

1

Write $(3x + 2) \div \left(\frac{3x^2 - 7x - 6}{5} \right) - \frac{5}{x + 3}$ as a single fraction in its simplest form.

Show clear algebraic working.

.....
(Total for Question 1 is 4 marks)

2 Find the two values of x such that

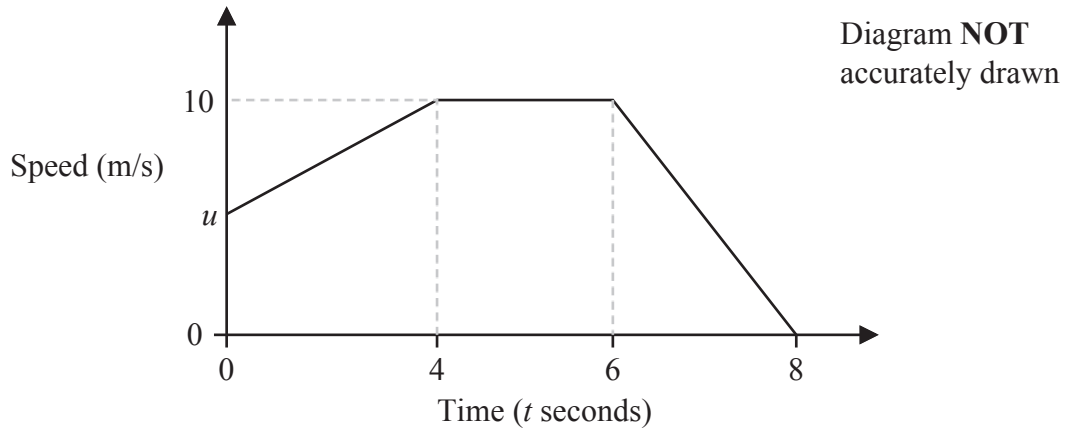
$$\frac{12^{3x} \times 3^{4x^2-3x} \times 3}{24^{2x}} = 27$$

Show your working clearly.

.....

(Total for Question 2 is 4 marks)

3



The diagram shows a sketch of the speed-time graph of part of a cyclist's journey along a straight horizontal road.

- (a) Calculate the deceleration, in m/s^2 , for the last 2 seconds of this part of the cyclist's journey.

..... m/s^2
(2)

At time $t = 0$ seconds, the speed of the cyclist is u m/s
The cyclist travelled a total distance of 65 m in the 8 seconds.

- (b) Calculate the value of u

$u =$
(3)

(Total for Question 3 is 5 marks)

4 The line L_1 has equation $5x + 4y = 16$

The line L_2 is parallel to L_1 and passes through the point with coordinates $(8, 15)$

L_2 crosses the x -axis at the point A and the y -axis at the point B .

Calculate the length, to the nearest whole number, of AB .

(Total for Question 4 is 5 marks)

- 5** y is directly proportional to x^3
 x is inversely proportional to the square root of w .

$$y = 729 \text{ when } x = 4.5$$

$$x = 25 \text{ when } w = 0.16$$

Find a formula for y in terms of w .

(Total for Question 5 is 5 marks)

.....
(Total for Question 5 is 5 marks)

6

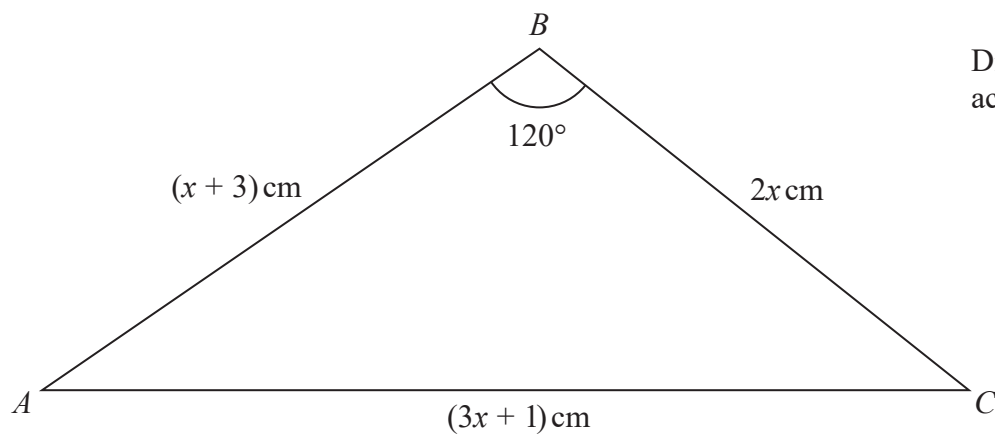


Diagram **NOT**
accurately drawn

The diagram shows triangle ABC in which

$$AB = (x + 3) \text{ cm}$$

$$BC = 2x \text{ cm}$$

$$AC = (3x + 1) \text{ cm}$$

$$\angle ABC = 120^\circ$$

Find the size, in degrees to 3 significant figures, of $\angle ACB$.

