Model-based and model-free characterization of epidemic outbreaks — Technical notes on Dehning et al., Science, 2020

Jonas Dehning ¹ , F. Paul Spitzner ¹ , Matthias Linden ² , Sebastian B. Mohr ^{1,3} , Joao Pinheiro
Neto ¹ , Johannes Zierenberg ¹ , Michael Wibral ⁴ , Michael Wilczek ^{1,5} , and Viola Priesemann ^{1,5,6}
¹ Max Planck Institute for Dynamics and Self-Organization, Am Fassberg 17, 37077 Göttingen.
² Institute for Theoretical Physics, Leibniz University, 30167 Hannover, Germany.
³ Institute for Theoretical Physics, University Leipzig, Postfach 100 920, 04009 Leipzig, Germany.
⁴ Campus Institute for Dynamics of Biological Networks, University of Göttingen,
Hermann-Rein-Straße 3, 37075 Göttingen, Germany.
for the Dynamics of Complex Systems, University of Göttingen Friedrich-Hund-Platz 1, 37077 Göttingen

⁵ Institute for the Dynamics of Complex Systems, University of Göttingen, Friedrich-Hund-Platz 1, 37077 Göttingen, Germany.

⁶ Bernstein Center for Computational Neuroscience, Hermann-Rein-Str. 3, 37075 Göttingen, Germany.

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In this technical note, we provide additional background on our Bayesian inference for change-point detection in COVID-19 case numbers (Dehning et al., Science, 2020). In particular, we explore basic properties of model-based and model-free estimates of the reproduction number, discuss what conclusions can be drawn from Bayesian analyses, further develop our model and apply it to newly available data, and discuss potential issues with changes in testing policies.

This technical note presents work in progress and should be considered like an internal draft. It is not ready for submission yet, and is being frequently updated.

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28 29 30 31	transient periods of $R < 1$ at change points. 5. Well chosen model-based methods can reconstruct complex disease dynamics III. What conclusions can one draw from a Bayesian	7	59 60 61	58 change points in the spread of COVID-19 reveals the effec- 59 tiveness of interventions" in Science [1], we have received 60 many constructive comments and interesting questions, 61 and have also faced some recurring misunderstandings.			
analysis? A. Modeling background B. Bayesian inference as reasoning under uncertainty, bound to be updated	7 7 8	63 64 65	This technical note is intended to answer the most impor- tant of these questions, to give additional background for understanding our results, and to also discuss the robust- ness and performance of our model in the light of newly available data, in particular data based on on symptom				
37 38 39 40	entering model comparison 8 D. Models as competing causal explanations of		67 68	The inspiration and comments we received can b broadly categorized into four topics:			
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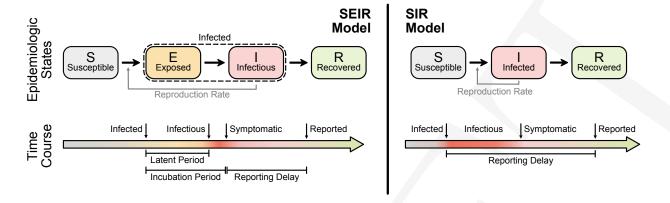


FIG. 1. Illustration of two basic compartmental models in epidemiology. The SEIR model (left) captures the basic steps that infections passes through: A healthy person becomes infected (leaves S, enters E) but not infectious; after some time ('latent period') the person becomes infectious (leaves E, enters I) but symptoms only show after some incubation period; after some time the person is no longer infectious (leaves I, enters R), which can have several reasons including isolation, conventional recovery, or death. The SIR model (right) is the most basic compartmental model and does not distinguish between infectious and infected: A healthy person becomes infected (leaves S, enters I) and by this begins to infect other persons, but only shows symptoms with some delay; after some time the person "recovers" (leaves I, enters R), which again includes isolation, recovery, or death.

apparent discrepancy arises from the comparison 108 of model-free estimates to those from a differential- 109 equation based modeling of disease dynamics. We 110 show how the model-free approach may substan- 111 tially underestimate the reproductive number R 112 immediately after a sudden drop in R has occurred. 113 From the comments we received it seems that this 114 very important fact related to estimating R is largely 115 unknown, and also counter-intuitive to most readers. 116 This effect, however, fully explains the apparent discrepancies between the RKI reports and our study. 117 here.

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- tion. As we will explain below, our approach selects 127 question of testing. the most plausible of multiple causal explanations of the observed data, but does not establish strict interventional causality.
- 3. New data have been released in the time since our analyses were completed. Most prominently, data on the exact times of symptom onsets (epi curve) are now available and supersede the case report data as the best data source for modeling the outbreak. 131

of performed tests, test capacity, and on delays between symptom onset, test and case report, we reanalyze in great detail the disease and testing dynamics, especially with respect to the timing of the peak in new symptom onsets. We conclude that all symptom onsets that are relevant for the main conclusions of our previous publication have been tested at a time when testing had sufficient capacity and was sufficiently constant.

We will in the following address the issues revolving We therefore derive and demonstrate it in detail 118 around the reproductive number R first, also introducing the basic terminology of disease spreading and the 120 fundamental difference between model-free and model-2. Questions revolving around the philosophy and inter- 121 based estimation of epidemiological parameters. Next, we pretation of our modeling approach that combines a 122 will discuss philosophy and interpretation of model-based differential equation model of the disease outbreak, 123 estimation in the Bayesian framework and the causality Bayesian parameter inference and Bayesian model 124 question. We then show how our original analyses can be comparison. Most frequently we were asked if and 125 evolved to incorporate new data, in particular on sympin what sense our results have a causal interpreta- 126 tom onset (epi curve). Last we turn to the important

ESTIMATING THE REPRODUCTIVE NUMBER

Basic SIR dynamics

Before we define the reproductive number R, we briefly As we will show below, our conclusions remain un- 132 recapitulate the basic SIR dynamics that we consider changed when updating our model to the new data. 133 (Fig. 1). In principle, the course on an infection can be 134 described as follows: A susceptible person (not infected Questions on how changes in testing capacity may 135 and not immune) becomes infected but is initially not have influenced our results. Given the data that 136 infectious; after some time, the person starts to be inhave become available on the weekly (daily) number 137 fectious but symptoms only show after the incubation

138 period; eventually, the person is no longer infectious be-139 cause they are either isolated, recover, or it die. The idea 140 of compartmental models is to group the population into compartments; in the most simple but established SIR 142 model these are susceptible (S), infected (I), and recov-143 ered (R). Assuming a well-mixed population (a mean-field approximation of everybody interacting with everybody), one can formulate differential equations that describe the 146 time development of these compartments:

$$\frac{dS}{dt} = -\lambda \frac{SI}{N} \tag{1}$$

$$\frac{dS}{dt} = -\lambda \frac{SI}{N} \tag{1}$$

$$\frac{dI}{dt} = \lambda \frac{SI}{N} - \mu I \tag{2}$$

$$\frac{dR}{dt} = \mu I \tag{3}$$

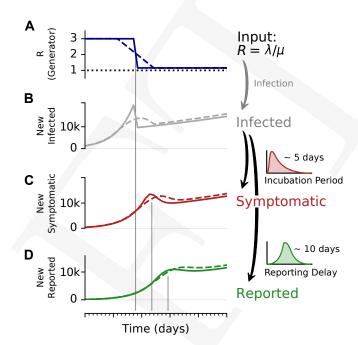
$$\frac{dR}{dt} = \mu I \tag{3}$$

This assumes a spreading rate λ for infected people to 148 infect susceptible people (who they meet randomly) and 149 a recovery rate μ for infected people to recover. These 150 differential equations can be extended to include various different compartments, in order to better resolve the temporal course of the disease, but typically keep the mean-field assumption of a well-mixed population unless evaluated on some (typically unknown) network. In this case, additional compartments reflect spatial information.

Observed case numbers are always delayed from the true infection date (Fig. 2). In general, when a person becomes infected, the onset of symptoms is delayed by the incubation period. Upon symptom onset, it typically takes a few days until the person undergoes a test and the case is reported (although some people are tested before symptom onset, e.g. if contacts are traced or tests are performed at random "Stichprobe"). However, for the modeling, one is usually interested in the actual time when a person becomes infected — but this information is not directly available in real-world data. One either works with the reporting date or with the dates of the symptom onset (epi curve) that can be reconstructed e.g. via nowcasting. Note that these are 170 still delayed with respect to the true infection dates due 171 to the incubation period. For the example models in 172 the following, we synthetically generate observed cases — 173 symptomatic or reported — by convolving the infected cases with a distribution of incubation periods or reporting delays, respectively (Fig. 2).

