

# Supplementary Material of “Total Variation Regularized Tensor Ring Decomposition for OCT Images Denoising and Super-resolution”

Parisa Ghaderi Daneshmand<sup>1</sup>, Hossein Rabbani<sup>\*,1</sup>, Senior Member, IEEE

<sup>1</sup>Medical Image & Signal Processing Research Center, School of Advanced Technologies in Medicine, Isfahan University of Medical Sciences, Isfahan, Iran

## I. Overview

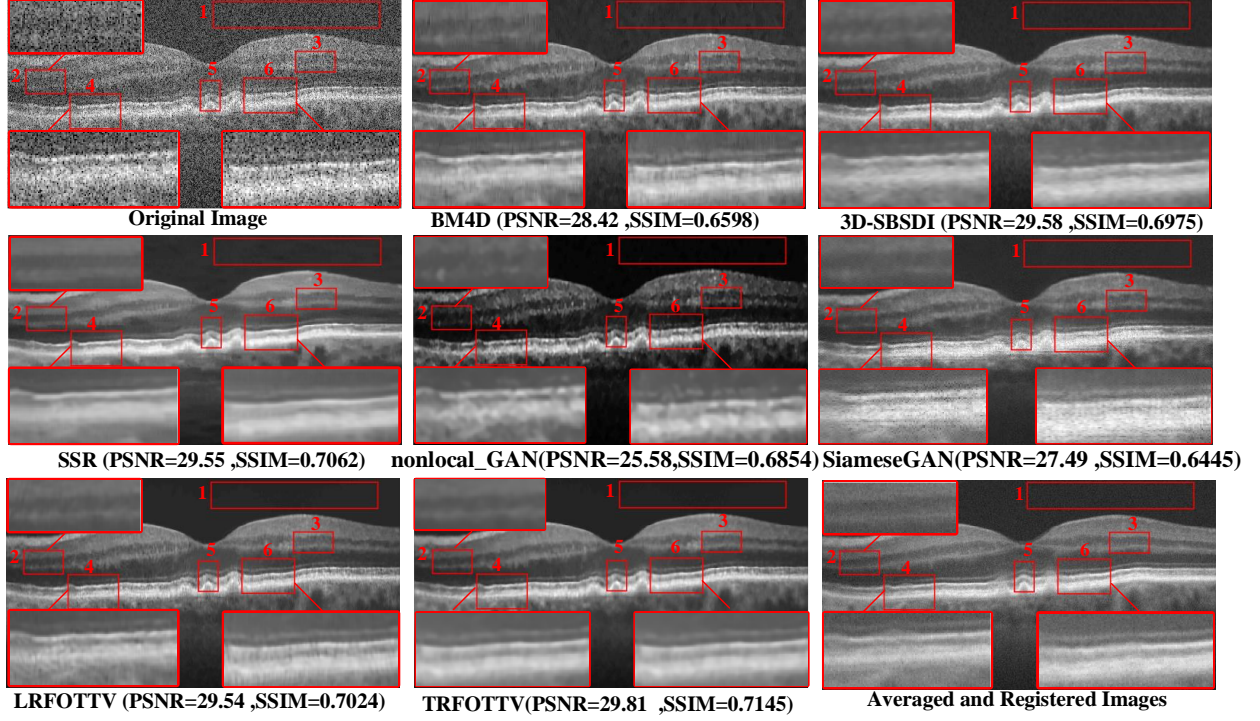
This supplementary material includes the following sections. Section II presents more visual results for the noise suppression experiment of dataset-1. Section III presents more visual results for super-resolution of OCT images of dataset-1 with 50% missing rate. In Section IV, we provided visual results for super-resolution of OCT images of dataset-1 with 75% missing rate. Finally, we validated the robustness of our proposed TRFOTTV model for different speckle noise levels in Section V.

