

Introduction to Classification

Classification is the process of categorizing data or objects into **predefined** classes or categories based on their features or attributes.

In **Machine Learning**, classification is a type of **supervised learning** where an algorithm is trained on a labeled dataset to predict the class or category of new, unseen data.

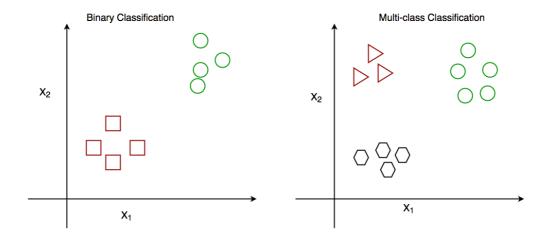
Objective of Classification

The main goal of classification is to build a model that can accurately assign a label or category to a new observation based on its features.

Example

- Problem: Classify images as either "dogs" or "cats."
- Dataset: Labeled images of dogs and cats.
- Features: Attributes such as color, texture, and shape.
- Goal: Predict whether a new, unseen image belongs to the "dog" or "cat" class.

Types of Classification



1. Binary Classification

In binary classification, the task is to classify the input into one of **two possible** classes.

Example

- Scenario: Predict if a person has a disease based on their health data.
- Classes:

- Positive Class: The person has the disease.
- Negative Class: The person does not have the disease.
- Features: Blood pressure, cholesterol level, age, etc.

Patient ID	Blood Pressure (mmHg)	Cholesterol (mg/dL)	Disease (Yes/No)
1	120	200	Yes
2	130	180	No
3	140	250	Yes
4	115	170	No

2. Multiclass Classification

In multiclass classification, the task is to classify the input into one of **several possible classes**.

Example

- Scenario: Classify flower species based on petal and sepal dimensions.
- Classes: Iris Setosa, Iris Versicolor, Iris Virginica.
- Features: Petal length, petal width, sepal length, sepal width.

Sample ID	Petal Length (cm)	Petal Width (cm)	Species
1	1.4	0.2	Iris Setosa
2	4.7	1.4	Iris Versicolor
3	5.5	2.1	Iris Virginica
4	1.5	0.3	Iris Setosa

Key Takeaways

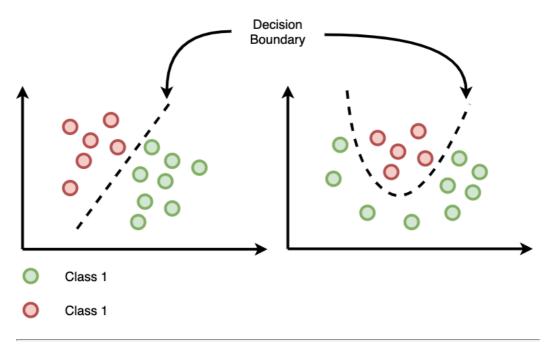
- 1. **Classification** involves predicting predefined categories or labels based on input features.
- 2. **Binary Classification** deals with two possible classes, while **Multiclass Classification** handles multiple categories.
- 3. Real-world applications include **spam detection**, **medical diagnosis**, and **image classification**.

By understanding the types and examples of classification, you can better design and implement models to solve a wide range of problems in machine learning.

Classification Algorithms

Classification algorithms are used to predict the category or class of a given observation based on its features. These algorithms can be broadly categorized into **Linear** and **Non-linear** classifiers, with a special mention for **Ensemble**

learning methods.



1. Linear Classifiers

Definition

Linear classifiers create a **linear decision boundary** between classes. They are simple, computationally efficient, and work well when the data is linearly separable.

Examples of Linear Classifiers

1. Logistic Regression

- **Description**: Predicts the probability of a binary class outcome using a logistic function.
- Use Case: Spam detection.

2. Support Vector Machines (SVM) with Kernel = 'linear'

- **Description**: Maximizes the margin between classes with a linear boundary.
- Use Case: Text classification.

3. Single-Layer Perceptron

- **Description**: A basic neural network layer that classifies linearly separable data.
- Use Case: Predicting customer churn.

4. Stochastic Gradient Descent (SGD) Classifier

- **Description**: Optimizes the model by minimizing the loss function using stochastic gradient descent.
- Use Case: Large-scale classification tasks.

