Méthodes de conception de programmes Devoir 1



École polytechnique de Louvain

GROUPE J

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1 Introduction

L'objectif de ce premier devoir dans le cadre du cours de Méthodes de Conception de Programmes consiste à mettre au point un algorithme nommé **find_repeat(a, n)** prenant comme paramètres :

- a : une liste de caractères quelconques
- n: le nombre d'éléments identiques recherchés dans a

L'algorithme find_repeat(a, n) retourne donc la position de la première occurrence d'une répétition de n caracteres dans a. Par exemple, find_repeat("merciii xxx", 3) retourne 4 et find_repeat("merciii xxx", 4) retourne -1.

2 Implémentation de notre solution

Pour ce devoir, nous avons choisi une implémentation en Java... voici notre algorithme :

```
public static int find_repeat(String a, int n) {
      @Pre : prend en compte a (une chaine de caracteres
        quelconques) et n (le nombre d'elements identiques
        dans a)
     * @Post : return la position de la premiere occurence
        d'une repetition de n elements identiques dans a
    int len_list = a.length();
    int counter = 1;
    int index = 1;
    char sample = a.charAt(0);
    /* Boucle 1 */
    while(index < len_list){</pre>
        if(a.charAt(index) == sample){
            counter++;
        } else {
            sample = a.charAt(index);
            counter = 1;
        }
        if(counter == n){
            return index - counter +1;
        index++;
    }
    return -1;
}
```

3 Spécification complète et formelle

@Pre: $0 < n \le |a| \land |a| > 0 \Longrightarrow 0 < n \le |a|$

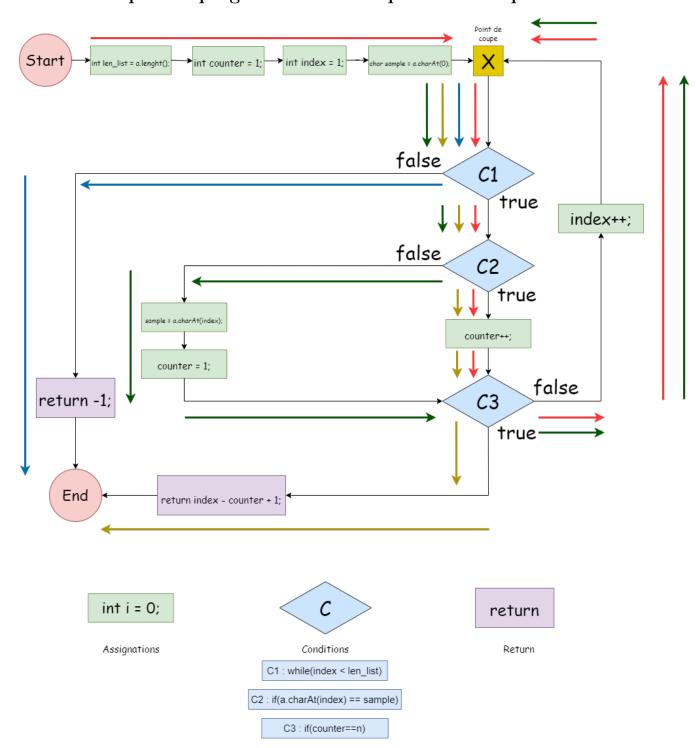
 $\textbf{@Post:} \ (Result = index - counter + 1 \ \land \ counter == n) \ \lor \ (Result = -1 \ \land \ index ==$

 $|a| \land counter < n$

Invariant: $1 \le index < |a| \land counter \le n$

Variant: |a| - index

4 Graphe du programme avec les points de coupe



5 Preuve

Assertions inductives

```
Chemin 1
```

Chemin 2

```
 @I[1\leqslant index < |a| \land counter \leqslant n] \\ [index \geqslant len\_list \implies ((result = index - counter + 1 \land counter == n) \lor (result = -1 \land index == |a| \land counter < n))] \\ assume index \geqslant len\_list; \\ [(-1 = index - counter + 1 \land counter == n) \lor (-1 = -1 \land index == |a| \land counter < n)] \\ result := -1; \\ @Post[(Result = index - counter + 1 \land counter == n) \lor (Result = -1 \land index == |a| \land counter < n)]
```