---

<sup>\*</sup>Corresponding author

## II. OCT Images Denoising Results for Dataset-1

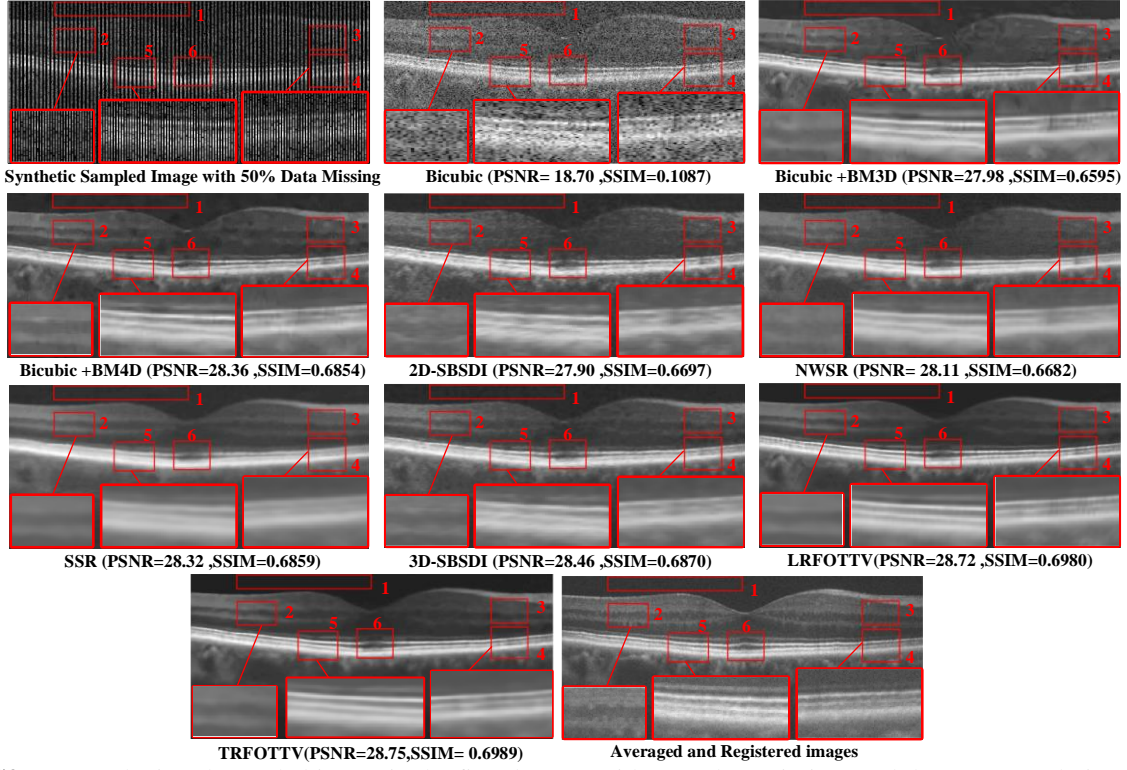
This section provides more visual results for the noise suppression experiment of dataset-1. As Fig.S1 shows, the proposed TRFOTTV has the most pleasing performance in maintaining layer structures and reducing the noise.



**Fig.S1** One retinal OCT image in the dataset-1 and their denoising results utilizing the BM4D [1], 3D-SBSDI [2], SSR [3], nonlocal\_GAN [4], SiameseGAN [5], LRFOTTV [6], and the suggested approach.

