

# 1 Site-specific multilevel modeling of 2 potato response to nitrogen 3 fertilization

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## ABSTRACT

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Technologies of precision agriculture, digital soil maps and meteorological stations provide a minimum data set to guide precision farming operations. However, determining optimal nutrient requirements for potato (*Solanum tuberosum* L.) crops at subfield scale remains a challenge given specific climatic, edaphic and managerial conditions. Multilevel modeling can generalize yield response to fertilizer additions using data easily accessible to growers. Our objective was to elaborate a multilevel N fertilizer response model for potato crops using the Mitscherlich equation and a core data set of 93 N fertilizer trials conducted in Quebec, Canada. Daily climatic data were collected at 10 km x 10 km resolution. Soils were characterized by organic matter content, pH and texture in the arable layer, and by texture and tools of pedometrics across a gleization-podzolization continuum in subsoil layers. There were five categories of preceding crops and five cultivar maturity orders. The three Mitscherlich parameters (*Asymptote*, *Rate* and *Environment*) were most often site-specific. Sensitivity analysis showed that optimum N dosage increased with non-leguminous high-residue preceding crops, coarser soils, podzolization, drier climatic condition and late cultivar maturity. The inferential model could guide site-specific N fertilization using an accessible minimum data set to support fertilization decisions. As decision-support system, the model could also provide a range of optimum N doses across a large spectrum of site-specific conditions including climate change.

**Keywords:** Crop modeling; Potato; Nitrogen; Precision agriculture

Abbreviations:  $[M \cdot S^{-1}]$ : unit of mass per surface;  $[\$ \cdot S^{-1}]$ : unit cost per surface; C: carbon; CND: Canadian dollars, DAP: days after planting; ETC: crop evapotranspiration; GDD: number of growing degree days; ha: hectare; ILR: isometric log-ratio; Mg: mega gram

(ton); N: nitrogen; NLE: number of leaching events; SOM: soil organic matter; PPT: cumulative precipitation during the growing period; SBP: sequential binary partition; SDI: Shannon diversity index for rainfall distribution; TC Thornthwaite class.

## 1 INTRODUCTION

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The main forcing variables for potato (*Solanum tuberosum* L.) growth and development are air temperature, photoperiod, intercepted radiation, precipitation, soils, and nutrient management (Fortin et al. 2008; Hanks and Ritchie 1991; White et al. 2007). The potential yield of potato is the theoretical yield that can be achieved with a well-adapted cultivar grown from the best possible seeds under optimal conditions, including weather, soil and agronomic practices (Haverkort and Struik 2015).

The N fertilization limits the productivity of potato agroecosystems (Dueri et al. 2007; Hirel et al. 2007) but fertilizer N recovery varies from 10 to 70% in potato crops (Tran and Giroux 1991). Because response curves show that economic loss is much larger with under- than over-fertilization, growers tend to apply more N than suggested by extension services (Joern and Vitosh 1995; Prunty and Greenland 1997). Reducing fertilizer N rates appears to be the only effective approach to reduce environmental risk (Peralta and Stockle 2002). Fertilizer recommendations thus need to be adjusted more accurately to reflect site characteristics (Rajsic and Weersink 2008). Nitrogen fertilizer trials can support decisions fitted to specific soil management zones (Cambouris et al. 2006).

Fertilization for optimum crop yield depends on soil quality (Boiteau et al. 2014), landform (Moulin et al. 2012), weather conditions (Sands et al. 1979), preceding crops (Li et al. 1999a), the timing, location and chemical form of the fertilizer being applied (Kelling et al. 2014), genetic factors such as longevity, growth rate (Gregory and

60 Simmonds 1992), nutrient requirements of cultivars (Gianquinto and Bona 2000;  
61 Saluzzo et al. 1999; White et al. 2007; Zebarth et al. 2004), and economic  
62 considerations (Colwell 1994). Although field trials could identify *ex post* nutrient optima  
63 at a specific location, optima cannot be generalized to conditions different from those of  
64 particular experiments (Kyveryga et al. 2007a, 2007b). In order to adjust nutrient  
65 management to local conditions as required by precision agriculture (Inman et al. 2005),  
66 site-specific fertilizer applications rely on models' ability to capture the major yield-  
67 determining factors.

68 Meta-analysis (Tremblay et al. 2012), empirical (Hofman and Salomez 2000) and  
69 process-based growth models (Brisson et al. 2003; Kabat 1995) have been developed to  
70 model crop yield and N requirements. Meta-analysis allocates fertilizer trials to  
71 subgroups hence averaging out continuous input data such as fertilizer rates, and  
72 requires a data set large enough to build response subgroups of sufficient size, hence  
73 limiting the number of categories. Empirical models require measuring periodically soil  
74 nitrate content down to 60 cm as soil test N, and providing provisional N budgets and fair  
75 estimates of mineralization rates of soil organic matter and crop residues and their  
76 controlling factors such as pH, texture and weather. Process-based models require large  
77 amounts of input data such as intercepted radiation and varietal parameters that are not  
78 readily available. Soil classification that provides information on subsoil properties  
79 important for plant growth is absent in such models.

80 Decision support systems for site-specific fertilization could be elaborated using a  
81 minimum data set of readily accessible weather, soil, and management data influencing  
82 key biological processes. Weather has a large influence on soil biological activity  
83 (Bolinder et al. 2007) and potato growth (Sands et al. 1979). Transformations of stable  
84 and labile organic matter are related to soil properties and weather variables available

from local meteorological stations (Bolinder et al. 2013). Soil tests such as pH and organic matter content are provided by routine laboratories. Soil texture (and sometimes organic matter) as input variable can be measured using geophysical (Alfred et al. 2008) and spectrometric (Viscarra Rossel et al. 2016) methods. Soil series can be quantified as continuous variables using tools of pedometrics (Leblanc et al. 2016). Potato cultivars can be assigned to maturity groups as indicated by the supplier and government agencies.

Multilevel models (J. C. Pinheiro and Bates 2000) have high generalization and interpolation capabilities. Where parameters of a nonlinear model can be generated from linear combinations of variables, multilevel models can provide a broad and interpretable framework useful for descriptive modeling. Hence, multilevel models can synthesize readily available soil and meteorological data impacting on potato growth and development and thus provide an estimate for on-the-go fertilizer dosage adjusted to local conditions. Such models could also adjust N dosage to local yield potential (Inman et al. 2005).

Our objectives were to develop multilevel models to describe potato response to added N across gradients of weather, soil and crop management and at plot scale, and to test model sensitivity using a dataset of fertilizer trials from Quebec, Canada.

## **2 THEORY**

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### **2.1 MITSCHERLICH MODEL**

The law of minimum, popularized by J. von Liebig, states that growth is limited by the rarest resource, all other factors being equal. G. Liebscher came with the law of optimum, where a resource in minimum supply contributes more to production, the

closer other production factors are to their optimum (de Wit 1992). Liebig's and Liebscher's laws are statements that were formulated as mathematical expression. Several non-linear models are available to describe crop response to added nutrients (Dahnke and Olson 1990). Curvilinear models often tend to recommend too much fertilizer in relation to the amount of yield increase obtained at or near maximum yield (Dahnke and Olson 1990). Nevertheless, the Mitscherlich model has been found to be satisfactory for the site-by-site analysis of N fertilizer trials (Harmsen 2000; Rajsic and Weersink 2008; Valkama et al. 2013). We thus selected the Mitscherlich model given that the point where maximum yield is reached may also be indicated by the linear-plateau curve (Dahnke and Olson 1990). Other non-linear models such as the linear-plateau and quadratic models showed poor performance (Supplementatry material 1) but could nevertheless be selected at need (Bélanger et al. 2000; Colwell 1994).

In the Mitscherlich equation, the rate of yield increase gets progressively smaller as soil nutrient levels and nutrient additions increase, as follows (Rajsic and Weersink 2008):

$$Yield = Asymptote \times (1 - e^{-Rate \times (Environment + Dose)}) ,$$

*Equation 1*

where *Yield* is crop production per unit area [ $M \cdot S^{-1}$ ] (mass per surface), and *Dose* is fertilizer dosage per unit area [ $M \cdot S^{-1}$ ]. The Mitscherlich parameters represented in Figure 1 are defined as follows:

- *Asymptote* is the yield [ $M \cdot S^{-1}$ ] toward which the curve converges with increasing dose;
- *Environment*, represented on the left side of the abscissa intercept (x-axis), describes the fertilizer-equivalent dose provided by environmental conditions [ $M \cdot S^{-1}$ ]; a more positive value for *Environment* returns a more negative intercept,

- indicating N credit provided by the environment; conversely, a negative value for *Environment* (positive x-intercept) indicates N loss from or N immobilization by the environment; the x-intercept in the Mitscherlich equation allows the possibility for different repeated measures to cross the y-axis (zero fertilizer) at different places for equal *Environments* and *Rates*, but different *Asymptote* values (to which a random effect can be assigned – see the Methodology section);
- *Rate* is the steepness of the curve relating *Environment* to *Asymptote* [dimensionless]. A higher *Rate* indicates a steeper curve.

