead of reporting delay distributions is conducted in Sec. VC. Let's turn back to Fig. 11 A. The onsets in week 11, 827 the estimated position of the peak, should be robustly measured by the testing in week 12, with a high number of total tests. From Fig. 11 C, we can see, that the number 830 of onsets of illness peak at the end of week 11 or the beginning of week 12. This time point doesn't suffer from

#### Decomposing the epi curve into weeks of testing

832 lower testing numbers in week 11.

841 In more detail, for all the cases within a chosen test- 899 in week 11 amplifies this observation. Weeks 13 onward

842 ing period, we also know the respective date of onset of 843 symptoms, for complete datasets. Borrowing from [7], 844 the remaining 40% of test dates can be imputed from the known onsets dataset. In Fig. 12 A,B we apply this 846 method to collect all the symptom onsets that were found by testing in weeks 12 and 13. Through this allocation of 848 "which part of the curve stems from which tests", we can 849 thoroughly justify the connection that we made above, 850 when we said that growth in weeks 11 and 12 stems from the tests in week 12 and 13. As we see, the peak on March 16 stems almost completely from tests of week 12 and reporting delay between onsets of symptoms and reporting. 853 13; these weeks already featured the high level of tests 854 performed. Based on the decomposition, we can conclude 855 that in week 11, every day could have been identified as 856 the peak based on testing in weeks 12 and 13.

We can extend this method in an attempt to reduce 858 the influence of changing number of tests per week on 859 the estimation of the change in the number of onsets of 860 symptoms from one week to the next. We compare the 861 number of onsets in different weeks, that were confirmed by one week of testing. Think: distribution of onsets per week seen by the testing in one single week. Some cases 864 with onset of symptoms on Monday will receive their 865 positive result within the same week as the symptom 866 onset itself, others get tested further away from their 867 onset of symptoms. As viewed from one single week of testing, we distinguish 4 categories: onsets 3 weeks, 2 869 weeks and 1 week earlier than the test and onset in the 870 same week as testing. The number of onsets in each 871 of the 4 categories compared with the total number of 872 onsets confirmed in the week of testing, the fraction per 873 category, is characteristic for the epidemiological dynamic 874 in the time span of those four weeks. This method is 875 more robust to changes in the number of tests week-over-876 week, than the other methods outlined so far. In Fig. 13 877 three different scenarios are considered and their effect 878 on the fraction of cases in each week-category is worked 879 out. All three scenarios show distinctive combination 880 of fractions per week-category. Comparing the artificial 881 result with Fig. 12 C, we find that in week 11 most of the \*\*2 tests (52%) found symptom onsets within the same week. <sup>883</sup> This indicates weeks 10 and 9 had significantly less new 884 onsets of illness. This is consistent with the exponential 885 growth uncovered in sec. VA. In the extreme case that no 886 tests were performed in week 10 and we were to observer 887 that the number of onsets in week 10 were comparable or 888 higher than in week 11, the backlog from week 10 would 889 lead to higher fraction of 1-week-earlier onsets than same 890 week onsets, for testing in week 11. As the fraction of 891 1-week-earlier onsets is lower than same-week for testing Having established the delay between symptom onset 892 in week 11, we can see that the assumption, no tests and reporting, we can decompose the epi curve and iden- 893 and highter number of cases in week 10, cannot be valid. tify parts of the curve that stem from certain weeks of 894 Reaffirming the observation of growth from week 10 to testing. Fortunately the publicly available RKI database 895 week 11. Testing in week 12 shows a significant peak for contains both onsets and reporting for individual cases 896 onsets 1 week earlier. That indicates the number of new 839 for 60% of the total cases and thus also the date of test-897 onsets is comparable in week 11 and week 12 (see artificial 840 ing, which in general is one day earlier than the report. 898 result, Fig. 12). Note, that a lower total number of tests