2. Non-linear Classifiers

Definition

Non-linear classifiers create a **non-linear decision boundary**, allowing them to capture complex relationships between features and target variables.

Examples of Non-linear Classifiers

1. K-Nearest Neighbours (KNN)

- Description: Classifies data points based on the majority vote of their knearest neighbors.
- Use Case: Handwritten digit recognition.

2. Kernel SVM

- **Description**: Extends SVM with non-linear kernels like RBF or polynomial.
- Use Case: Image classification.

3. Naive Bayes

- **Description**: A probabilistic classifier based on Bayes' theorem.
- Use Case: Sentiment analysis.

4. Decision Tree Classification

- Description: Splits the data into subsets based on feature values, creating a tree-like structure.
- **Use Case**: Predicting customer segmentation.

3. Ensemble Learning Classifiers

Definition

Ensemble learning combines predictions from multiple models to improve overall accuracy and robustness.

Examples of Ensemble Classifiers

1. Random Forests

- Description: An ensemble of decision trees built using bootstrapped datasets.
- **Use Case**: Loan approval prediction.

2. AdaBoost

- Description: Combines weak classifiers iteratively to create a strong classifier.
- Use Case: Fraud detection.

3. Bagging Classifier

- **Description**: Aggregates predictions from multiple base models trained on random subsets of the data.
- Use Case: Credit scoring.

4. Voting Classifier

- **Description**: Combines predictions from multiple classifiers using majority voting.
- Use Case: Diagnosing diseases.

5. ExtraTrees Classifier

- Description: Similar to Random Forest but uses random thresholds for splitting.
- Use Case: Stock market predictions.

4. Multi-layer Artificial Neural Networks (ANN)

Description

ANNs are a class of deep learning models consisting of multiple layers of interconnected nodes (neurons). They can handle highly complex and non-linear relationships.

• **Use Case**: Image recognition, speech recognition, and natural language processing.

Choosing the Right Classifier

Scenario	Recommended Algorithm
Linear relationships in data	Logistic Regression, Linear SVM
Complex non-linear relationships	Kernel SVM, Decision Trees
Robust performance across large datasets	Random Forest, AdaBoost
Handling imbalanced datasets	Ensemble methods (e.g., Bagging)
High-dimensional data	Naive Bayes, Neural Networks

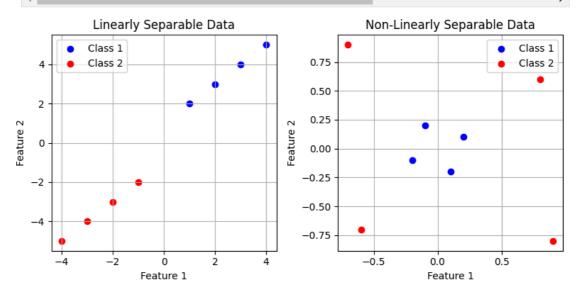
By understanding the strengths of each classification algorithm, you can select the most appropriate one for your problem domain and dataset characteristics.

```
In []: # Import necessary libraries
import matplotlib.pyplot as plt

# Predefined linearly separable data
linear_x1 = [[1, 2], [2, 3], [3, 4], [4, 5]] # Class 1 points
linear_x2 = [[-1, -2], [-2, -3], [-3, -4], [-4, -5]] # Class 2 point

# Predefined non-linearly separable data
nonlinear_x1 = [[0.2, 0.1], [0.1, -0.2], [-0.2, -0.1], [-0.1, 0.2]]
```

```
nonlinear x2 = [[0.8, 0.6], [-0.7, 0.9], [0.9, -0.8], [-0.6, -0.7]]
# Convert to separate x and y coordinates for easier plotting
linear x1 = list(zip(*linear x1))
linear x2 = list(zip(*linear x2))
nonlinear x1 = list(zip(*nonlinear x1))
nonlinear x2 = list(zip(*nonlinear x2))
# Plot linearly separable data
plt.figure(figsize=(8, 4))
plt.subplot(1, 2, 1)
plt.scatter(linear_x1[0], linear_x1[1], color='blue', label='Class 1'
plt.scatter(linear x2[0], linear x2[1], color='red', label='Class 2')
plt.title("Linearly Separable Data")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.legend()
plt.grid(True)
# Plot non-linearly separable data
plt.subplot(1, 2, 2)
plt.scatter(nonlinear x1[0], nonlinear x1[1], color='blue', label='Cl
plt.scatter(nonlinear x2[0], nonlinear x2[1], color='red', label='Cla
plt.title("Non-Linearly Separable Data")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.legend()
plt.grid(True)
plt.tight_layout()
plt.show()
```



Evaluating a Classification Model

Evaluating a classification model is a critical step in machine learning to assess its **performance** and **generalization ability** on unseen data. Several metrics can be used for this purpose, depending on the specific problem and requirements.