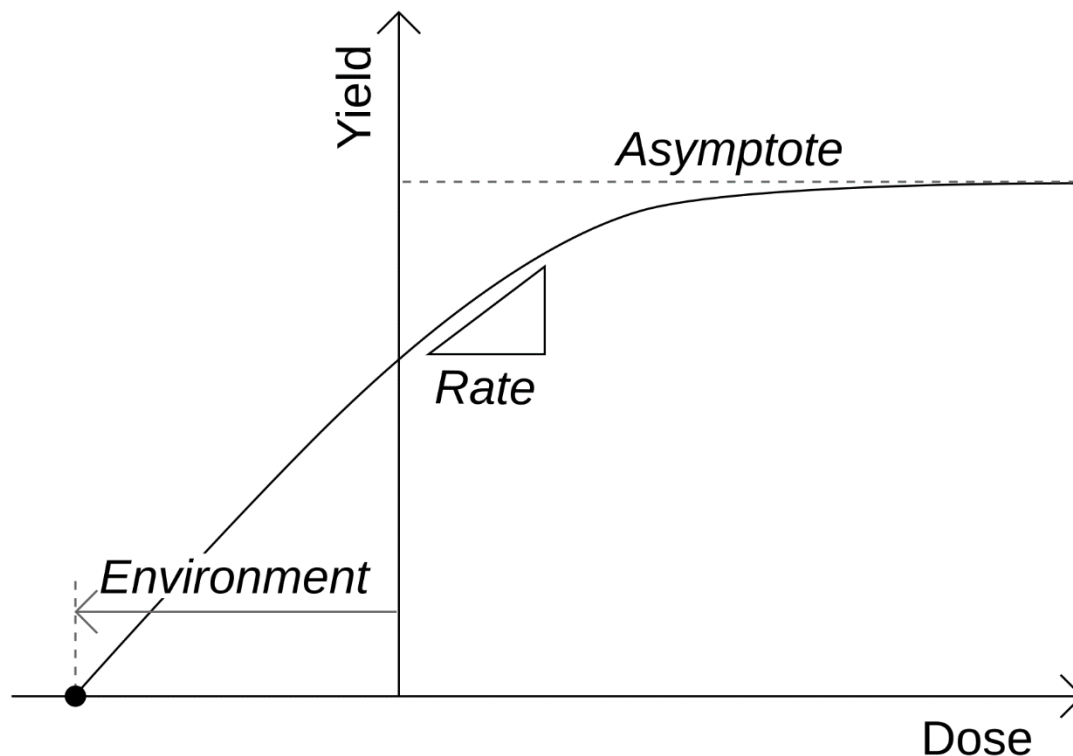


Figure 1. Scheme of the Mitscherlich parameters.

## 2.2 OPTIMAL ECONOMICAL DOSE

The optimal nutrient dose is the point on the yield curve at which the additional cost of fertilizer is not justified by marginal yield gain with extra N (Shepherd 2000). The optimal economic fertilizer dose was computed as follows (Colwell 1994):

$$\Pi = Yield \times V - Dose \times C \times (1 + I)^t - Q,$$

Equation 2

where  $\Pi$  is crude profit per cropped surface [ $\$ \cdot S^{-1}$ ] (economic value per surface),  $V$  is the value of one unit of crop Yield [ $\$$ ],  $C$  is the cost of one fertilizer unit [ $\$ \cdot M^{-1}$ ] (economic value per mass),  $I$  is the interest rate of return,  $t$  is the number of interest periods and  $Q$  represents the fixed costs [ $\$$ ].  $Dose_{opt}$ , the optimal fertilizer dose [ $M \cdot S^{-1}$ ], is computed at the point on the curve where the first derivative of  $\Pi$  over  $Rate$  is null, as follows:

$$\frac{d\Pi}{dDose} = \frac{dYield}{dDose} \times V - C \times (1 + I)^t = 0,$$

Equation 3

where  $Yield$  as a function of dose can be described by the Mitscherlich model (Equation 1). The equation for Mitscherlich optimum dosage is derived as follows:

$$Dose_{opt} = \frac{\ln\left(\frac{Asymptote \times Rate \times V}{C \times (1 + I)^t}\right)}{Rate} - Environment.$$

Equation 4

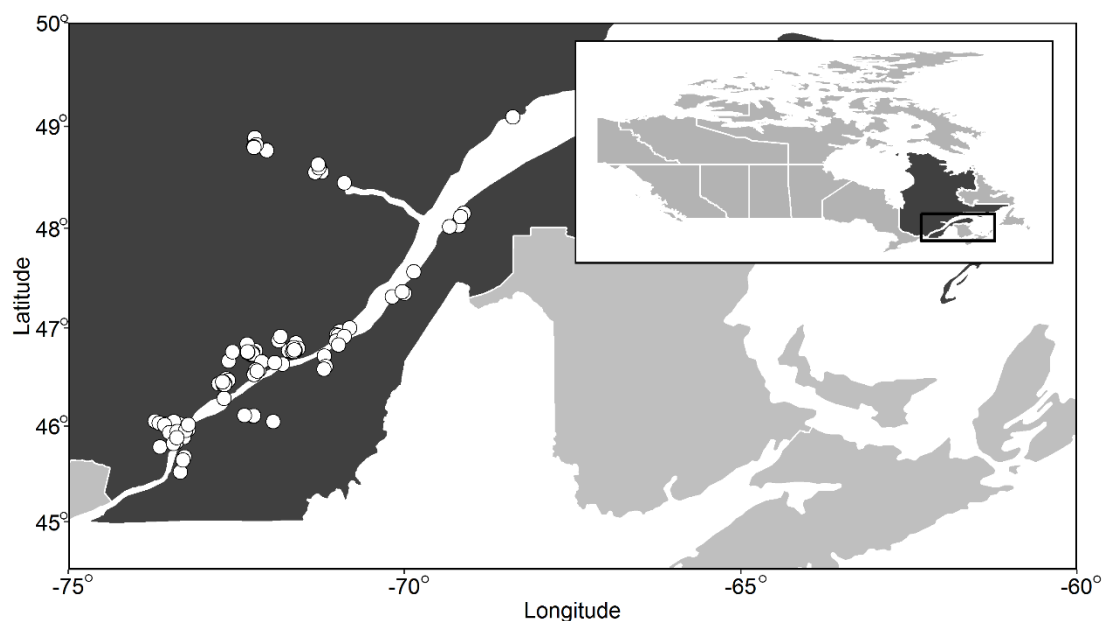
## 3 METHODOLOGY

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### 3.1 DATA SET

The Québec potato data set is a collection of fertilizer trials conducted since 1970 between the US border (45<sup>th</sup> parallel) and the Northern limit of cultivation at the 49<sup>th</sup> parallel (Figure 2).





*Figure 2. Location of experimental sites in the Quebec potato data set.*

The data set was cleaned to retain only N fertilizer trials conducted with sufficient P and K doses to avoid misguided trends and where minimum N dosage was less than or equal to 50 kg N ha<sup>-1</sup> and maximum dosage was at least 100 kg N ha<sup>-1</sup> to avoid fitting a response curve over a restricted range of doses. Trials were also inspected to assure the high quality of data, which led to the exclusion of one trial and one block of a trial. We retained a total of 2166 observations from 284 experimental blocks in 93 N trials (sites). Most trials were arranged as randomized block designs, where random variables were Block nested in Trial. The dataset contained repeated treatments and specific variables (Table 1). Cultivars were amalgamated into ordinal maturity categories as reported on the web by the Canadian Food Inspection Agency (Table 1, Maturity order), and the preceding crops were grouped into the five meta-levels (Table 2). Grain corn, pearl millet and rye were considered as high-residue crops because corn stubble was left on soil and pearl millet and rye were grown as high-yielding cover crops.

Description	Type	Variables
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Maturity order	Ordinal	<p><b>1</b> (Early cultivar): AC Belmont, AC Chaleur, Bijou Rouge, Caribe, Conestoga, Eramosa, Hilite Russet, Jemseg, Russet Norkota</p> <p><b>2</b> (Early to mid-season cultivar): Andover, Norland, Peribonka, Superior, Vivaldi</p> <p><b>3</b> (Mid-season cultivar): Amandine, Aquilon, Atlantic, Chieftain, Coastal Russet, Dakota Pearl, Dark Red Chieftain, Estima, FL 1533, Frontier Russet, Goldrush, Harmony, Kanona, Kennebec, Keuka Gold, Krantz, Lanorma, Monona, Nordonna, Pike, Prospect, Reba, Red Cloud, Shepody, Viking, Yukon Gold.</p> <p><b>4</b> (Mid-season to late cultivar): FL 1207, Mystère, NY-115, W 1386.</p> <p><b>5</b> (Late cultivar): Argos, Gemstar, Green Mountain, Katahdin, Lamoka, Russet Burbank, Snowden, Valor, Waneta.</p>
Preceding crop	Categorical	See Table 2
Basic soil composition	Continuous	[C   Clay ,Silt,Sand], [Clay   Silt,Sand], [Silt   Sand]
Soil profile	Continuous	[Gleyed   Podzolized], [Loamy gleyed   Sandy gleyed]
Soil pH	Continuous	pH
Weather	Continuous	See Table 3

Random effect on <i>Asymptote</i> , Trial level	Continuous	Random effect at the trial (site) level (level 1), $\sim N(0, \sigma_1)$
Random effect on <i>Asymptote</i> , Trial/Block level	Continuous	Random effect of Block nested in trial (site) applied to the slope (level 2), $\sim N(0, \sigma_2)$

Table 1. Variables used in the multilevel models.

Preceding crop	Meta- level
Oat, oat and mustard, wheat, canola, cereal, mustard, white mustard, barley, barley and mustard, sunola and cereal	Small grain
Grain corn, pearl millet, rye	High-residue crops
Perennial legumes: birdsfoot trefoil, alfalfa, legume mix, clover, ryegrass and clover	Legume
Orchard grass, ryegrass, ryegrass and cereal	Grassland
Annual low-residue crops: broccoli, cabbage, Chinese cabbage, beans, strawberry, silage corn, onion, pea, potato, potato followed by green manure, buckwheat, soybean	Low-residue crops

Table 2. Classification of preceding crops

### 3.2 COMPOSITIONAL DATA ANALYSIS

Because several soil data such as particle-size distributions are compositional, techniques of compositional data analysis (CoDa) (Aitchison 1986; Egozcue et al. 2003; Parent et al. 2013) are required to avoid generating methodological biases in the multilevel models.

Data related to soil texture are constrained to a constant sum, e.g. 100 %. Such data are compositional and multivariate in nature (Pawlowsky-Glahn and Egozcue 2006). There are  $D - 1$  degrees of freedom for a  $D$ -part composition because one component can be computed by difference (Aitchison and Greenacre 2002). Parent et al. (2013) stressed that such data should be log-ratio transformed prior to statistical analysis to avoid distorting the results with spurious correlations.