(Total for Question 6 is 5 marks)

7

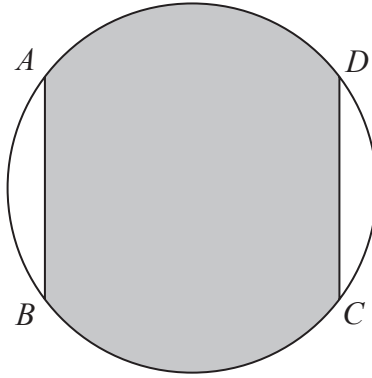


Diagram **NOT**
accurately drawn

The diagram shows a circle of radius $2x$ cm.

The lines AB and DC are parallel and $AB = DC = 2x$ cm.

The area of the region shown shaded in the diagram is kx^2 cm²

Find the exact value of k .

$k = \dots\dots\dots$

(Total for Question 7 is 5 marks)

- 8 A bag contains n beads.
There are 4 orange beads in the bag.
The rest of the beads are purple.

Donald is going to take at random 2 beads from the bag.

The probability that both beads will be the same colour is $\frac{51}{91}$

Find the value of n .

Show clear algebraic working.

$n = \dots\dots\dots$

(Total for Question 8 is 6 marks)

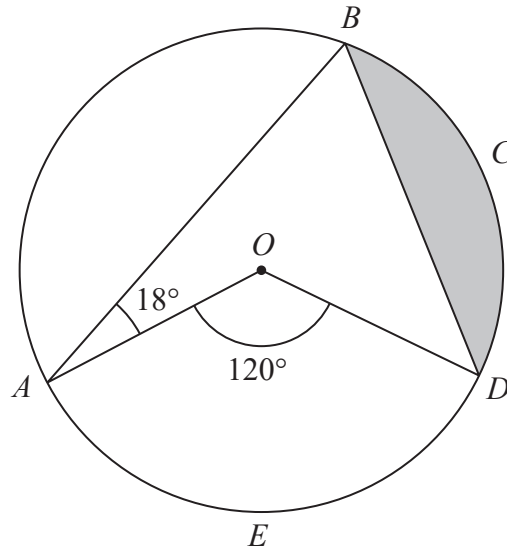


Diagram **NOT**
accurately drawn

Figure 2

Figure 2 shows a circle $ABCDE$ with centre O .

$$\angle BAO = 18^\circ \qquad \angle AOD = 120^\circ$$

The area of segment BCD , shown shaded in Figure 2, is $T \text{ cm}^2$

Given that the perimeter of the sector $AODE$ is $5(3 + \pi) \text{ cm}$,

calculate the value, to one decimal place, of T .

(Total for Question 9 is 6 marks)

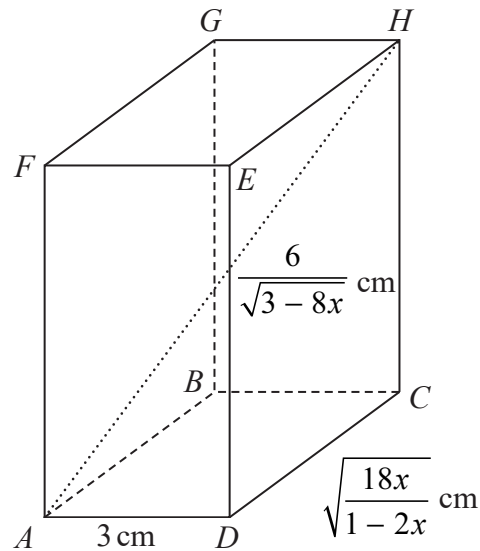


Diagram **NOT**
accurately drawn

The diagram shows cuboid $ABCDEFGH$ in which

$$AD = 3 \text{ cm} \quad DC = \sqrt{\frac{18x}{1-2x}} \text{ cm} \quad AH = \frac{6}{\sqrt{3-8x}} \text{ cm}$$

where $0 < x < \frac{3}{8}$

Given that the length of CH is L cm, where $L = \frac{k}{\sqrt{(3-8x)(1-2x)}}$ and k is a positive integer,