1. Popular Evaluation Metrics

1.1 Accuracy

Definition:

Accuracy is the ratio of the number of correct predictions to the total number of predictions.

$$Accuracy = \frac{Number of Correct Predictions}{Total Number of Predictions}$$

- Strengths: Simple and intuitive.
- Limitations: Can be misleading in imbalanced datasets.

Example:

Suppose we have a spam classification task with 1,000 emails:

- 950 are **not spam** (Negative class).
- 50 are **spam** (Positive class).

If the model predicts all emails as **not spam**, the accuracy will be:

Accuracy =
$$\frac{950}{1000} = 95\%$$

Issue: Despite high accuracy, the model fails to identify any spam emails, making it unsuitable for this task.

2. Confusion Matrix

The **Confusion Matrix** groups classification results into four categories:

Actual Values

Positive (1) Negative (0)

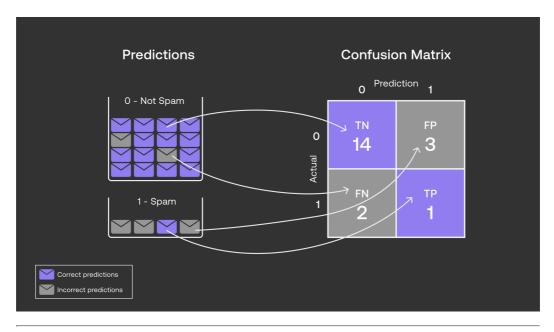
Positive (1) TP FP

Negative (0) FN TN

Definitions:

• True Positive (TP): Correctly predicted as positive.

- True Negative (TN): Correctly predicted as negative.
- False Positive (FP): Predicted positive but is actually negative.
- False Negative (FN): Predicted negative but is actually positive.



Type 1 and Type 2 Errors in Classification

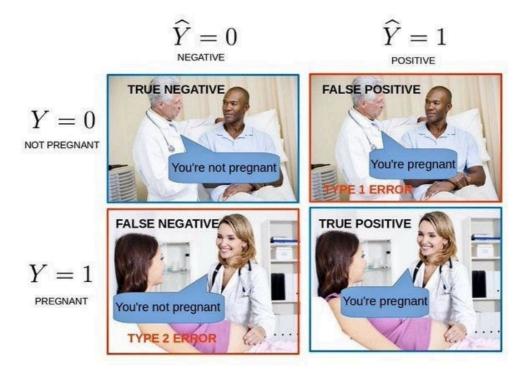
• Type 1 Error (False Positive):

Occurs when the model incorrectly predicts a negative instance as positive.

- **Example**: A healthy patient is diagnosed with a disease.
- Impact: Can lead to unnecessary actions or treatments.
- Type 2 Error (False Negative):

Occurs when the model incorrectly predicts a positive instance as negative.

- **Example**: A patient with a disease is diagnosed as healthy.
- **Impact**: Critical in cases like medical diagnosis, as it may delay necessary treatment.



3. Precision

Definition:

Precision measures the proportion of true positives out of all positive predictions:

$$Precision = \frac{TP}{TP + FP}$$

- Focus: Highlights how many predicted positives are actually correct.
- Use Case: Important when the cost of false positives is high.

Example:

In spam detection, Precision measures how many emails flagged as spam are actually spam.

4. Recall (Sensitivity)

Definition:

Recall (also known as Sensitivity) measures the proportion of true positives out of all actual positives:

$$Recall = \frac{TP}{TP + FN}$$

- Focus: Highlights how many actual positives are correctly identified.
- Use Case: Important when the cost of false negatives is high.

Example:

In spam detection, Recall measures how many actual spam emails are correctly detected.