The isometric log-ratio (*ilr*) is a data-transformation technique that maps  $D$ -part compositional vectors as  $D - 1$  orthonormal variables or dimensions interpreted as balances between predefined subsets of components (Egozcue et al. 2003). Balances can be designed in a  $(D - 1) \times D$  matrix called sequential binary partition (SBP). In each row of the SBP, parts within subset “+” at numerator of the log ratio are contrasted with parts within subset “-” at denominator. Parts within subset “0” are excluded from the contrast. The composition is partitioned sequentially into non-overlapping subsets at every ordered row into two contrasts until the + and - subsets each contain a single part. Each balance is computed as isometric log-ratio (*ilr*) as follows (Egozcue et al. 2003):

$$ilr_k = \sqrt{\frac{r_k s_k}{r_k + s_k}} \ln \frac{(x_{i_1} x_{i_2} \dots x_{i_{r_k}})^{\frac{1}{r_k}}}{(x_{j_1} x_{j_2} \dots x_{j_{s_k}})^{\frac{1}{s_k}}},$$

Equation 5

where, for the  $k^{th}$  balance ( $k \in [1:D-1]$ ) of a composition,  $r_k$  and  $s_k$  are the numbers of components in the “+” and the “-” subsets, respectively, on the  $k^{th}$  row of the SBP. Parts  $x_{i_1} x_{i_2} \dots x_{i_{r_k}}$  belong to the “+” subset at numerator and parts  $x_{j_1} x_{j_2} \dots x_{j_{s_k}}$  belong to the “-” subset at denominator. The coefficient  $\sqrt{r_k s_k / (r_k + s_k)}$  is a normalization coefficient used to obtain unitary vectors. In this paper, balances are designated as [subset at denominator | subset at numerator] (e.g. basic soil composition and soil profile

in Table 1) to indicate that larger numbers at numerator make *ilrs* leaning to the right as in classical algebra. More details on the *ilr*-transformation applied to agricultural sciences can namely be found in Parent et al. (2013).

### **3.3 SOIL CHARACTERISTICS**

#### **3.3.1 Basic soil composition**

The data set included soil texture of surface layers reported as % clay (0-0.002 mm), % silt (0.002-0.05 mm) and % sand (0.05-2 mm) (Bouyoucos 1962) or as textural class (Soil Classification Working Group 1998). Using centroids in the data set of Tabi et al. (1990), who surveyed Québec soils, textural classes were converted into percentages of sand, silt and clay. Soil organic matter (SOM) content was quantified by combustion (Leco-CNS) or using the Walkley-Black procedure (Nelson and Sommers 1982), assuming 58% C content in SOM. Soil texture was determined by sedimentation (Gee and Bauder 1986). Organic matter as carbon content (C) and textural components were included into the soil simplex then transformed into isometric log-ratios as the [C | Clay, Silt, Sand], [Clay | Silt, Sand], and [Silt | Sand] balances.

#### **3.3.2 Soil pH**

Reported soil pH values were measured in water or in a 0.01 M CaCl<sub>2</sub> solution (1 :1 v/v). The pH(CaCl<sub>2</sub>) was converted into pH (water) as follows (Cescas 1978):

$$pH_{water} = 0.27 + 1.03 pH_{CaCl_2}$$

*Equation 6*

#### **3.3.3 Soil profile class**

The potato fertilizer trials in the Québec data set have been conducted on 46 soil series.

The subsoil has a large influence on crop growth, not least by regulating water

availability (Piikki et al. 2015). Using soil profile morphological descriptions in Québec soil surveys, soil series were aggregated into a limited number of entities using a numerical clustering procedure (Leblanc et al. 2016). In brief, the textural gradient and the major pedogenic processes (gleization and podzolization) occurring in potato soil profiles were partitioned into three soil classes as follows: (1) loamy gleyed profiles (poorly drained loam), (2) sandy gleyed profiles (poorly drained sand), and (3) sandy podzolized profiles (well drained sand). A set of fuzzy memberships to soil classes up to 100% was allocated to each observation to produce a continuous expression of soil type and thus facilitate modeling. Percentages were transformed into isometric log-ratios as [Gleyed | Podzolized] and [Loamy gleyed | Sandy gleyed] balances.

### **3.4 WEATHER INDICES**

Weather data were obtained from the Environment Canada system (Hutchinson et al. 2009). Climatic indices were collected as follows to characterize weather conditions that prevailed at experimental sites: the cumulative precipitation during the growing period – PPT, the Shannon diversity index for rainfall distribution – SDI (Tremblay et al. 2012), the crop evapotranspiration – ETC (Allen et al. 1998; Baier and Robertson 1965), the number of growing degree days – GDD (Moulin et al. 2012) and the number of leaching events – NLE, i.e. precipitation events of at least 3 inches or 76 mm during three consecutive days (Chleborad 2000; Liu et al. 2015). Weather indices were computed using the Canada daily precipitation and temperature data (University of Toronto 2013). Table 3 provides equations to compute climatic indices for two growing periods: (1) beginning of the season (seedling) to 45 days after planting (DAP), approximately at beginning of tuber formation, and (2) 46 DAP to harvest. In general, N application is split

256 between seeding and 45 DAP. Hence it was deemed informative to include two seasonal  
 257 growing periods in the model.

Index	Description	Unit	Formula
PPT	Cumulative precipitation	mm	$PPT = \sum_{i=1}^n Rd_i$
SDI	Shannon Diversity Index for rainfall	-	$SDI = \frac{-\sum_{i=1}^n [P_i \ln(P_i)]}{\ln(n)}, P_i = \frac{Rd_i}{PPT}$
ETC	Crop evapotranspiration	mm	$ETC = \sum_{i=1}^n [ETP_i Kc_i]$
GDD	Growing degree-days	°C	$GDD = \begin{cases} 0 & \text{if } Tm_i < 5 \\ \sum_{i=1}^n Tm_i & \text{if } Tm_i \geq 5 \end{cases}$
NLE	Number of leaching events, i.e. precipitations ≥ 3 inches for 3 consecutive days	-	$NLE = \sum_{i=2}^{n-1} E_i$ , where $E_i = 1$ if $\sum_{j=i-1}^{i+1} Rd_j \geq 3$ , otherwise $E_i = 0$
TC	Thornthwaite class	-	$TC = \begin{cases} \text{dry, if } HI < -0.100 \\ \text{optimal, if } -0.100 \leq HI \leq 0.167 \\ \text{wet, if } HI > 0.167 \end{cases}$ ,  $HI = \frac{\text{Water availability}}{\text{Water needed}},$  $\text{Water availability} = PPT - ETC,$  $\text{Water needed} = ETC$

258 Table 3. Equations to compute climatic indices: Rd is daily rainfall, n is the number of days, ETP is potential  
 259 evapotranspiration, Kc is crop coefficient depending on potato growth stage, and Tm is daily mean  
 260 temperature.

### 261 3.5 MULTILEVEL MODEL

262 Multilevel modeling is a statistical tool to assess the effects of driving variables on a  
 263 response of features measured at different levels of randomization. Levels of interest in  
 264 this study are blocks and trials: for each trial and each block within trials, we computed a

random effect assumed to be normally distributed with zero mean and a computed variance-covariance matrix (J. C. Pinheiro and Bates 2000).

Parameters of non-linear multilevel models can themselves be modelled from a set of features, usually by a linear combination of them – hence the “multilevel” concept can be understood through modelling the randomization and parameters of a non-linear model from the measured features. *Asymptote*, *Rate* and *Environment* parameters of the Mitscherlich equation (Equation 1) were modelled as linear combinations of predictors with random effect applied to the intercept of the *Asymptote* parameter, as follows:

$$Asymptote = \beta X + uZ + e_A ,$$

*Equation 7*

$$Environment = \gamma X + e_E ,$$

*Equation 8*

$$Rate = \delta X + e_R ,$$

*Equation 9*

where *Asymptote*, *Environment* and *Rate* are parameters of the Mitscherlich equation (Equation 1),  $\beta$ ,  $\gamma$  and  $\delta$  are vectors of fixed effect coefficients associated to *Asymptote*, *Environment* and *Rate*, respectively,  $X$  is the fixed effect model matrix (which could be designed differently for each parameter, but was set as similar across *Asymptote*, *Environment* and *Rate* in this study for the sake of descriptive modeling),  $u$  is the vector of random effect coefficients,  $Z$  is the random effect model matrix and  $e_A$ ,  $e_E$  and  $e_R$  are modeling errors associated to their respective subscript. In this paper, the term «parameters» refers to parameters of the first level model (Mitscherlich equation), i.e.



287 *Asymptote*, *Environment* and *Rate*. Also, the term «coefficients» refers to the  $\beta$ ,  $\gamma$  and  $\delta$   
288 vectors. Finally, the term «variables» refers to the predictors in  $X$ .

289 Random effects at levels of the trial and block were applied to the *Asymptote* parameter  
290 only, because maximum yield was likely to vary more among trials compared to  
291 *Environment* and *Rate*. No random effect was applied on *Environment* and *Rate* to avoid  
292 over-parametrization and facilitate model convergence. One random effect is computed  
293 for each trial (site), and another one is computed for each block within trials. The level 0  
294 refers to no random effect, level 1 to random effects of trials only, and level 2 to random  
295 effects on both trials and blocks. Variables presented in Table 1 were included into a  
296 multilevel model subjected to the Mitscherlich equation. The preceding crop category  
297 was dummy-coded, i.e. each category except the reference one (which is included in the  
298 intercept – the small grain class was selected as reference) is analyzed in a new column  
299 where one (1) indicates category membership; otherwise zero (0) is indicated. The  
300 maturity order was transformed by linear encoding from -0.63 for order 1 to 0.63 for  
301 order 5 passing through 0 for order 3. Numerical variables were normalized to null mean  
302 and unit variance to ensure a common scale in the assessment of effects from  
303 coefficients.

304 The solution was reached from a set of *Asymptote*, *Environment* and *Rate* starting  
305 values. Because different starting values could lead to different optima, we created a  
306 grid of 648 starting values among and selected the set returning the lowest Akaike  
307 information criterion (AIC). The multilevel mixed model provided estimates of the mean  
308 and covariance of regression coefficients. Coefficients were declared significant at  $P <$   
309 0.05.

310 The optimal economical fertilizer dosage (Equation 4) was computed for five case  
311 studies. Unit fertilizer costs ( $C$ ) were set at 1.20 CDN \$ kg<sup>-1</sup> of N and unit crop price ( $V$ )

at 275 CDN \$ Mg<sup>-1</sup>. The interest ( $I$ ), time ( $t$ ) and fixed costs ( $Q$ ) were set at zero.  
Because a single curve was presented per trial, the block (level 2) random effect was not considered, and the curves were computed using only the trial random effect (level 1).

