### Introduction to Classification

Classification is the process of categorizing data or objects into **predefined classes** or **categories** based on their features or attributes.

In **Machine Learning**, classification is a type of **supervised learning** where an algorithm is trained on a labeled dataset to predict the class or category of new, unseen data.

# **Objective of Classification**

The main goal of classification is to build a model that can accurately assign a label or category to a new observation based on its features.

### Example

- Problem: Classify images as either "dogs" or "cats."
- Dataset: Labeled images of dogs and cats.
- **Features**: Attributes such as color, texture, and shape.
- Goal: Predict whether a new, unseen image belongs to the "dog" or "cat" class.

# **Types of Classification**

### 1. Binary Classification

In binary classification, the task is to classify the input into one of **two possible classes**.

### Example

- **Scenario**: Predict if a person has a disease based on their health data.
- Classes:
  - Positive Class: The person has the disease.
  - Negative Class: The person does not have the disease.
- Features: Blood pressure, cholesterol level, age, etc.

Patient ID	Blood Pressure (mmHg)	Cholesterol (mg/dL)	Disease (Yes/No)
1	120	200	Yes
2	130	180	No
3	140	250	Yes
4	115	170	No

### 2. Multiclass Classification

In multiclass classification, the task is to classify the input into one of **several possible classes**.

#### Example

- **Scenario**: Classify flower species based on petal and sepal dimensions.
- Classes: Iris Setosa, Iris Versicolor, Iris Virginica.
- Features: Petal length, petal width, sepal length, sepal width.

Sample ID	Petal Length (cm)	Petal Width (cm)	Species
1	1.4	0.2	Iris Setosa
2	4.7	1.4	Iris Versicolor
3	5.5	2.1	Iris Virginica
4	1.5	0.3	Iris Setosa

### **Key Takeaways**

- Classification involves predicting predefined categories or labels based on input features.
- 2. **Binary Classification** deals with two possible classes, while **Multiclass Classification** handles multiple categories.
- 3. Real-world applications include **spam detection**, **medical diagnosis**, and **image classification**.

By understanding the types and examples of classification, you can better design and implement models to solve a wide range of problems in machine learning. []

# **Classification Algorithms**

Classification algorithms are used to predict the category or class of a given observation based on its features. These algorithms can be broadly categorized into **Linear** and **Non-linear** classifiers, with a special mention for **Ensemble learning methods**.

### 1. Linear Classifiers

### **Definition**

Linear classifiers create a **linear decision boundary** between classes. They are simple, computationally efficient, and work well when the data is linearly separable.

### **Examples of Linear Classifiers**

- 1. Logistic Regression
  - Description: Predicts the probability of a binary class outcome using a logistic function.
  - Use Case: Spam detection.
- 2. Support Vector Machines (SVM) with Kernel = 'linear'
  - Description: Maximizes the margin between classes with a linear boundary.
  - Use Case: Text classification.
- 3. Single-Layer Perceptron
  - **Description**: A basic neural network layer that classifies linearly separable data.
  - Use Case: Predicting customer churn.
- 4. Stochastic Gradient Descent (SGD) Classifier
  - Description: Optimizes the model by minimizing the loss function using stochastic gradient descent.
  - Use Case: Large-scale classification tasks.

### 2. Non-linear Classifiers

#### **Definition**

Non-linear classifiers create a **non-linear decision boundary**, allowing them to capture complex relationships between features and target variables.

### **Examples of Non-linear Classifiers**

- 1. K-Nearest Neighbours (KNN)
  - Description: Classifies data points based on the majority vote of their k-nearest neighbors.
  - Use Case: Handwritten digit recognition.
- 2. Kernel SVM
  - Description: Extends SVM with non-linear kernels like RBF or polynomial.
  - Use Case: Image classification.
- 3. Naive Bayes
  - Description: A probabilistic classifier based on Bayes' theorem.
  - Use Case: Sentiment analysis.
- 4. Decision Tree Classification
  - Description: Splits the data into subsets based on feature values, creating a treelike structure.
  - Use Case: Predicting customer segmentation.

# 3. Ensemble Learning Classifiers

#### **Definition**

Ensemble learning combines predictions from multiple models to improve overall accuracy and robustness.

### **Examples of Ensemble Classifiers**

- 1. Random Forests
  - Description: An ensemble of decision trees built using bootstrapped datasets.
  - Use Case: Loan approval prediction.