- (a) find the value of k
Show your working clearly.

$$k = \dots\dots\dots (5)$$

Given that $x = 0.3$

(b) calculate the volume, in cm^3 , of the cuboid.

$$\dots\dots\dots \text{cm}^3 (2)$$

(Total for Question 10 is 7 marks)

11 x is directly proportional to w^3

y is inversely proportional to \sqrt{w}

$$y = 2 \text{ when } x = \frac{1}{4}$$

Find the value of p and the value of q such that $xy^p = q$

$$p = \dots\dots\dots$$

$$q = \dots\dots\dots$$

(Total for Question 11 is 4 marks)

12

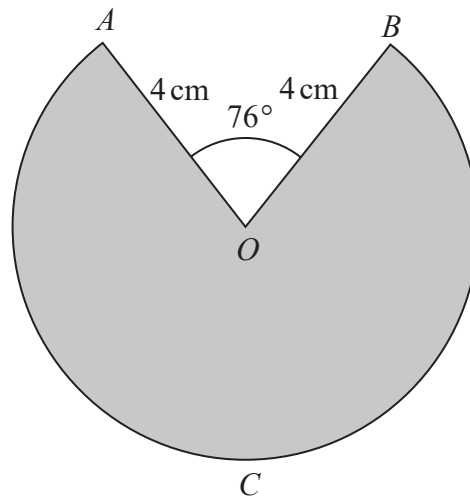


Diagram **NOT**
accurately drawn

The diagram shows a sector $OACB$ of a circle, centre O .

$$OA = OB = 4 \text{ cm}$$

$$\text{Angle } AOB = 76^\circ$$

(a) Calculate the area, in cm^2 to 3 significant figures, of the shaded sector $OACB$.

..... cm^2
(2)

(b) Calculate the perimeter, in cm to 3 significant figures, of the shaded sector $OACB$.

.....cm
(3)

(Total for Question 12 is 5 marks)

Diagram **NOT**
accurately drawn

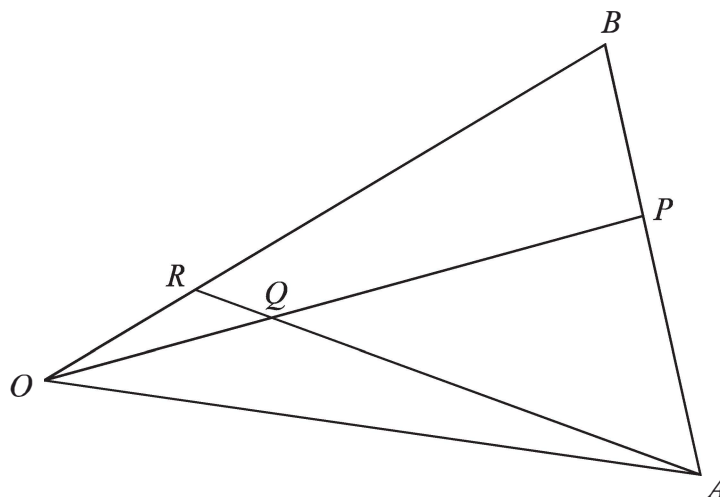


Figure 4

Figure 4 shows triangle OAB in which $\vec{OA} = \mathbf{a}$ and $\vec{OB} = \mathbf{b}$

P is the point on AB such that $AP : PB = 2 : 1$

Q is the point on OP such that $OQ : QP = 1 : 3$

R is the point on OB such that RQA is a straight line.

Calculate, in its simplest form, the ratio $OR : RB$

(Total for Question 13 is 6 marks)