### III. Results for OCT Images Super-Resolution of Dataset-1 with 50% missing rate

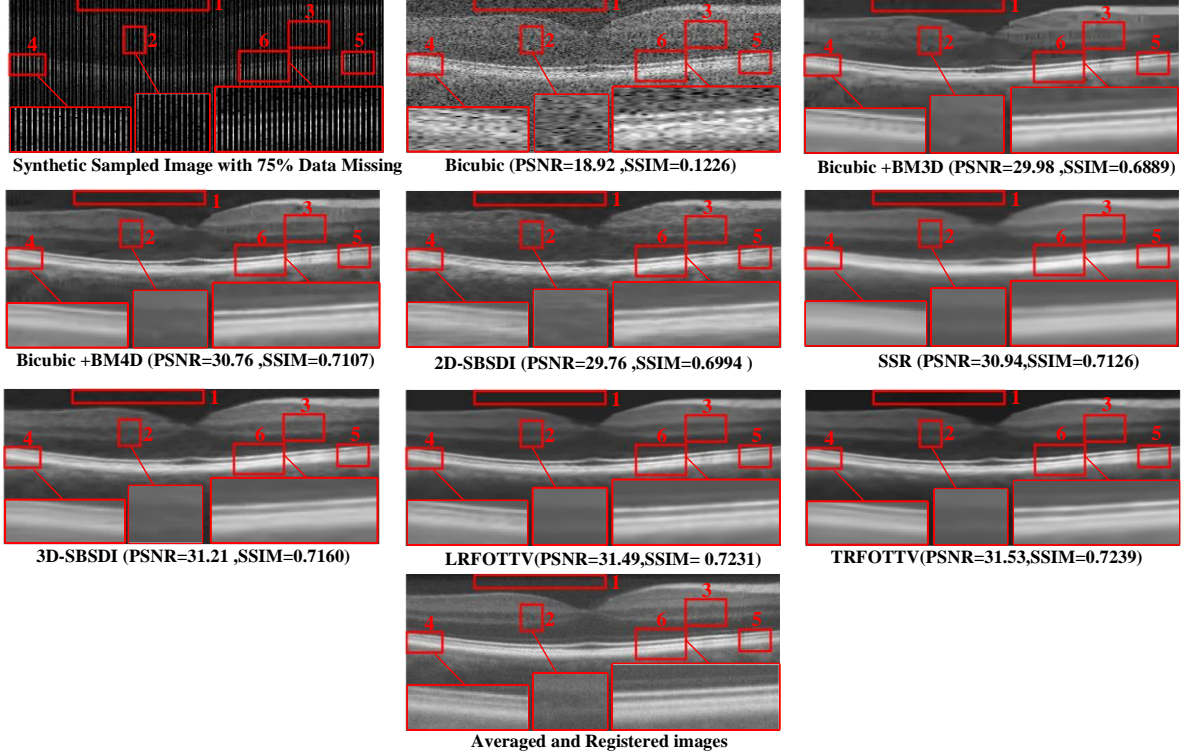
This section presents more visual results for super-resolution of OCT images of dataset-1 with 50% missing rate. Fig.S2 shows a visual comparison between the proposed TRFOTTV method and compared methods for super-resolution of OCT images with 50% data missing on synthetic subsampled images of dataset-1.