#### 2. AdaBoost

- Description: Combines weak classifiers iteratively to create a strong classifier.
- Use Case: Fraud detection.

#### 3. Bagging Classifier

- Description: Aggregates predictions from multiple base models trained on random subsets of the data.
- Use Case: Credit scoring.

#### 4. Voting Classifier

- Description: Combines predictions from multiple classifiers using majority voting.
- Use Case: Diagnosing diseases.

#### 5. ExtraTrees Classifier

- Description: Similar to Random Forest but uses random thresholds for splitting.
- Use Case: Stock market predictions.

## 4. Multi-layer Artificial Neural Networks (ANN)

### **Description**

ANNs are a class of deep learning models consisting of multiple layers of interconnected nodes (neurons). They can handle highly complex and non-linear relationships.

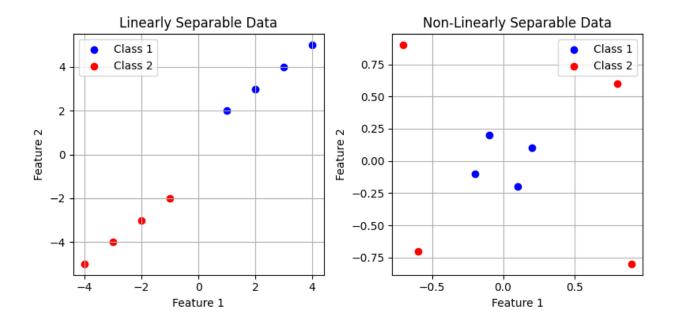
• Use Case: Image recognition, speech recognition, and natural language processing.

# **Choosing the Right Classifier**

Scenario	Recommended Algorithm	
Linear relationships in data	Logistic Regression, Linear SVM	
Complex non-linear relationships	Kernel SVM, Decision Trees	
Robust performance across large datasets	Random Forest, AdaBoost	
Handling imbalanced datasets	Ensemble methods (e.g., Bagging)	
High-dimensional data	Naive Bayes, Neural Networks	

By understanding the strengths of each classification algorithm, you can select the most appropriate one for your problem domain and dataset characteristics. [

```
# Import necessary libraries
import matplotlib.pyplot as plt
# Predefined linearly separable data
linear_x1 = [[1, 2], [2, 3], [3, 4], [4, 5]] # Class 1 points
linear_x2 = [[-1, -2], [-2, -3], [-3, -4], [-4, -5]] # Class 2 points
# Predefined non-linearly separable data
nonlinear_x1 = [[0.2, 0.1], [0.1, -0.2], [-0.2, -0.1], [-0.1, 0.2]]
Class 1 points (inside a circle)
nonlinear x2 = [[0.8, 0.6], [-0.7, 0.9], [0.9, -0.8], [-0.6, -0.7]]
Class 2 points (outside the circle)
# Convert to separate x and y coordinates for easier plotting
linear x1 = list(zip(*linear x1))
linear x2 = list(zip(*linear x2))
nonlinear x1 = list(zip(*nonlinear x1))
nonlinear x2 = list(zip(*nonlinear x2))
# Plot linearly separable data
plt.figure(figsize=(8, 4))
plt.subplot(1, 2, 1)
plt.scatter(linear x1[0], linear x1[1], color='blue', label='Class 1')
plt.scatter(linear x2[0], linear x2[1], color='red', label='Class 2')
plt.title("Linearly Separable Data")
plt.xlabel("Feature 1")
plt.vlabel("Feature 2")
plt.legend()
plt.grid(True)
# Plot non-linearly separable data
plt.subplot(1, 2, 2)
plt.scatter(nonlinear x1[0], nonlinear x1[1], color='blue',
label='Class 1')
plt.scatter(nonlinear x2[0], nonlinear x2[1], color='red',
label='Class 2')
plt.title("Non-Linearly Separable Data")
plt.xlabel("Feature 1")
plt.ylabel("Feature 2")
plt.legend()
plt.grid(True)
plt.tight layout()
plt.show()
```



# **Evaluating a Classification Model**

Evaluating a classification model is a critical step in machine learning to assess its **performance** and **generalization ability** on unseen data. Several metrics can be used for this purpose, depending on the specific problem and requirements.

