1.	Find	
	$\int \left(8x^3 - \frac{3}{2\sqrt{x}} + 5\right) \mathrm{d}x$	
	giving your answer in simplest form.	(4)

2.	Find $\int \left(\frac{2}{3}x^3 - 6\sqrt{x} + 1\right) dx$	
	giving your answer in its simplest form.	(4)

3.	Find	
	$\int \frac{3x^4 - 4}{2x^3}  \mathrm{d}x$	
	writing your answer in simplest form.	(4)

Use integration to find $\int_{1}^{\sqrt{3}} \left( \frac{x^3}{6} + \frac{1}{3x^2} \right) dx$	
giving your answer in the form $a + b\sqrt{3}$ , where a and b are constants to	be determined. (5)

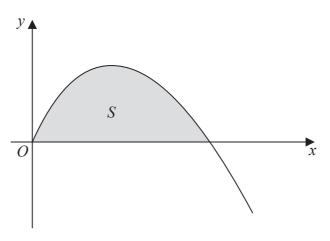


Figure 3

Figure 3 shows a sketch of part of the curve with equation

$$y = 3x - x^{\frac{3}{2}}, \qquad x \geqslant 0$$

The finite region S, bounded by the x-axis and the curve, is shown shaded in Figure 3.

(a) Find

$$\int \left(3x - x^{\frac{3}{2}}\right) \mathrm{d}x \tag{3}$$

(b) Hence find the area of S.

(3)



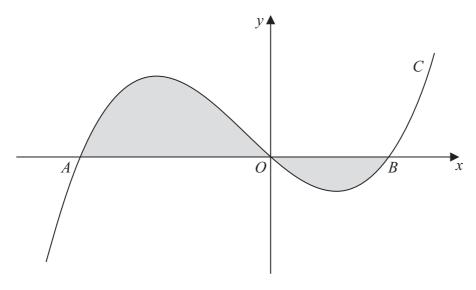


Figure 3

Figure 3 shows a sketch of part of the curve C with equation

$$y = x(x+4)(x-2)$$

The curve C crosses the x-axis at the origin O and at the points A and B.

(a) Write down the x-coordinates of the points A and B.

**(1)** 

The finite region, shown shaded in Figure 3, is bounded by the curve C and the x-axis.

(b) Use integration to find the total area of the finite region shown shaded in Figure 3. (7)

7. (a) Find

$$\int 10x(x^{\frac{1}{2}}-2)\mathrm{d}x$$

giving each term in its simplest form.

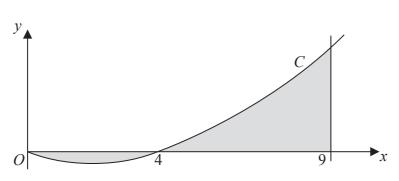


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = 10x(x^{\frac{1}{2}} - 2), \qquad x \geqslant 0$$

The curve C starts at the origin and crosses the x-axis at the point (4, 0).

The area, shown shaded in Figure 2, consists of two finite regions and is bounded by the curve C, the x-axis and the line x = 9

(b) Use your answer from part (a) to find the total area of the shaded regions.

**(5)** 

**(4)** 


**8.** A curve C has equation y = f(x) where

$$f(x) = -3x^2 + 12x + 8$$

(a) Write f(x) in the form

$$a(x+b)^2+c$$

where a, b and c are constants to be found.

**(3)** 

The curve C has a maximum turning point at M.

(b) Find the coordinates of M.

**(2)** 

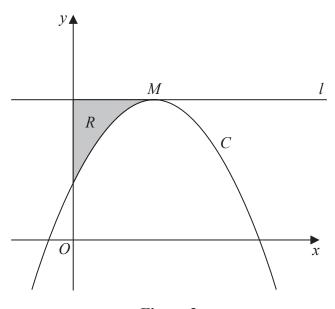


Figure 3

Figure 3 shows a sketch of the curve *C*.

The line l passes through M and is parallel to the x-axis.

The region R, shown shaded in Figure 3, is bounded by C, l and the y-axis.

(c) Using algebraic integration, find the area of R.

**(5)** 

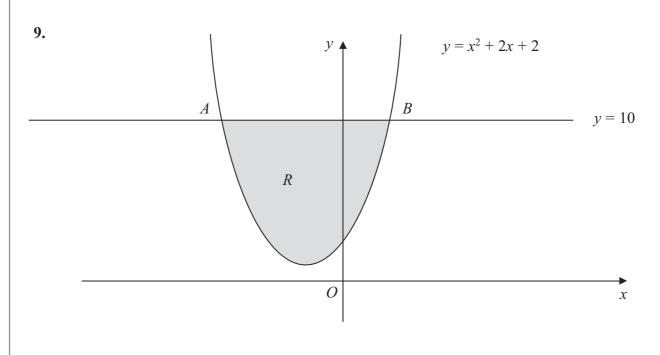


Figure 1

The line with equation y = 10 cuts the curve with equation  $y = x^2 + 2x + 2$  at the points A and B as shown in Figure 1. The figure is not drawn to scale.

(a) Find by calculation the x-coordinate of A and the x-coordinate of B. (2)

The shaded region R is bounded by the line with equation y = 10 and the curve as shown in Figure 1.