# decomposition of the epicurve into weeks of testing

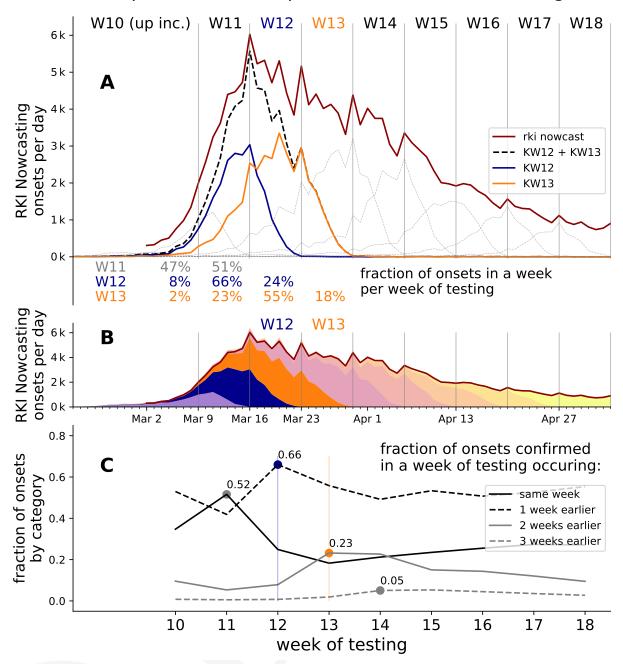
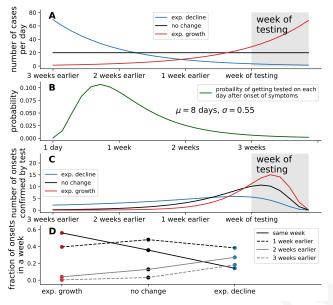


FIG. 12. Testing in one week confirms onsets of symptoms that occur up to 4 weeks earlier. The extend of this effect is analyzed based on the RKI database through decomposition by allocation of onsets of symptoms to weeks of testing. It is assumed that the delay between the time of testing and *Meldedatum* is 1 day. Tue-Mon *Meldedatum* is taken as a proxy for Mon-Sun testing. A Onsets of symptoms per day curves allocated to weeks of testing, weeks 12 and 13 are highlighted. Most known onsets around the peak of the epi curve in week 11 are confirmed by the testing in weeks 12 and 13. B stacked decomposition of the epi curve into weeks of testing. C To reveal crucial information about week-to-week change in the number of total onsets based on one week of testing, the shape of the distributions of onsets of symptoms confirmed by that week of testing is characterized. The fraction of onsets in the same week and each preceding week out of the total onsets confirmed by the week of testing is calculated. This indicates, the portion of a week's positive tests confirming onsets in the same week or in preceding weeks (max. 3 weeks earlier). The evolution of these 4 values is plotted by the week of testing. The peak of the epi curve can be tracked through testing results of weeks 11 to 14 as a maximum in the same-week/n-weeks earlier fraction of onsets confirmed in those respective weeks: 52% of all cases confirmed through testing in week 11 had onset of symptoms in the same week. Even more notable: 66% of positive tests in week 12 are linked to onsets 1 week earlier: in week 11. For comparison, see Fig. 12

900 show distributions which indicate decline in onsets week 912 weeks, the alleged period of the peak in new onsets of 902 their fraction of same-week onsets is smaller than 30%.

#### impact of evolution of cases on the shape of the distribution of onsets of symtoms confirmed in a week of testing



Changes in the number of onsets of symptoms from one week to the next can be estimated from the distribution of onsets of symptoms confirmed by testing in the latter week, if we group those onsets by week of onset. A Three 937 different scenarios for the evolution of the number of cases 938 are considered, whereby the number of onsets of symptoms 939 per day is plotted. B Each case from A has a probability to  $_{940}$ be tested on every day. Half of the cases get tested within 8 days. The distribution is derived from observed data. C Number of onsets confirmed by the week of testing for each day of onset of symptoms. As a result of A and B. The shape of the distribution is characteristic for the change in cases and can be compared with Fig. 12, B. D As a last step the onsets confirmed by the testing in the highlighted week are summed up by week of onset and the group's respective fraction of the total number of positive tests in the highlighted week is computed. If no change in the number of cases occurs, more onsets in the week preceding testing are confirmed (45% of total) than from the same week as testing (35% of total). In case the number of cases rises, onsets from the same week as testing constitute the majority of onsets confirmed by tests in the week. If the number of cases declines, old onsets (older than 1 week) take over a significant fraction of total onsets tested in the week.

In Summary: Even though the number of total tests performed changed until week 12, the available data indicates strong exponential growth in new onsets of symptoms into week 11, constraining the peak in new onsets of illness to no earlier than March 9. The declining phase of the wave is well documented. The exponential decline in cases from week 13 onward is measured with consistent 910 high level in the number of tests. As testing in one week is 911 shown to uncover onsets of symptoms in the 3 preceding 962

over week, their 2 weeks earlier fractions are larger, while 913 symptoms in week 11 is covered by robust testing from 914 weeks 12 and 13. Based on testing in weeks 12-13, the 915 peak can be identified at the end of week 11 or beginning 916 of week 12.