# 1. Popular Evaluation Metrics

### 1.1 Accuracy

#### **Definition:**

Accuracy is the ratio of the number of correct predictions to the total number of predictions.

$$Accuracy = \frac{Number of Correct Predictions}{Total Number of Predictions}$$

- Strengths: Simple and intuitive.
- Limitations: Can be misleading in imbalanced datasets.

### **Example:**

Suppose we have a spam classification task with 1,000 emails:

- 950 are **not spam** (Negative class).
- 50 are spam (Positive class).

If the model predicts all emails as **not spam**, the accuracy will be:

Accuracy = 
$$\frac{950}{1000}$$
 = 95%

**Issue**: Despite high accuracy, the model fails to identify any spam emails, making it unsuitable for this task.

### 2. Confusion Matrix

The **Confusion Matrix** groups classification results into four categories:

### **Definitions:**

- True Positive (TP): Correctly predicted as positive.
- True Negative (TN): Correctly predicted as negative.
- False Positive (FP): Predicted positive but is actually negative.
- False Negative (FN): Predicted negative but is actually positive.

#### Type 1 and Type 2 Errors in Classification

Type 1 Error (False Positive):

Occurs when the model incorrectly predicts a negative instance as positive.

- Example: A healthy patient is diagnosed with a disease.
- Impact: Can lead to unnecessary actions or treatments.
- Type 2 Error (False Negative):

Occurs when the model incorrectly predicts a positive instance as negative.

- Example: A patient with a disease is diagnosed as healthy.
- Impact: Critical in cases like medical diagnosis, as it may delay necessary treatment.

### 3. Precision

#### **Definition:**

Precision measures the proportion of true positives out of all positive predictions:

$$Precision = \frac{TP}{TP + FP}$$

- **Focus**: Highlights how many predicted positives are actually correct.
- Use Case: Important when the cost of false positives is high.

#### Example:

In spam detection, Precision measures how many emails flagged as spam are actually spam.

# 4. Recall (Sensitivity)

#### **Definition:**

Recall (also known as Sensitivity) measures the proportion of true positives out of all actual positives:

$$Recall = \frac{TP}{TP + FN}$$

- Focus: Highlights how many actual positives are correctly identified.
- Use Case: Important when the cost of false negatives is high.

#### Example:

In spam detection, Recall measures how many actual spam emails are correctly detected.

### 5. Precision vs Recall

#### Tradeoff:

- Improving **Precision** often reduces **Recall**, and vice versa.
- The choice depends on the specific task:
  - For spam detection, prioritize **Precision** to avoid important emails being flagged as spam.
  - For disease detection, prioritize **Recall** to minimize missed diagnoses.

### 6. F1 Score

#### **Definition:**

The **F1 Score** provides a balance between Precision and Recall:

$$F1=2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

• Use Case: Useful when both Precision and Recall are equally important.

#### Example:

For a model with Precision = 0.8 and Recall = 0.6:

$$F1=2\times\frac{0.8\times0.6}{0.8+0.6}=2\times\frac{0.48}{1.4}=0.686$$

# 7. Choosing the Right Metric

- Accuracy: Suitable for balanced datasets.
- **Precision**: Prioritize when false positives have higher costs.
- **Recall**: Prioritize when false negatives have higher costs.
- **F1 Score**: Use when you need a balance between Precision and Recall.

### **Summary**

- Accuracy is simple but insufficient for imbalanced datasets.
- The **Confusion Matrix** helps understand the distribution of predictions.
- Metrics like Precision, Recall, and F1 Score provide deeper insights into model performance.
- Choosing the right metric depends on the specific task and its requirements.