5. Precision vs Recall

Tradeoff:

- Improving **Precision** often reduces **Recall**, and vice versa.
- The choice depends on the specific task:
 - For spam detection, prioritize **Precision** to avoid important emails being flagged as spam.
 - For disease detection, prioritize **Recall** to minimize missed diagnoses.

Scenario A Scenario B

High Precision, Low Recall High Recall, Low Precision

O Prediction 1

O Prediction 1

O More pon-span



6. F1 Score

Definition:

The **F1 Score** provides a balance between Precision and Recall:

$$F1 = 2 imes rac{ ext{Precision} imes ext{Recall}}{ ext{Precision} + ext{Recall}}$$

• **Use Case**: Useful when both Precision and Recall are equally important.

Example:

For a model with Precision = 0.8 and Recall = 0.6:

$$F1 = 2 imes rac{0.8 imes 0.6}{0.8 + 0.6} = 2 imes rac{0.48}{1.4} = 0.686$$

7. Choosing the Right Metric

- Accuracy: Suitable for balanced datasets.
- Precision: Prioritize when false positives have higher costs.
- Recall: Prioritize when false negatives have higher costs.
- F1 Score: Use when you need a balance between Precision and Recall.

Summary

- Accuracy is simple but insufficient for imbalanced datasets.
- The **Confusion Matrix** helps understand the distribution of predictions.
- Metrics like Precision, Recall, and F1 Score provide deeper insights into model performance.
- Choosing the right metric depends on the specific task and its requirements.

```
import numpy as np
from sklearn.metrics import confusion_matrix, accuracy_score, precisi

# Binary vectors
y_true = np.array([1, 0, 1, 1, 0, 0, 1, 1]) # Actual labels
y_pred = np.array([1, 0, 0, 1, 1, 0, 1, 0]) # Predicted labels

# Confusion Matrix
```

```
26/02/2025, 16:32
                  machine_learning/Class/4_Classification_Task_and_Evaluation_Metrics.ipynb at main · sujoysarkarcs/machin...
                 # CUIIIUSTUII MALITX
                 cm = confusion matrix(y true, y pred)
                 tn, fp, fn, tp = cm.ravel()
                 print("Confusion Matrix:")
                 print(cm)
                 print(f"True Negative (TN): {tn}, False Positive (FP): {fp}, False N€
                 # Accuracy
                 accuracy = accuracy_score(y_true, y_pred)
                 print(f"\nAccuracy: {accuracy:.2f}")
                 # Precision
                 precision = precision_score(y_true, y_pred)
                 print(f"Precision: {precision:.2f}")
                 # Recall
                 recall = recall score(y true, y pred)
                 print(f"Recall: {recall:.2f}")
                 # F1 Score
                 f1 = f1 score(y true, y pred)
                 print(f"F1 Score: {f1:.2f}")
               Confusion Matrix:
               [[2 1]
                [2 3]]
               True Negative (TN): 2, False Positive (FP): 1, False Negative (FN): 2,
               True Positive (TP): 3
               Accuracy: 0.62
               Precision: 0.75
               Recall: 0.60
               F1 Score: 0.67
       In [ ]:
                 from sklearn.metrics import classification_report
                 # Generate Classification Report
                 report = classification_report(y_true, y_pred, target_names=['Class @
                 print("Classification Report:\n")
                 print(report)
               Classification Report:
                              precision
                                           recall f1-score
                                                                support
                    Class 0
                                   0.50
                                              0.67
                                                        0.57
                                                                      3
                    Class 1
                                   0.75
                                                        0.67
                                                                      5
                                              0.60
                                                        0.62
                                                                      8
                   accuracy
                  macro avg
                                   0.62
                                              0.63
                                                        0.62
                                                                      8
               weighted avg
                                   0.66
                                              0.62
                                                        0.63
       In [ ]:
                 import numpy as np
                 import matplotlib.pyplot as plt
                 import seaborn as sns
```

```
https://github.com/sujoysarkarcs/machine_learning/blob/main/Class/4_Classification_Task_and_Evaluation_Metrics.ipynb
```