### 3.6 SENSITIVITY ANALYSIS

Sensitivity analyses were conducted by varying one variable (Table 1) at the time while keeping others at their mean values. Sensitivity analysis provides general trends. However, because an average situation may not occur in practice, the simulations should be interpreted with care.

### 3.7 NUMERICAL ANALYSIS

Numerical analyses were performed in the R statistical computing environment: the `compositions` package (van den Boogaart et al. 2014) to transform compositional data into isometric log-ratios; the `dplyr` package (Wickham and Francois 2015) for general data manipulation; the `ggplot2` package (Wickham and Chang 2015) for data visualization; the `mvoutlier` package (Filzmoser and Gschwandtner 2015) to identify outliers; the `nlme` package (J. Pinheiro et al. 2015) to fit nonlinear multilevel models; the `robCompositions` package (Templ et al. 2015) to impute missing values robustly; the `vegan` package (Oksanen et al. 2015) for principal component analysis. The R code and data are available as Supplementary material 1.

# 4 RESULTS

## 4.1 WEATHER

Pearson correlations between weather variables (Figure 3) showed high correlation coefficients between cumulated precipitations and number of leaching events (0.83), between number of leaching events and evapotranspiration (0.81) and between evapotranspiration and growing degree-days (0.96). Principal component analysis (PCA) was performed across the two periods altogether, i.e. from the beginning of the season to 45 DAP and from 46 DAP to harvest, using all climatic indices. In agreement with Figure 3, the biplot of the PCA in Figure 4 showed redundant information between evapotranspiration (ETC) and growing degree-day (GDD) and between cumulated precipitations (PPT) and number of leaching events (NLE). We thus selected GDD, PPT and SDI as weather indices and removed ETC and NLE that are indices more difficult to measure and compute.

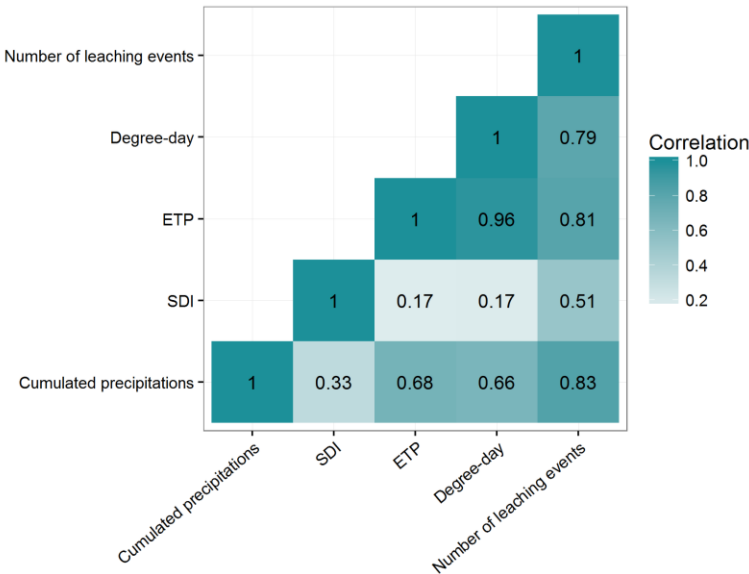


Figure 3. Pearson correlations between weather variables in the potato data set.

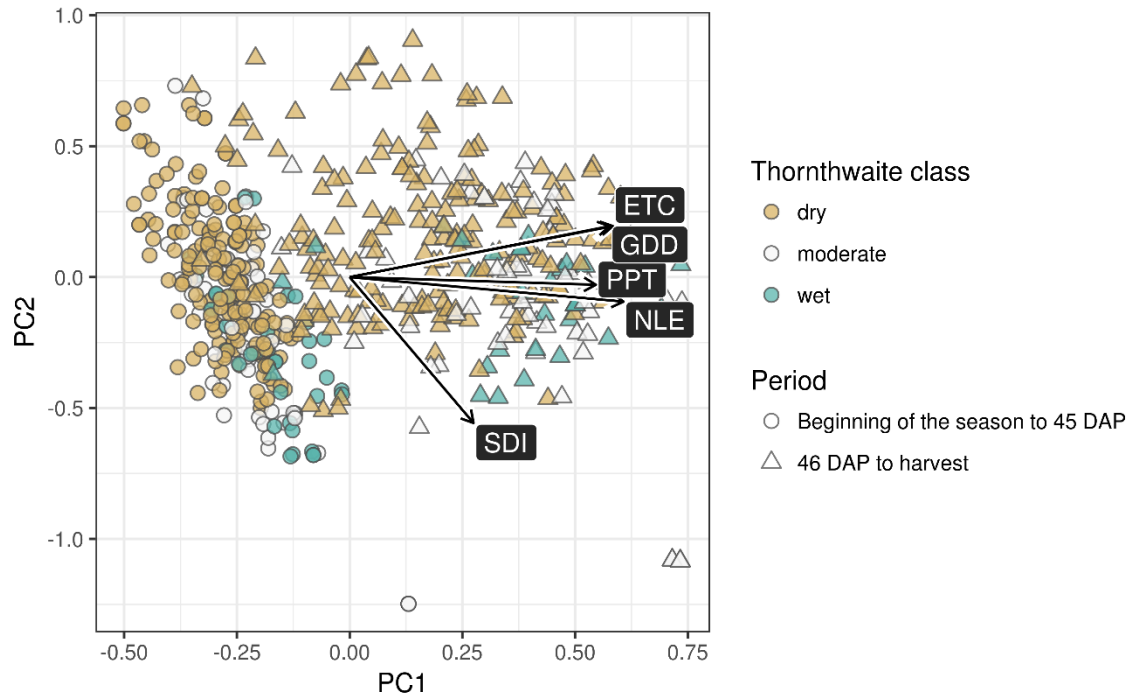


Figure 4. Biplot of the principal component analysis of weather indices (scaling 2).

## 4.2 MULTILEVEL MODEL

The Mitscherlich equation fitted to the experimental data returned a  $R^2$  value of 0.70 for the random effects of blocks and trials, 0.66 for the random effects of trials only (similar to  $R^2$  obtained on non-irrigated sites by Bélanger et al. (2000)), and 0.47 without random effect.

We also tested linear-plateau ( $y = \min(a + bx, \text{max yield})$ ), quadratic ( $y = a + bx + cx^2$ ) and square-root ( $y = a + b\sqrt{x} + cx$ ) equations, that are often used for fertilizer-response models (Colwell 1994). The linear-plateau model did not converge. Parameters  $a$ ,  $b$ , and  $c$  of the quadratic and square-root models are difficult to interpret. The  $R^2$  values were lower for both the quadratic equation [0.66 at block level, 0.63 at trial level and 0.43 without random effect] and square root equation [0.68 at block level, 0.65 at trial level and 0.44 without random effect] compared to the Mitscherlich equation.

#### 4.2.1 Mitscherlich parameters

As indicated in the Methodology section, random effects are applied to the *Asymptote* parameter only at trial and at block levels to account for local variabilities. The random effect at the trial level was normally distributed (Shapiro-Wilk normality test with  $P = 0.58$ ) with zero mean and standard deviation of 5.02. The random effect at block level was normally distributed (Shapiro-Wilk normality test with  $P = 0.14$ ) with zero mean and standard deviation of 1.40. Considering that fixed effects on *Asymptote* ranged from -2.74 to 8.26 Mg ha<sup>-1</sup> with an intercept at 35.2 Mg ha<sup>-1</sup>, the standard deviation of the trial-level random effect of 5.02 Mg ha<sup>-1</sup> was large (14% of the intercept), possibly because other growth-limiting factors such as pest damage and some attributes of soil quality were not documented.

The distributions, paired points and correlations between parameters *Asymptote*, *Environment*, *Rate* as well as the obtained optimal economical dose are shown in Figure 5. The correlations between parameters *Environment* and *Rate* were highly significant and negative (-0.696), indicating high collinearity in our application of the Mitscherlich equation (Equation 1). Moreover, the optimal dose was closely related with *Rate* using an approximate exponential relationship: larger *Rates* led to steeper slopes and consequently smaller optimal doses. The optimal dosage was moderately positively correlated with the *Environment* parameter (0.438), and was less dependent on the *Asymptote* (0.230).

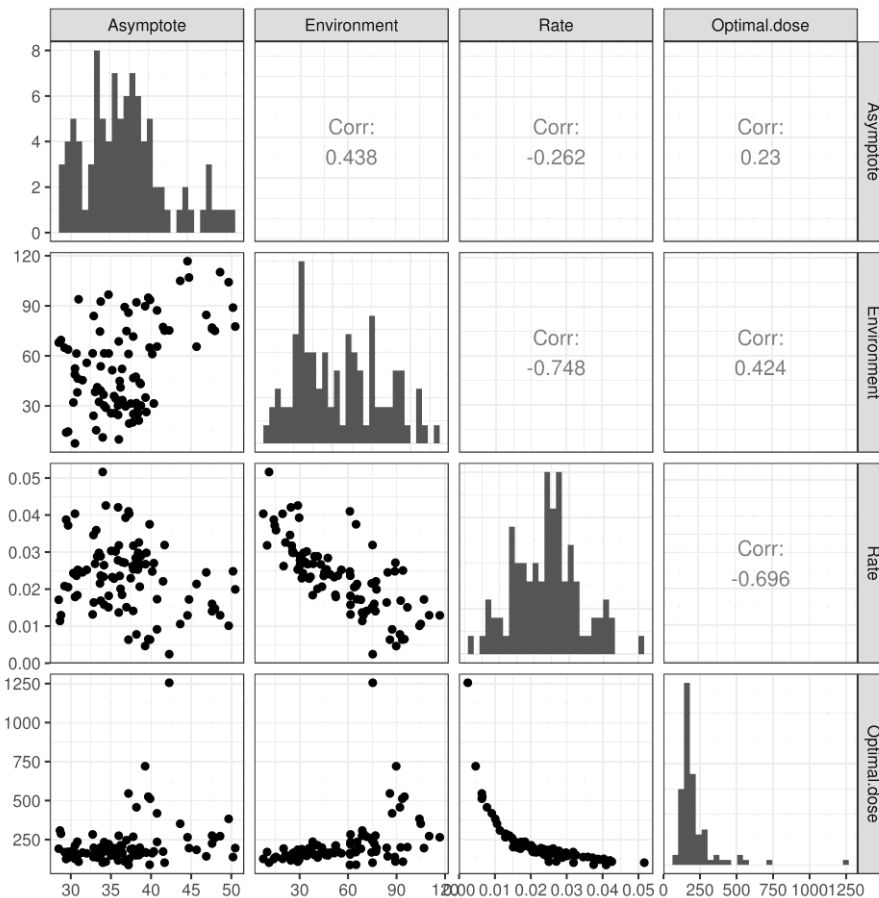


Figure 5. Pairs plot of Mitscherlich parameters and the optimal economical dose obtained with the potato data set. Lower: paired points. Diagonal: distribution histograms. Upper: Pearson correlations.