Model-free estimation of reproduction number

Definition of R. The reproductive number R quantifies how many susceptible persons are on average infected 180 by one infected person. If one infected person infects on average more than one other person (R > 1), then case 182 numbers are growing exponentially. In contrast, if less than one other person gets infected (R < 1), then case



A change-point in R can lead to a transient decay in case numbers. To illustrate the effect of a change point, and the delays in observing symptomatic and reported cases, we consider an SIR model with a fast or slow decay of R, and generate synthetic case numbers. A: The reproductive number R exhibits a change point from R=3 to R=1.15, with a duration of either 1 day (solid) or 9 days (dashed). **B:** The number of new infections can show a transient decrease caused by the change point in R, even though the underlying dynamics are always in the exponentially growing regime of R > 1. Such a decrease can be misinterpreted as R < 1. The number of C new symptomatic cases, and D reported cases is generated by convolving the new infected with a lognormal incubation period (median 5 days) or reporting delay (median 10 days), respectively. Note that the convolution shifts and smooths the curve of the new infected. Nonetheless, the counter-intuitive effects of a transient decrease in case numbers caused by a change points, is still very well visible (See Fig. 4 for the challenges of estimate R in around the change point.)

numbers are declining. Therefore, R=1 marks the criti-185 cal transition between growth and decline of case numbers. 186 Estimating the reproductive number R in principle can be done in two manners, either by inferring it from observed case numbers, or by following infection chains step by 189 step. If one infers it from observed case numbers, there 190 are a number of possible approaches. Some approaches 191 are summarized in Fig. 4 and detailed below. All of these approaches are applied to the observed case numbers (day 193 of symptom onset, i.e., epi curve, or day of reporting). In 194 the following, we assume that they are applied to the epi

The most straight-forward definition of the reproductive

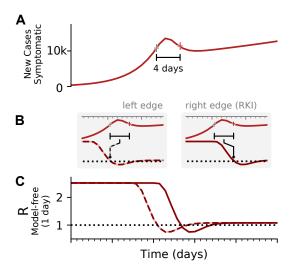


FIG. 3. Two different conventions to define the reproductive number R: Infections in the future or infections from the past. A: Synthetic data for new symptomatic cases. The marked interval indicates an assumed generation time of 4 days. B: The basic reproductive number can be defined either on the left edge of the generation interval (left, dashed line), describing the average number of future infections that are cause at time t, or on the right edge of the interval (right, solid line), describing the average number of infections at time t that were caused by the past ones. C: Depending on the convention, the resulting curve of R is shifted by the generation time q. Note that in both cases the R is estimated erroneously to fall below R = 1, although in the underlying model it was was R > 1 all the time. This is an effect of the SIR dynamics together with a change point in the underlying R. (See Fig. 4 for model details.

197 number assumes a reproductive process with offspring 198 generation, such as a branching process [2]. For this, one assumes a generation time q in which an infectious person 200 can generate offspring infections. In the simplest case, one 201 could consider that offspring infections occur exactly after $_{202}$ one generation time g. This allows to infer the effective $_{203}$ spreading rate R precisely:

$$\hat{R}_t = \frac{\text{number of newly infected at time } t + g}{\text{number of newly infected at time } t}$$
 (4)

$$=\frac{C_{t+g}}{C_t}. (5)$$

In reality, these newly infected case numbers C_t have to be approximated, e.g., by using new symptomatic cases or new reported cases. Moreover, the generation times g of each infection are widely distributed, so that using the average value g (or an estimate of it) is a further 213 with respect to the case numbers (Fig. 3). Above, we conwidely applied and has proven quite useful.

212 tions for the timing of the estimated reproductive number 217 the number of infections at time t that were caused by

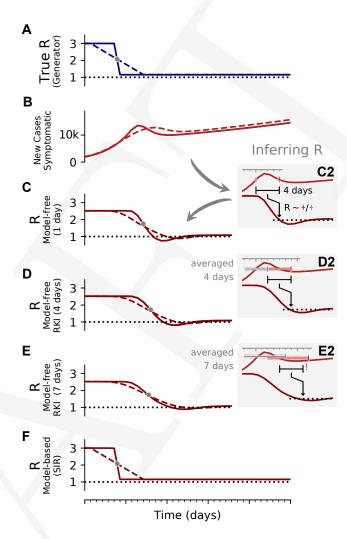
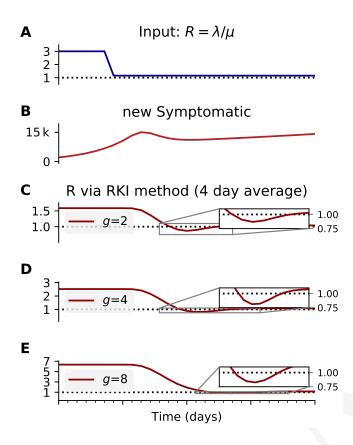


FIG. 4. The inferred reproductive number R depends on the inference method. A, B: Synthetic data for new symptomatic cases generated with SIR dynamics from an underlying Rwith one change point of duration 1 day (solid) or 9 days (dashed). C: Model-free inference of R based on the ratio of case numbers at time t and time t-g, marked by a red and gray cross (inset), respectively ('right-edge convention', cf. Fig. 3). **D:** Model-free inference of R following the Robert Koch Institute convention, i.e. using the definition of C but with averaging over a window of the past 4 days (inset, red and gray bars). E: Same as D but averaging over 7 days. Note the overlap of intervals. All the model-free methods (C-E) can show an erroneous estimate of R < 1 transiently, due to the change point in the underlying true R. F: The inferred R using change-point detection with an underlying dynamic model (SIR) does not show a transient erroneous R < 1 period. If the underlying dynamic model corresponds well enough to the true disease dynamics, then this approach reproduces the true R that was used to generate the data.

approximation. For its simplicity, this inference of R is $_{214}$ sider R_t to characterize the number of future infections $_{215}$ that are caused by infections at time t (left-edge conven-When going into detail, there are two different conven- $_{216}$ tion). Alternatively, one can consider R_t to characterize



The inferred reproductive number depends on the assumed generation time g. A, B: We generate synthetic data using SIR dynamics with time-dependent R including a 1-day change point (A) that yields new symptomatic cases with transient decrease (B) despite all R > 1. C-E: Using the RKI convention to infer R (4-day average, right-edge convention), we demonstrate how generation times g result in different R curves. In particular, we find different initial levels of R (left plateau), differently long crossover duration (time from left plateau to right plateau), and differently deep transients of R < 1 (insets).

218 the past pool of infected (right-edge convention), defined 219 as

$$\hat{R}_t = \frac{\text{number of newly infected at time } t}{\text{number of newly infected at time } t - g} = \frac{C_t}{C_{t-g}}$$
(6)

The results for R are exactly equivalent, apart from a 220 shift in time by exactly q.

R as calculated by the RKI. Real-world data are often noisy, and therefore averaging over a certain time window can help to smooth the estimate. This procedure is used in two variants by the RKI, smoothing over four days or over seven days. The details of the procedure are documented in detail in [3]. In both cases, they assume a constant serial interval (generation time) of q = 4 days (Fig. 4). The four-day smoothing has the advantage that it reacts a bit faster, the seven-day smoothing has the advantage that it smooths out weekend-related modulations

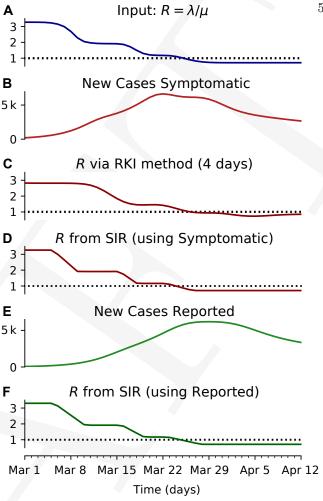


FIG. 6. The model-based methodology yields consistent results irrespective of whether it is applied to the new reported cases or the new symptomatic cases (e.g. obtained by nowcasting). A: Time-dependent reproductive number as inferred from case numbers in Germany [1]. B: Synthetic data for new symptomatic cases generated with SIR dynamics from the underlying time-dependent R. C: Inferred R from new symptomatic cases using RKI method (4 days generation time, right-edge convention) would reproduce step-like behavior (no noise present) but prematurely drops below R = 1 (dashed line). **D:** Inferred R from new symptomatic cases using change-point detection with dynamic model (SIR) correctly reproduces the input. E: Synthetic data for new reported cases generate with SIR dynamics as in B (cf. Fig. 2). **F:** Inferred R from new reported cases (E) using change-point detection with dynamic model (SIR) also correctly reproduces the input. Note that both, D and F show sharper steps because of the assumed piece-wise linear change points in the model, and that they perform so well because they employ the true dynamic model that is used for the synthetic data. Both are model assumptions that need to be justified in our approach.

of test numbers. In particular,

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$$R_{t,4} = \frac{\sum_{s=t-3}^{t} C_s}{\sum_{s=t-3}^{t} C_{s-g}}$$
 (7)

$$R_{t,4} = \frac{\sum_{s=t-3}^{t} C_s}{\sum_{s=t-3}^{t} C_{s-g}}$$

$$R_{t-1,7} = \frac{\sum_{s=t-6}^{t} C_s}{\sum_{s=t-6}^{t} C_{s-g}},$$
(8)

where q = 4 is the assumed generation duration, and the 223 averaging is done over 4 and 7 days, respectively. Note 224 the shift by one day in the 7-day version Eq. (8).

Model-free methods versus model-based methods to infer reproductive number.

In order to demonstrate potential issues when inferring the reproductive number R, we systematically compare model-free methods and model-based methods on synthetic data from an SIR model (Fig. 2). With model-free methods, we refer to inference methods for R, which do not explicitly incorporate disease dynamics (SIR). The three methods we presented above belong to this group. These methods to estimate R are straight forward and easy to implement. However, they might lead to biased estimates when R is changing rapidly. More precisely, in the following we show that these methods (1.) smooth out fast changes in R, (2.) produce some delay compared to the underlying R, (3.) the estimate depends on the assumed generation time, and (4.) around change points they may return transiently R < 1, even if the true value was never smaller than 1. While these methods have the $_{243}$ above limitations when R is changing quickly, they are still very useful for an easy-to-obtain estimate of R.

Model-free methods may smooth out fast changes.

