



2.

$$f(x) = 2x^3 - 7x^2 - 10x + 24$$

- (a) Use the factor theorem to show that  $(x + 2)$  is a factor of  $f(x)$ .

(2)

- (b) Factorise  $f(x)$  completely.

(4)

3.

$$f(x) = 2x^3 - 7x^2 - 5x + 4$$

- (a) Find the remainder when  $f(x)$  is divided by  $(x-1)$ .

(2)

- (b) Use the factor theorem to show that  $(x+1)$  is a factor of  $f(x)$ .

(2)

- (c) Factorise  $f(x)$  completely.

(4)

4.

$$f(x) = 6x^3 + 13x^2 - 4$$

- Use the remainder theorem to find the remainder when  $f(x)$  is divided by  $(2x + 3)$ .  
(2)
- Use the factor theorem to show that  $(x + 2)$  is a factor of  $f(x)$ .  
(2)
- Factorise  $f(x)$  completely.  
(4)

5.

$$f(x) = 2x^3 + 5x^2 + 2x + 15$$

(a) Use the factor theorem to show that  $(x + 3)$  is a factor of  $f(x)$ .

(2)

(b) Find the constants  $a$ ,  $b$  and  $c$  such that

$$f(x) = (x + 3)(ax^2 + bx + c)$$

(2)

(c) Hence show that  $f(x) = 0$  has only one real root.

(2)

(d) Write down the real root of the equation  $f(x - 5) = 0$

(1)

6

$f(x) = ax^3 + bx^2 - 4x - 3$ , where  $a$  and  $b$  are constants.

Given that  $(x - 1)$  is a factor of  $f(x)$ ,

(a) show that

$$a + b = 7$$

(2)

Given also that, when  $f(x)$  is divided by  $(x + 2)$ , the remainder is 9,

(b) find the value of  $a$  and the value of  $b$ , showing each step in your working.

(4)

7.  $f(x) = 6x^3 + 3x^2 + Ax + B$ , where  $A$  and  $B$  are constants.

Given that when  $f(x)$  is divided by  $(x + 1)$  the remainder is 45,

(a) show that  $B - A = 48$

(2)

Given also that  $(2x + 1)$  is a factor of  $f(x)$ ,

(b) find the value of  $A$  and the value of  $B$ .

(4)

(c) Factorise  $f(x)$  fully.

(3)

[illegible]

8.  $f(x) = ax^3 - 11x^2 + bx + 4$ , where  $a$  and  $b$  are constants.

When  $f(x)$  is divided by  $(x - 3)$  the remainder is 55

When  $f(x)$  is divided by  $(x + 1)$  the remainder is  $-9$

(a) Find the value of  $a$  and the value of  $b$ .

(5)

Given that  $(3x + 2)$  is a factor of  $f(x)$ ,

(b) factorise  $f(x)$  completely.

(4)



9.

$$f(x) = 2x^3 - 5x^2 + ax + 18$$

where  $a$  is a constant.

Given that  $(x - 3)$  is a factor of  $f(x)$ ,

(a) show that  $a = -9$

**(2)**

(b) factorise  $f(x)$  completely.

(4)

Given that

$$g(y) = 2(3^{3y}) - 5(3^{2y}) - 9(3^y) + 18$$

(c) find the values of  $y$  that satisfy  $g(y) = 0$ , giving your answers to 2 decimal places where appropriate.

(3)

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10.

$$f(x) = -6x^3 - 7x^2 + 40x + 21$$

- (a) Use the factor theorem to show that  $(x + 3)$  is a factor of  $f(x)$

(2)

- (b) Factorise  $f(x)$  completely.

(4)

- (c) Hence solve the equation

$$6(2^{3y}) + 7(2^{2y}) = 40(2^y) + 21$$

giving your answer to 2 decimal places.

(3)

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12.