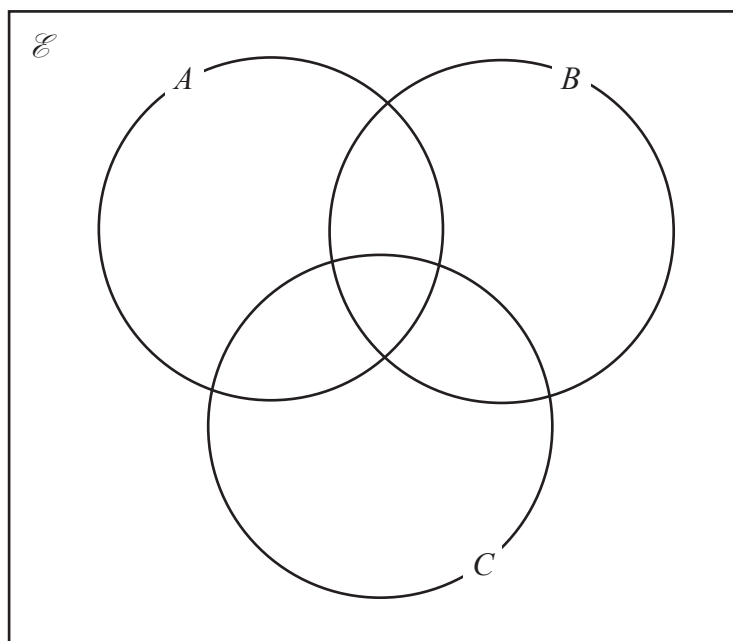
14 $\mathcal{E} = \{\text{odd numbers between 0 and 30}\}$

$A = \{\text{multiples of 3}\}$

$B = \{\text{prime numbers}\}$

$C = \{\text{factors of 30}\}$

- (a) Complete the Venn diagram for this information showing the position of each of the numbers in the universal set.



(3)

(b) Find (i) $n([A \cup C] \cap B)$

(ii) $n([B \cap C'] \cup A')$

(2)

A number is chosen at random from the universal set, \mathcal{E}

(c) Write down the probability that the number is in the set $C \cap A'$

(2)

Given that the number chosen from \mathcal{E} is a multiple of 3

(d) find the probability that the number is also a factor of 30

(2)

(Total for Question 14 is 9 marks)

Diagram **NOT**
accurately drawn

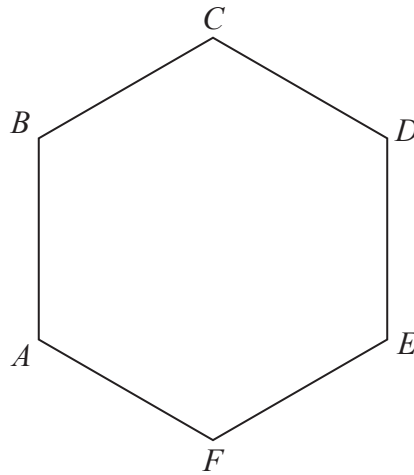


Figure 4

Figure 4 shows a regular hexagon $ABCDEF$

Given that the area of hexagon $ABCDEF = 150\sqrt{3} \text{ cm}^2$

(a) find the perimeter, in cm, of the hexagon.

(4)

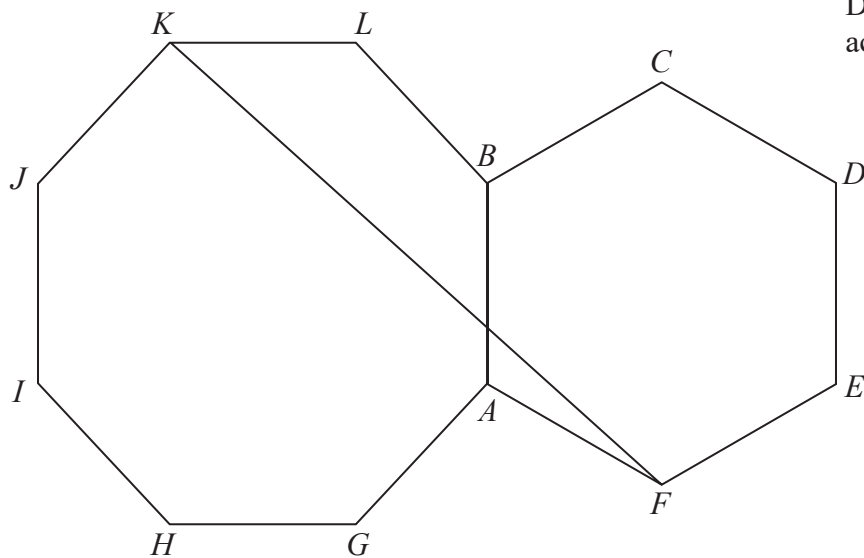


Diagram **NOT**
accurately drawn

Figure 5

Figure 5 shows a shape $AGHIJKLBCDEF$ made from a regular octagon $GHIJKLBA$ and the regular hexagon $ABCDEF$ from part (a).