In Fig. 4, the \hat{R} that is inferred by model-free methods undergoes a smoother change than the true R. The smoothing has two origins: First, when using the slidingwindow of four or seven days (RKI methods), multiple days are combined to obtain an R value for one day. Second, R has to be calculated from the daily new symptomatic or reported cases (Fig. 2 C, D), because the dates of infection (Fig. 2 B) are not directly accessible in realworld data. As discussed before, symptom onset and reporting date are delayed from the infection date. Because the delays vary from case-to-case, these two curves 310 ₂₆₂ appear slower than they truly are, and successive fast ₃₁₆ case numbers change by a factor R from one generation 263 changes may appear as a long transient.

Model-free methods produce delayed estimates that are difficult to interpret

In our example in Fig. 4, we estimated \hat{R} based on the 267 number of new symptomatic cases as produces by our \tilde{R} model. The \tilde{R} of all three model-free methods is shifted 269 in time compared to the true R (Fig. 4 A).

How does one interpret the shift and where does it come from? To interpret the shift and compare between the different methods, we focus on the time point where half of the steep step in R has been detected (gray dots). 274 This shift has multiple contributions. One contribution 275 originates from using the dates of symptom onset, which 276 is shifted on average by the incubation period (in our example ≈ 5 days). This generates the 4–5 day shift of 278 the one-day method (Fig. 4 C). Because the incubation 279 period is not constant and typically is asymmetric, there is an additional asymmetric distortion towards either di-281 rection, depending on the shape of the actual distribution of incubation periods. Another source for the shift comes from the time average, which explains the additional (ap-284 proximate) 1-2 day shift in the four-day and seven-day 285 methods employed by the RKI (Fig. 4 D, E). Because of 286 the specific definition of the position of the 4 and 7-day $_{287}$ window of the RKI, the two versions of R have a very 288 similar average delay of 5-6 days in total with respect to the true R.

Both, the variable incubation time and the time aver-291 aging also impact the start- and end-points of the change 292 in a non-trivial manner. In combination, multiple sources cause shifts that can point into opposite directions. While 294 the sources can be identified conceptually, the combined effect cannot perfectly be disentangled or compensated.

Due to multiple sources of shifts and smoothing, a 297 simple post-hoc shift of the R-curve cannot reproduce the 298 true R around a change point. For example, a shift of ²⁹⁹ Fig. 4D by 5 days would suggest a start of the change point 300 before it starts in reality (Fig. 4 A). This fact has led to 301 multiple prominent misunderstandings in relation to the 302 RKI data and the effects of governmental interventions. Instead of shifting curves to partially correct for one or another potential delay, an inference of R using modelbased methods can account for this and other potential biases. When using a good model, such a model-based $_{307}$ approach returns the correct R with the correct steepness 308 and time point (Fig. 4 E).

R-estimates depend on the assumed generation time.

The assumed generation time g impacts the absolute are smoothed out compared to the infection curve (In $_{311}$ value of the estimated reproductive number R (Fig. 5). other words, the smoothing originates from the variance 312 We exemplify this effect using the method of the RKI in incubation period and reporting delay, see later Fig. 10 313 (4-day average), where we vary the assumed generation in the section about testing). Hence, if smoothing is not 314 time g. (Note that the same effect applies to model-based explicitly incorporated in the inference of R, fast changes 315 inference.) In a stationary phase with constant R, the 317 to the next. Within two generations, they change by the

 $_{318}$ factor R^2 , and so on. Hence, when assuming erroneously $_{370}$ demonstrate the robustness of model-based inference, we generally, $\hat{R} = R^{g_{\text{assumed}}/g_{\text{true}}}$.

estimating the absolute value of the reproductive number 381 Fig. S4). 330 from observed case numbers without knowing the precise generation time may lead to misestimates.

Model-free methods may return erroneous transient periods of R < 1 at change points.

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In our examples (Figs. 4 and 5), we consider that Rchanges rapidly from $R_0 = 3$ to $R_1 = 1.15$ within one day. Such a sudden change leads to a transient decrease 385 line). 348

ods in our example (Figs. 4 and 5) correspondingly yield 404 in Bayesian inference. non-negligible periods of R < 1, even though the under- $_{405}$ ³⁵⁸ approaches, on the other hand, can account for transient ⁴⁰⁷ models of measurements and random errors. Bayesian $_{362}$ if one infers R in a model-free manner, by computing $_{411}$ (say, a t-test) but need to be formulated anew for each ³⁶³ ratios of case numbers, then the local minimum leads to ⁴¹² case. The fact that the assumptions are hand-tailored to an erroneous estimate of $\hat{R} < 1$ (Fig. 4 C–E).

Well chosen model-based methods can reconstruct complex disease dynamics

368 namics well, robust inference of the true underlying repro- 420 main manuscript [1], but we here give a much deeper and 369 duction number (and other parameters) is possible. To 421 broader and more educational treatment.

double (or half) generation time, then one obtains the 371 generate synthetic data using an SIR-model as inferred square (or square root) of the true R as estimate. More 372 from case numbers in Germany between March 2 and 373 April 21 [1] (Fig. 6). The Bayesian model inference can In the example, we assumed three different generation 374 recover the reproductive rate (Fig. 6D,F), whereas with times (2, 4, and 8). At the onset, $\hat{R} = 2.5$, $\hat{R} = 2.5$, 375 the model-free method, the recovered R is slightly biased and $\hat{R} \simeq 6.3$ for g=8, as expected from theory. In 376 (Fig. 6C). Note, however, that the model has to match absolute terms, this dependence is less pronounced near 377 at least approximately the disease dynamics, to allow a a reproductive number of 1; assuming e.g. R = 1.1 then ³⁷⁸ good inference. This is why we used different models to assuming double (or half) the generation time results in 379 assess the robustness of our results in Ref. [1] (SIR: Fig. 3, R=1.21 (or R=1.05). This small example shows that 380 SEIR-like: Fig. S3, SIR without weekend modulation:

III. WHAT CONCLUSIONS CAN ONE DRAW FROM A BAYESIAN ANALYSIS?

Modeling background

When the Coronavirus-pandemic arrived in Germany in new case numbers — despite R > 1 always. How 386 we set out to model the spread of the disease as rapidly as can there be decrease in new cases although R > 1? 387 possible. Thus, our model from the start was aimed at giv-The transient decrease results from the pool of infected 388 ing estimates with their corresponding error bounds based suddenly infecting considerably less people. This decrease 389 on the data available at that time. To this end we decided in infections causes the sharp peak and a sudden drop in 390 to use a Bayesian strategy as it allowed formulating wellnew infections (Fig. 2B, solid line). It then carries over to 391 documented assumptions on those aspects not available the number of new symptomatic and new reported cases, 392 from data at that time. Within the Bayesian framework with the respective delay and smoothing (Fig. 2C,D]). 393 these assumptions can and should be replaced by data This transient decrease depends on the duration of the 394 as soon as these become available, and we implement change point: While it is strongest for steep changes, it 395 such an improvement below for the case of information on also occurs for a nine-day change point (Fig. 2, dashed 396 symptom onset times that have become available in the 397 meantime. Given such new data it will also be interesting Naively, a transient decrease might be interpreted as 398 to evaluate post-hoc the assumptions and the performance transient R < 1, but that is not the case here. A 399 of our model. This will also give some guidance as to model-free method cannot distinguish between different 400 whether to employ a model of this kind again in a new scecauses for transient decreases in case numbers, being it 401 nario (another disease outbreak or pandemic) where some due to transient non-linear effects (Fig. 2) or due to a 402 relevant data will also not be available immediately. We true exponential decay (R < 1). The model-free meth- 403 note that taking these steps is the intended development

We also note that all statistical procedures come with lying model dynamics have R > 1 always. Model-based 406 their own assumptions, e.g. on distribution of the data, non-linear effects if included in the model, e.g., as change $_{408}$ analysis is no exception to this rule; in our view the only points, and — if the model is correct — even reproduce 409 difference is that modeling assumptions are not taken for the true underlying dynamics (Fig. 4 F). To conclude, 410 granted based on the long-established used of a method 413 the application case may seem subjective sometimes; yet, 414 similar assumptions are being made, more tacitly perhaps, 415 in other frameworks, as well. This said, it is neverthe-416 less important to question and discuss (our) modeling 417 assumptions and to test the sensitivity of our results to 418 the modeling assumptions. As far as space restrictions When the chosen model describes the true disease dy- 419 allowed we have discussed our assumptions already in the

Bayesian inference as reasoning under uncertainty, bound to be updated

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424 425 time point T represent what we should believe in at that 477 and a recent rise in λ^* from its all-time low, and also in time point T, given the knowledge available at T (causes 478 the light of country to country comparisons, Fig. 7). and data known at T). These results represent something 479 437 former model counterparts. The important question is 489 made. thus not whether a model is correct in absolute terms, 490 at T comprise those obtained at $T + \Delta_T$.

tant data in this respect are the reliable data on putative 500 we have to take. infection dates which at present take about 7 days to come in for at last 80% of the cases (Fig. 10), and which were only published more recently than our internal anal-452 ysis cut-off. We present results obtained using these data 502 below and compare them to our published results.