## 4.2.2 Coefficients

The means and confidence intervals of the linear coefficients of variables in the multilevel model are presented in Figure 6. The means, standard errors and p-values of the coefficients are presented in detail in a separate table as Supplementary material 2. Note that intercepts are values fitted by the model to account for the reference preceding crop (small grain), zero balances and other sources of variation such as soil pH and climatic variables. Intercepts are thus catchalls not directly amenable to interpretation.

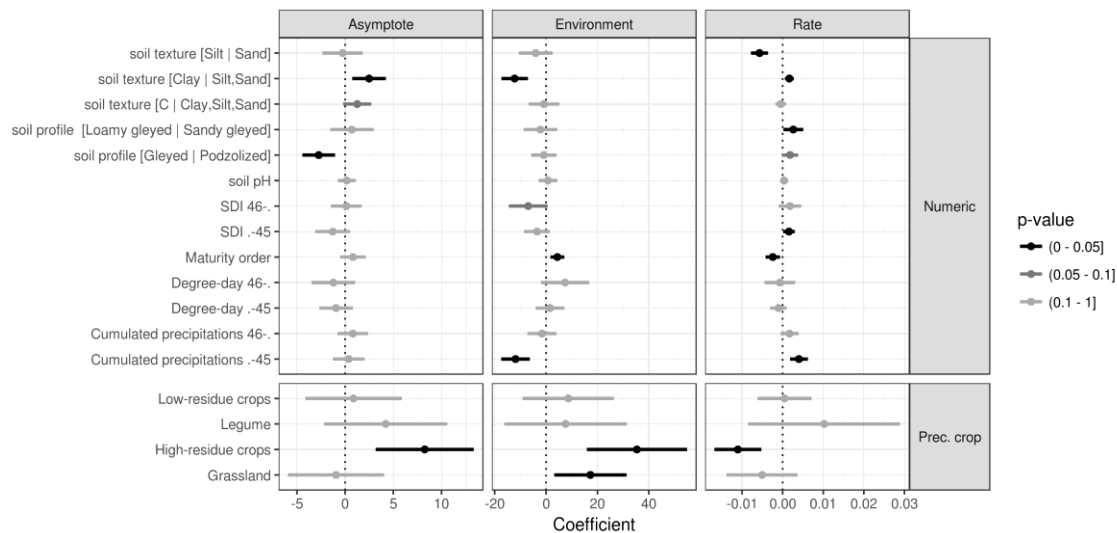


Figure 6. Regression coefficients of the nitrogen multilevel model with 95% confidence intervals.

Parameters *Environment* and *Rate* changed in opposite directions (Figure 6), in agreement with correlations between Mitscherlich parameters (Figure 5). Indeed, for given values of *Asymptote*, *Rate* must get gentler as the contribution of *Environment* to crop N supply increases (i.e. the value of *Environment* becomes more positive).

The characteristics of surface and subsurface soil layers significantly influenced at least one of the three Mitscherlich parameters. The coefficients associated with balances should be carefully interpreted. Because left hand-side components pull the balance variable toward more negative values, and conversely, a positive coefficient indicates that the parameter (i.e. *Asymptote*, *Environment* or *Rate*) increases when the right-hand side of the balance increases in importance relatively to the left-hand side. For instance, the negative coefficient on *Asymptote* (Figure 6) associated with the [Gleyed | Podzolized] balance indicates that greater podzolisation than gleization tends to decrease *Asymptote*. In a similar way, if clay increases in the surface soil layer the contribution of *Environment* to crop N supply also increases. The effect of soil pH on the three Mitscherlich parameters was not significant.

#### 4.2.2.1 *Asymptote*

The parameter representing the maximum reachable yield, *Asymptote*, significantly ( $P = 0.0016$ ) decreased with pedological group leaning towards the podzolized, well drained, soil profiles (coefficient of variable [Gleyed | Podzolized] is negative). The soil texture balance [Clay | Silt,Sand] significantly ( $P = 0.0054$ ) increased the *Asymptote*. All other things being equal, increasing the proportion of clay relatively to proportions of silt and sand would tend to decrease *Asymptote*. While soil organic matter accumulation showed no significant effect ( $P = 0.094$ ), the high-residue preceding crops increased the *Asymptote* significantly ( $P = 0.0015$ ) compared to the small grain class, indicating that organic matter quality could be an important driver for high yield. Other classes of preceding crops did not depart significantly from small grain.

#### 4.2.2.2 *Environment*

The *Environment*, i.e. the parameter representing the fertilizer-equivalent dose provided by environmental conditions, decreased significantly ( $P = 3.9 \times 10^{-6}$ ) with the [Clay | Silt,Sand] textural balance, indicating larger fertilizer-equivalent doses in fine-textured soils. The *Environment* increased significantly ( $P = 0.0015$ ) as the cultivar maturity order increased, probably because cultivar of higher maturity is typically harvested later in the season. Increasing cumulated precipitations from beginning of season to 45 DAP significantly decreased the *Environment* parameter ( $P = 3.1 \times 10^{-5}$ ). As preceding crops, high-residue crops and grassland increased *Environment* significantly (respectively,  $P = 0.00039$  and  $P = 0.016$ ) compared to small grain.

#### 4.2.2.3 *Rate*

A relatively large proportion of the coefficients related to the *Rate* (the steepness of the response curve) showed significance (7 out of 17). While the [Clay | Silt,Sand] balance significantly ( $P = 0.0035$ ) increased *Rate*, the [Silt | Sand] balance significantly ( $P =$



1.4×10<sup>-7</sup>) decreased *Rate*, but the [C | Clay,Silt,Sand] balance had no effect (P = 0.51). The *Rate* tended to increase (P = 0.075) towards well drained profiles (positive [Gleyed | Podzolized] coefficient), and increased significantly (P = 0.035) with the [Loamy | Sandy] balance of gleyed soil profiles. Cumulated precipitations showed significant (P = 0.00032) positive effect on *Rate* from the beginning of season to 45 DAP, but its effect from 46 DAP to harvest, also positive, was not significant (P = 0.13). The Shannon diversity index (SDI) only had a significant (P = 0.033) effect from the beginning of the season to 45 DAP. The *Rate* decreased significantly (P = 0.0081) as the cultivar maturity order increased. The high-residue crops preceding crop class decreased the *Rate* significantly (P = 0.00019) compared to small grain.

### 4.3 SIMULATIONS OF N RESPONSE IN SELECTED TRIALS

Trials 4, 71, 89 and 342 were selected to represent contrasting classes and levels of variables, as follows:

1. **Trial 4.** 'Bijou Rouge' (maturity order 1) and grassland as preceding crop; subsoil texture is sandy and moderately podzolized; surface soil texture is sandy loam.
2. **Trial 71.** 'Superior' (maturity order 2) grown under the wettest conditions after low-residue crops as preceding crops; the subsoil is highly gleyed and its texture is loamy; the texture of the surface soil is medium (loam).
3. **Trial 157.** 'Russet Burbank' (maturity order 5) grown under highly podzolized, sandy subsoil; coarse soil in the arable layer (loamy sand) with high organic matter content; very high growing degree days through the first period and very low precipitations through the second period; small grain is the preceding crop class.
4. **Trial 342.** 'W 1386' (maturity order 4) grown under highly podzolized, sandy subsoil; coarse soil in the arable layer (loamy sand) with high organic matter content (similar

to trial 157); small grain is the preceding crop class; soil pH is higher than the 75% quantile.

The mean values of coefficients are presented in Figure 7.