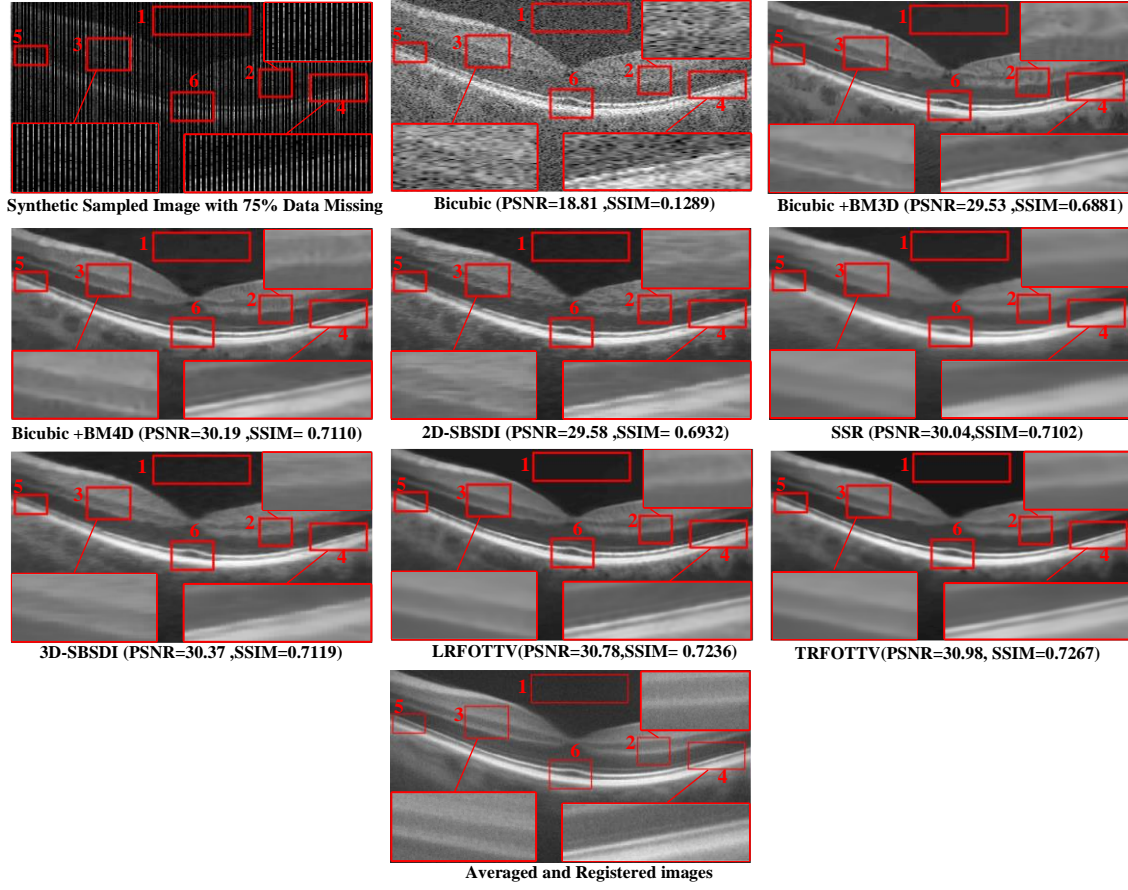
**Fig.S2** One synthetic subsampled image in the first dataset (with 50% data missing) and the super-resolution results by utilizing the bicubic, BM3D [7] + bicubic, BM4D [1] + bicubic, 2D-SBDSI [2], NWSR [8], 3D-SBDSI [2], SSR [3], LRFOTTV [6], and the suggested approach.

#### IV. Results for OCT Images Super-Resolution of Dataset-1 with 75% missing rate

This part presents visual results for super-resolution of OCT images of dataset-1 with 75% missing rate. Fig.S3 and Fig.S4 represent a visual comparison between the proposed TRFOTTV method and rival methods for super-resolution of OCT images with 75% data missing on synthetic subsampled images of dataset-1.



**Fig.S3** One synthetic subsampled image in the first dataset (with 75% data missing) and the super-resolution results by utilizing the bicubic, BM3D [7] + bicubic, BM4D [1] + bicubic, 2D-SBSDI [2], 3D-SBSDI [2], SSR [3], LRFOTTV [6], and the suggested approach.



**Fig.S4** One synthetic subsampled image in the first dataset (with 75% data missing) and the super-resolution results by utilizing the bicubic, BM3D [7] + bicubic, BM4D [1] + bicubic, 2D-SBSDI [2], 3D-SBSDI [2], SSR [3], LRFOTTV [6], and the suggested approach.