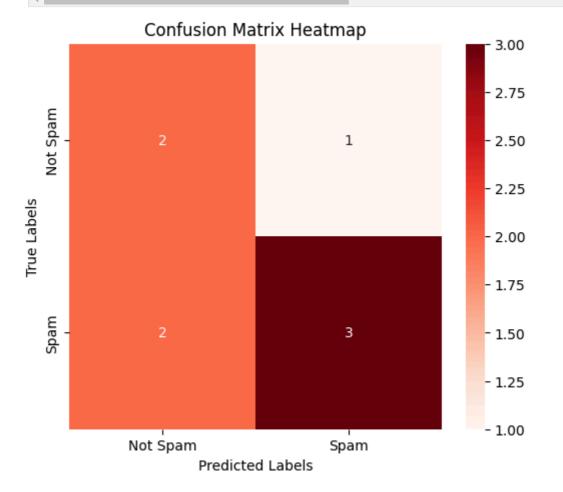
from sklearn.metrics import confusion matrix

Example data

```
y_true = np.array([1, 0, 1, 1, 0, 0, 1, 1]) # Actual labels
y_pred = np.array([1, 0, 0, 1, 1, 0, 1, 0]) # Predicted labels

# Compute confusion matrix
cm = confusion_matrix(y_true, y_pred)

# Plot confusion matrix heatmap
plt.figure(figsize=(6, 5))
sns.heatmap(cm, annot=True, fmt='d', cmap='Reds', xticklabels=['Not splt.xlabel('Predicted Labels')
plt.ylabel('True Labels')
plt.title('Confusion Matrix Heatmap')
plt.show()
```



Multi-Class Classification

When we have more than two classes (e.g., Class 0, Class 1, Class 2), classification tasks become **multi-class classification** problems. The metrics for binary classification like **Accuracy**, **Precision**, **Recall**, and **F1 Score** can still be applied, but with some modifications.

1. Dataset Example

Let's consider a **customer support email classification** problem with three classes:

- Class 0: Shipping
- Class 1: Returns
- Class 2: Tracking

Below is the example dataset showing Actual vs Predicted values:

	Email	Actual	Predicted
1	Do you offer same day shipping?	0 - Shipping	0 - Shipping
2	Can you ship to Italy?	0 - Shipping	0 - Shipping
3	How long does shipping take?	0 - Shipping	2 - Tracking
4	Can I buy online and pick up in store?	0 - Shipping	0 - Shipping
5	What are your shipping options?	0 - Shipping	2 - Tracking
6	My order arrived damaged, can I get a refund?	1 - Returns	1 - Returns
7	You sent me the wrong item	1 - Returns	1 - Returns
8	I want to exchange my item for another colour	1 - Returns	1 - Returns
9	I ordered something and it wasn't what I expected. Can I return it?	1 - Returns	0 - Shipping
10	What's your return policy?	1 - Returns	1 - Returns
11	Where's my package?	2 - Tracking	1 - Returns
12	When will my order arrive?	2 - Tracking	1 - Returns
13	What's my shipping number?	2 - Tracking	2 - Tracking
14	Which carrier is my package with?	2 - Tracking	2 - Tracking
15	Is my package delayed?	2 - Tracking	2 - Tracking
	71 0		

2. Confusion Matrix

For multi-class problems, the confusion matrix becomes a **3x3 matrix**. Each row represents the **actual class**, and each column represents the **predicted class**.



3. Accuracy

Accuracy is calculated as:

$$\label{eq:accuracy} \text{Accuracy} = \frac{\text{Correct Predictions}}{\text{Total Predictions}}$$

- Correct Predictions = (3 + 4 + 3 = 10)
- Total Predictions = (15)

Accuracy:

$$Accuracy = \frac{10}{15} = 67\%$$

4. Precision, Recall, and F1 Score (Per Class)

Class 0 - Shipping

• Precision:

$$Precision = \frac{TP}{TP + FP} = \frac{3}{3+1} = 75\%$$

Recall:

$$ext{Recall} = rac{ ext{TP}}{ ext{TP} + ext{FN}} = rac{3}{3+2} = 60\%$$

• F1 Score:

$$F1 = 2 imes rac{ ext{Precision} imes ext{Recall}}{ ext{Precision} + ext{Recall}} = 67\%$$

Class 1 - Returns

• Precision:

$$\text{Precision} = \frac{4}{4+2} = 67\%$$

• Recall:

$$Recall = \frac{4}{4+1} = 80\%$$

• F1 Score:

$$F1 = 2 imes rac{67 imes 80}{67 + 80} = 79\%$$

Class 2 - Tracking

• Precision:

$$Precision = \frac{3}{3+2} = 60\%$$

• Recall:

$$\text{Recall} = \frac{3}{3+2} = 60\%$$

• F1 Score:

$$F1 = 2 imes rac{60 imes 60}{60 + 60} = 53\%$$

5. Macro-Average Precision, Recall, and F1 Score

When dealing with multi-class problems, we use **Macro-Average** to summarize the metrics across all classes.