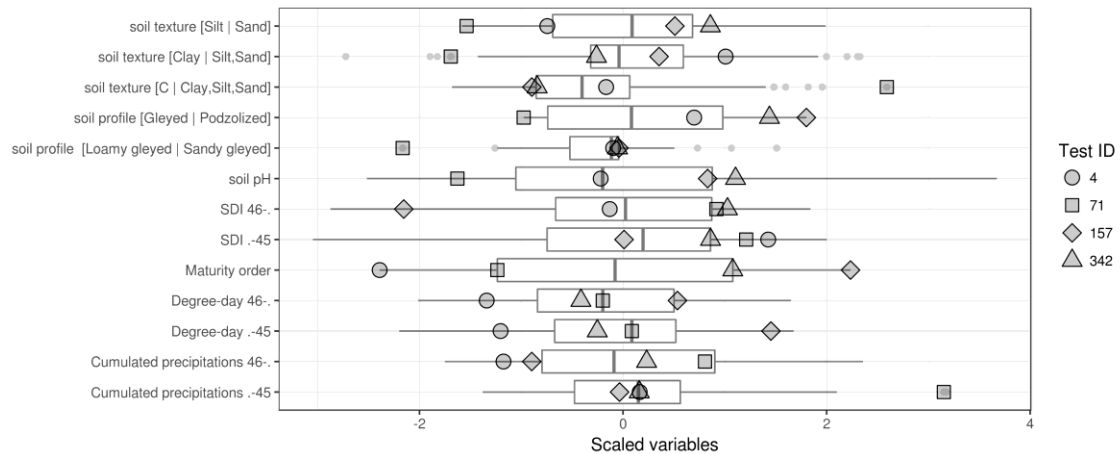
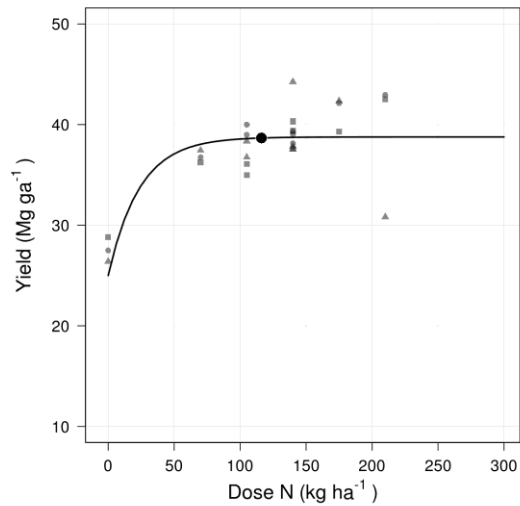
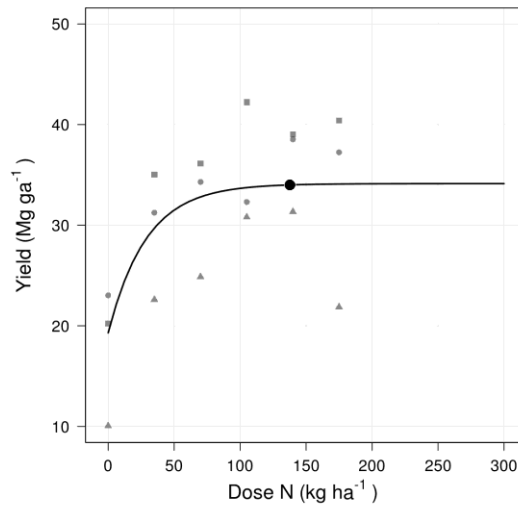


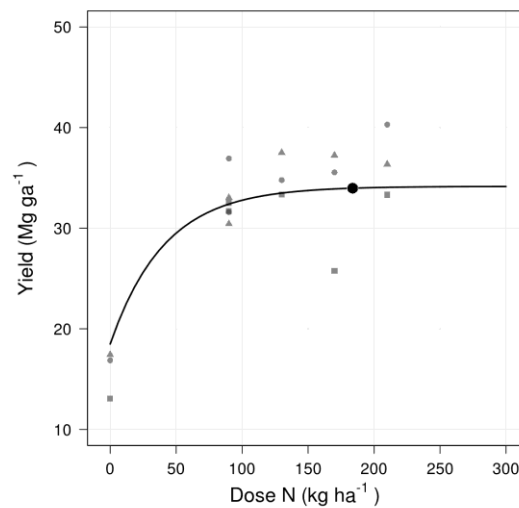
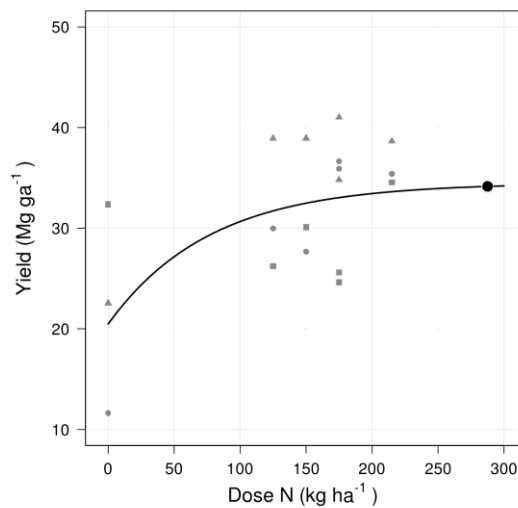
Figure 7. Boxplots of scaled numerical variables to evaluate the N-model.

Results of the fitted response curves of the selected trials are presented in Figure 8. The black dots are observations, and the symbols represent blocks. The curves are drawn using the trial-level random effect (level 1). The model was fitted across the whole data set: trials are specific application of the model. Unusual cases returning optimal doses lower than  $50 \text{ kg N ha}^{-1}$  (the minimum non-null dosage used in most trials) should be interpreted with care.



(a)

(b)



(c)

(d)

Figure 8. Estimated Mitscherlich curves obtained from the multilevel model. The line is computed from coefficients estimated by the multilevel model. Points are measures, and the symbols represent experimental blocks. Large filled circles are optimal doses and their associated yield. (a) Trial 4, (b) Trial 71, (c) Trial 157 and (d) 342.

#### 4.3.1 Trial 4

Trial 4 (Figure 8a) returned an  $R^2$  value of 0.41, lower than the  $R^2$  value of 0.67 for the whole set of N experiments using the trial-level (level 1) random effects. The optimal

dose computed from the estimated coefficients was 138 kg N ha<sup>-1</sup>. Without the random effect of 1.3 Mg ha<sup>-1</sup>, the *Asymptote* was 33 Mg ha<sup>-1</sup>, as limited by the low cultivar maturity order, the high SDI from the beginning of the season to 45 DAP and the high podzolization, but was compensated in part by the high [Clay | Sil,Sand] balance. The *Environment* parameter was low at 24 kg N ha<sup>-1</sup>, related to the high [Clay | Sil,Sand] texture balance (low clay content or high silt and sand contents) and the low numbers of growing degree-days from 46 DAP to harvest. It was however promoted by the grassland preceding crop class. The *Rate*, on the other hand, was high (0.035), thanks to the low [Silt | Sand] balance and the low cultivar maturity order, but was lowered by the grassland preceding crop class.

#### **4.3.2 Trial 71**

Trial 71 (Figure 8b) returned a high R<sup>2</sup> value of 0.93. The optimal economic dose was 116 kg N ha<sup>-1</sup>. The *Asymptote* of 36 Mg ha<sup>-1</sup> (without the random effect of 4.3 Mg ha<sup>-1</sup>) was near the median value obtained in the potato data set (36 Mg ha<sup>-1</sup>). The low [Gleyed | Podzolized] and high [C | Clay,Silt,Sand] balances (gleyfied and low organic content), that pushed the *Asymptote* up, was offset by the low [Clay | Silt,Sand] balance. The *Environment* supplied 35 kg N ha<sup>-1</sup>, apparently related to unusually high cumulated precipitations from beginning of season to 45 DAP. The contribution of the *Environment* enhanced due to the low [Clay | Silt,Sand] balance. Finally, the *Rate* was high (0.042), pushed up mainly by high cumulated precipitations from beginning of season to 45 DAP and the low [Silt | Sand] balance, but was lowered by the low [Loamy gleyed | Sandy gleyed] balance.

#### **4.3.3 Trial 157**

Trial 157 (Figure 8c) returned an R<sup>2</sup> value of 0.42. The optimal dose was 288 kg N ha<sup>-1</sup>, i.e. beyond the maximal dose of the trial. The *Asymptote* was 29 Mg ha<sup>-1</sup> (without the

random effect of  $5.9 \text{ Mg ha}^{-1}$ ), which is among the lowest values obtained across the 93 trials. The *Asymptote* was mainly dragged down by a high podzolization, i.e. high [Gleyed | Podzolized] balance, although pushed up by the high maturity order of the Russet Burbank cultivar. The *Environment* parameter was of  $69 \text{ kg N ha}^{-1}$ , which is above the median obtained in the potato data set ( $52 \text{ kg N ha}^{-1}$ ), as dragged down by a high [Clay | Silt, Sand] balance but pushed up by a high maturity order and high numbers of growing degree-days for both periods. The *Rate* of 0.013 was quite low. The *Rate* was increased by a high [Gleyed | Podzolized] balance but decreased by the high maturity order, the high numbers of growing degree-days through the first period and low cumulated precipitation through the second period.

#### 4.3.4 Trial 342

Trial 342 (Figure 8d) returned an  $R^2$  value of 0.55. The optimal dosage was  $184 \text{ kg N ha}^{-1}$ . Without the random effect of  $3.7 \text{ Mg ha}^{-1}$ , the *Asymptote* was  $30 \text{ Mg ha}^{-1}$ , which was low mainly due to a high podzolization, i.e. high [Gleyed | Podzolized] balance. The *Environment* parameter was  $32 \text{ kg N ha}^{-1}$ , which was also low, although *Environment* was promoted by the high maturity order of the W 1386 cultivar. The *Environment* was lowered by a very high [Silt | Sand] balance and a slightly low numbers of growing degree-days from 46 DAP to harvest. The *Rate* of 0.024 was equivalent to the median *Rate* of the potato data set (0.024). The *Rate* was lowered by the high [Silt | Sand] balance and high maturity order, and enhanced by a high [Gleyed | Podzolized] balance.

## 4.4 SENSITIVITY ANALYSES

### 4.4.1 Optimal dosage

Optimal doses were computed over the range of a single parameter (Equation 1: *Asymptote*, *Environment* and *Rate*), keeping the two other parameters at their median

values, with unit fertilizer costs set at 1.20 CDN \$ kg<sup>-1</sup> of N and unit crop price at 275  
 CDN \$ Mg<sup>-1</sup>. Results shown in Figure 9 are cuts taken from a hyper-plane. For a given  
 parameter, slopes and intercepts (for *Asymptote* and *Environment*) or trend (for *Rate*)  
 depend on the values used for the two other parameters, as well as on the unit fertilizer  
 cost and the unit crop price. However, it can be shown that holding other variables at  
 constant values the slope of the *Environment* parameter was -1. While optimal doses  
 slightly increased linearly with higher *Asymptote*, and decreased linearly where the  
 contribution of the *Environment* increased, the impact on *Rate* was approximatively  
 exponential - higher *Rate* returning steeper response curves. This sensitivity analysis  
 agreed with the paired plots shown in Figure 5 and with case studies presented  
 previously, where *Rates* had a major impact on optimal economical doses.

