Variational Bayes methods for clinical real-world data

Rationale



The identification of specific patient groups sharing similar disease-related phenotypes is fundamental to many clinical studies

Electronic Health Records (EHR) data has long been incorporated in phenotypic studies, which makes more complex the models to identify patient phenotypes.

Rationale

Bayesian approach: **Prior information + current information** at clinical trials **But!**

Patient phenotyping has been **limited by the computational challenges associated with applying the Markov-Chain Monte Carlo (MCMC)** approach to large real-world data.

Computational Time



Storage Requirements



Main objective

Benchmark a VI implementation against MCMC in estimating a posterior model, predictive performance and computational performance in terms of time.

Dataset

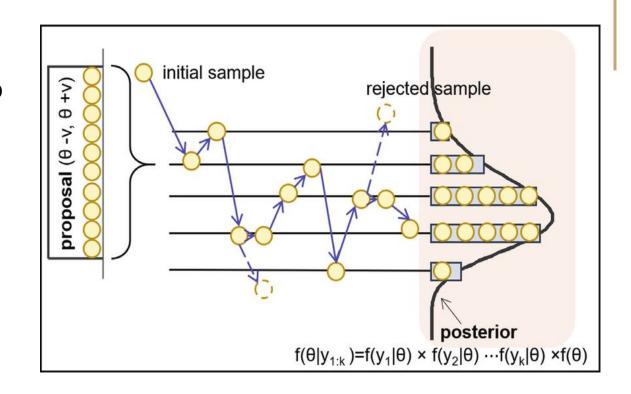
We analysed Type 2 Diabetes data. The response variable is "diagnosed type 2 diabetes". The predictors are all continuous variables (Pregnancies, Glucose, BloodPressure, SkinThickness, Insulin, BMI, DiabetesPedigree, Age). Size: 768 rows. https://www.kaggle.com/datasets/uciml/pima-indians-diabetes-database

Predictive model

Since clinical data analyses commonly employ logistic regression, we chose this approach for comparative purposes.

MARKOV CHAIN - MONTECARLO

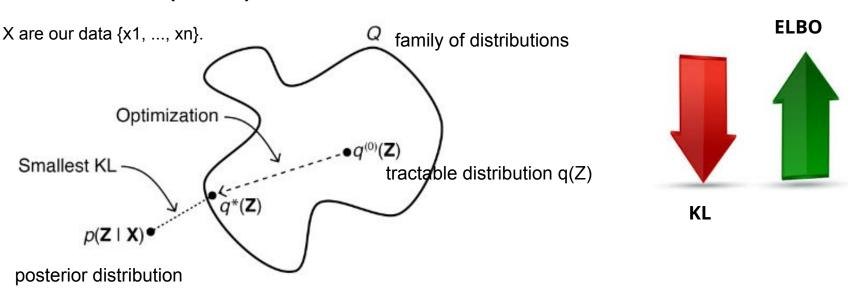
In order to sample from an unknown **p** distribution, using the un-normalized distribution $\tilde{\mathbf{p}}$ we create a Markov chain that has **p** as its stationary distribution and we sample from it.



Variational Inference (VI)

Optimization process

Z are latent variables {z1, ..., zn}



This optimisation approach is often significantly more computationally efficient than MCMC in the posterior distribution estimation.

Metrics

Diagnostic Testing Accuracy: Sensitivity, Specificity, Predictive Values and Likelihood Ratios

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Definition/Introduction

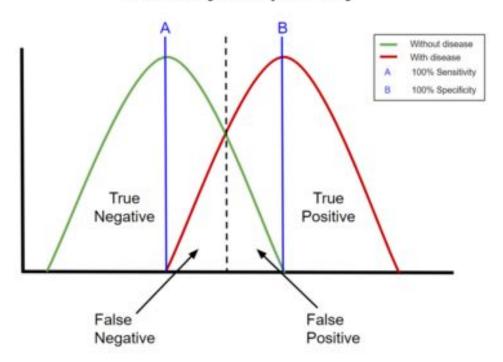
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To make clinical decisions and guide patient care, providers must comprehend the likelihood of a patient having a disease, combining an understanding of pretest probability and diagnostic assessments.[1] Diagnostic tools are routinely utilized in healthcare settings to determine treatment methods; however, many of these tools are subject to error.

