

Integral Cheat sheet

Common Functions

Equation	Antiderivative
0	C
k	$kx + C$
$kf(x) dx$	$k \int f(x) dx$
$\int [f(x) \pm g(x)] dx$	$\int f(x) dx \pm \int g(x) dx$
e^x	$e^x + C$
a^x	$(\frac{1}{\ln(a)})a^x + C$
$\frac{1}{x}$	$\ln x + C$

Trigonometric Integrals

$$\int \sin = -\cos + C$$

$$\int \cos = \sin + C$$

$$\int \tan = -\ln|\cos| + C$$

$$\int \cot = \ln|\sin| + C$$

$$\int \sec = \ln|\sec + \tan| + C$$

$$\int \csc = -\ln|\csc + \cot| + C$$

Abnormal Trigonometric Integrals

$$\int \sec^2 = \tan + C$$

$$\int \sec * \tan = \sec + C$$

$$\int \csc^2 = -\cot + C$$

$$\int \csc * \cot = -\csc + C$$

Inverse Trigonometric Integrals (a is positive)

$$\int \frac{1}{\sqrt{a^2 - x^2}} = \arcsin\left(\frac{x}{a}\right) + C$$

$$\int \frac{1}{a^2 + x^2} = \frac{1}{a} \arctan\left(\frac{x}{a}\right) + C$$

$$\int \frac{1}{x\sqrt{x^2 - a^2}} = \frac{1}{a} \operatorname{arcsec}\left(\frac{|x|}{a}\right) + C$$

Derivative Rules

Power Rule

$$dx(x^n) = n * x^{n-1}$$

Product Rule

$$dx(f(x) * g(x)) = f'(x)g(x) + g'(x)f(x)$$

Quotient Rule

$$dx\left(\frac{f(x)}{g(x)}\right) = \frac{f'(x)g(x) - g'(x)f(x)}{(g(x))^2}$$

Chain Rule

$$dx f(g(x)) = f'(g(x)) * g'(x)$$

Nested Chain Rule

$$\begin{aligned} dx f(g(h(x))) &= f'(g(h(x))) \\ &\quad * g'(h(x)) \\ &\quad * h'(x) \end{aligned}$$

Other things to note

$$\ln\left(\frac{x}{y}\right) = \ln(x) - \ln(y)$$

$$\ln(xy) = \ln(x) + \ln(y)$$

$$\ln(x^y) = y * \ln(x)$$