(b) Work out the length, in cm to one decimal place, of the straight line KF

(6)

(Total for Question 15 is 10 marks)

- 16** (a) Solve the inequality $5(x + 1) < x$
Show clear algebraic working.

(2)

- (b) Solve the simultaneous equations

$$3x^2 + y^2 - 7 = 0$$

$$y - 3x - 5 = 0$$

Show clear algebraic working.

(5)

- (c) Hence find the value of x for which

$$5(x + 1) < x \quad \text{and} \quad 3x^2 + y^2 - 7 = 0 \quad \text{and} \quad y - 3x - 5 = 0$$

(1)

(Total for Question 16 is 8 marks)

17 A box contains 8 green counters and 2 white counters only.

Peter takes at random 2 counters from the box.

- (a) Calculate the probability that Peter will take 1 green counter and 1 white counter. (3)

A bag contains 28 blue beads and n red beads only.

Naasir selects a bead from the bag at random.

- (b) Explain why the probability of the bead being red cannot be $\frac{6}{11}$ (3)

Naasir keeps the first bead and selects a second bead at random from the bag.

The probability of both beads being different colours is $\frac{1}{2}$

Given that there are fewer blue beads than red beads,

- (c) calculate the probability that both beads are blue.
Show clear algebraic working. (5)

(Total for Question 17 is 11 marks)

18 A curve **C** and a straight line **L** are drawn on a grid.

C has equation $y = 5x^2 - 16x - 5$

L has equation $y + 5x = 7$

- (a) Find the coordinates of the points of intersection of **C** and **L**
Show clear algebraic working.

(5)

P is the point on the curve with equation $y = 5x^2 - 16x - 5$ with *x* coordinate 2

The line **Q** is the tangent to the curve at the point *P*

The line **Q** crosses the *x*-axis at the point *X* and the *y*-axis at the point *Y*

The point *M* lies on **Q** and is such that $XM = MY$

- (b) Calculate the coordinates of the point *M*
Give your coordinates as exact values.

(5)

(Total for Question 18 is 10 marks)