Metrics

Sensitivity = TP/(TP+FN) Specificity = TN/(TN+FP)

Sensitivity vs. Specificity



Metrics

5-Folds Cross validation



MARKOV CHAIN MONTECARLO

NUTS Kernel:

A variation of Hamiltonian MCMC that authomatically determines the trajectory length, avoiding the need for manual hyperparameter tuning

- 2 Chains
- 200 warmup steps per chain
- 200 samples per chain

Coeficient * variable	Effective_ samples	R_hat
W1* Pregnancies	177.36	1
W2 * Glucose	600.87	1
W3 * BloodPressure	516.45	1
W4* SkinThickness	445.51	1
W5* Insulin	459.31	1
W6* BMI	303.77	1
W7* Diabetes Pedigree Function	137.09	1.01
W8 * Age	289.83	1

STOCHASTIC VARIATIONAL INFERENCE (SVI)

- SVI employs Monte Carlo estimation to estimate the gradients of the ELBO.
- SVI randomly selects a subset or mini-batch of data points to compute the gradients on the ELBO. This allows for efficient and scalable inference.
- Lastly, SVI sacrifices some accuracy compared to exact Bayesian inference. The
 convergence to the true posterior distribution depends on the quality of the approximation
 and the number of iterations in the optimization process.

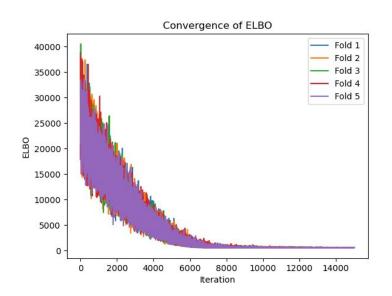
SVI implementation setting

Bayesian logistic regression model with Normal prior distributions for the model parameters. The logits are calculated based on the feature matrix X, and the observed data y is modeled using a Bernoulli likelihood. After, during SVI, a guide (variational distribution) function is used to approximate the true posterior distribution of the model parameters given the observed data.

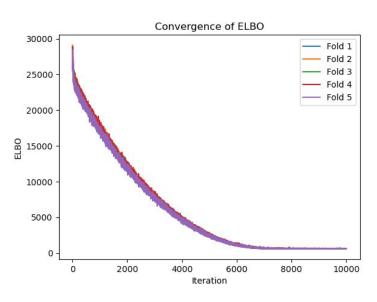
- **Optimizer: Adam** (Adaptive Moment Estimation) update the parameters (weights) during training. It is an extension of the stochastic gradient descent (SGD) optimization algorithm. Compute Gradients: In each iteration (or mini-batch), the gradients of the model's parameters with respect to the loss function are computed.
- Learning rate: 0.01. The learning rate (ηn) controls the step size in each iteration.
- Number of Iterations: 7000
- Mini-batch size (determines the number of samples used for Monte Carlo estimation in the ELBO computation): 64

OPTIMIZATION PROCESS Metric of convergence: ELBO

Before minibathes

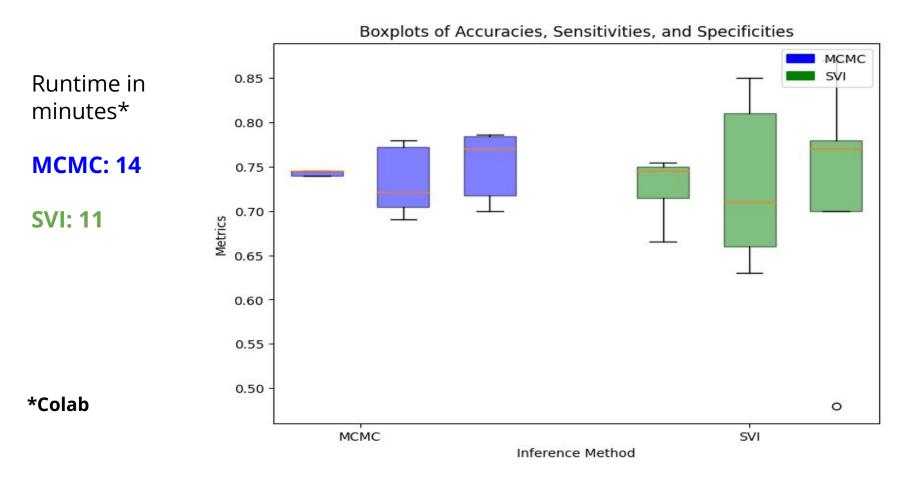


After minibathes



Minibatches allows to update the variational parameters more frequently, making the optimization process more efficient and reducing the variance in the parameter estimates.