(b) Use calculus to find the exact area of $R$ .	

10.	$g(x) = 2x^3 + x^2 - 41x - 70$	
	(a) Use the factor theorem to show that $g(x)$ is divisible by $(x - 5)$ .	(2)
	(b) Hence, showing all your working, write $g(x)$ as a product of three linear factors.	(4)
	The finite region $R$ is bounded by the curve with equation $y = g(x)$ and the $x$ -axis, and lies below the $x$ -axis.	
	(c) Find, using algebraic integration, the exact value of the area of $R$ .	(4)

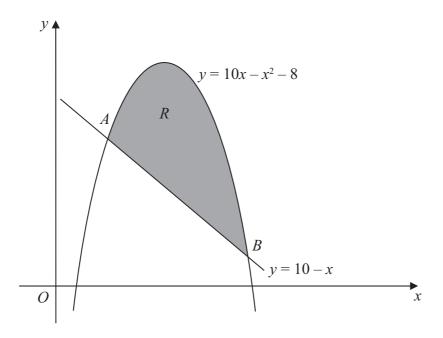


Figure 2

Figure 2 shows the line with equation y = 10 - x and the curve with equation  $y = 10x - x^2 - 8$ 

The line and the curve intersect at the points A and B, and O is the origin.

(a) Calculate the coordinates of A and the coordinates of B.

**(5)** 

The shaded area R is bounded by the line and the curve, as shown in Figure 2.

(b) Calculate the exact area of R.

**(7)** 

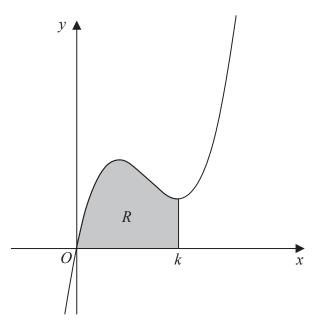


Figure 3

Figure 3 shows a sketch of part of the curve with equation

$$y = 2x^3 - 17x^2 + 40x$$

The curve has a minimum turning point at x = k.

The region R, shown shaded in Figure 3, is bounded by the curve, the x-axis and the line with equation x = k.

Show that the area of *R* is  $\frac{256}{3}$ 

 $(Solutions\ based\ entirely\ on\ graphical\ or\ numerical\ methods\ are\ not\ acceptable.)$ 

(7)

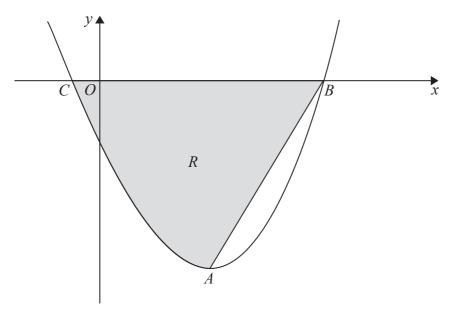



Figure 2

Figure 2 shows a sketch of part of the curve with equation

$$y = 4x^3 + 9x^2 - 30x - 8$$
,  $-0.5 \le x \le 2.2$ 

The curve has a turning point at the point A.

(a) Using calculus, show that the x coordinate of A is 1

**(3)** 

The curve crosses the *x*-axis at the points B(2, 0) and  $C\left(-\frac{1}{4}, 0\right)$ 

The finite region R, shown shaded in Figure 2, is bounded by the curve, the line AB, and the x-axis.

(b) Use integration to find the area of the finite region *R*, giving your answer to 2 decimal places.

**(7)** 

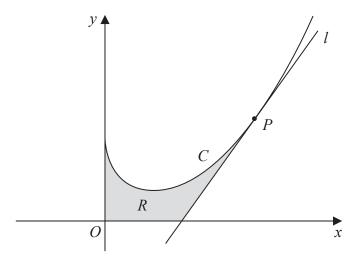



Figure 2

In this question you must show all stages of your working.  $\hspace{-0.5cm}$ 

Solutions relying on calculator technology are not acceptable.

Figure 2 shows a sketch of part of the curve C with equation

$$y = \frac{1}{3}x^2 - 2\sqrt{x} + 3 \qquad x \geqslant 0$$

The point P lies on C and has x coordinate 4

The line l is the tangent to C at P.

(a) Show that l has equation

$$13x - 6y - 26 = 0 ag{5}$$

The region R, shown shaded in Figure 2, is bounded by the y-axis, the curve C, the line l and the x-axis.

(b) Find the exact area of R.

**(5)** 

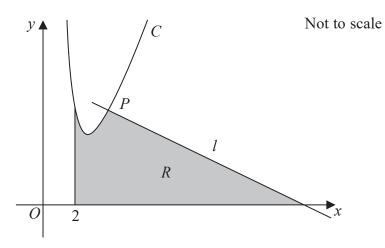


Figure 4

Figure 4 shows a sketch of part of the curve C with equation

$$y = \frac{32}{x^2} + 3x - 8, \qquad x > 0$$

The point P(4, 6) lies on C.

The line l is the normal to C at the point P.

The region R, shown shaded in Figure 4, is bounded by the line l, the curve C, the line with equation x = 2 and the x-axis.

Show that the area of R is 46

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(10)