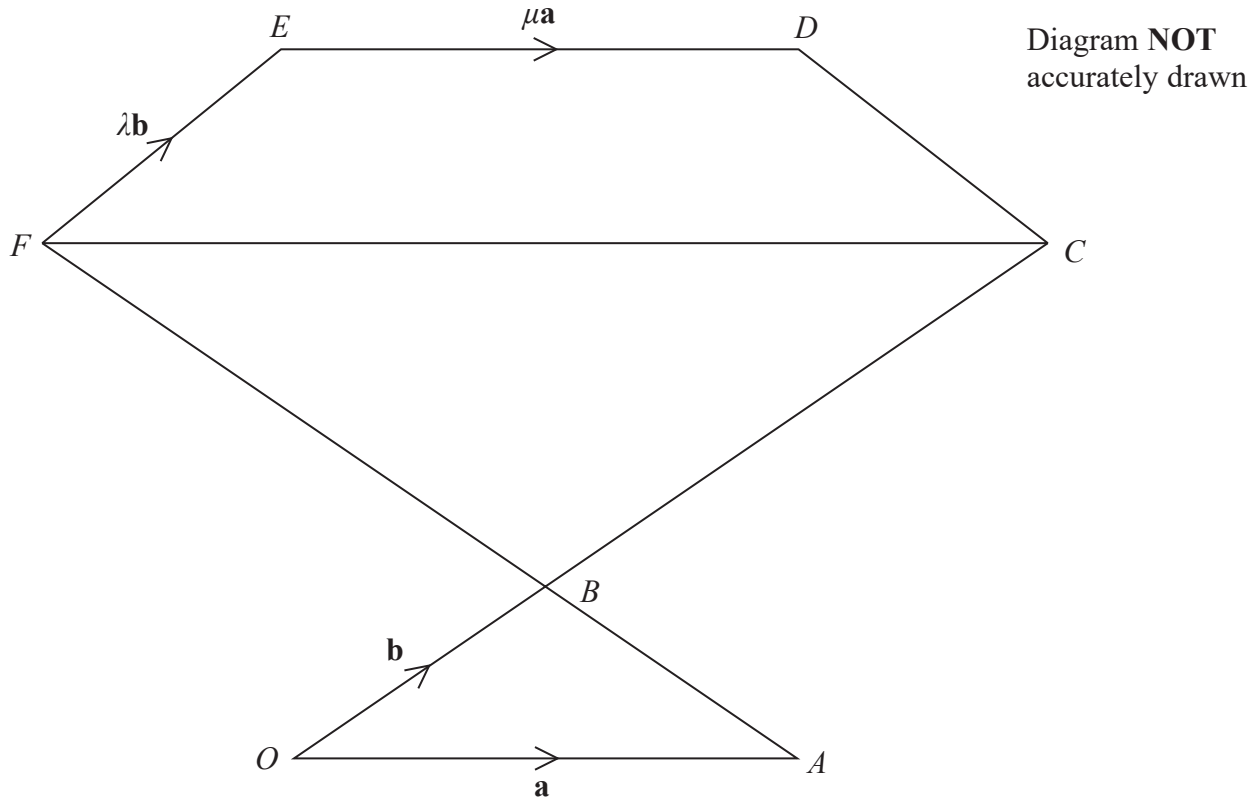


Figure 2

In Figure 2, $\vec{OA} = \mathbf{a}$, $\vec{OB} = \mathbf{b}$, $\vec{FE} = \lambda\mathbf{b}$ and $\vec{ED} = \mu\mathbf{a}$, where λ and μ are positive constants.

B is the point of intersection of OC and AF such that $OB:OC = AB:AF = 1:3$

(a) Find, in terms of \mathbf{a} or \mathbf{b} or \mathbf{a} and \mathbf{b} , simplifying your answers where possible,

$$(i) \vec{AB} \qquad (ii) \vec{CF} \qquad (2)$$

(b) Find, in terms of \mathbf{a} , \mathbf{b} , λ and where necessary μ , simplifying your answers where possible,

$$(i) \vec{CD} \qquad (ii) \vec{AE} \qquad (3)$$

Given that $\vec{AE} = 4\vec{CD}$

(c) find the value of μ and the value of λ . (4)

Given also that $|\mathbf{a}| = 4\text{ cm}$, $|\mathbf{b}| = 1\text{ cm}$ and that the area of the trapezium $CDEF$ is 5 cm^2

(d) calculate the size, in degrees to 3 significant figures, of $\angle CFE$. (4)

(Total for Question 19 is 13 marks)

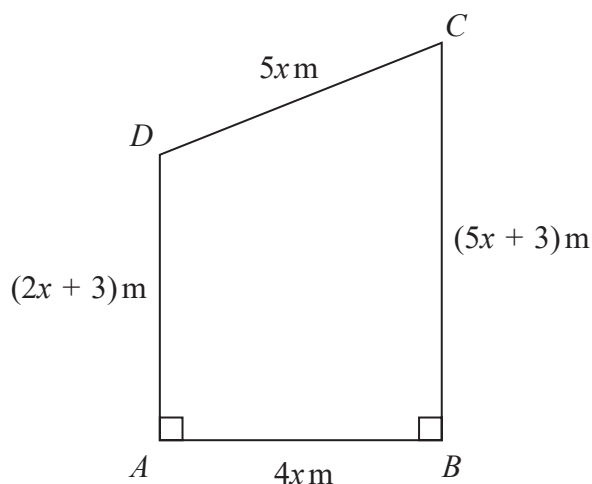


Diagram **NOT**
accurately drawn

Figure 3

Figure 3 shows the plan for a lawn that is in the shape of a trapezium $ABCD$ in which

$$AB = 4x \text{ metres} \quad BC = (5x + 3) \text{ metres} \quad CD = 5x \text{ metres} \quad DA = (2x + 3) \text{ metres}$$

The perimeter of the lawn is P metres.

- (a) Find and simplify an expression for P in terms of x .

(2)

The area of the lawn is $A \text{ m}^2$

- (b) Show that $A = 14x^2 + 12x$

(2)

The owner of the lawn wants the perimeter of the lawn to be greater than 52 m.
He also wants the area of the lawn to be at most 162 m^2

- (c) Find the range of possible values of x .
Show clear algebraic working.

