

1

Given that the point  $A$  has position vector  $4\mathbf{i} - 5\mathbf{j}$  and the point  $B$  has position vector  $-5\mathbf{i} - 2\mathbf{j}$ ,

(a) find the vector  $\overrightarrow{AB}$ ,

(2)

(b) find  $|\overrightarrow{AB}|$ .

Give your answer as a simplified surd.

(2)



3

[In this question the unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are due east and due north respectively.]

A stone slides horizontally across ice.

Initially the stone is at the point  $A(-24\mathbf{i} - 10\mathbf{j})\text{ m}$  relative to a fixed point  $O$ .

After 4 seconds the stone is at the point  $B(12\mathbf{i} + 5\mathbf{j})$  m relative to the fixed point  $O$ .

The motion of the stone is modelled as that of a particle moving in a straight line at constant speed.

Using the model,

(a) prove that the stone passes through  $O$ ,

(2)

(b) calculate the speed of the stone.

(3)

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4

[In this question the unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are due east and due north respectively.]

A coastguard station  $O$  monitors the movements of a small boat.

At 10:00 the boat is at the point  $(4\mathbf{i} - 2\mathbf{j})$  km relative to  $O$ .

At 12:45 the boat is at the point  $(-3\mathbf{i} - 5\mathbf{j})$  km relative to  $O$ .

The motion of the boat is modelled as that of a particle moving in a straight line at constant speed.

- (a) Calculate the bearing on which the boat is moving, giving your answer in degrees to one decimal place.

(3)

- (b) Calculate the speed of the boat, giving your answer in  $\text{km h}^{-1}$

(3)

[illegible]

**5. (i)** Two non-zero vectors,  $\mathbf{a}$  and  $\mathbf{b}$ , are such that

$$|\mathbf{a} + \mathbf{b}| = |\mathbf{a}| + |\mathbf{b}|$$

Explain, geometrically, the significance of this statement.

(1)

(ii) Two different vectors,  $\mathbf{m}$  and  $\mathbf{n}$ , are such that  $|\mathbf{m}| = 3$  and  $|\mathbf{m} - \mathbf{n}| = 6$

The angle between vector **m** and vector **n** is  $30^\circ$

Find the angle between vector  $\mathbf{m}$  and vector  $\mathbf{m} - \mathbf{n}$ , giving your answer, in degrees, to one decimal place.

(4)

6

Relative to a fixed origin, points  $P$ ,  $Q$  and  $R$  have position vectors  $\mathbf{p}$ ,  $\mathbf{q}$  and  $\mathbf{r}$  respectively.

Given that

- $P$ ,  $Q$  and  $R$  lie on a straight line
- $Q$  lies one third of the way from  $P$  to  $R$

show that

$$\mathbf{q} = \frac{1}{3}(\mathbf{r} + 2\mathbf{p})$$

(3)

Relative to a fixed origin  $O$

- the point  $A$  has position vector  $5\mathbf{i} + 3\mathbf{j} + 2\mathbf{k}$
- the point  $B$  has position vector  $2\mathbf{i} + 4\mathbf{j} + a\mathbf{k}$

where  $a$  is a positive integer.

(a) Show that  $|\vec{OA}| = \sqrt{38}$

**(1)**

(b) Find the smallest value of  $a$  for which

$$|\vec{OB}| > |\vec{OA}| \quad (2)$$

Relative to a fixed origin  $O$

- point  $A$  has position vector  $2\mathbf{i} + 5\mathbf{j} - 6\mathbf{k}$
- point  $B$  has position vector  $3\mathbf{i} - 3\mathbf{j} - 4\mathbf{k}$
- point  $C$  has position vector  $2\mathbf{i} - 16\mathbf{j} + 4\mathbf{k}$

(a) Find  $\vec{AB}$

(2)

(b) Show that quadrilateral  $OABC$  is a trapezium, giving reasons for your answer.

(2)



Relative to a fixed origin  $O$ ,

- $A$  is the point with position vector  $12\mathbf{i}$
- $B$  is the point with position vector  $16\mathbf{j}$
- $C$  is the point with position vector  $(50\mathbf{i} + 136\mathbf{j})$
- $D$  is the point with position vector  $(22\mathbf{i} + 24\mathbf{j})$

(a) Show that  $AD$  is parallel to  $BC$ .

(2)

Points  $A$ ,  $B$ ,  $C$  and  $D$  are used to model the vertices of a running track in the shape of a quadrilateral.

Runners complete one lap by running along all four sides of the track.

The lengths of the sides are measured in metres.

Given that a particular runner takes exactly 5 minutes to complete 2 laps,

(b) calculate the average speed of this runner, giving the answer in kilometres per hour.