$\mathbf{C}.$ Conditions for plausible alternative models entering model comparison

A frequent, and important misunderstanding around 456 457 Bayesian model comparison is that one is allowed to formulate very many models at random and then let the data decide on the best model via the Bayesian model 460 evidence (or the LOO-scores). This notion fails to notice that the model evidence $p(D|M_i)$ is only one part of the decision on the preferred model. The formal equation for 463 deciding between models i and j would be:

$$\frac{p(M_i|D)}{p(M_i|D)} = \frac{p(D|M_i)}{p(D|M_i)} \frac{p(M_i)}{p(M_i)} , \qquad (9)$$

464 i.e. taking such a decision entails accounting for a-priori 519 variations from country to country. In sum, the results Rather, each model subjected to a model comparison 524 most plausible model. 470 needs to be well justified. This is one of the reasons why we 525 Later, discussions (such as the one presented here) of 471 did not consider for example models of sustained, constant 526 the selected models and the inferred parameter ranges 472 drifts in the effective spreading rate λ^* (or, equivalently 527 should then investigate and update modeling assumptions,

473 the reproductive number R), as we did not come up 474 with plausible explanations for such a behavior (except 475 perhaps arguments based on herd-immunity, which seem The results of a Bayesian analysis at some publication 476 implausible now, in the light of second waves of infections

On a practical note, useful modeling also has to reflect that we should be able to agree on given the knowledge at 480 certain limits on model complexity in relation to the T (and some practical constraints, see below), but these 481 available data, and also computational resources. Known results may change given more information at a later time 482 phenomena, that can nevertheless not be modeled must $T + \Delta_T$. Changing ones mind with the availability of 483 therefore often be integrated into noise terms that are additional information is designed into Bayesian inference 484 designed accordingly (as was done with the modeling as "the logic of science" (E.T. Jaynes) from the start. 495 of observation noise in our case, instead of using full In other words, scientific inference and the associated 486 stochastic differential equations). The best that can be models are bound to be updated - just like the relativity 487 done then is to investigate the sensitivity of results with theory and quantum theory in physics overrode their 488 respect to the simplifying assumptions that have been

It is also in order to explain in simple terms how results but whether it was possible to agree on the model (and 491 of a Bayesian analysis may be interpreted: In the Bayesian the inference provided by it) at time T, and also if the 492 framework probabilities are measures of the plausibility of inference provided at T was robust, for example in the 493 statements about the world, given our present knowledge. sense that the credible intervals for the model parameters 494 Thus, the results of Bayesian parameter inference for 495 example indicate credible (plausible) ranges in which we From this perspective it is obvious that now, more than 496 should assume the unknown parameters to be. Assuming a month after finalization of our published analyses on 497 them to be elsewhere with high probability would be April 21st, new data have become available and that the 498 inconsistent with the information we have. In this sense, model can, and should, be improved accordingly. Impor- 499 these credible intervals may form the basis for decisions

D. Models as competing causal explanations of data

Last, we note that the notion of causality resides only 504 in the construction of the models – with different models 505 incorporating different possible causal explanations (e.g. 506 in the form of differential equations for the disease dy-507 namics) of the data. Performing model comparisons then selects more plausible over less plausible explanations, 509 but does not provide a proof of causality in the strict 510 sense advocated for example by Pearl [4] or by Ay and ⁵¹¹ Polani [5]. Yet, fulfilling the formal criteria for causality 512 in this strict sense would need multiple replications of 513 the pandemic process, each time with different settings of 514 the relevant variables, such as interventions. Even when 515 treating the SARS-CoV-2 outbreaks in different countries 516 around the world, with their different interventions (or 517 lack thereof), as replications establishiung formal casu-518 ality may remain an elusive goal due to multiple other plausibility of different models, i.e. $p(M_i)$ and $p(M_i)$. 520 of our Bayesian analysis must be seen as a search for While it is customary to assign equal a-priori plausibility 521 the most plausible causal model of the data, given the to all the models being considered, this does not mean that 522 data available at the time of analysis, and as providing just any model qualifies for use in this decision procedure. 523 credible ranges of the parameter values relative to this

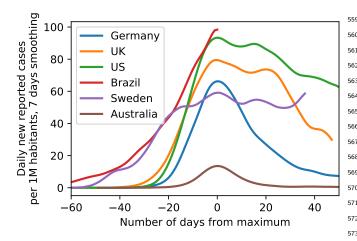


FIG. 7. Comparison of the case numbers per one million inhabitants of exemplary countries as illustration of the range of possible case numbers developments. Note how both the peak height as well as peak width of some countries are con- 575 A. saturation effects ('herd immunity') in Germany (Data until 577 June 3, 2020).

528 and reason whether the causal model can be maintained, or not.

When analyzing improved data that reflect the dates of symptom onset rather than case reports to improve our modeling we find that both the preference for a three change point model as well as the inferred parameter ranges do not change drastically, and we maintain our original interpretation of the pandemic process and the effectiveness of governmental interventions.

Last, alternative models assuming herd immunity as a reason for the sustained observed drop in infection rates still do not seem plausible to us in the light of rapidly surging second waves or sustained high levels of new infections (such as in Sweden, see Figure 7).

MODEL EVOLUTION

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these latter models are useful for a better understanding 604 delay distribution. after the fact, they cannot be applied early on due to a 605 (here usefulness means that the early models describe the 610 are shown). ₅₅₆ epidemiological parameters and their uncertainties well ₆₁₁ ₅₅₇ enough to inform decisions). For the case of the COVD-19 ₆₁₂ presented in [1]. Specifically, model comparison still favors 558 outbreak in Germany, the initially available data were 613 the three change point models over their simpler counter-

559 sorted based on date of reporting, where the reporting occurred after an unknown delay between symptom onset and report. Only later, data organized by time of symptom onset, the so-called epi curve, became available. Even after their initial release, these data were still updated and refined (see Fig. 8); also note that data for symptom onsets still take some time to arrive and be compiled, i.e. the delay between symptom onset and testing/reporting is 567 still considerable (see Fig. 13). In particular, this means 568 that reliable epi curve data for April 21^{st} , our analysis cut-off date in [1], were not available until much later. Now that these data are available, however, we can compare models based on data organized by reporting date, 572 modeling the reporting delay and incubation period, and 573 models based on the epi curve, modeling the incubation 574 period only.

Model updates based on time of symptom onset siderably larger than for Germany, providing evidence against 576 and comparison to previous results based on time of reporting

Ideally, modeling of an epidemic outbreak should rely on data organized by infection date - yet, such data are 580 rarely available outside of the analysis of individual, wellconfined infection chains. The next best option then are data organized by date of symptom onset - the epi curve. 583 Naturally, symptom onset precedes the test and report in 584 time. Thus, the epi curve is only available after a certain 585 delay, which can be substantial. Furthermore, the time 586 of symptom onset may remain unknown for a significant 587 fraction of reported cases. If so, then reconstructing the 588 epi curve requires data imputation and further modeling 589 (e.g. nowcasting [6, 7]), which may further delay the avail-590 ability of this curve. At the initial stages of an outbreak 591 one may therefore decide to analyze data organized by 592 reporting data. For a comparison of analyses it is impor-593 tant to understand how the curve of reporting dates and 594 the epi curve are linked. Both curves originate from the 595 curve of initial infections by a convolution (see Fig. 2). The epi curve is the curve of initial infections convolved 597 by the distribution of incubation periods, while the curve Modeling efforts at the beginning of an epidemic out- 598 based on reporting date is the curve of true infections break are aimed at providing a rough but timely and 599 convolved by the (less well known) distribution of delays robust description of the disease outbreak, making use 600 between infection data and reporting date. Technically, a of data available at that time. Later modeling efforts, in 601 report can happen before symptom onset, albeit this may contrast, can make use of more detailed data and provide 602 be rare. Therefore, the curve of reporting dates is not deeper insights into how the outbreak unfolded. While 603 exactly a convolution of the epi curve with an additional

We have reanalyzed the initial stages of the outbreak lack of data, and often cannot inform decisions sufficiently 606 until April 21^{st} based on the epi curve that has become fast. However, a comparison of early and later models can 607 available (see Figs. 17 and 19), using models with one, two provide important insights about the robustness and use- 608 and three change points, based both on SIR and SEIR fulness of the early models with respect to the later ones 609 dynamics (only figures for the three change points models

These new results do not change our main conclusions

614 parts (see table I), and only the third change point leads 615 to a value of the spreading rate λ^* that is clearly below zero. At the quantitative level, however, we see some evidence for a larger drop introduced by the first change point when using the epi curve data, and smaller drops 619 induced by the second and third change point, especially 620 when using an SEIR model (see Fig. 19). These quantita-621 tive changes are driven by the epi curve dropping faster 622 than the curve reflecting reporting date (see Fig. 9C).

TABLE I. Model comparison: Using leave-one-out (LOO) cross-validation, we compare the SIR and SEIR model variants using the epi curve as data (Figs. 17 and 19). Lower LOO-scores represent a better match between model and data (pLOO is the effective number of parameters).

Model	# c-pts.	LOO-score	pLOO
SIR main	0	900 ± 13	6.36
SIR main	1	774 ± 14	12.72
SIR main	2	755 ± 13	12.17
SIR main	3	725 ± 15	19.66
SEIR-like	0	900 ± 14	6.65
SEIR-like	1	749 ± 12	8.05
SEIR-like	2	739 ± 13	10.28
SEIR -like	3	726 ± 14	14.04

In sum, we conclude that the original model based on data organized by reporting date was useful to understand disease dynamics in the absence of the epi curve and robust in the sense that its main results still hold.

Differences between results based on RKI versus JHU data sources

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At the beginning of the out break data were made avail- 664 the actual disease dynamics. 630 able on a daily basis both by John Hopkins University 665 ter interface for automated analyses. The RKI resources were updated only a few days later, as information always has to be transmitted from regional agencies to the RKI, whereas the JHU data for Germany are gathered from a few reputed online media (Berliner Morgenpost, Taggesspiegel and Zeit Online [8]). However the JHU resources have been partially criticised for lacking quality control (see issues section on the Github page [9]). We therefore compared the JHU data used in [1] to the official 643 RKI count (Fig. 14) and have rerun the analysis using the RKI reported cases (the "Meldedatum", Fig. 15 and 645 16). The differences are minor.