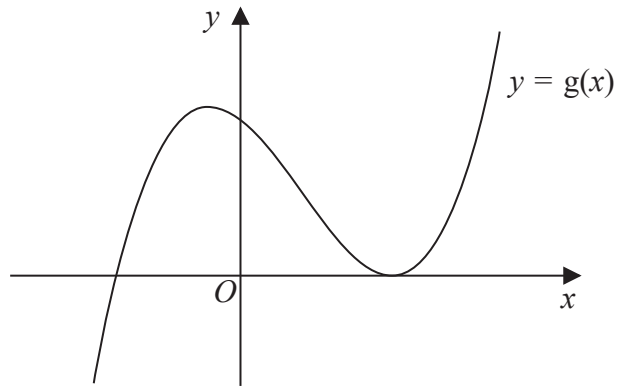
$$g(x) = 4x^3 - 12x^2 - 15x + 50$$

- (a) Use the factor theorem to show that  $(x + 2)$  is a factor of  $g(x)$ .

(2)

- (b) Hence show that  $g(x)$  can be written in the form  $g(x) = (x + 2)(ax + b)^2$ , where  $a$  and  $b$  are integers to be found.

(4)



### Figure 2

Figure 2 shows a sketch of part of the curve with equation  $y = g(x)$

- (c) Use your answer to part (b), and the sketch, to deduce the values of  $x$  for which

- $$(i) \quad g(x) \leq 0$$

- (ii)  $g(2x) = 0$

(3)

13.

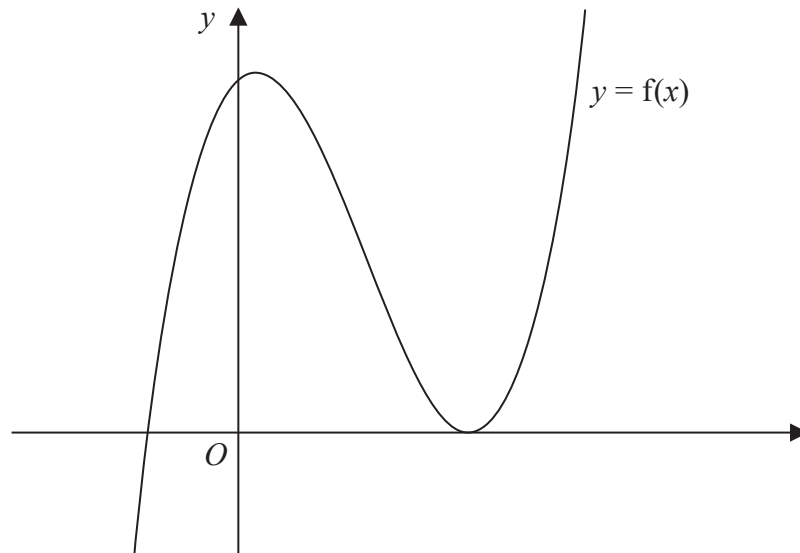
$$f(x) = 2x^3 - 13x^2 + 8x + 48$$

(a) Prove that  $(x - 4)$  is a factor of  $f(x)$ .

(2)

(b) Hence, using algebra, show that the equation  $f(x) = 0$  has only two distinct roots.

(4)



## Figure 2

Figure 2 shows a sketch of part of the curve with equation  $y = f(x)$ .

(c) Deduce, giving reasons for your answer, the number of real roots of the equation

$$2x^3 - 13x^2 + 8x + 46 = 0$$

(2)

Given that  $k$  is a constant and the curve with equation  $y = f(x + k)$  passes through the origin,

(d) find the two possible values of  $k$ .

(2)

14.

$$g(x) = 2x^3 + x^2 - 41x - 70$$

- (a) Use the factor theorem to show that  $g(x)$  is divisible by  $(x - 5)$ . (2)

- (b) Hence, showing all your working, write  $g(x)$  as a product of three linear factors. (4)

The finite region  $R$  is bounded by the curve with equation  $y = g(x)$  and the  $x$ -axis, and lies below the  $x$ -axis.

- (c) Find, using algebraic integration, the exact value of the area of  $R$ . (4)

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