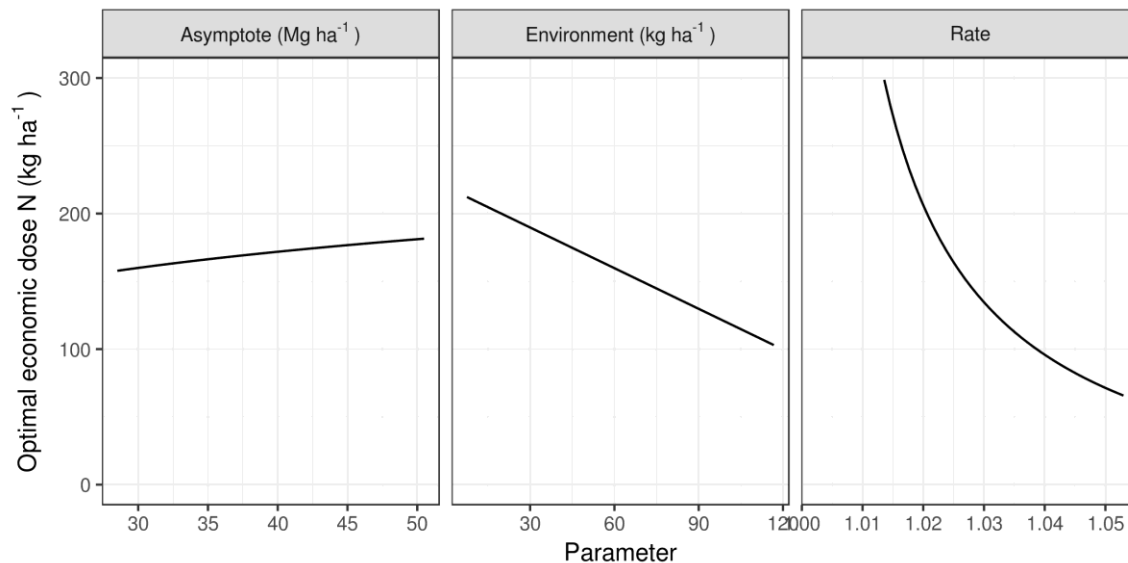
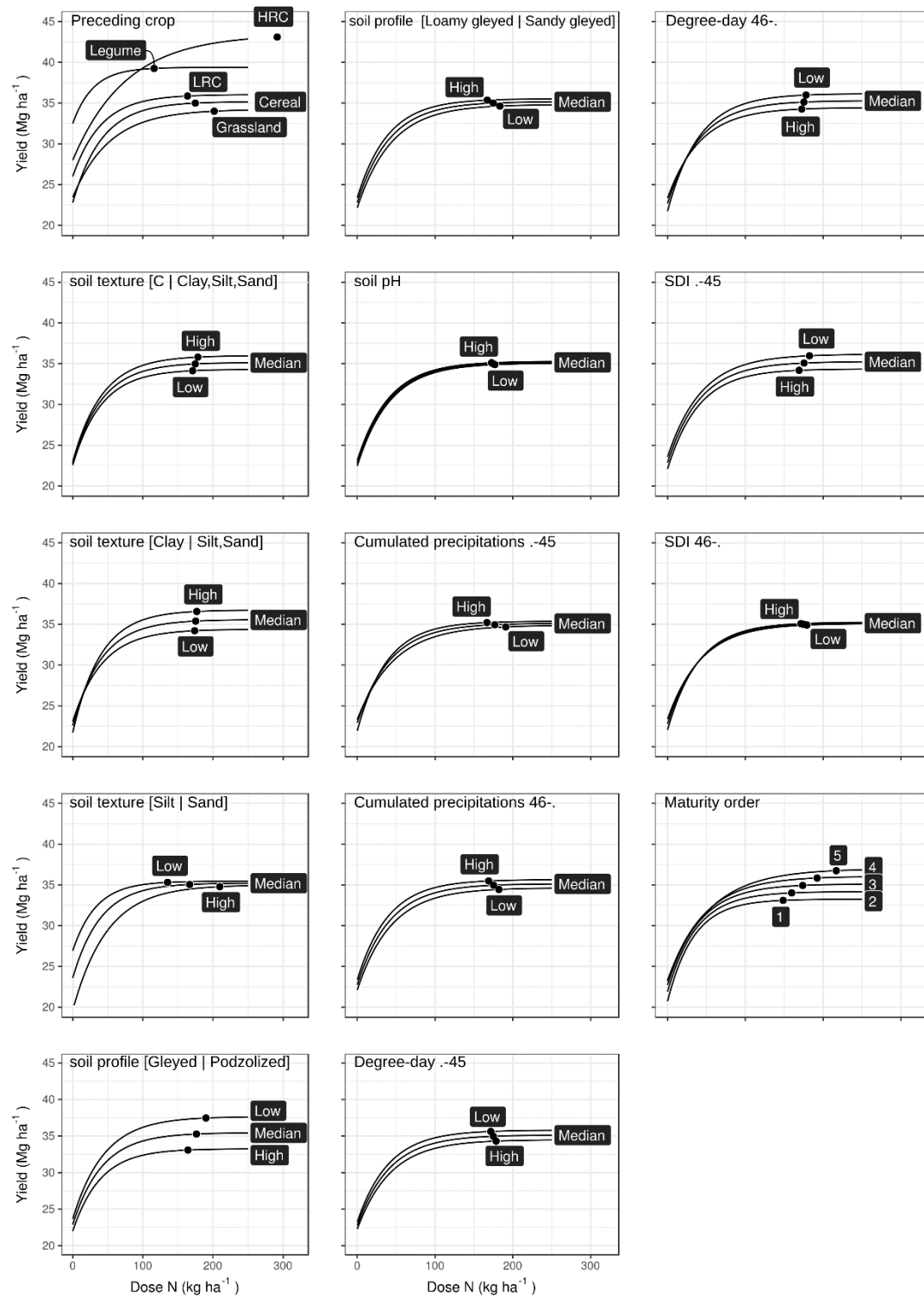


Figure 9. Sensibility analyses conducted on Mitscherlich parameters defined in Equation 1.

#### 4.4.2 Multilevel mixed model variables

We conducted a sensitivity analysis for each variable included in the model, with only  
 one variable varying in each case. Other numeric variables were set to their mean in the  
 data set (which was 0, since they were scaled), and the preceding crop was set to small

543 grain when not tested for sensitivity. Varying numeric variables were set to the 25%  
544 quantile (low), the median and the 75% quantile (high). The sensitivity analysis only  
545 accounted for the magnitude of the coefficients and avoided uncertainty. Results are  
546 presented in Figure 10.



547

548 *Figure 10. Sensitivity of the multilevel mixed model. In each case, small grain was the preceding crop.*



549 The coefficient for soil profile class [Gleyed | Podzolized] was significant (Figure 6) and  
550 thus impacted on *Asymptote* (Figure 10, range: 33 to 38 Mg ha<sup>-1</sup>). More gleization  
551 (hence larger amounts of available water in the soil profile) led to higher yield. In the  
552 sensitivity analysis, the *Environment* ranged from 42.5 to 43.9 kg N ha<sup>-1</sup> and *Rate* from  
553 0.023 to 0.025. Average optimal N dosage varied between 164 and 190 kg N ha<sup>-1</sup>.

554 The [Silt | Sand] balance in the arable layer (Figure 10) resulted in a narrow range for  
555 *Asymptotes*, from 35.0 to 35.5 Mg ha<sup>-1</sup>. *Environment* ranged from 40 to 47 kg N ha<sup>-1</sup>, and  
556 *Rate* from 0.020 to 0.030. Although the *Asymptote* varied barely, the *Environment* and  
557 *Rate* parameter impacted on optimal dosage that varied between 135 and 210 kg N ha<sup>-1</sup>.

558 The preceding crop (Figure 10) influenced markedly the shape of the response curves.  
559 The *Asymptote* varied from 34 (grassland) to 43 (high-residue crops) Mg ha<sup>-1</sup>,  
560 *Environment* from 43 (small grain) to 78 (high-residue crops) kg N ha<sup>-1</sup> and *Rate* from  
561 0.013 (high-residue crops) to 0.034 (legume). The optimal doses ranged from 175 (low-  
562 residue crops) to 292 kg (high-residue crops) N ha<sup>-1</sup> among preceding crop classes.

563 The maturity order from 1 to 5, i.e. 1 = early and 5 = late, (Figure 10) returned optimal  
564 doses ranging from 149 (maturity 1) to 217 (maturity 5) kg ha<sup>-1</sup>. The *Asymptote* varied  
565 from 33 (maturity 1) to 37 (maturity 5) Mg ha<sup>-1</sup>, while *Environment* ranged from 33  
566 (maturity 1) to 53 (maturity 5) kg N ha<sup>-1</sup> and *Rate* from 0.019 (maturity 5) to 0.030  
567 (maturity 1).

## 5 DISCUSSION

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### 5.1 SELECTION OF THE RESPONSE FUNCTION

The Mitscherlich equation assumes sufficient supply of nutrients other than the one being varied to ensure constant exponential coefficient and the most efficient use of the nutrients being varied as prescribed by Liebscher's law of optimum. However, our application of Mitscherlich's equation incorporated the Liebscherian view that the *Rate* parameter in the Mitscherlich function (Equation 1) was not a constant, but depended on how local conditions are close to their optima.

Where *ex-ante* N recommended dosage proved to be lower than *ex-post* optimal dosage, it tended to occur on less productive sites (Rajsic and Weersink 2008). Soil compaction increases soil strength and decreases soil physical fertility through decreasing storage and supply of water and nutrients, which leads to lower yields and higher fertilizer requirements (Hamza and Anderson 2005; Stalham et al. 2005).

Nevertheless, Inman et al. (2005) suggested that low-yielding areas in a field should receive less nutrient dosage. The present multilevel mixed model indicated that under stressful conditions, potato response to added N tended to level off at relatively low N dosage as suggested by Inman et al. (2005). As more limiting factors are relieved, nutrient use efficiency must increase. In the case of potato crops, irrigation scheduling (Haverkort and Struik 2015), remedial measures against soil compaction (Rees et al. 2015; Stalham et al. 2005) and crop sequences could improve nutrient use efficiency.

On the other hand, growers often think that higher yields can be attained just by adding an incremental dosage of nutrients based on nutrient removal by the incremental yield computed by difference between yield target and some yield average. However, incremental dosage of fertilizers denies the law of diminishing returns and the law of

optimum. Our results support the view that higher yields that could only be obtained with appropriate measures to raise the level of other factors closer to their optimum (de Wit 1992) required more N input in average (Figure 9).

