

Graph of Equations

Set Notation

Roster Notation: $A = \{a, b, c\}$ or $A = \{a, b, c, \dots, z\}$

Set Builder Notation: $A = \{x \mid x \text{ is a lowercase character in the Latin alphabet}\}$

Terminology and implications

Given sets...

$$\begin{aligned}A &= \{a, b, c\} \\B &= \{a, b, c, \dots, z\} \\C &= \{a, e, i, o, u\} \\D &= \{a, i, u, e, o\} \\E &= \{a, e, i\}\end{aligned}$$

We know

$a \in A$	a is an element of A
$e \notin A$	e is not an element of A
$A \notin A$	A set cannot be an element of a set
$\emptyset = \{\}$	
$U = \text{All elements of interest}$	
$C = D$	
$C \neq E$	
$E \subset C$	E is a proper subset of C
$E \subseteq C$	E is a subset of C
$A \cup E = \{a, b, c, e, i\}$	A union E equals everything in A or E
$A \cap E = \{a\}$	A join E equals everything in A and E
$A^c = \{d, e, f, \dots, z\}$	The compliment of A is all elements in the universal set and not in A

Laws and Properties

Commutative

$$\begin{aligned}A \cup B &= B \cup A \\A \cap B &= B \cap A\end{aligned}$$

Associative

$$\begin{aligned}A \cup (B \cup C) &= (A \cup B) \cup C \\A \cap (B \cap C) &= (A \cap B) \cap C\end{aligned}$$

Distributive

$$\begin{aligned}A \cup (B \cap C) &= (A \cup B) \cap (A \cup C) \\A \cap (B \cup C) &= (A \cap B) \cup (A \cap C)\end{aligned}$$

De Morgans Laws

$$\begin{aligned}(A \cup B)^c &= A^c \cap B^c \\(A \cap B)^c &= A^c \cup B^c\end{aligned}$$

Combinatorics

$$\begin{aligned}n(S) &= \text{Number of unique items in set } S \\n(A \cup B) &= n(A) + n(B) - n(A \cap B) \\n(A \cup B \cup C) &= n(A) + n(B) + n(C) \\&\quad - n(A \cap B) - n(A \cap C) \\&\quad - n(B \cap C) + n(A \cap B \cap C)\end{aligned}$$

Graphing Trigonometric Functions

Assume...

$$y = d + a * f(bx - c)$$

$$\text{Amplitude} = |a|$$

$$\text{Vertical Shift} = d$$

$$\text{Phase Shift} = \frac{c}{b}$$

$$\text{X-Scale (change between critical points)} = \frac{\text{period}}{4}$$

Period depends on what functions

$$\sin, \cos, \csc, \sec = \frac{2\pi}{b}$$

$$\tan, \cot = \frac{\pi}{b}$$

Examples...