#### Available data on testing

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The epi bulletin [15] outlines the different networks that the RKI uses to source information on testing: Voxco, Resp Vir, the antibiotics-resistance-surveillance (ARS) [14] and lab-accociation queries. These sources are compiled into weekly data-sets with total number of tests and positive tests, which are published in the daily situation report once a week.

925 Data from the ARS contains daily number on testing and 926 a separate weekly report is published on the RKI website. The ARS dataset covers 25-30% of the total number of tests reported by the RKI, as only 62 of 180+ labs participate. The ARS data-set shows a mean delay between sampling and testing between 1 and 1.2 days except for 931 weeks 12 to 15, where the delay is 1.5 days, peaking in 932 week 13 at 1.8 days.

933 An overview of all publicly available data on testing for 934 march 2020 is presented in Fig 9. The following observations along with additional comments are based on this presentation:

- From week 8 to week 12 the number of tests rises week to week by a factor greater than 2. 120k is a combined number for weeks up to 10. Individual numbers of tests for those weeks has to be estimated with help from the ARS-subset (Fig. 9 B may26 lab. Surveilance). Assuming ARS is representative the number of test performed in week 10 should be around 60k, 30k in week 9 and 30k in all weeks up to and including 8, extending the exponential pattern.
- The number of tests remains on a high level from week 12 on. In the range of 340-430k.
- The number of positive test rises faster than the total number of tests until week 14.
- The fraction of positive tests per week peaks around 10%, relatively low compared with neighbouring countries.
- The fraction of positive tests per day varies with time from 2% around March 1 to around 10% in weeks 13 and 14, peaking at 14% at the end of March. Afterwards declining to less than 2% in week 20 (not shown in figure). The day-to-day rise in week 10 and 11 is more pronounced than the weekly average would suggest.
- The increase in the fraction of positive tests does not correlate to the rise in number of reported cases

as the total number of tests fluctuates around 380k 1000 rate. tests per week on a high level. The correlation with 1001 the epi-curve is coincidental.

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- of positive results than week 9.

individual states exceeded 20% positive results.

#### VI. SUMMARY & CONCLUSIONS

dressed questions and comments regarding our recent 1029 Most importantly, we find that while data from the initial publication [1]. First, we compared direct, model-free es-1030 onset of the pandemic is presumably affected by a rise in timates of the reproduction number to the ones obtained 1031 test capacities, the crucial part of our analysis is based from dynamical modeling. To this end, we established 1032 on a regime of comparably stable testing. In particular, synthetic ground-truth data based on an SIR model and 1033 we find that the inference of the second and third change subsequently inferred the reproduction number based on 1034 point is unaffected by testing. various complementary approaches that are in practical 1035 use. We reveal how sudden changes in the spreading 1036 our previously reported results with respect to statistical rate, as expected from the broad implementation of non-1037 and dynamical modeling assumptions as well as complepharmaceutical interventions, can lead to counterintuitive 1038 mentary data sources and provides additional support for transient drops in new reported cases. Most importantly, 1039 the central conclusions of our publication [1].

until week 13, but correlates with the decline in 998 we find that only modeling of spreading dynamics can correported cases from week 13 on, which is expected 999 rectly capture effects of sudden changes in the spreading

Second, we provided extensive background on our mod-1002 eling rationale which combines differential-equation based 1003 modeling of dynamics with Bayesian parameter infer-The ARS data shows a steady day to day increase in 1004 ence and formal model comparison. Within the Bayesian positive fraction of test in weeks 10 and 11. Week-1005 framework, we argue that based on prior knowledge, the ends show a higher fraction, while the total number 1006 most plausible models explaining the data can be systemof tests is lower (daily total number not shown in 1007 atically identified and also updated as new information the figure). Deviating from the rise in the positive 1008 becomes available. We also discuss why we do not think fraction, weeks up to 8 have a 3 times higher fraction 1009 that models based on herd immunity are plausible given 1010 our present knowledge.