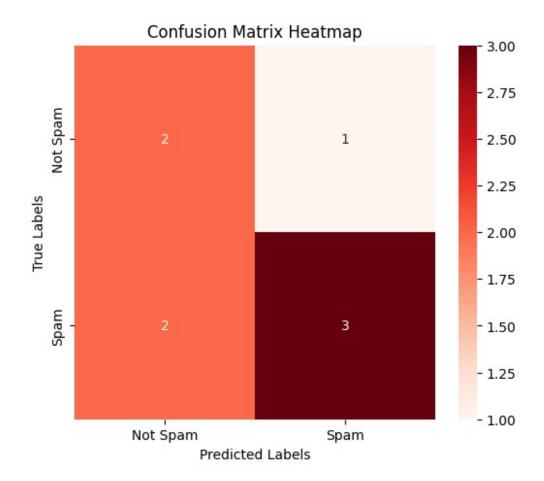
```
import numpy as np
from sklearn.metrics import confusion_matrix, accuracy_score,
precision_score, recall_score, f1_score

# Binary vectors
y_true = np.array([1, 0, 1, 1, 0, 0, 1, 1]) # Actual labels
y_pred = np.array([1, 0, 0, 1, 1, 0, 1, 0]) # Predicted labels

# Confusion Matrix
cm = confusion_matrix(y_true, y_pred)
```

```
tn, fp, fn, tp = cm.ravel()
print("Confusion Matrix:")
print(cm)
print(f"True Negative (TN): {tn}, False Positive (FP): {fp}, False
Negative (FN): {fn}, True Positive (TP): {tp}")
# Accuracy
accuracy = accuracy_score(y_true, y_pred)
print(f"\nAccuracy: {accuracy:.2f}")
# Precision
precision = precision_score(y_true, y_pred)
print(f"Precision: {precision:.2f}")
# Recall
recall = recall_score(y_true, y_pred)
print(f"Recall: {recall:.2f}")
# F1 Score
f1 = f1_score(y_true, y_pred)
print(f"F1 Score: {f1:.2f}")
Confusion Matrix:
[[2 1]
[2 3]]
True Negative (TN): 2, False Positive (FP): 1, False Negative (FN): 2,
True Positive (TP): 3
Accuracy: 0.62
Precision: 0.75
Recall: 0.60
F1 Score: 0.67
from sklearn.metrics import classification_report
# Generate Classification Report
report = classification report(y true, y pred, target names=['Class
0', 'Class 1'])
print("Classification Report:\n")
print(report)
Classification Report:
                           recall f1-score
              precision
                                               support
                                                     3
     Class 0
                   0.50
                             0.67
                                       0.57
                                                     5
     Class 1
                   0.75
                             0.60
                                       0.67
                                       0.62
                                                     8
    accuracy
                   0.62
                             0.63
                                       0.62
                                                     8
   macro avg
```

```
weighted avg
                     0.66
                                0.62
                                           0.63
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.metrics import confusion matrix
# Example data
y_{true} = np.array([1, 0, 1, 1, 0, 0, 1, 1]) # Actual labels y_pred = np.array([1, 0, 0, 1, 1, 0, 1, 0]) # Predicted labels
# Compute confusion matrix
cm = confusion matrix(y true, y pred)
# Plot confusion matrix heatmap
plt.figure(figsize=(6, 5))
sns.heatmap(cm, annot=True, fmt='d', cmap='Reds', xticklabels=['Not
Spam', 'Spam'], yticklabels=['Not Spam', 'Spam'])
plt.xlabel('Predicted Labels')
plt.ylabel('True Labels')
plt.title('Confusion Matrix Heatmap')
plt.show()
```



# **Multi-Class Classification**

When we have more than two classes (e.g., Class 0, Class 1, Class 2), classification tasks become **multi-class classification** problems. The metrics for binary classification like **Accuracy**, **Precision**, **Recall**, and **F1 Score** can still be applied, but with some modifications.

# 1. Dataset Example

Let's consider a **customer support email classification** problem with three classes:

- Class 0: Shipping
- **Class 1**: Returns
- Class 2: Tracking

Below is the example dataset showing **Actual vs Predicted** values:

### 2. Confusion Matrix

For multi-class problems, the confusion matrix becomes a **3x3 matrix**. Each row represents the **actual class**, and each column represents the **predicted class**.

# 3. Accuracy

Accuracy is calculated as:

$$Accuracy = \frac{Correct \ Predictions}{Total \ Predictions}$$

- Correct Predictions = (3 + 4 + 3 = 10)
- Total Predictions = (15)

Accuracy:

Accuracy = 
$$\frac{10}{15}$$
 = 67 %

# 4. Precision, Recall, and F1 Score (Per Class)

### Class 0 - Shipping

Precision:

$$Precision = \frac{TP}{TP + FP} = \frac{3}{3+1} = 75\%$$

Recall:

Recall = 
$$\frac{\text{TP}}{\text{TP} + \text{FN}} = \frac{3}{3+2} = 60\%$$

F1 Score:

$$F1=2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}} = 67\%$$

#### Class 1 - Returns

Precision:

$$Precision = \frac{4}{4+2} = 67\%$$

Recall:

Recall = 
$$\frac{4}{4+1}$$
 = 80 %

F1 Score:

$$F1=2\times\frac{67\times80}{67+80}=79\%$$

### Class 2 - Tracking

• Precision:

$$Precision = \frac{3}{3+2} = 60\%$$

Recall:

Recall = 
$$\frac{3}{3+2}$$
 = 60 %

F1 Score:

$$F1=2\times\frac{60\times60}{60+60}=53\%$$

# 5. Macro-Average Precision, Recall, and F1 Score

When dealing with multi-class problems, we use **Macro-Average** to summarize the metrics across all classes.

### **Macro-Average Precision:**

Macro Precision = 
$$\frac{\text{Precision}_0 + \text{Precision}_1 + \text{Precision}_2}{3}$$
Macro Precision = 
$$\frac{75 + 67 + 60}{3} = 67.3\%$$

### Macro-Average Recall:

Macro Recall = 
$$\frac{\text{Recall}_0 + \text{Recall}_1 + \text{Recall}_2}{3}$$
Macro Recall = 
$$\frac{60 + 80 + 60}{3} = 66.7 \%$$

### Macro-Average F1 Score:

Macro F1=
$$\frac{F1_0+F1_1+F1_2}{3}$$

Macro F1=
$$\frac{67+79+53}{3}$$
=66.3%

# 6. Summary Table

Class	Precision	Recall	F1 Score
0 - Shipping	75%	60%	67%
1 - Returns	67%	80%	79%
2 - Tracking	60%	60%	53%
Macro-Average	67.3%	66.7%	66.3%

### Conclusion

- 1. **Confusion Matrix** helps in understanding misclassifications for each class.
- 2. **Precision, Recall,** and **F1 Score** can be computed per class.
- 3. **Macro-Average** provides a single value for each metric, summarizing overall performance.

These metrics are critical in evaluating multi-class classification models, ensuring a balanced understanding of their strengths and weaknesses.

```
# Compute confusion matrix
conf matrix = confusion matrix(y true, y pred, labels=class labels)
print("Confusion Matrix:\n", conf matrix)
# Plot the confusion matrix
disp = ConfusionMatrixDisplay(confusion matrix=conf matrix,
display labels=class labels)
disp.plot(cmap="Blues")
plt.title("Confusion Matrix")
plt.show()
# Calculate Accuracy
accuracy = accuracy_score(y_true, y_pred)
print(f"Accuracy: {accuracy:.2f}")
# Calculate Precision, Recall, and F1 Score (Per Class and Macro-
Average)
precision = precision score(y true, y pred, average=None,
labels=class labels)
recall = recall_score(y_true, y_pred, average=None,
labels=class labels)
f1 = f1 score(y true, y pred, average=None, labels=class labels)
macro_precision = precision_score(y_true, y_pred, average='macro')
macro recall = recall score(y true, y pred, average='macro')
macro f1 = f1 score(y true, y pred, average='macro')
# Display Metrics
print("\nClass-wise Metrics:")
for i, label in enumerate(class labels):
    print(f"Class '{label}' -> Precision: {precision[i]*100:.2f}%,
Recall: {recall[i]*100:.2f}%, F1: {f1[i]*100:.2f}%")
print("\nMacro-Averaged Metrics:")
print(f"Precision: {macro precision*100:.2f}%")
print(f"Recall: {macro recall*100:.2f}%")
print(f"F1 Score: {macro f1*100:.2f}%")
Confusion Matrix:
 [[3 0 2]
 [1 4 0]
 [0 2 3]]
```



```
Accuracy: 0.67
Class-wise Metrics:
Class 'Shipping' -> Precision: 75.00%, Recall: 60.00%, F1: 66.67%
Class 'Returns' -> Precision: 66.67%, Recall: 80.00%, F1: 72.73%
Class 'Tracking' -> Precision: 60.00%, Recall: 60.00%, F1: 60.00%
Macro-Averaged Metrics:
Precision: 67.22%
Recall: 66.67%
F1 Score: 66.46%
# Import libraries
from sklearn.metrics import confusion matrix, classification report,
accuracy score, ConfusionMatrixDisplay
import matplotlib.pyplot as plt
# Define actual and predicted labels
y_true = ["Shipping", "Shipping", "Shipping", "Shipping", "Shipping", "Returns", "R
                                      "Tracking", "Tracking", "Tracking", "Tracking"]
y_pred = ["Shipping", "Shipping", "Tracking", "Shipping", "Tracking",
```

```
"Returns", "Returns", "Shipping", "Returns", "Returns", "Tracking", "Tracking", "Tracking"]
# Unique class labels
class_labels = ["Shipping", "Returns", "Tracking"]
# Generate Classification Report
print("Classification Report:")
print(classification report(y true, y pred,
target names=class labels))
Classification Report:
               precision
                              recall f1-score
                                                   support
                                                          5
    Shipping
                     0.67
                                0.80
                                           0.73
                                                          5
     Returns
                     0.75
                                0.60
                                           0.67
                                                          5
    Tracking
                     0.60
                                0.60
                                           0.60
    accuracy
                                           0.67
                                                         15
                                                         15
   macro avq
                     0.67
                                0.67
                                           0.66
weighted avg
                     0.67
                                0.67
                                           0.66
                                                         15
```