IMPACT OF TESTING

648 in turn depend on testing. Throughout the COVID-19 686 larger than the prevalence and ii) tests are not performed 649 spread, test availability, test requirements and known case 657 randomly, both of which were met in Germany.



FIG. 8. The numbers of known onsets of symptoms per day as reported at different dates in the past. As testing confirms onset of symptoms in the past with varying delay, the epi curve not only grows at its tail, but over a wide time period with each new publication. Known onsets are reproduced from the RKI's daily situation reports and the publicly available RKI-database. Unknown onsets of symptoms, which account for 40% of total number of cases, are not considered. The estimated total epi curves from the RKI (imputation and Nowcasting), as reported on a past date, are not publicly available for the month of April, hence the focus on the numbers of known onsets here.

650 numbers changed continuously over time, see Fig. 8. Such 651 an inconsistent and fluctuating data-acquisition obviously 652 introduces additional sources of uncertainty. While we 653 decided to exclude the effects of testing in previous mod-654 els, concerns about results derived from data that stem from inconsistent testing should be taken seriously. Thus, 656 we analyze possible distortions in more detail. As we 657 will demonstrate below, our major conclusions remain 658 unchanged.

Please also note that at the time of writing of the initial 660 manuscript, only very preliminary data and statistics on 661 testing was available. Now, with better data, we come to 662 the conclusion that reported case numbers, although they 663 might derive from variable testing, are still useful to infer

In particular, evidence for the key characteristics of the (JHU) and the German Robert Koch Institute (RKI). 666 first wave, i.e. strong exponential growth in new cases, Both sources initially provided only reported cases, with 667 change in transmission dynamics over a limited time pethe JHU resources providing data faster and with a bet- 668 riod and slow exponential decline, can be derived from 669 the available data, even if changes in testing are taken 670 into account.

> We start our analysis by considering two central 672 quantities: i) the number of tests that are performed, say, 673 on a given day or in a given week and ii) the fraction of 674 the performed tests that are positive — a positive tests 675 translates to a confirmed case.

Let us consider two simple limiting cases, in which only one of these quantities changes, whereas the other one 678 remains constant. In the case that a constant number of 679 tests is performed day-over-day and we observe a growing 680 fraction of positive test results, this corresponds to an 681 increase of the underlying case numbers. Conversely, if 682 the number of tests is increased and we find a constant fraction of positive tests, this implies the same, an increase 684 of underlying cases. The second case only holds with Our modeling depends on reported case numbers, which 685 additional assumptions: i) the fraction of positive tests is

dicates a significant growth in new case numbers.

Strong growth until week 12

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Focusing on testing in weeks 10 & 11 in Fig. 9 A and B, 693 we can clearly deduce a strong growth in daily new cases, as both the fraction of positives as well as the number of performed tests rise, matching the combination of the two scenarios described earlier. The rise in the fraction of positive tests is apparent in the daily values, especially as the daily number of tests can be taken as constant throughout the week, see Fig. 8 in [10]. For weeks 14 onward, the number of performed tests stays constant and thus, the fraction of positive tests correlates with the number of reported cases, exhibiting a decline in underlying case numbers. A similar direct comparison 759

be shorter than 1 week. In a time frame of less than a 769 fraction of positive tests. week, more new infections occur than in the period since 770 over the span of one week, a difference in the fraction of $_{772}$ describe well what happened in week i-1. 721 of week 12 (Fig. 9 B). A more in depth analysis of Fig. 9 776 is uncovered), and the reporting date (when a positive is attached in Sec. VD. The important questions that 777 test-result is registered). remain are: When did the number of new infections peak? 778 And when did it start to decline?

of new infections, confirming that testing can properly 786 the reporting delay. 732 measure the underlying epidemiological dynamics in this 787 733

case numbers was indeed present, as well as a decline.

741 however, deem highly implausible. As this scenario has 796 week of onset of symptoms. Until and including week 742 frequently occurred in the public debate on the spread of 797 12, the distributions have heavy tails. After week 12,

Fig. 9 A,B shows that in Germany in early March both, 743 COVID-19 in Germany, we discuss it briefly. The underthe number of tests as well as the fraction of positives 744 lying assumption in this scenario is that the few tests that increased simultaneously. This simultaneous increase in- 745 were performed during the initial outbreak until week 746 11 missed most of the actual cases, i.e. a large pool of 747 infected persons would have existed unobserved. Then, at 748 the same time at which the amount of tests was increased 749 from weeks 11 to 12, coincidentally the effectiveness of 750 the testing could have increased, so that the unobserved 751 pool (of constant size!) is identified and, thus, apparent case numbers rise. Given the rigorous criteria (based on symptoms and risk of exposition) that were required from patients in order to qualify for one of the early tests, we 755 deem this scenario of an unobserved and constant pool 756 to be quite unlikely. Especially so because the fraction of 757 positive tests stayed below 10% during the entire time.

Locating the peak position

We are now interested in the peak position in the curve for weeks 10-12 is unfortunately not that simple, as the 760 of onsets of symptoms, see again Fig. 9, C, red. The number of tests changed week-to-week in that time period. 761 day of the peak is constrained by the initial simultaneous For a better understanding of the following part of 762 increase in tests and fraction of positive tests to occur no the analysis, we recall an important fact on exponential 763 earlier than week 11, as the peak would indicate the end growth: In each doubling period the same number of new 764 of the growth. In this section we're focusing on how it infections occurs as in all preceding periods combined. As 765 can be reliably identified from the stable period of testing: the number of tests approximately doubles every week 766 From week 12 and onward, the number of tests remained until week 12 and the fraction of positive tests increases $_{767}$ on an almost constant, high level \sim 400k and changes in to week 13, the doubling period of new infections has to 768 the daily new cases reported are directly reflected by the

To understand this in more detail, we introduce the the onset of the outbreak. If we assume constant testing 771 following important rule of thumb here: Tests of week i

positive tests on each day during that week should be 773 The key is the connection between the date of symptoms observable, and this is indeed what we see for testing in 774 onset (when symptoms first show), the testing (when the weeks 10 and 11 and to a lesser extent from start to end 775 symptom onset is confirmed or an asymptomatic case

Any reported case must inherently be preceded by 779 a test and according to the RKI, positive test results Deferring the first question to Sec. VB, we answer the 780 are reported within 24 hours to the responsible health second: From week 14 on, there is an approximately con-781 department. The remaining task then is to reveal the stant high level of testing, but a decline in the number of 782 connection between symptom onset and reporting date, cases reported, and an accompanying day-to-day decrease 783 i.e. the reporting delay for each individual case. The date in the fraction of positive test results. These observations 784 of testing is taken as the day before reporting in the rest are consistent with an exponential decline in the number 785 of the analysis, the testing delay is one day shorter than

In Fig. 10 we detail the reporting delay by plotting 788 distributions of how many days after the symptom onset Summing up the above analysis so far, we have indi- 789 a case is reported. For example, if each and every infected cations that during the epidemic outbreak, a growth in 790 person would receive a test result (become a reported 791 case) exactly three days after they showed symptoms, Hypothetical Scenario: If we were to reject the 792 then the plotted distributions would have only one entry: above simple explanation that growing case numbers re- 793 a delta-peak at three days. However, we see that most flect growing numbers of infections, there is one alter- 794 reports arrive 1-7 days after symptom onset, where the native scenario to explain the observed trend, which we, 795 details of the (lognormal) distribution depend on the

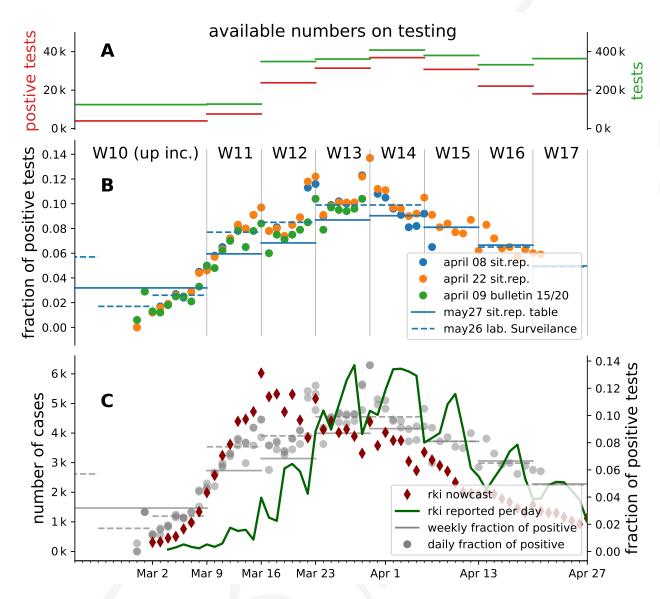


FIG. 9. The evolution of the fraction of positive tests in weeks 10 to 17. Weeks 10 to 12 strong exponential growth in in the number of new cases, which was not limited by the early testing capacity. A Comparison of number of positive test results with the number of tests performed for each week. Reproduced from Table 5 in [10]. Note: Numbers for week 10 and earlier are represented by a single data point. B Mid-term changes in the fraction of positive tests is more obvious in the daily data (points) than in the weekly (bars), especially in early March. Daily values are taken from situation reports [10–12] (full dataset) and the epi bulletin [13, 14] (ARS dataset). Weekly values, represented as horizontal lines, are taken from a situation report table and a weekly lab surveillance report (ARS dataset). Note: the latter represents a subset of all tests. Compared to the situation report, the ARS dataset lists weeks 8 to 10 individually. C Overlay of Panel 2 with the number of cases reported per day by the RKI and the estimated epi curve (imputation and Nowcasting, as described in [7]). The fraction of positive tests correlates with the number of reported cases from week 13 onward, as the total number of tests reaches a constant level.