Third, we analyzed additional data on the COVID-19 • The maximum test-capacity per week as reported by 1012 spread in Germany, which has become available since the labs increased to 1M in week 19, showing strong 1013 the completion of the analysis presented in [1]. Most growth till week 14. A week to week doubling in test 1014 importantly, we include data sets from the German Robert capacity continues for two more weeks compared to  $^{1015}$  Koch Institute based on the reporting date as well as based growth in number of tests performed (not shown). 1016 on the onset of symptoms (epi curve). We analyzed the 1017 data in the framework of SIR and SEIR models, and we Additional information relevant to the discussion can be 1018 also tested a broad range of varying prior assumptions. found in the publications cited earlier. For the total 1019 We find our results to be robust across these varying data-set, the fraction of positive tests varies from 1.5 to  $^{1020}$  modeling assumptions and data sets, and to support the 7.2% for different states. Not a single day of testing for  $^{1021}$  conclusions drawn in [1]. In turn, this leads us to conclude 1022 that under the conditions comparable to those in Germany, 1023 models based on reporting date are a viable alternative for analyzing the early stages of a disease outbreak, before the epi curve becomes available — as long as the reporting delay is properly modeled.

Finally, we address the issue of changes in the testing In these technical notes, we have comprehensively ad-1028 capacities and procedures over the course of our analysis.

Overall, the analysis here evaluates the robustness of

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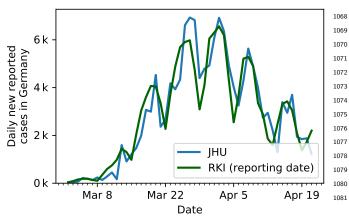


FIG. 14. Comparison of the German case numbers as published by the John Hopkins University (JHU) used in our  $_{1082}$  previous publication [1], to the case number of the Robert  $_{1083}$  Koch Institute (RKI). The difference is limited.

- 1068 [10] Täglicher Lagebericht des RKI zur Coronavirus-1069 Krankheit-2019 2020-05-27, 2020.
- 1070 [11] Täglicher Lagebericht des RKI zur Coronavirus 1071 Krankheit-2019 2020-04-22, 2020.
- 1072 [12] Täglicher Lagebericht des RKI zur Coronavirus-1073 Krankheit-2019 2020-05-22, 2020.
- 1074 [13] A. Hoffmann, I. Noll, N. Willrich, A. Reuss, M. Feig, M.J.
   1075 Schneider, T. Eckmanns, O. Hamouda, and M. Abu Sin.
   1076 Laborbasierte Surveillance SARS-CoV-2. Epid. Bull.,
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- 1078 [14] SARS-CoV2-Surveillance Wochenbericht vom 26.05.2020, 2020.
- 1080 [15] J. Seifried and O. Hamouda. Erfassung der SARS-CoV-2
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# VII. SUPPLEMENTARY INFORMATION: FIGURES

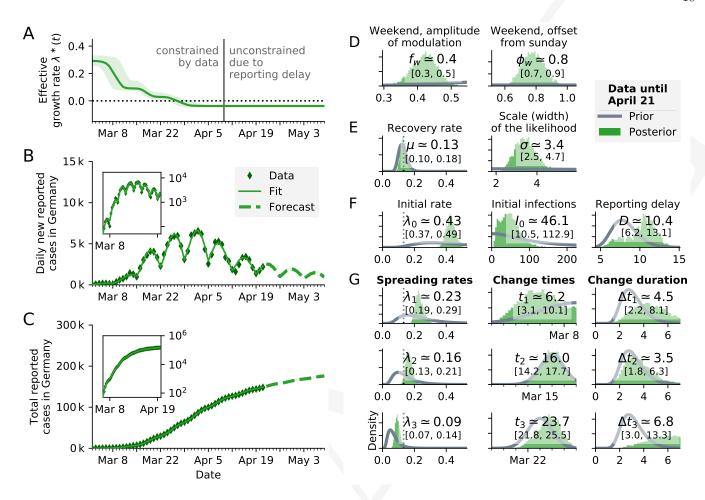


FIG. 15. SIR model (see Fig. 3 of [1]) using the reporting date (Meldedatum) of the RKI data for inference. A Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C: Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

