

1. In an arithmetic series

- the first term is 16
- the 21st term is 24

(a) Find the common difference of the series.

(2)

(b) Hence find the sum of the first 500 terms of the series.

(2)

2

A car has six forward gears.

The fastest speed of the car

- in 1<sup>st</sup> gear is 28 km h<sup>-1</sup>
- in 6<sup>th</sup> gear is 115 km h<sup>-1</sup>

Given that the fastest speed of the car in successive gears is modelled by an **arithmetic sequence**,

(a) find the fastest speed of the car in 3<sup>rd</sup> gear.

(3)

Given that the fastest speed of the car in successive gears is modelled by a **geometric sequence**,

(b) find the fastest speed of the car in 5<sup>th</sup> gear.

(3)



4

Jess started work 20 years ago. In year 1 her annual salary was £17 000. Her annual salary increased by £1 500 each year, so that her annual salary in year 2 was £18 500, in year 3 it was £20 000 and so on, forming an arithmetic sequence. This continued until she reached her maximum annual salary of £32 000 in year  $k$ . Her annual salary then remained at £32 000.

- (a) Find the value of the constant  $k$ . (2)
- (b) Calculate the total amount that Jess has earned in the 20 years. (5)

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

5

A boy saves some money over a period of 60 weeks. He saves 10p in week 1, 15p in week 2, 20p in week 3 and so on until week 60. His weekly savings form an arithmetic sequence.

- (a) Find how much he saves in week 15 (2)

- (b) Calculate the total amount he saves over the 60 week period. (3)

The boy's sister also saves some money each week over a period of  $m$  weeks. She saves 10p in week 1, 20p in week 2, 30p in week 3 and so on so that her weekly savings form an arithmetic sequence. She saves a total of £63 in the  $m$  weeks.

- (c) Show that

$$m(m+1) = 35 \times 36 \quad (4)$$

- (d) Hence write down the value of  $m$ . (1)

6

In the year 2000 a shop sold 150 computers. Each year the shop sold 10 more computers than the year before, so that the shop sold 160 computers in 2001, 170 computers in 2002, and so on forming an arithmetic sequence.

- (a) Show that the shop sold 220 computers in 2007. (2)
- (b) Calculate the total number of computers the shop sold from 2000 to 2013 inclusive. (3)

In the year 2000, the selling price of each computer was £900. The selling price fell by £20 each year, so that in 2001 the selling price was £880, in 2002 the selling price was £860, and so on forming an arithmetic sequence.

- (c) In a particular year, the selling price of each computer in £s was equal to three times the number of computers the shop sold in that year. By forming and solving an equation, find the year in which this occurred. (4)

- When John had received  $n$  of these birthday gifts, the total money that he had received from these gifts was £3375

- (d) Show that  $n^2 + 7n = 25 \times 18$  (3)
- (e) Find the value of  $n$ , when he had received £3375 in total, and so determine John's age at this time. (2)





**9. (i)** In an arithmetic series, the first term is  $a$  and the common difference is  $d$ .

Show that

$$S_n = \frac{n}{2} [2a + (n-1)d] \quad (3)$$

(ii) James saves money over a number of weeks to buy a printer that costs £64

He saves £10 in week 1, £9.20 in week 2, £8.40 in week 3 and so on, so that the weekly amounts he saves form an arithmetic sequence.

Given that James takes  $n$  weeks to save exactly £64

(a) show that

$$n^2 - 26n + 160 = 0 \quad (2)$$

(b) Solve the equation

$$n^2 - 26n + 160 = 0 \quad (1)$$

(c) Hence state the number of weeks James takes to save enough money to buy the printer, giving a brief reason for your answer.

(1)