798 the distributions have lighter tails. This provides some 807 are only reported weeks later — when more testing was 800 tails: most of the symptom onsets are reported within 809 of symptoms in week 11 are reported within 5 days, 80% 805 effect is what we see for the onsets during the first weeks 814 Without explicitly working out the details, it's fair to 806 until 11; due to limited testing capacities, many cases 815 declare the initial rule of thumb valid. A more thorough

intuition of the distributions and the meaning of the heavy 808 available. To rephrase based on Fig. 11: Half of the onsets the first week but some will be reported much later, so 810 within 9 days. The crucial example here is: Half the that shape of the distribution still keeps changing. If 811 onsets on Wednesday get tested until Sunday, the other the test level is low, more cases will be reported later 812 half in the following weeks for every following day of the and the tails of the distribution are heavier. This latter 813 week the fraction of test performed in the next week rises.

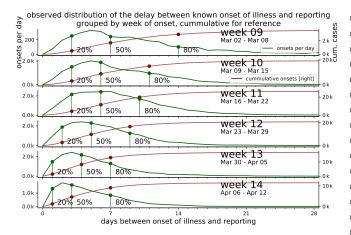


FIG. 10. The onsets of symptoms are confirmed by testing at later point in time, which accounts for most of the delay till all or the main fraction of known onset of symptoms (IstErkrankungsbeginn in RKI-database) are reported. From the RKI data, the number of cases per delay between onset of illness and reporting (i.e. RefDatum and Meldedatum) for cases with known onset of symptoms (IstErkrankungsbeginn) are counted for each week. The fraction of reported cases out of the total onsets up to a delay are highlighted for 20%, 50% and 80%. The cumulative number of cases reported up to each delay is displayed for reference.

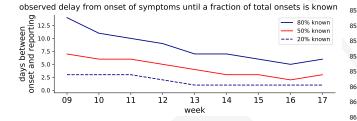


FIG. 11. Overview of the delay between onset of symptoms and the reporting of a fraction of total known onsets for a day changes with time. The 50% fraction represents the median reporting delay between onsets of symptoms and reporting. Derived from Fig. 10

816 analysis based on actual per case testing-delays instead of reporting delay distributions is conducted in Sec. V C. Let's turn back to Fig. 11 A. The onsets in week 11, 819 the estimated position of the peak, should be robustly measured by the testing in week 12, with a high number of total tests. From Fig. 11 C, we can see, that the number of onsets of illness peak at the end of week 11 or the beginning of week 12. This time point doesn't suffer from lower testing numbers in week 11.

Decomposing the epi curve into weeks of testing

827 and reporting, we can decompose the epi curve and iden- 885 and highter number of cases in week 10, cannot be valid. 828 tify parts of the curve that stem from certain weeks of 886 Reaffirming the observation of growth from week 10 to

829 testing. Fortunately the publicly available RKI database 830 contains both onsets and reporting for individual cases 831 for 60% of the total cases and thus also the date of test-832 ing, which in general is one day earlier than the report. 833 In more detail, for all the cases within a chosen test-834 ing period, we also know the respective date of onset of 835 symptoms, for complete datasets. Borrowing from [7], 836 the remaining 40% of test dates can be imputed from the known onsets dataset. In Fig. 12 A.B we apply this 838 method to collect all the symptom onsets that were found by testing in weeks 12 and 13. Through this allocation of 840 "which part of the curve stems from which tests", we can 841 thoroughly justify the connection that we made above, 842 when we said that growth in weeks 11 and 12 stems from 843 the tests in week 12 and 13. As we see, the peak on March 16 stems almost completely from tests of week 12 and 13; these weeks already featured the high level of tests 846 performed. Based on the decomposition, we can conclude 847 that in week 11, every day could have been identified as 848 the peak based on testing in weeks 12 and 13.

We can extend this method in an attempt to reduce 850 the influence of changing number of tests per week on 851 the estimation of the change in the number of onsets of 852 symptoms from one week to the next. We compare the 853 number of onsets in different weeks, that were confirmed by one week of testing. Think: distribution of onsets per week seen by the testing in one single week. Some cases with onset of symptoms on Monday will receive their positive result within the same week as the symptom onset itself, others get tested further away from their onset of symptoms. As viewed from one single week of testing, we distinguish 4 categories: onsets 3 weeks, 2 weeks and 1 week earlier than the test and onset in the same week as testing. The number of onsets in each of the 4 categories compared with the total number of onsets confirmed in the week of testing, the fraction per category, is characteristic for the epidemiological dynamic in the time span of those four weeks. This method is 867 more robust to changes in the number of tests week-over-868 week, than the other methods outlined so far. In Fig. 13 869 three different scenarios are considered and their effect 870 on the fraction of cases in each week-category is worked 871 out. All three scenarios show distinctive combination 872 of fractions per week-category. Comparing the artificial 873 result with Fig. 12 C, we find that in week 11 most of the 874 tests (52%) found symptom onsets within the same week. 875 This indicates weeks 10 and 9 had significantly less new 876 onsets of illness. This is consistent with the exponential growth uncovered in sec. VA. In the extreme case that no 878 tests were performed in week 10 and we were to observer 879 that the number of onsets in week 10 were comparable or 880 higher than in week 11, the backlog from week 10 would 881 lead to higher fraction of 1-week-earlier onsets than same 882 week onsets, for testing in week 11. As the fraction of 883 1-week-earlier onsets is lower than same-week for testing Having established the delay between symptom onset 884 in week 11, we can see that the assumption, no tests

decomposition of the epicurve into weeks of testing

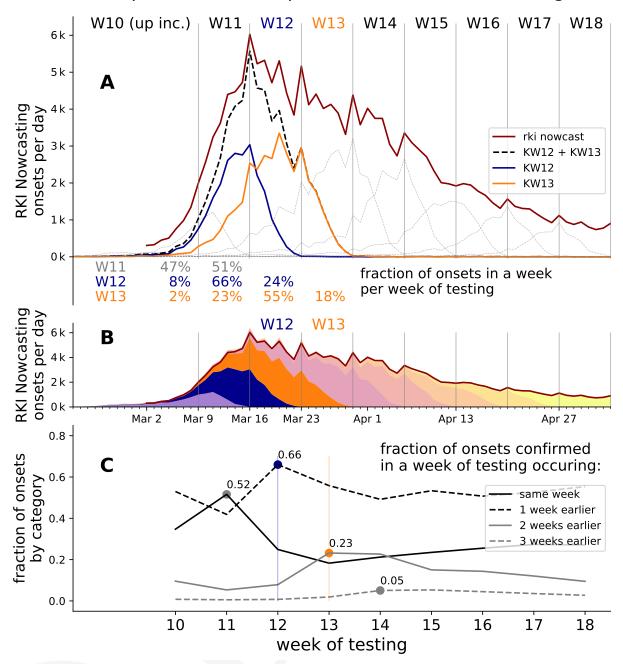
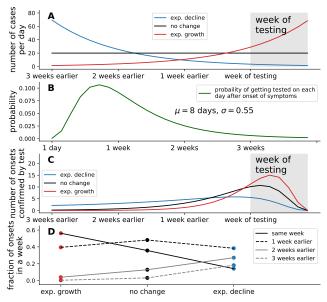


FIG. 12. Testing in one week confirms onsets of symptoms that occur up to 4 weeks earlier. The extend of this effect is analyzed based on the RKI database through decomposition by allocation of onsets of symptoms to weeks of testing. It is assumed that the delay between the time of testing and *Meldedatum* is 1 day. Tue-Mon *Meldedatum* is taken as a proxy for Mon-Sun testing. A Onsets of symptoms per day curves allocated to weeks of testing, weeks 12 and 13 are highlighted. Most known onsets around the peak of the epi curve in week 11 are confirmed by the testing in weeks 12 and 13. B stacked decomposition of the epi curve into weeks of testing. C To reveal crucial information about week-to-week change in the number of total onsets based on one week of testing, the shape of the distributions of onsets of symptoms confirmed by that week of testing is characterized. The fraction of onsets in the same week and each preceding week out of the total onsets confirmed by the week of testing is calculated. This indicates, the portion of a week's positive tests confirming onsets in the same week or in preceding weeks (max. 3 weeks earlier). The evolution of these 4 values is plotted by the week of testing. The peak of the epi curve can be tracked through testing results of weeks 11 to 14 as a maximum in the same-week/n-weeks earlier fraction of onsets confirmed in those respective weeks: 52% of all cases confirmed through testing in week 11 had onset of symptoms in the same week. Even more notable: 66% of positive tests in week 12 are linked to onsets 1 week earlier: in week 11. For comparison, see Fig. 12

887 week 11. Testing in week 12 shows a significant peak for 899 illness to no earlier than March 9. The declining phase of 893 over week, their 2 weeks earlier fractions are larger, while 905 symptoms in week 11 is covered by robust testing from their fraction of same-week onsets is smaller than 30%.

impact of evolution of cases on the shape of the distribution of onsets of symtoms confirmed in a week of testing



Changes in the number of onsets of symptoms FIG. 13. from one week to the next can be estimated from the distribution of onsets of symptoms confirmed by testing in the latter week, if we group those onsets by week of onset. A Three different scenarios for the evolution of the number of cases are considered, whereby the number of onsets of symptoms per day is plotted. **B** Each case from A has a probability to be tested on every day. Half of the cases get tested within 8 days. The distribution is derived from observed data. C Number of onsets confirmed by the week of testing for each day of onset of symptoms. As a result of A and B. The shape of the distribution is characteristic for the change in cases and can be compared with Fig. 12, B. D As a last step the onsets confirmed by the testing in the highlighted week are summed up by week of onset and the group's respective fraction of the total number of positive tests in the highlighted week is computed. If no change in the number of cases occurs, more onsets in the week preceding testing are confirmed (45% of total) than from the same week as testing (35% of total). In case the number of cases rises, onsets from the same week as testing constitute the majority of onsets confirmed by tests in the week. If the number of cases declines, old onsets (older than 1 week) take over a significant fraction of total onsets tested in the week.