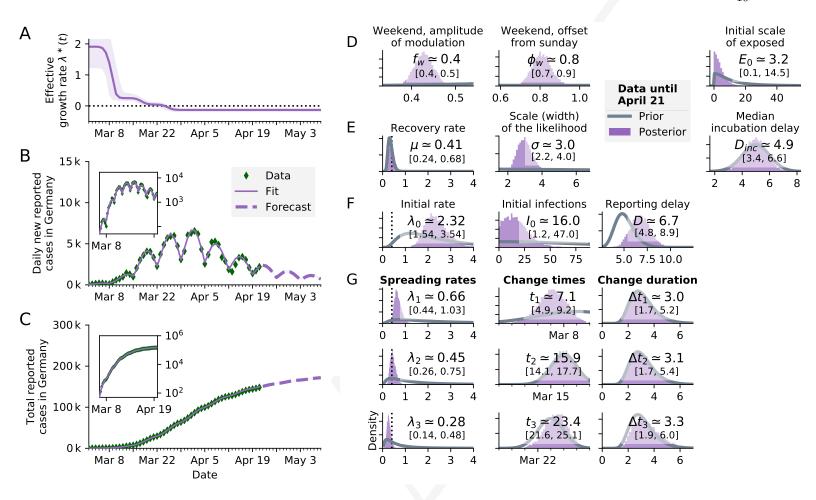


FIG. 16. SEIR-like model (see Fig. S3 in Supplementary Information of [1]) using the reporting date (Meldedatum) of the RKI data for inference. A Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . B Comparison of daily new reported cases and the model (purple solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D-G Priors (gray lines) and posteriors (purple histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

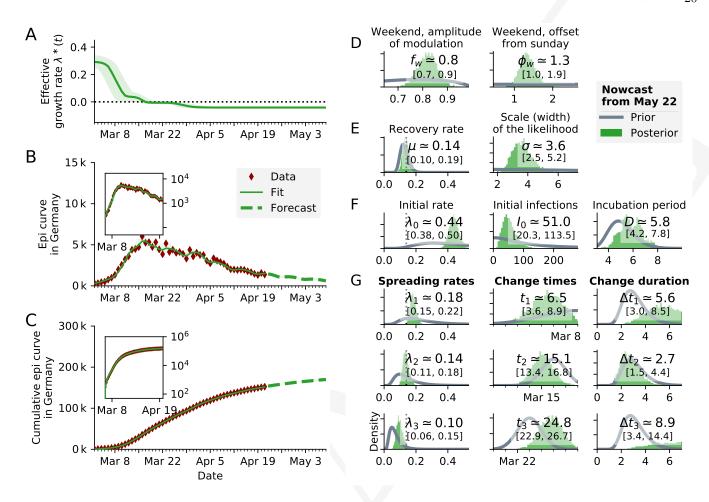


FIG. 17. SIR model using the onset of symptoms (nowcast from May 22) of the RKI data for inference. The median of the lognormal prior of the delay between infection and onset of symptoms has been set to 5 days (right-most panel F). A Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset: same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

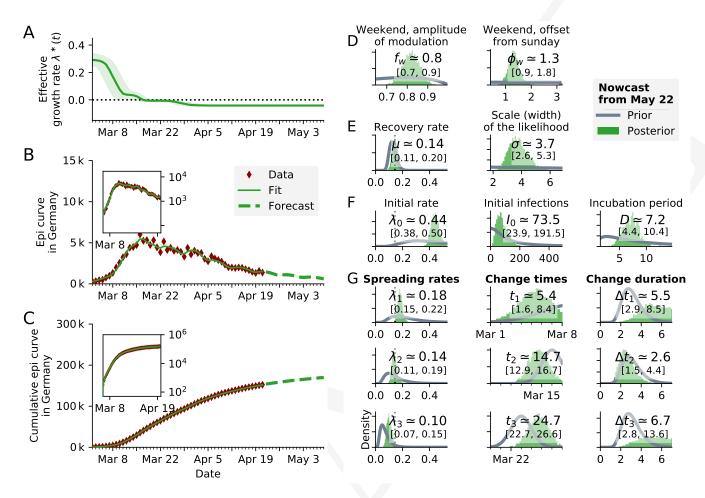


FIG. 18. SIR model using the onset of symptoms (nowcast from May 22) of the RKI data for inference. The median of the lognormal prior of the delay between infection and onset of symptoms has been set to a relatively uninformative prior (right-most panel F). The posterior of the delay has as median 7.2 days, which is close to the expected incubation period of 5 days. A Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

