1.	A curve C has parametric equations
	$x = 2t - 1$, $y = 4t - 7 + \frac{3}{t}$, $t \neq 0$
	Show that the Cartesian equation of the curve C can be written in the form
	$y = \frac{2x^2 + ax + b}{x+1}, \qquad x \neq -1$
	where a and b are integers to be found. (3)

2	A curve	Chas	parametric	equations
∠•	A curve	Chas	parametric	cquations

$$x = 4t + 3$$
, $y = 4t + 8 + \frac{5}{2t}$, $t \neq 0$

(a) Find the value of $\frac{dy}{dx}$ at the point on C where t = 2, giving your answer as a fraction in its simplest form.

(3)

(b) Show that the cartesian equation of the curve C can be written in the form

$$y = \frac{x^2 + ax + b}{x - 3}, \quad x \neq 3$$

where a and b are integers to be determined.

(3)

3. A curve C has parametric equations				
	$x = \frac{t^2 + 5}{t^2 + 1}$	$y = \frac{4t}{t^2 + 1}$	$t \in \mathbb{R}$	
Show that all points on C	satisfy			
		$(x-3)^2 + y^2 = 4$		
				(3)

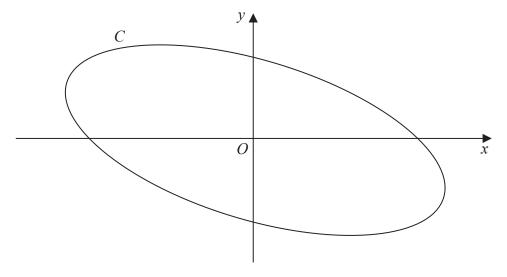


Figure 3

Figure 3 shows a sketch of the curve C with parametric equations

$$x = 4\cos\left(t + \frac{\pi}{6}\right), \quad y = 2\sin t, \quad 0 \leqslant t < 2\pi$$

(a) Show that

$$x + y = 2\sqrt{3} \cos t \tag{3}$$

(b) Show that a cartesian equation of C is

$$(x+y)^2 + ay^2 = b$$

where a and b are integers to be determined.

(2)

5	The ourse	Chag	parametric	aquations
J.	THE CUIVE	C mas	parametric	cquations

$$x = 3t - 4$$
, $y = 5 - \frac{6}{t}$, $t > 0$

(a) Find $\frac{dy}{dx}$ in terms of t

(2)

The point *P* lies on *C* where $t = \frac{1}{2}$

(b) Find the equation of the tangent to C at the point P. Give your answer in the form y = px + q, where p and q are integers to be determined.

(3)

(c) Show that the cartesian equation for C can be written in the form

$$y = \frac{ax+b}{x+4}, \quad x > -4$$

where a and b are integers to be determined.

(3)

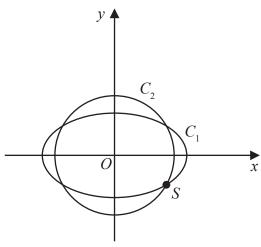


Figure 2

The curve C_1 with parametric equations

$$x = 10\cos t, \quad y = 4\sqrt{2}\sin t, \quad 0 \leqslant t < 2\pi$$

meets the circle C_2 with equation

$$x^2 + y^2 = 66$$

at four distinct points as shown in Figure 2.

Given that one of these points, S, lies in the 4th quadrant, find the Cartesian coordinates of S.

(6)



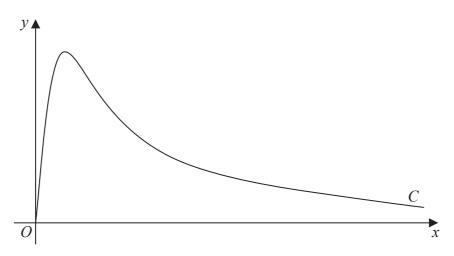


Figure 2

Figure 2 shows a sketch of the curve C with parametric equations

$$x = 4 \tan t$$
, $y = 5\sqrt{3} \sin 2t$, $0 \leqslant t < \frac{\pi}{2}$

The point *P* lies on *C* and has coordinates $\left(4\sqrt{3}, \frac{15}{2}\right)$.