## V. Robustness on TRFOTTV method for Different speckle Noise Levels

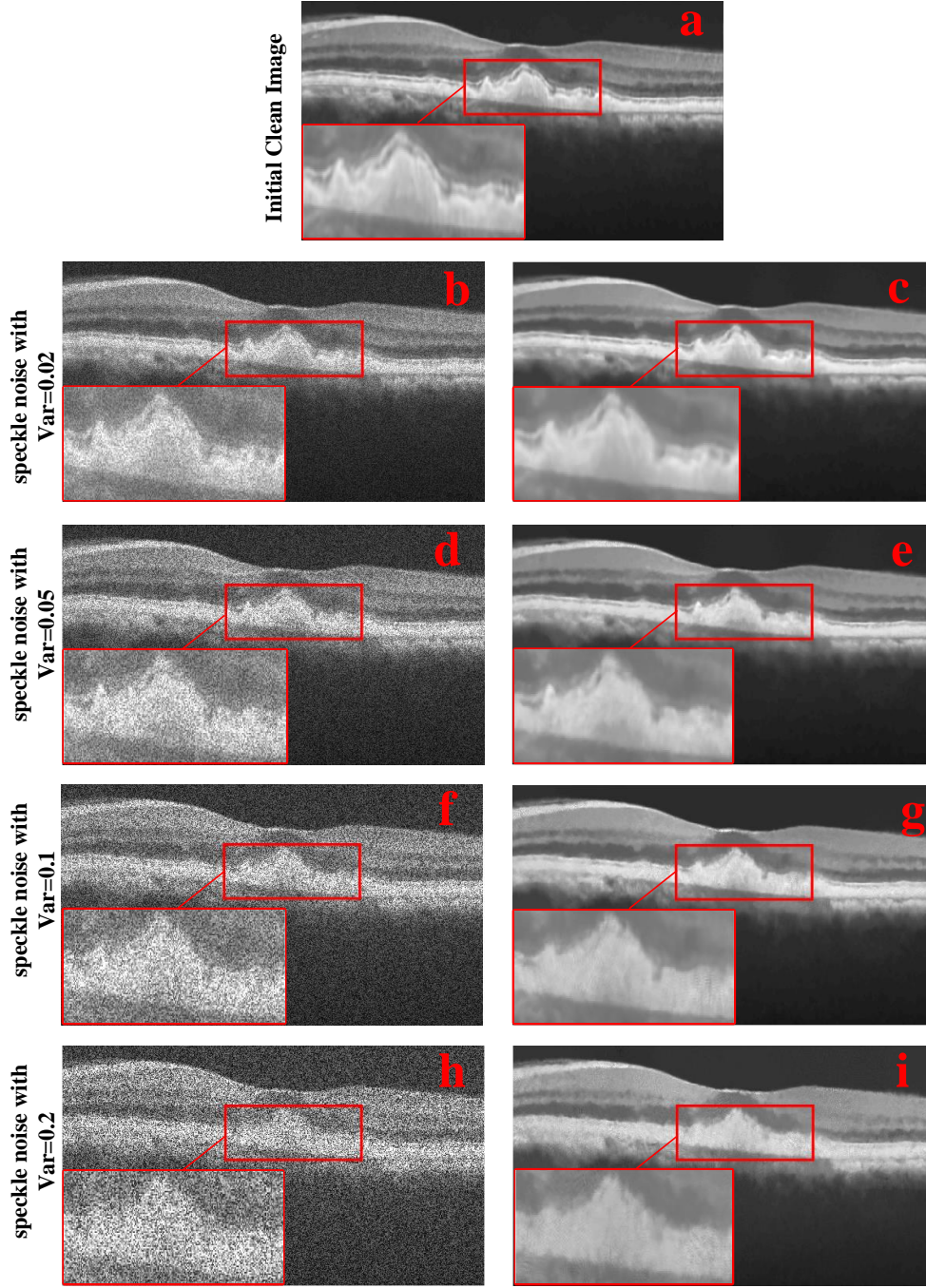
In this section, we validated the robustness of our proposed TRFOTTV method for different speckle noise levels. For this purpose, given that the proposed TRFOTTV method is a three-dimensional model, we require at least three B-scans as the input of our algorithm. Therefore, to evaluate the performance of our TRFOTTV model in reducing speck noise, we must have a clean OCT volume of at least three B-scans and artificially add speckle noise to it. Due to the fact that the dataset-1 for each subject consists of 5 noisy B-scans and only one clean B-scan (a high SNR-high-resolution (HH) image) and we do not have access to clean OCT volume, to generate clean 3D OCT volumes, we used the LRSOTTV method [6] which is one of the state-of-the-art OCT denoising techniques that have been proposed recently. Then, using this method, we generated clean 3D OCT volumes in the dataset-1. Next, we artificially added speckle noise with various strengths to the clean 3D OCT volumes and validated the robustness of our proposed TRFOTTV model for different speckle noise levels. For this purpose, the speckle noise model is formulated as:

$$\mathcal{Y} = \mathcal{X} + \mathcal{X} \cdot \mathcal{V} \quad (\text{S.1})$$

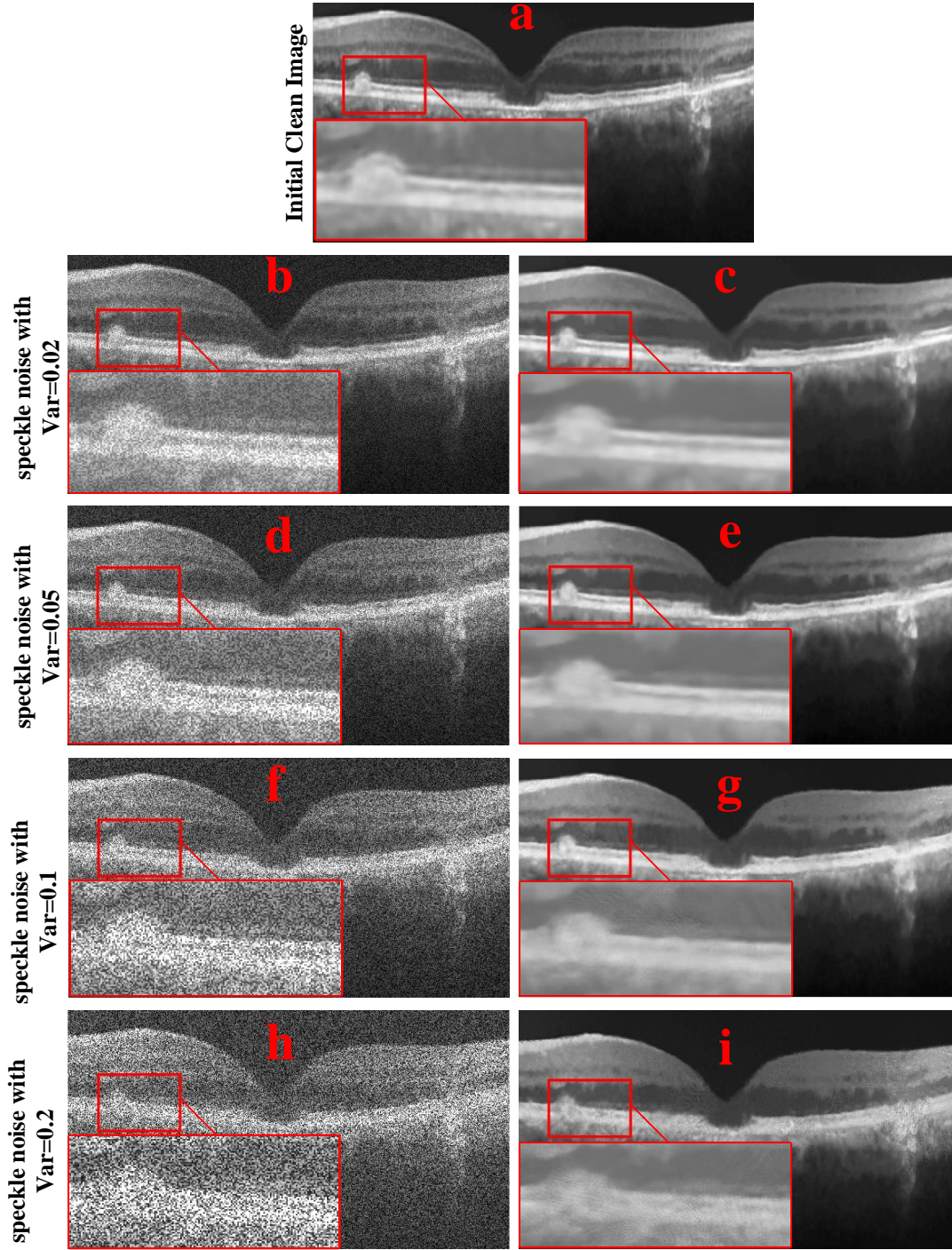
where  $\mathcal{X}$  represents the clean OCT tensor and  $\mathcal{V} \sim \mathcal{N}(0, \sigma^2)$  denotes multiplicative noise part. In our experiment, we considered for  $\sigma^2$  (or noise variance) ranges from 0.02 to 0.2. Fig.S5 and Fig.S6 present the denoising result of the OCT images artificially corrupted by speckle noise with different noise values for two sample subjects in dataset-1.