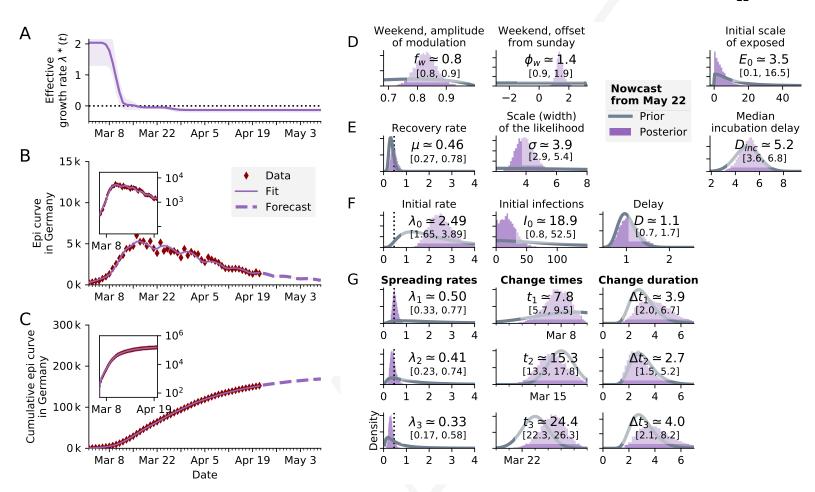


FIG. 19. **SEIR-like model using the onset of symptoms** (nowcast from May 22) of the RKI data for inference. The median of the lognormal prior of the delay between infectious and onset of symptoms has been set to 1 day (right-most panel F). **A** Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . **B** Comparison of daily new reported cases and the model (purple solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); **inset** same data in log-lin scale. **C** Comparison of total reported cases and the model (same representation as in B). **D**–**G** Priors (gray lines) and posteriors (purple histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

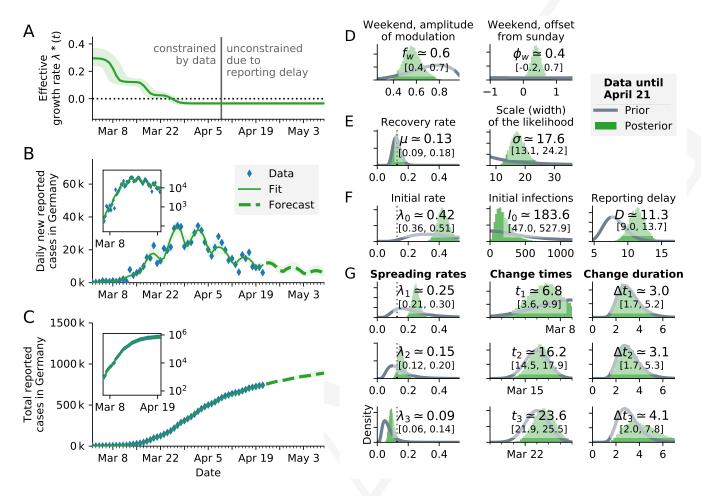


FIG. 20. SIR model with reported case number multiplied by 5, to account for an eventual factor five of unknown cases. Results are nearly identical to original non-multiplied plot (Fig 3. in [1]), showing that a constant underreporting has a negligible effect. The median inferred spreading rates  $\lambda$  are about 0.01 larger. A Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

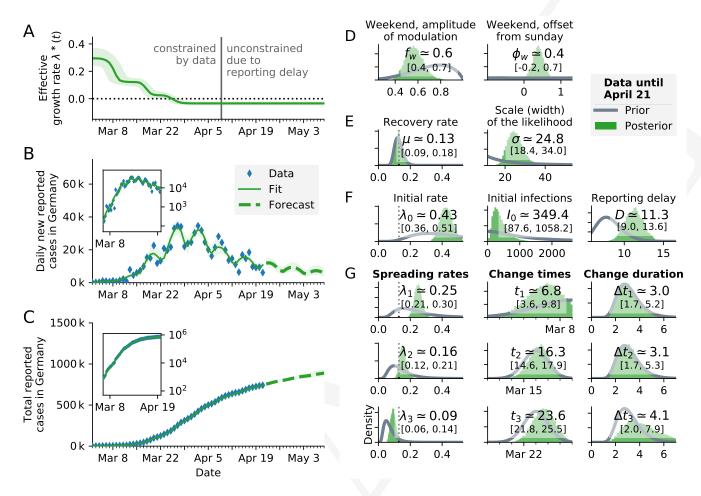


FIG. 21. SIR model with reported case number multiplied by 10, to account for an eventual factor 10 of unknown cases. Results are nearly identical to original non-multiplied plot (Fig 3. in [1]), showing that a constant under-reporting has a negligible effect, similar to Fig. 20. The median inferred spreading rates  $\lambda$  are 0.01-0.02 larger. A Time-dependent model estimate of the effective spreading rate  $\lambda^*(t)$ . B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.