(a) Find the exact value of $\frac{dy}{dx}$ at the point P.

Give your answer as a simplified surd.

(4)

The point Q lies on the curve C, where $\frac{dy}{dx} = 0$

(b) Find the exact coordinates of the point Q.

(2)

8.	The curve C has parametric equations	
	$x = t^2 + 6t - 16$ $y = 6\ln(t+3)$ $t > -3$	
	(a) Show that a Cartesian equation for <i>C</i> is	
	$y = A \ln (x + B) \qquad x > -B$	
	where A and B are integers to be found.	(2)
	The curve C cuts the y-axis at the point P	(3)
	(b) Show that the equation of the tangent to C at P can be written in the form	
	$ax + by = c \ln 5$	
	where a , b and c are integers to be found.	
		(4)

(4)
(3)
(2)

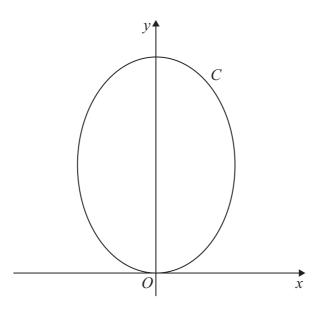


Figure 2

Figure 2 shows a sketch of the curve C with parametric equations

$$x = (\sqrt{3})\sin 2t$$
, $y = 4\cos^2 t$, $0 \le t \le \pi$

- (a) Sh that $\frac{dy}{dx} = k(\sqrt{3})\tan 2t$, where k is a constant to be determined. (5)
- (b) Find an equation of the tangent to C at the point where $t = \frac{\pi}{3}$. Give your answer in the form y = ax + b, where a and b are constants.
- (c) Find a cartesian equation of C.

(3)

11. The curve C has parametric equations				
$x = \sin 2\theta \qquad y = \csc^3 \theta \qquad 0 < \theta < \frac{\pi}{2}$				
(a) Find an expression for $\frac{dy}{dx}$ in terms of θ				
(b) Hence find the exact value of the gradient of the tangent to C at the point where $y = 8$ (3)				

12. The curve C has parametric equations	
$x = 2\cos t, y = \sqrt{3}\cos 2t, 0 \leqslant t \leqslant \pi$	
(a) Find an expression for $\frac{dy}{dx}$ in terms of t.	(2)
The point <i>P</i> lies on <i>C</i> where $t = \frac{2\pi}{3}$	
The line l is the normal to C at P .	
(b) Show that an equation for l is	
$2x - 2\sqrt{3}y - 1 = 0$	(5)
The line l intersects the curve C again at the point Q .	
(c) Find the exact coordinates of Q .	
You must show clearly how you obtained your answers.	(6)

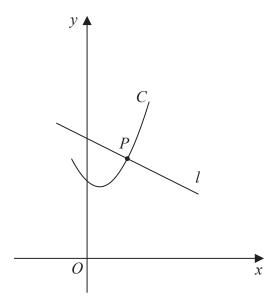


Figure 6

Figure 6 shows a sketch of the curve C with parametric equations

$$x = 2\tan t + 1 \qquad \qquad y = 2\sec^2 t + 3 \qquad \qquad -\frac{\pi}{4} \leqslant t \leqslant \frac{\pi}{3}$$

The line *l* is the normal to *C* at the point *P* where $t = \frac{\pi}{4}$

(a) Using parametric differentiation, show that an equation for l is

$$y = -\frac{1}{2}x + \frac{17}{2} \tag{5}$$

(b) Show that all points on C satisfy the equation

$$y = \frac{1}{2} (x - 1)^2 + 5$$
 (2)

The straight line with equation

$$y = -\frac{1}{2}x + k$$
 where k is a constant

intersects C at two distinct points.

(c) Find the range of possible values for k.

(5)