(4)

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Relative to a fixed origin  $O$

- the point  $A$  has position vector  $4\mathbf{i} - 3\mathbf{j} + 5\mathbf{k}$
- the point  $B$  has position vector  $4\mathbf{j} + 6\mathbf{k}$
- the point  $C$  has position vector  $-16\mathbf{i} + p\mathbf{j} + 10\mathbf{k}$

where  $p$  is a constant.

Given that  $A$ ,  $B$  and  $C$  lie on a straight line,

(a) find the value of  $p$ .

(3)

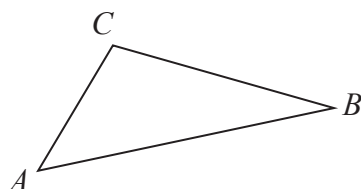
The line segment  $OB$  is extended to a point  $D$  so that  $\overrightarrow{CD}$  is parallel to  $\overrightarrow{OA}$

(b) Find  $|\overrightarrow{OD}|$ , writing your answer as a fully simplified surd.

(3)

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**11.**



### Figure 1

Figure 1 shows a sketch of triangle  $ABC$ .

Given that

- $\vec{AB} = -3\mathbf{i} - 4\mathbf{j} - 5\mathbf{k}$
- $\vec{BC} = \mathbf{i} + \mathbf{j} + 4\mathbf{k}$

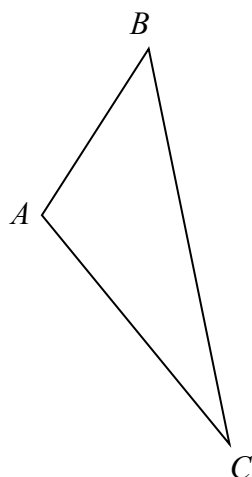
(a) find  $\vec{AC}$

(2)

(b) show that  $\cos ABC = \frac{9}{10}$

(3)

12.



## Figure 2

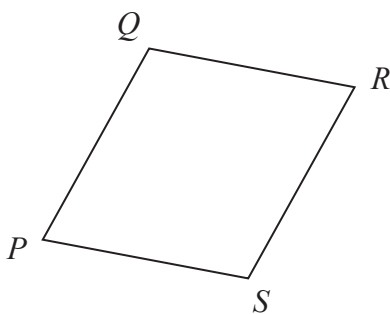
Figure 2 shows a sketch of a triangle  $ABC$ .

Given  $\overrightarrow{AB} = 2\mathbf{i} + 3\mathbf{j} + \mathbf{k}$  and  $\overrightarrow{BC} = \mathbf{i} - 9\mathbf{j} + 3\mathbf{k}$ ,

show that  $\angle BAC = 105.9^\circ$  to one decimal place.

(5)

**13.**



### Figure 3

Figure 3 shows a sketch of a parallelogram  $PQRS$ .

Given that

- $\vec{PQ} = 2\mathbf{i} + 3\mathbf{j} - 4\mathbf{k}$
- $\vec{QR} = 5\mathbf{i} - 2\mathbf{k}$

(a) show that parallelogram  $PQRS$  is a rhombus.

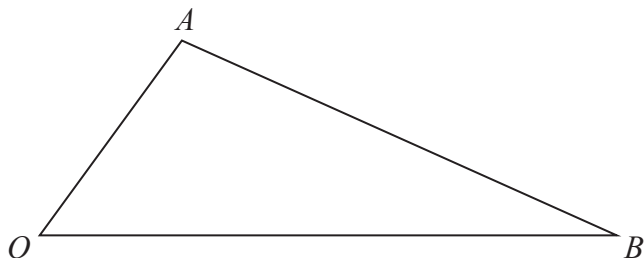
(2)

(b) Find the exact area of the rhombus  $PQRS$ .

(4)

This image shows a full page of blank, lined paper. It features approximately 20 evenly spaced horizontal grey lines across its entire width, providing a template for handwriting practice or general note-taking. The margins are consistent on all sides.

14.



### Figure 7

Figure 7 shows a sketch of triangle  $OAB$ .

The point  $C$  is such that  $\overrightarrow{OC} = 2\overrightarrow{OA}$ .

The point  $M$  is the midpoint of  $AB$ .

The straight line through  $C$  and  $M$  cuts  $OB$  at the point  $N$ .

Given  $\overrightarrow{OA} = \mathbf{a}$  and  $\overrightarrow{OB} = \mathbf{b}$

- (a) Find  $\overrightarrow{CM}$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$  (2)
- (b) Show that  $\overrightarrow{ON} = \left(2 - \frac{3}{2}\lambda\right)\mathbf{a} + \frac{1}{2}\lambda\mathbf{b}$ , where  $\lambda$  is a scalar constant. (2)
- (c) Hence prove that  $ON:NB = 2:1$  (2)