Chemin 3

```
@I[1 \leqslant index < |a| \land counter \leqslant n]
                        [index < len \ list \implies a.charAt(index) = sample \implies counter + 1 == n \implies ((index - list) + list) = (index - lis
                       counter + 1 = index - counter + 1 \land counter == n) \lor (index - counter + 1 = -1 \land index ==
                       |a| \wedge counter < n)
                       assume index < len list;
                       assume a.charAt(index) = sample;
                       [counter + 1 == n \implies ((index - counter + 2 = index - counter + 2 \land counter + 1 ==
                       n) \lor (index - counter + 2 = -1 \land index == |a| \land counter + 1 < n))]
                       counter++;
                        [counter == n \Longrightarrow ((index - counter + 1 = index - counter + 1 \land counter == n) \lor (index - counter
                       counter + 1 = -1 \land index == |a| \land counter < n)
                       assume counter == n;
                       [(index-counter+1=index-counter+1 \land counter==n) \lor (index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-cou
                           -1 \wedge index == |a| \wedge counter < n
                       result := index - counter + 1;
@Post[(Result = index - counter + 1 \land counter == n) \lor (Result = -1 \land index ==
|a| \wedge counter < n
```

Chemin 4

```
 @I[1 \leqslant index < |a| \land counter \leqslant n] \\ [index < len\_list \implies a.charAt(index) \neq sample \implies 1 = n \implies ((index - 1 + 1 = index - 1 + 1 \land 1 == n) \lor (index - 1 + 1 = -1 \land index == |a| \land 1 < n))] \\ assume index < len\_list; \\ assume a.charAt(index) \neq sample; \\ sample = a.charAt(index); \\ [1 = n \implies ((index - 1 + 1 = index - 1 + 1 \land 1 == n) \lor (index - 1 + 1 = -1 \land index == |a| \land 1 < n))] \\ counter = 1; \\ [counter = n \implies ((index - counter + 1 = index - counter + 1 \land counter == n) \lor (index - counter == n) \lor (i
```

```
counter + 1 = -1 \land index == |a| \land counter < n))
              assume counter = n;
              [(index-counter+1=index-counter+1 \land counter==n) \lor (index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter+1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-counter-1=index-cou
                -1 \land index == |a| \land counter < n
              result := index - counter + 1;
@Post[(Result = index - counter + 1 \land counter == n) \lor (Result = -1 \land index ==
 |a| \wedge counter < n
Chemin 5
@I[1 \leqslant index < |a| \land counter \leqslant n]
               [index < len \ list \implies a.charAt(index) \neq sample \implies 1 \neq n \implies (1 \leq index + 1 < |a| \land 1 \leq n)]
              assume index < len list;
              assume a.charAt(index) \neq sample;
              sample = a.charAt(index);
              [1 \neq n \Longrightarrow (1 \leqslant index + 1 < |a| \land 1 \leqslant n)]
              counter = 1;
               [counter \neq n \Longrightarrow (1 \leqslant index + 1 < |a| \land counter \leqslant n)]
              assume counter \neq n;
              [1 \leqslant index + 1 < |a| \land counter \leqslant n]
              index++;
@I[1 \leqslant index < |a| \land counter \leqslant n]
Chemin 6
@I[1 \leqslant index < |a| \land counter \leqslant n]
               [index < len \ list \implies a.charAt(index) = sample \implies counter + 1 \neq n \implies (1 \leq index + 1 < 1 \leq index + 1 \leq 1 \leq index + 1 \leq 1 \leq index + 1 \leq 1 \leq index \leq 1 \leq 
               |a| \wedge counter + 1 \leq n
              assume index < len list;
              assume a.charAt(index) = sample;
               [counter + 1 \neq n \Longrightarrow (1 \leqslant index + 1 < |a| \land counter + 1 \leqslant n)]
              counter++;
              [counter \neq n \Longrightarrow (1 \leqslant index + 1 < |a| \land counter \leqslant n)]
              assume counter \neq n;
              [1 \leqslant index + 1 < |a| \land counter \leqslant n]
              index++;
@I[1 \leqslant index < |a| \land counter \leqslant n]
Diminution des variants
[1 \leqslant index < |a| \land counter \leqslant n \land |a| - index = v_0]
              assume index < len list;
              assume a.charAt(index) \neq sample;
              sample = a.charAt(index);
              counter = 1;
              assume counter \neq n;
              index++;
[|a| - index > 0]
[1 \leqslant index < |a| \land counter \leqslant n \land |a| - index = v_0]
              assume index < len list;
              assume a.charAt(index) = sample;
              counter++;
```

```
\begin{array}{l} {\rm assume~counter} \neq {\rm n}\,;\\ {\rm index} + +\,;\\ [|a| - index > 0] \end{array}
```

6 Conclusion

Ceci conclu donc ce premier devoir dans le cadre du cours de Méthodes de conception de programmes.