Macro-Average Precision:

$$ext{Macro Precision} = rac{ ext{Precision}_0 + ext{Precision}_1 + ext{Precision}_2}{3} \ ext{Macro Precision} = rac{75 + 67 + 60}{3} = 67.3\%$$

Macro-Average Recall:

$$ext{Macro Recall} = rac{ ext{Recall}_0 + ext{Recall}_1 + ext{Recall}_2}{3} \ ext{Macro Recall} = rac{60 + 80 + 60}{3} = 66.7\%$$

Macro-Average F1 Score:

$$\begin{aligned} \text{Macro F1} &= \frac{F1_0 + F1_1 + F1_2}{3} \\ \text{Macro F1} &= \frac{67 + 79 + 53}{3} = 66.3\% \end{aligned}$$

6. Summary Table

Class	Precision	Recall	F1 Score
0 - Shipping	75%	60%	67%
1 - Returns	67%	80%	79%
2 - Tracking	60%	60%	53%
Macro-Average	67.3%	66.7%	66.3%

Conclusion

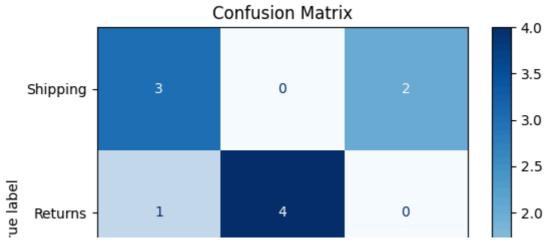
- 1. **Confusion Matrix** helps in understanding misclassifications for each class.
- 2. Precision, Recall, and F1 Score can be computed per class.
- 3. **Macro-Average** provides a single value for each metric, summarizing overall performance.

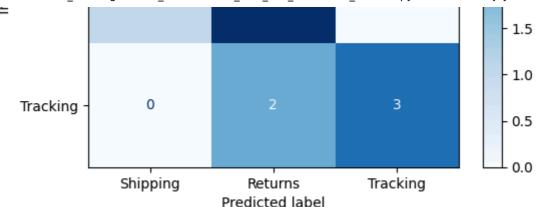
These metrics are critical in evaluating multi-class classification models, ensuring a balanced understanding of their strengths and weaknesses.

```
"Iracking", "Iracking", "Iracking", "Iracking", "Iracking",
"Returns", "Returns", "Tracking", "Tracking", "Tracking"]
# Unique class labels
class labels = ["Shipping", "Returns", "Tracking"]
# Compute confusion matrix
conf_matrix = confusion_matrix(y_true, y_pred, labels=class_labels)
print("Confusion Matrix:\n", conf matrix)
# Plot the confusion matrix
disp = ConfusionMatrixDisplay(confusion matrix=conf matrix, display 1
disp.plot(cmap="Blues")
plt.title("Confusion Matrix")
plt.show()
# Calculate Accuracy
accuracy = accuracy score(y true, y pred)
print(f"Accuracy: {accuracy:.2f}")
# Calculate Precision, Recall, and F1 Score (Per Class and Macro-Aver
precision = precision_score(y_true, y_pred, average=None, labels=clas
recall = recall_score(y_true, y_pred, average=None, labels=class_labels
f1 = f1 score(y true, y pred, average=None, labels=class labels)
macro_precision = precision_score(y_true, y_pred, average='macro')
macro recall = recall score(y true, y pred, average='macro')
macro_f1 = f1_score(y_true, y_pred, average='macro')
# Display Metrics
print("\nClass-wise Metrics:")
for i, label in enumerate(class labels):
    print(f"Class '{label}' -> Precision: {precision[i]*100:.2f}%, R€
print("\nMacro-Averaged Metrics:")
print(f"Precision: {macro_precision*100:.2f}%")
print(f"Recall: {macro_recall*100:.2f}%")
print(f"F1 Score: {macro_f1*100:.2f}%")
```