# Additional Metrics for Evaluating Classification Models

In addition to Accuracy, Precision, Recall, and F1-Score, there are other important metrics for evaluating classification models. These include **Specificity**, **ROC-AUC Curve**, and **Log Loss**. Each metric provides unique insights into model performance.

# 1. Specificity

#### **Definition**

Specificity measures the proportion of **actual negatives** that are correctly identified as negative. It is also known as the **True Negative Rate**.

$$Specificity = \frac{True \ Negatives \ (TN)}{True \ Negatives \ (TN) + False \ Positives \ (FP)}$$

### **Key Points**

 Specificity complements Recall (True Positive Rate) to give a holistic understanding of model performance. • A high specificity means the model has fewer **False Positives**.

#### When to Use

Specificity is particularly useful when correctly identifying negatives is critical.

• **Example**: In fraud detection, it is important to minimize False Positives to avoid flagging legitimate transactions.

### 2. ROC-AUC Curve

#### **Definition**

- The ROC (Receiver Operating Characteristic) curve is a graphical plot that shows the tradeoff between the True Positive Rate (Recall) and the False Positive Rate as the decision threshold changes.
- The **AUC (Area Under the Curve)** represents the probability that the model will rank a randomly chosen positive instance higher than a randomly chosen negative one.

False Positive Rate = 1 – Specificity

### Interpretation

- **AUC = 1**: Perfect classifier (ideal).
- AUC = 0.5: Random guessing.
- **Higher AUC**: Indicates better model performance.

#### When to Use

- Use ROC-AUC when you need to evaluate how well the model separates positive and negative classes across different thresholds.
- **Example**: Medical diagnosis models where balancing False Positives and False Negatives is critical.

```
# Import libraries
from sklearn.metrics import confusion_matrix, roc_auc_score, roc_curve
import numpy as np
import matplotlib.pyplot as plt

# Actual labels and predicted probabilities
y_true = [1, 0, 1, 0, 0, 1, 0, 0, 1, 1]
y_pred_prob = [0.9, 0.2, 0.8, 0.7, 0.3, 0.85, 0.1, 0.4, 0.95, 0.05]

# Convert probabilities to binary predictions (threshold = 0.5)
y_pred = [1 if prob >= 0.5 else 0 for prob in y_pred_prob]
```

```
# Compute Confusion Matrix
tn, fp, fn, tp = confusion matrix(y true, y pred).ravel()
# Calculate Specificity
specificity = tn / (tn + fp)
print(f"Specificity: {specificity:.2f}")
# Calculate ROC-AUC Score
roc auc = roc auc score(y true, y pred prob)
print(f"ROC-AUC Score: {roc auc:.2f}")
# Plot ROC Curve
fpr, tpr, thresholds = roc curve(y true, y pred prob)
plt.figure(figsize=(8, 6))
plt.plot(fpr, tpr, color='blue', lw=2, label=f'ROC curve (AUC =
{roc auc:.2f})')
plt.plot([0, 1], [0, 1], color='grey', linestyle='--')
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('ROC Curve')
plt.legend(loc="lower right")
plt.grid()
plt.show()
Specificity: 0.80
ROC-AUC Score: 0.80
Log Loss: 0.59
```