In Summary: Even though the number of total tests 947 performed changed until week 12, the available data indi- 948 cates **strong** exponential growth in new onsets of symptoms into week 11, constraining the peak in new onsets of 950

onsets 1 week earlier. That indicates the number of new 900 the wave is well documented. The exponential decline in onsets is comparable in week 11 and week 12 (see artificial 901 cases from week 13 onward is measured with consistent result, Fig. 12). Note, that a lower total number of tests 902 high level in the number of tests. As testing in one week is in week 11 amplifies this observation. Weeks 13 onward 903 shown to uncover onsets of symptoms in the 3 preceding show distributions which indicate decline in onsets week 904 weeks, the alleged period of the peak in new onsets of 906 weeks 12 and 13. Based on testing in weeks 12-13, the 907 peak can be identified at the end of week 11 or beginning 908 of week 12.

Available data on testing

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The epi bulletin [15] outlines the different networks that 911 the RKI uses to source information on testing: Voxco, 912 Resp Vir, the antibiotics-resistance-surveillance (ARS) [14] 913 and lab-accociation queries. These sources are compiled 914 into weekly data-sets with total number of tests and positive tests, which are published in the daily situation report once a week.

Data from the ARS contains daily number on testing and a separate weekly report is published on the RKI website. 919 The ARS dataset covers 25-30% of the total number of tests reported by the RKI, as only 62 of 180+ labs participate. The ARS data-set shows a mean delay between sampling and testing between 1 and 1.2 days except for weeks 12 to 15, where the delay is 1.5 days, peaking in 924 week 13 at 1.8 days.

925 An overview of all publicly available data on testing for 926 march 2020 is presented in Fig. 9. The following observations along with additional comments are based on this presentation:

- From week 8 to week 12 the number of tests rises week to week by a factor greater than 2. 120k is a combined number for weeks up to 10. Individual numbers of tests for those weeks has to be estimated with help from the ARS-subset (Fig. 9 B may26 lab. Surveilance). Assuming ARS is representative the number of test performed in week 10 should be around 60k, 30k in week 9 and 30k in all weeks up to and including 8, extending the exponential pattern.
- The number of tests remains on a high level from week 12 on. In the range of 340-430k.
- The number of positive test rises faster than the total number of tests until week 14.
- The fraction of positive tests per week peaks around 10%, relatively low compared with neighbouring countries.
- The fraction of positive tests per day varies with time from 2% around March 1 to around 10% in weeks 13 and 14, peaking at 14% at the end of March. Afterwards declining to less than 2\% in week 20 (not shown in figure). The day-to-day rise

weekly average would suggest.

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- The increase in the fraction of positive tests does not correlate to the rise in number of reported cases until week 13, but correlates with the decline in reported cases from week 13 on, which is expected as the total number of tests fluctuates around 380k tests per week on a high level. The correlation with the epi-curve is coincidental.
- of tests is lower (daily total number not shown in 1002 our present knowledge. the figure). Deviating from the rise in the positive 1003 of positive results than week 9.
- The maximum test-capacity per week as reported by growth in number of tests performed (not shown).

972 Additional information relevant to the discussion can be found in the publications cited earlier. For the total data-set, the fraction of positive tests varies from 1.5 to 7.2% for different states. Not a single day of testing for 976 individual states exceeded 20% positive results.

SUMMARY & CONCLUSIONS

dressed questions and comments regarding our recent 1022 onset of the pandemic is presumably affected by a rise in publication [1]. First, we compared direct, model-free 1023 test capacities, the crucial part of our analysis is based estimates of the reproduction number to the ones ob- 1024 on a regime of comparably stable testing. In particular, tained from dynamical modeling. To this end, we es-1025 we find that the inference of the second and third change tablished synthetic ground-truth data based on an SIR 1026 point is unaffected by testing. model and subsequently inferred the reproduction num- 1027 ber based on various complementary approaches that are 1028 our previously reported results with respect to statistical in practical use. We reveal how sudden changes in the 1029 and dynamical modeling assumptions as well as comple-987 spreading rate, as expected from the broad implemen-1030 mentary data sources and provides additional support for 988 tation of non-pharmaceutical interventions, can lead to 1031 the central conclusions of our publication [1].

in week 10 and 11 is more pronounced than the 989 counter-intuitive transient drops in new reported cases. 990 Most importantly, we find that only modeling of spreading 991 dynamics can correctly capture effects of sudden changes in the spreading rate.

Second, we provided extensive background on our mod-994 eling rationale which combines differential-equation based modeling of dynamics with Bayesian parameter infer-996 ence and formal model comparison. Within the Bayesian 997 framework, we argue that based on prior knowledge, the 998 most plausible models explaining the data can be system-• The ARS data shows a steady day to day increase in 999 atically identified and also updated as new information positive fraction of test in weeks 10 and 11. Week-1000 becomes available. We also discuss why we do not think ends show a higher fraction, while the total number 1001 that models based on herd immunity are plausible given

Third, we analyzed additional data on the COVID-19 fraction, weeks up to 8 have a 3 times higher fraction 1004 spread in Germany, which has become available since 1005 the completion of the analysis presented in [1]. Most 1006 importantly, we include data sets from the German Robert 1007 Koch Institute based on the reporting date as well as based the labs increased to 1M in week 19, showing strong 1008 on the onset of symptoms (epi curve). We analyzed the growth till week 14. A week to week doubling in test 1009 data in the framework of SIR and SEIR models, and we capacity continues for two more weeks compared to 1010 also tested a broad range of varying prior assumptions. 1011 We find our results to be robust across these varying 1012 modeling assumptions and data sets, and to support the 1013 conclusions drawn in [1]. In turn, this leads us to conclude 1014 that under the conditions comparable to those in Germany, 1015 models based on reporting date are a viable alternative 1016 for analyzing the early stages of a disease outbreak, before 1017 the epi curve becomes available — as long as the reporting 1018 delay is properly modeled.

Finally, we address the issue of changes in the testing 1020 capacities and procedures over the course of our analysis. In these technical notes, we have comprehensively ad-1021 Most importantly, we find that while data from the initial

Overall, the analysis here evaluates the robustness of

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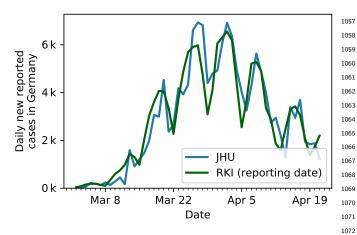


FIG. 14. Comparison of the German case numbers as pub- 1073 [15] lished by the John Hopkins University (JHU) used in our 1074 previous publication [1], to the case number of the Robert 1075 Koch Institute (RKI). The difference is limited.

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VII. SUPPLEMENTARY INFORMATION: FIGURES

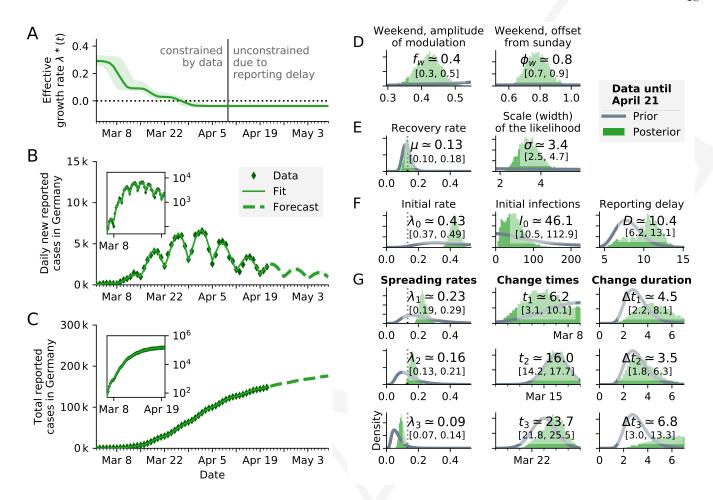


FIG. 15. SIR model (see Fig. 3 of [1]) using the reporting date (Meldedatum) of the RKI data for inference. A Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