Confusion Matrix:

[[3 0 2] [1 4 0] [0 2 3]]





Accuracy: 0.67

Class-wise Metrics:

Class 'Shipping' -> Precision: 75.00%, Recall: 60.00%, F1: 66.67% Class 'Returns' -> Precision: 66.67%, Recall: 80.00%, F1: 72.73% Class 'Tracking' -> Precision: 60.00%, Recall: 60.00%, F1: 60.00%

Macro-Averaged Metrics:

Precision: 67.22% Recall: 66.67% F1 Score: 66.46%

```
In [ ]:
```

Classification Report:

	precision	recall	fl-score	support
Shipping Returns Tracking	0.67 0.75 0.60	0.80 0.60 0.60	0.73 0.67 0.60	5 5 5
accuracy macro avg weighted avg	0.67 0.67	0.67 0.67	0.67 0.66 0.66	15 15 15

Additional Metrics for Evaluating Classification Models

In addition to Accuracy, Precision, Recall, and F1-Score, there are other important metrics for evaluating classification models. These include **Specificity**, **ROC-AUC Curve**, and **Log Loss**. Each metric provides unique insights into model performance.

1. Specificity

Definition

Specificity measures the proportion of **actual negatives** that are correctly identified as negative. It is also known as the **True Negative Rate**.

$$Specificity = \frac{True Negatives (TN)}{True Negatives (TN) + False Positives (FP)}$$

Key Points

- Specificity complements Recall (True Positive Rate) to give a holistic understanding of model performance.
- A high specificity means the model has fewer False Positives.

When to Use

Specificity is particularly useful when correctly identifying negatives is critical.

• **Example**: In fraud detection, it is important to minimize False Positives to avoid flagging legitimate transactions.

2. ROC-AUC Curve

Definition

- The ROC (Receiver Operating Characteristic) curve is a graphical plot that shows the tradeoff between the True Positive Rate (Recall) and the False Positive Rate as the decision threshold changes.
- The AUC (Area Under the Curve) represents the probability that the model will rank a randomly chosen positive instance higher than a randomly chosen negative one.

False Positive Rate = 1 - Specificity

Interpretation

- AUC = 1: Perfect classifier (ideal).
- AUC = 0.5: Random guessing.
- **Higher AUC**: Indicates better model performance.

When to Use

- Use ROC-AUC when you need to evaluate how well the model separates positive and negative classes across different thresholds.
- **Example**: Medical diagnosis models where balancing False Positives and False Negatives is critical.

```
In [ ]:
         # Import libraries
         from sklearn.metrics import confusion matrix, roc auc score, roc curv
         import numpy as np
         import matplotlib.pyplot as plt
         # Actual labels and predicted probabilities
         y \text{ true} = [1, 0, 1, 0, 0, 1, 0, 0, 1, 1]
         y pred prob = [0.9, 0.2, 0.8, 0.7, 0.3, 0.85, 0.1, 0.4, 0.95, 0.05]
         # Convert probabilities to binary predictions (threshold = 0.5)
         y pred = [1 \text{ if prob} >= 0.5 \text{ else } 0 \text{ for prob in y pred prob}]
         # Compute Confusion Matrix
         tn, fp, fn, tp = confusion matrix(y true, y pred).ravel()
         # Calculate Specificity
         specificity = tn / (tn + fp)
         print(f"Specificity: {specificity:.2f}")
         # Calculate ROC-AUC Score
         roc auc = roc auc score(y true, y pred prob)
         print(f"ROC-AUC Score: {roc auc:.2f}")
         # Plot ROC Curve
         fpr, tpr, thresholds = roc curve(y true, y pred prob)
         plt.figure(figsize=(8, 6))
         plt.plot(fpr, tpr, color='blue', lw=2, label=f'ROC curve (AUC = {roc
         plt.plot([0, 1], [0, 1], color='grey', linestyle='--')
         plt.xlabel('False Positive Rate')
         plt.ylabel('True Positive Rate')
         plt.title('ROC Curve')
         plt.legend(loc="lower right")
         plt.grid()
         plt.show()
       Specificity: 0.80
       ROC-AUC Score: 0.80
       Log Loss: 0.59
                                         ROC Curve
```