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Find, giving your answer to 3 significant figures where appropriate, the value of  $x$  for which

(a)  $5^x = 10$ ,

(2)

(b)  $\log_3(x-2) = -1$ .

(2)

**In this question you must show all stages of your working.**

**Solutions relying on calculator technology are not acceptable.**

(i) Solve the equation

$$x\sqrt{2} - \sqrt{18} = x$$

writing the answer as a surd in simplest form.

(3)

(ii) Solve the equation

$$4^{3x-2} = \frac{1}{2\sqrt{2}}$$

(3)

3. (a) Sketch the graph of

$$y = 3^x, \quad x \in \mathbb{R}$$

showing the coordinates of any points at which the graph crosses the axes.

**(2)**

- (b) Use algebra to solve the equation

$$3^{2x} - 9(3^x) + 18 = 0$$

giving your answers to 2 decimal places where appropriate.

**(5)**

4. Find the values of  $x$  such that

$$2\log_3 x - \log_3(x - 2) = 2$$

(5)



6. Given that  $y = 3x^2$ ,

(a) show that  $\log_3 y = 1 + 2\log_3 x$

(3)

(b) Hence, or otherwise, solve the equation

$$1 + 2\log_3 x = \log_3 (28x - 9)$$

(3)

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Given that

$$2\log_2(x+15) - \log_2 x = 6$$

(a) Show that

$$x^2 - 34x + 225 = 0$$

(5)

(b) Hence, or otherwise, solve the equation

$$2\log_2(x+15) - \log_2 x = 6$$

(2)

8

Given that  $\log_3 x = a$ , find in terms of  $a$ ,

(a)  $\log_3 (9x)$

(2)

$$(b) \log_3 \left( \frac{x^5}{81} \right)$$

(3)

giving each answer in its simplest form.

(c) Solve, for  $x$ ,

$$\log_3(9x) + \log_3\left(\frac{x^5}{81}\right) = 3$$

giving your answer to 4 significant figures.

(4)



9. (a) Given that  $p = \log_3 x$ , where  $x > 0$ , find in simplest form in terms of  $p$ ,

(i)  $\log_3\left(\frac{x}{9}\right)$

$$(ii) \log_3(\sqrt{x})$$

(2)

(b) Hence, or otherwise, solve

$$2\log_3\left(\frac{x}{9}\right) + 3\log_3(\sqrt{x}) = -11$$

giving your answer as a simplified fraction.

**Solutions relying on calculator technology are not acceptable.**

(4)

10. (i) Find the exact value of  $x$  for which

$$\log_2(2x) = \log_2(5x + 4) - 3$$

(4)

(ii) Given that

$$\log_a y + 3\log_a 2 = 5$$

express  $y$  in terms of  $a$ .

Give your answer in its simplest form.

(3)





**13.** (i) Given that

$$\log_3(3b + 1) - \log_3(a - 2) = -1, \quad a > 2$$

express  $b$  in terms of  $a$ .

(3)

(ii) Solve the equation

$$2^{2x+5} - 7(2^x) = 0$$

giving your answer to 2 decimal places.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(4)

14.

$$a = \log_2 x$$

$$b = \log_2(x + 8)$$

Express in terms of  $a$  and/or  $b$

(a)  $\log_2 \sqrt{x}$

(1)

(b)  $\log_2(x^2 + 8x)$

(2)

(c)  $\log_2\left(8 + \frac{64}{x}\right)$

Give your answer in simplest form.

(3)

**15.** Given that  $a > b > 0$  and that  $a$  and  $b$  satisfy the equation

$$\log a - \log b = \log(a - b)$$

(a) show that

$$a = \frac{b^2}{b-1} \quad (3)$$

(b) Write down the full restriction on the value of  $b$ , explaining the reason for this restriction. (2)