As can be observed in Fig.S5 and Fig.S6, our proposed TRFOTTV method is strong technique for speckle noise suppression in OCT images and can preserve the layer structural details in these images. Moreover, for various speckle noise levels, TRFOTTV method efficiently removes the noise to differing degrees. When the speckle noise level increases, the performance of TRFOTTV method decays slightly. In summary, the proposed TRFOTTV method is robust to various speckle noise levels to a large extent.





**Fig.S5** Visual results for denoising result of the OCT images artificially corrupted by speckle noise with different variance (or  $\sigma^2$  values). (a) Clean OCT image (b-c) OCT image corrupted by speckle noise with Var=0.02, and the corresponding denoised image by TRFOTTV model. (d-e) OCT image corrupted by speckle noise with Var=0.05, and the corresponding denoised image by TRFOTTV model. (f-g) OCT image corrupted by speckle noise with Var=0.1, and the corresponding denoised image by TRFOTTV model. (h-i) OCT image corrupted by speckle noise with Var=0.2, and the corresponding denoised image by TRFOTTV model.



**Fig.S6** Visual results for denoising result of the OCT images artificially corrupted by speckle noise with different variance (or  $\sigma^2$  values). (a) Clean OCT image (b-c) OCT image corrupted by speckle noise with  $\text{Var}=0.02$ , and the corresponding denoised image by TRFOTTV model. (d-e) OCT image corrupted by speckle noise with  $\text{Var}=0.05$ , and the corresponding denoised image by TRFOTTV model. (f-g) OCT image corrupted by speckle noise with  $\text{Var}=0.1$ , and the corresponding denoised image by TRFOTTV model. (h-i) OCT image corrupted by speckle noise with  $\text{Var}=0.2$ , and the corresponding denoised image by TRFOTTV model.



## Bibliography

- [1] M. Maggioni, V. Katkovnik, K. Egiazarian, and A. Foi, "Nonlocal transform-domain filter for volumetric data denoising and reconstruction," *IEEE transactions on image processing*, vol. 22, no. 1, pp. 119-133, 2012.
- [2] L. Fang *et al.*, "Fast acquisition and reconstruction of optical coherence tomography images via sparse representation," *IEEE transactions on medical imaging*, vol. 32, no. 11, pp. 2034-2049, 2013.
- [3] L. Fang, S. Li, D. Cunefare, and S. Farsiu, "Segmentation based sparse reconstruction of optical coherence tomography images," *IEEE transactions on medical imaging*, vol. 36, no. 2, pp. 407-421, 2016.
- [4] A. Guo, L. Fang, M. Qi, and S. Li, "Unsupervised denoising of optical coherence tomography images with nonlocal-generative adversarial network," *IEEE Transactions on Instrumentation and Measurement*, vol. 70, pp. 1-12, 2020.
- [5] N. A. Kande, R. Dakhane, A. Dukkupati, and P. K. Yalavarthy, "SiameseGAN: A generative model for denoising of spectral domain optical coherence tomography images," *IEEE Transactions on Medical Imaging*, vol. 40, no. 1, pp. 180-192, 2020.
- [6] P. G. Daneshmand, A. Mehridehnavi, and H. Rabbani, "Reconstruction of optical coherence tomography images using mixed low rank approximation and second order tensor based total variation method," *IEEE Transactions on Medical Imaging*, vol. 40, no. 3, pp. 865-878, 2020.
- [7] K. Dabov, A. Foi, V. Katkovnik, and K. Egiazarian, "Image denoising by sparse 3-D transform-domain collaborative filtering," *IEEE Transactions on image processing*, vol. 16, no. 8, pp. 2080-2095, 2007.
- [8] A. Abbasi, A. Monadjemi, L. Fang, and H. Rabbani, "Optical coherence tomography retinal image reconstruction via nonlocal weighted sparse representation," *Journal of biomedical optics*, vol. 23, no. 3, pp. 036011-036011, 2018.