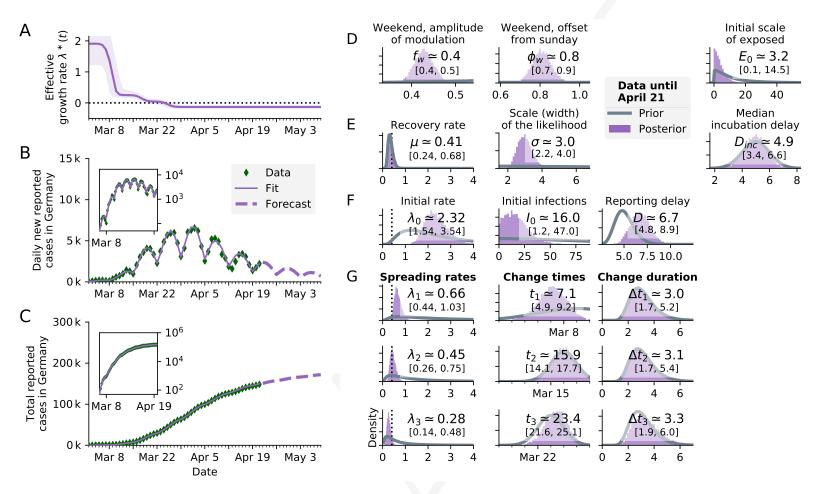


FIG. 16. SEIR-like model (see Fig. S3 in Supplementary Information of [1]) using the **reporting date (Meldedatum) of** the RKI data for inference. A: Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. Note: Due to different model dynamics, $\lambda^*(t)$ can only be compared qualitatively between SEIR and SIR models. The numeric values of the rates (μ, λ) etc.) differ between models because they reflect the duration a person remains in a given compartment. B: Comparison of daily new reported cases and the model (purple solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. Note: We currently do not (yet) incorporate the uncertainties that are introduced by nowcasting, compared to using the reported cases. This leads to over-confident parameter estimates, including the effective spreading rate $\lambda^*(t)$; the shown uncertainties are underestimated. C: Comparison of total reported cases and the model (same representation as in B). D-G: Priors (gray lines) and posteriors (purple histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

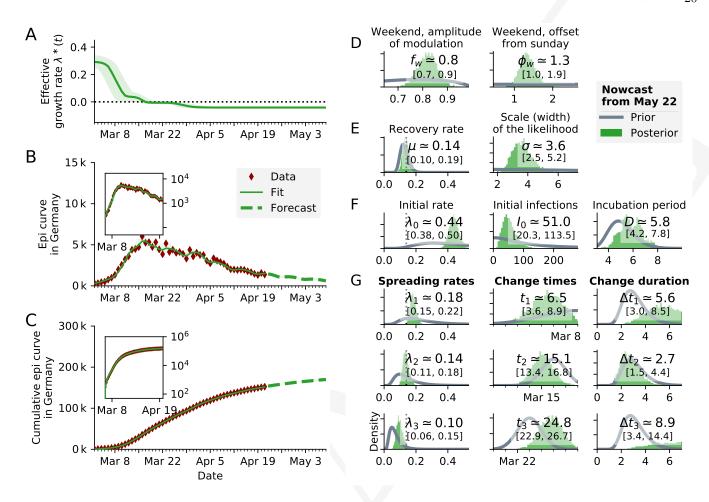


FIG. 17. SIR model using the onset of symptoms (nowcast from May 22) of the RKI data for inference. The median of the lognormal prior of the delay between infection and onset of symptoms has been set to 5 days (right-most panel F). A: Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. B: Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset: same data in log-lin scale. Note: We currently do not (yet) incorporate the uncertainties that are introduced by nowcasting, compared to using the reported cases. This leads to over-confident parameter estimates, including the effective spreading rate $\lambda^*(t)$; the shown uncertainties are underestimated. C: Comparison of total reported cases and the model (same representation as in B). D-G: Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

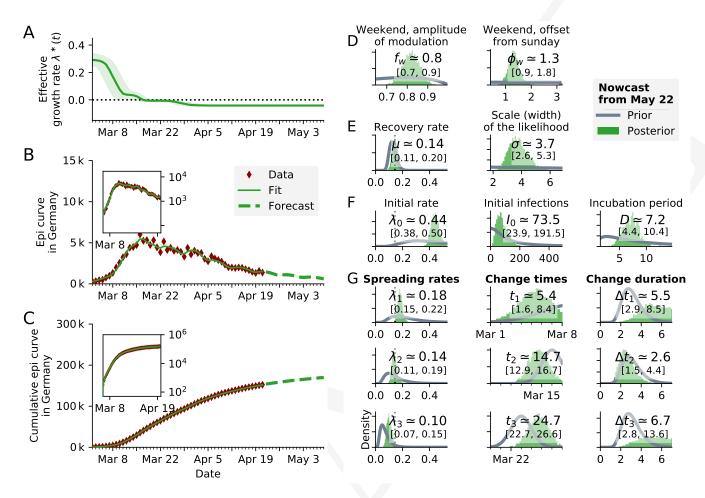


FIG. 18. SIR model using the onset of symptoms (nowcast from May 22) of the RKI data for inference. The median of the lognormal prior of the delay between infection and onset of symptoms has been set to a relatively uninformative prior (right-most panel F). The posterior of the delay has as median 7.2 days, which is close to the expected incubation period of 5 days. A Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

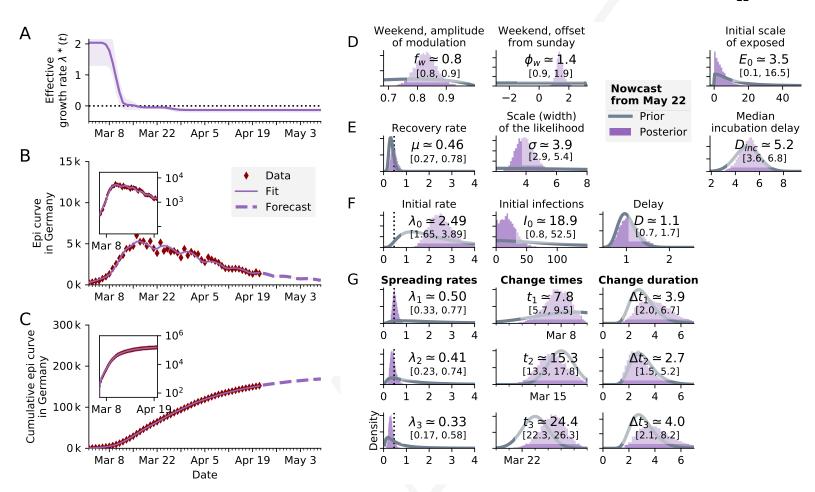


FIG. 19. **SEIR-like model using the onset of symptoms** (nowcast from May 22) of the RKI data for inference. The median of the lognormal prior of the delay between infectious and onset of symptoms has been set to 1 day (right-most panel F). **A** Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. **B** Comparison of daily new reported cases and the model (purple solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); **inset** same data in log-lin scale. **C** Comparison of total reported cases and the model (same representation as in B). **D**–**G** Priors (gray lines) and posteriors (purple histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

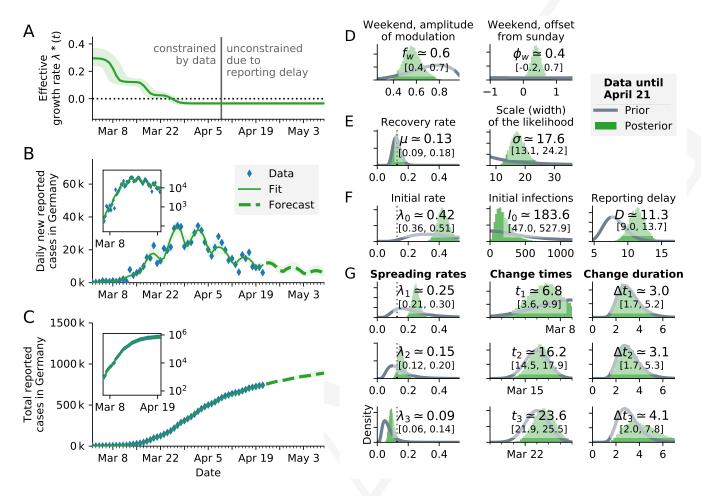


FIG. 20. SIR model with reported case number multiplied by 5, to account for an eventual factor five of unknown cases. Results are nearly identical to original non-multiplied plot (Fig 3. in [1]), showing that a constant underreporting has a negligible effect. The median inferred spreading rates λ are about 0.01 larger. A Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.

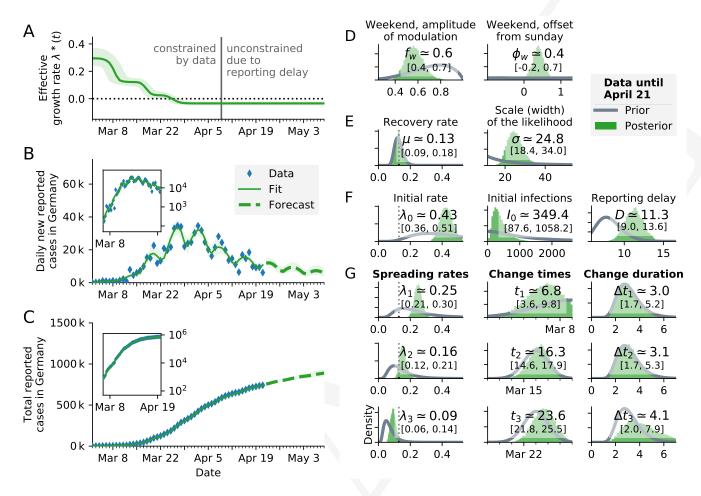


FIG. 21. SIR model with reported case number multiplied by 10, to account for an eventual factor 10 of unknown cases. Results are nearly identical to original non-multiplied plot (Fig 3. in [1]), showing that a constant under-reporting has a negligible effect, similar to Fig. 20. The median inferred spreading rates λ are 0.01-0.02 larger. A Time-dependent model estimate of the effective spreading rate $\lambda^*(t)$. B Comparison of daily new reported cases and the model (green solid line for median fit with 95% credible intervals, dashed line for median forecast with 95% CI); inset same data in log-lin scale. C Comparison of total reported cases and the model (same representation as in B). D–G Priors (gray lines) and posteriors (green histograms) of all model parameters; inset values indicate the median and 95% credible intervals of the posteriors.