

**1.**

Relative to a fixed origin  $O$

- the point  $A$  has position vector  $5\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$
- the point  $B$  has position vector  $2\mathbf{i} + 4\mathbf{j} + a\mathbf{k}$

where  $a$  is a positive integer.

(a) Show that  $|\vec{OA}| = \sqrt{38}$

**(1)**

(b) Find the smallest value of  $a$  for which

$$|\vec{OB}| > |\vec{OA}| \quad (2)$$

2.

Relative to a fixed origin  $O$

- point  $A$  has position vector  $2\mathbf{i} + 5\mathbf{j} - 6\mathbf{k}$
- point  $B$  has position vector  $3\mathbf{i} - 3\mathbf{j} - 4\mathbf{k}$
- point  $C$  has position vector  $2\mathbf{i} - 16\mathbf{j} + 4\mathbf{k}$

(a) Find  $\overrightarrow{AB}$

(2)

(b) Show that quadrilateral  $OABC$  is a trapezium, giving reasons for your answer.

(2)

3.

Relative to a fixed origin, points  $P$ ,  $Q$  and  $R$  have position vectors  $\mathbf{p}$ ,  $\mathbf{q}$  and  $\mathbf{r}$  respectively.

Given that

- $P$ ,  $Q$  and  $R$  lie on a straight line
- $Q$  lies one third of the way from  $P$  to  $R$

show that

$$\mathbf{q} = \frac{1}{3}(\mathbf{r} + 2\mathbf{p})$$

(3)

4.

Relative to a fixed origin  $O$ ,

- $A$  is the point with position vector  $12\mathbf{i}$
- $B$  is the point with position vector  $16\mathbf{j}$
- $C$  is the point with position vector  $(50\mathbf{i} + 136\mathbf{j})$
- $D$  is the point with position vector  $(22\mathbf{i} + 24\mathbf{j})$

(a) Show that  $AD$  is parallel to  $BC$ .

(2)

Points  $A$ ,  $B$ ,  $C$  and  $D$  are used to model the vertices of a running track in the shape of a quadrilateral.

Runners complete one lap by running along all four sides of the track.

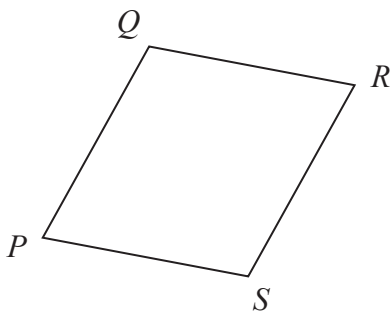
The lengths of the sides are measured in metres.

Given that a particular runner takes exactly 5 minutes to complete 2 laps,

(b) calculate the average speed of this runner, giving the answer in kilometres per hour.

(4)

5.



### Figure 3

Figure 3 shows a sketch of a parallelogram  $PQRS$ .

Given that

- $\vec{PQ} = 2\mathbf{i} + 3\mathbf{j} - 4\mathbf{k}$
- $\vec{QR} = 5\mathbf{i} - 2\mathbf{k}$

(a) show that parallelogram  $PQRS$  is a rhombus.

(2)

(b) Find the exact area of the rhombus  $PQRS$ .

(4)

**6.**

Relative to a fixed origin  $O$

- the point  $A$  has position vector  $4\mathbf{i} - 3\mathbf{j} + 5\mathbf{k}$
- the point  $B$  has position vector  $4\mathbf{j} + 6\mathbf{k}$
- the point  $C$  has position vector  $-16\mathbf{i} + p\mathbf{j} + 10\mathbf{k}$

where  $p$  is a constant.

Given that  $A$ ,  $B$  and  $C$  lie on a straight line,

(a) find the value of  $p$ .

**(3)**

The line segment  $OB$  is extended to a point  $D$  so that  $\overrightarrow{CD}$  is parallel to  $\overrightarrow{OA}$

(b) Find  $|\overrightarrow{OD}|$ , writing your answer as a fully simplified surd.

(3)