COMPARISON OF RESULTS



Conclusion

The Pima dataset is a valuable base to compare MCMC and VI. It is small enough for MCMC to reach convergence in a reasonable time.

We have seen that SVI needs less time than MCMC to converge and return the metric values while still having good results. However, based on the literature, we expected a more significant decrease in the runtime for SVI, we think that our SVI implementation needs for posterior optimization.

¡Many thanks!

Stanislaw Ulam (1909-1984)

S. Ulam is credited as the inventor of Monte Carlo method in 1940s, which solves mathematical problems using statistical sampling.





Andrey Markov

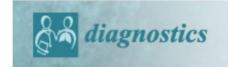
MARKOV CHAIN MONTECARLO

MARKOV CHAIN MONIECARLO						
Means of weights	Coeficient * variable	Mean	Sd	Effective_ samples	R_hat	
	b (intersect)	-5.52	0.55	299.91	1	
	W1* Pregnancies	0.11	0.03	177.36	1	
	W2 * Glucose	0.03	0.00	600.87	1	
	W3 * BloodPressure	-0.03	0.01	516.45	1	
	W4* SkinThickness	-0.01	0.01	445.51	1	
	W5* Insulin	0.00	0.00	459.31	1	
	W6* BMI	0,08	0.02	303.77	1	
	W7* Diabetes Pedigree Function	0.63	0.26	137.09	1.01	
	W8 * Age	0.02	0.01	289.83	1	

Stochastic Variational Inference

Means of weights

Coeficient * variable	Mean	Sd
b (intersect)	-6.435	1.069
W1* Pregnancies	0.124	1.014
W2 * Glucose	0.037	1.000
W3 * BloodPressure	-0.024	1.001
W4* SkinThickness	0.001	1.002
W5* Insulin	0.002	1.000
W6* BMI	0,068	1.002
W7* Diabetes Pedigree Function	0.63	1.179
W8 * Age	0.024	1.002





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Machine-Learning-Based Diabetes Mellitus Risk Prediction Using Multi-Layer Neural Network No-Prop Algorithm

<u>J. Jeba Sonia</u>, Prassanna Jayachandran, Abdul Quadir Md, Senthilkumar Mohan, Resources, Visualization, Arun Kumar Sivaraman, Formal analysis, Investigation, Resources, and Kong Fah Tee, Methodology, Investigation

Jae-Ho Han, Academic Editor

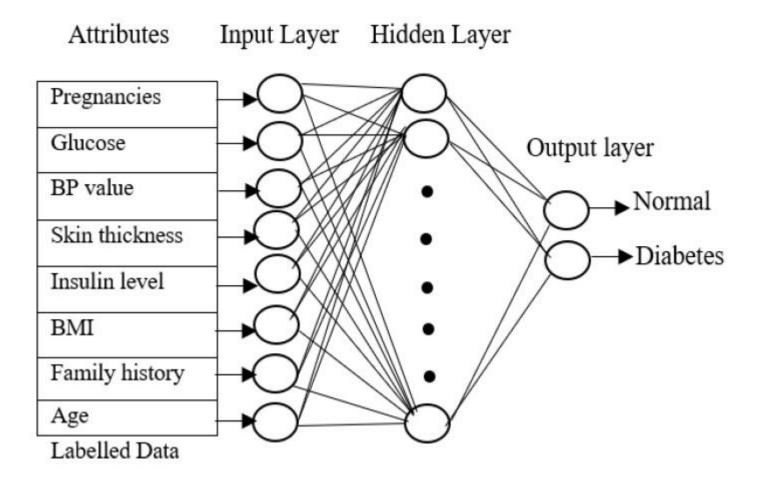


Table 5

TYPE 2 DIABETES

Classification of diabetes for dataset 2.

Parameters	Dataset		
	Class 2	Class 3	Class 4
Sensitivity	0.63	0.47	0.97
Specificity	0.93	0.99	0.96
Accuracy	0.89	0.97	0.98