(6)

(Total for Question 20 is 10 marks)

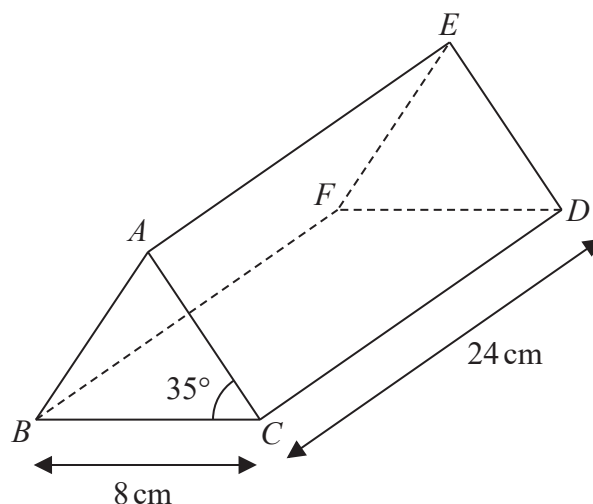


Diagram **NOT**
accurately drawn

Figure 3

Figure 3 shows a solid right triangular prism $ABCDEF$.

A cross section ABC of the prism is an isosceles triangle in which $AB = AC$.

$$\angle ACB = 35^\circ \quad CB = 8 \text{ cm} \quad CD = 24 \text{ cm}$$

- (a) Calculate the total surface area, in cm^2 to 3 significant figures, of the prism.

(5)

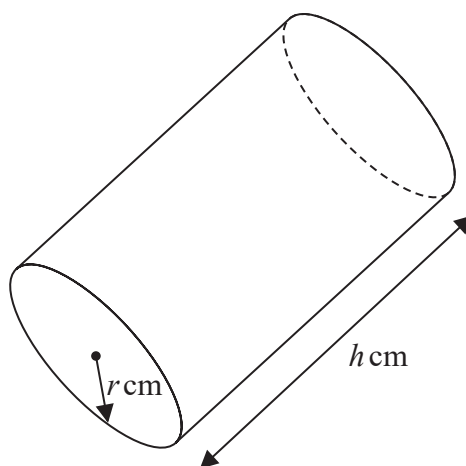


Diagram **NOT**
accurately drawn

Figure 4

Figure 4 shows a solid right circular cylinder with radius $r \text{ cm}$ and length $h \text{ cm}$.

The total surface area of the cylinder is $(224 + 60\sqrt{3})\pi \text{ cm}^2$

Given that $r = 3\sqrt{3} + 2$

- (b) find the exact value of h .

Show your working clearly and give your answer in the form $a\sqrt{27}$ where a is an integer.

(6)

(Total for Question 21 is 11 marks)

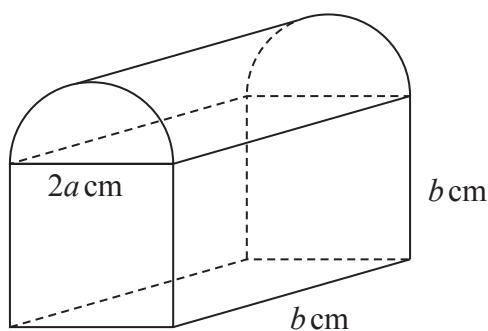


Diagram **NOT**
accurately drawn

Figure 3

Figure 3 shows a solid silver paperweight made from a cuboid and a half cylinder. The cuboid is $2a$ cm wide, b cm long and b cm high. The plane face of the half cylinder coincides with the top face of the cuboid. The total surface area of the paper weight is A cm²

(a) Find an expression for A in terms of π , a and b .

(2)

Given that $a = 6\sqrt{5}$ and that the surface area of the paperweight can be written as

$$(2b^2 + 6ab + 60\pi\sqrt{15}) \text{ cm}^2$$

(b) show that the exact value of b is $10\sqrt{3} - 6\sqrt{5}$

(5)

The paperweight is melted down to form a different cuboid.

This second cuboid is $2a$ cm wide, b cm long and h cm high, as shown in Figure 4.

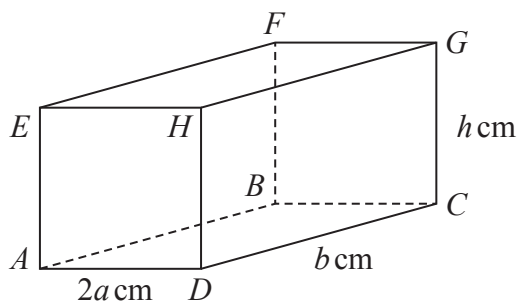


Diagram **NOT**
accurately drawn

Figure 4

(c) Calculate the size, to the nearest degree, of angle GAC .

(5)

(Total for Question 22 is 12 marks)