## 5.2 INPUT VARIABLES

The *Asymptote* parameter was driven primarily by soil texture, soil profile morphology and the preceding crop. Soil quality represented here by soil texture and the soil profile class is a primary driver of the potato agroecosystem productivity (Boiteau et al. 2014). The high-residue crops contributed to higher yield probably because (1) such crops were grown in the southern potato region of the St-Lawrence Lowlands where potato yields are higher; (2) labile organic matter temporarily immobilized soil N but contributed to water retention.

Although *Environment* is expressed in equivalent dosage units (e.g. kg N ha<sup>-1</sup>), it represents a set of conditions that determines yields at zero N supply from fertilizers. The model showed that the contribution of *Environment* to crop N supply increased with cultivar maturity class and high residue crops, and varied with the balances between the [Clay | Silt,Sand] balance. In terms of weather indices, higher cumulated precipitations across the first period drove the *Environment* parameter downward, possibly due to leaching. Organic matter decomposition could impact indirectly to *Environment* through its relationship with soil texture, moisture and temperature (Andr  n and K  tterer 1997; Thomsen et al. 1999) that mediate carbon sequestration (Stewart et al. 2008).

The preceding crop may mop up soil nitrate or fix molecular nitrogen, hence potentially contributing to the N supply of the following potato crop (Alva et al. 2002; Tonitto et al. 2006). While annual cropping depletes soil organic N, crop rotations including forages and the addition of animal manure are N building management practices (Bolinder et al.

2010). Crop N uptake and crop residues low in N and hence high in C/N ratio can decrease the N losses, demonstrating the importance of the quality of organic inputs in the N budget of agroecosystems (Persson and Kirchmann 1994). The composition of crop residues, mineral N concentration in the soil and soil aggregation determine the kinetics of N immobilization and the subsequent remobilization by feed-back effects (Mary et al. 1996). Grassland can accumulate large amounts of microbial biomass N by immobilizing mineral N in late spring and the fall (Corre et al. 2002), resulting in potential N credits of 55-99 kg N ha<sup>-1</sup> after sod breakup (Li et al. 1999b; Neeteson 1990). Maize and ryegrass were found to increase N requirements compared to other preceding crops probably due to buildup of high-C/N organic matter in the soil.

As expected from Liebscher's law of optimum, the *Rate* parameter varied markedly with growth factors (8 out of 17 in Figure 6). The model showed that a silty soil surface texture, a sandy and podzolized (well drained) soil profile, as well as cumulated precipitations and SDI from the beginning of the season to 45 DAP increased *Rate*; while late maturity and high-residue crops decreased it.

Although the potato harvested at tuber maturity generally reaches a plateau without negative effect of extra N dosage (Shepherd 2000) except in case of late N applications affecting tuber quality (Hofman and Salomez 2000), surplus N availability during the early growth stage can delay the transition from shoot accumulation to translocation of N to tubers until early August (Kleinkopf and Dwelle 1978). As a result, early-harvested potatoes generally show yield decrease at high N dose by retarding maturity (Shepherd 2000). Such yield decrease cannot be modelled by the ascending Mitscherlich curve. In this special case, other non-linear models, such as polynomial models, may be selected. However, most trials were conducted with storage rather than early harvest potatoes.

### 5.3 MODEL SENSITIVITY

Sensitivity analyses should be interpreted with care because the uncertainties about coefficients were not included. Sensitivity analyses showed that the source of water (rainfall or groundwater) influenced potato N requirements differently. Besides, mineral nitrogen is not available to the crop unless the water supply is within certain limits (Karvonen et al. 2000).

Case studies across weather indices (Figure 10) generated a narrow range of *Asymptotes* from 34 to 36 Mg ha<sup>-1</sup>, essentially due to the range of SDI from the beginning of season to 45 DAP. Moreover, *Environment* ranging from 29 to 48 kg N ha<sup>-1</sup> and *Rate* from 0.024 to 0.028, slightly impacted on optimal N dosage that varied between 164 and 186 kg N ha<sup>-1</sup>, essentially due to cumulated precipitations from 46 DAP to harvest. Wetter soil conditions favor microbially mediated processes (Bolinder et al. 2007) and the diffusion of mineral N across the root zone hence facilitating N uptake (Karvonen et al. 2000). Drier soil conditions generally increased N requirements possibly due to difficulties for fertilizer granules (most often 27-0-0, 18-46-0 and 11-52-0) to dissolve.

Wetter soil conditions increased nitrogen use efficiency (smaller optimal N for higher yield), indicating that the seasonal wet weather as defined here resulted in limited nitrate leaching events. The reported nitrate contamination of groundwater attributed to potato cropping (Levallois et al. 1998) may be the result of nitrate leaching during events outside the cropping growth period in the fall and winter and after snowmelt where soil surface is bare and water is abundant (Jiang et al. 2011; Peralta and Stockle 2002).

The interaction between available water and nitrogen must differ between rainfall water that contacts the arable layer well supplied with mineral N and the groundwater where

mineral N is less abundant. The [Gleyed | Podzolized] plot shown in Figure 10 illustrates water supply to the root zone that originates from the groundwater where mineral N supply capacity must be much smaller due to lower microbial activity below the arable layer. Gleyed soils produced higher yield potential (Figure 6) and required more fertilizer N compared to podzolized soils. Soil pedogenesis (gleization and podzolization) should be interpreted in the context of soil texture. Soil texture defined by the [Silt | Sand] balance in the arable layer indicated that higher silt proportions relative to sand proportions had a minor influence on expected maximal yield, but considerably drove N requirement downward (Figure 10) by increasing the *Rate* parameter (Figure 6). Silt increases soil water-holding capacity, hence stimulating microbial activity and phosphate transfer from soil particles to the roots.

Where overhead irrigation or rainfall maintain moist conditions in the arable layer, microbial activity may be stimulated (Bolinder et al. 2007) therefore increasing mineral N available in the root zone. Subsurface irrigation of potato crops with controlled drainage that maintains adequate moisture conditions in the arable layer is known to use less water and may lead to higher fertilizer use efficiency compared to overhead irrigation (Satchithanantham 2013). However, where subsurface drainage is installed in potato soils, drainage water may remove 14 to 70 kg N ha<sup>-1</sup> from the soil profile (Madramootoo et al. 1992, 1995).

The preceding crop is known to influence soil N supply capacity through the C/N ratio of crop residues (Stevenson 1986). The sensitivity analysis in Figure 10 shows that high-residue crops and grassland (generally showing high C/N ratios) require more fertilizer N compared to other preceding crops, especially legumes. Note that yield levels in Figure 10 must be interpreted with care because, compared to grassland grown mainly in

northern regions, maize is grown as rotation crop in more southerly regions where potato yields are higher due to longer growing seasons.

It is generally agreed that N requirements differ among cultivars (Gianquinto and Bona 2000; White et al. 2007). The daily rate of N accumulation in tubers is known to be higher for short and intermediate than long cycle cultivars (Kleinkopf et al. 1981; Saluzzo et al. 1999). For long cycle cultivars, a substantial fraction of the N remains in the aboveground biomass (Kleinkopf et al. 1981). The N input may also vary among cultivars with similar longevity (White et al. 2007). The present multilevel model classified the cultivar effect according to the assumed maturity order only. As expected, sensitivity analysis showed higher N requirements as tuber yield increased from early to late cultivars (Figure 10). Tuber yield has been shown to increase linearly with time from tuber formation to harvest (Fortin et al. 2010) as indicated, in the present study, by the effect of maturity group on tuber yield.

## **5.4 USING MULTILEVEL MIXED MODEL TO ESTIMATE OPTIMAL ECONOMIC DOSE**

Experiments to determine fertilizer N requirements for maximum and optimum tuber yields resulted in a wide range of N doses (Hill 1984; White et al. 2007) depending on soil type and weather conditions, agronomic factors such as timing, location and chemical form of the fertilizer applied, and genetic factors (Gregory and Simmonds 1992). In general, N optima depended on the response model and yield target, market (Hill 1984), weather, soil type and cropping systems (Hanks and Ritchie 1991), and cultivar (Gianquinto and Bona 2000; White et al. 2007). Bélanger et al. (2000) obtained N optima ranging from 108 to 230 kg N ha<sup>-1</sup>, averaging 171 kg N ha<sup>-1</sup>. Our model simulations returned optimal N doses within a wide range of values, from 87 kg N ha<sup>-1</sup> to

an outlier of 1255 kg N ha<sup>-1</sup> (Figure 5). Indeed, some response curves were so gentle (low *Rate* parameters) that optimal N doses were far above the highest N treatment. Such specific local conditions must be interpreted with care. Nevertheless, we obtained N optima between the 25% and 75% quantiles of 150 and 219 kg N ha<sup>-1</sup> with a median of 172 kg N ha<sup>-1</sup>. In the case of a descriptive model at field level where soil and managerial conditions are known, scenarios of climatic conditions could also be tested to facilitate selecting the most appropriate N dosage or past N management practices can be compared to those computed by the model.

The multilevel model presented here accounts for several factors that impact on potato yield. Marshall (2000) listed other factors including soil compaction and pest management. Using data from the Quebec soil degradation survey (Tabi et al. 1990), we estimated that 65% of potato soils were degraded compared to grassland used as reference, mainly due to compaction and loss of organic matter. Because N requirements depend on yield potential (Inman et al. 2005) and tuber yield is higher in high- compared to low-quality soils (Boiteau et al. 2014; Stalham et al. 2005), more research is needed to elucidate the relationship between fertilizer requirements, water input, other soil quality attributers and tuber yield and quality as soil conditions and crop management are improved.

## 6 CONCLUSION

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In this paper, we developed a multilevel optimization model using a Québec data set to assess potato N requirements across several combinations of growth-limiting factors and to provide a new insight into crop response patterns for use in precision farming. Geophysical technologies of precision agriculture, digital soil maps and meteorological stations can provide input data at low cost to run the model. The general model contains



categorical as well as continuous variables that can be interpolated to fit intermediate local conditions. The model can be expanded to include tuber quality such as tuber size and specific weight.

The model could be tested as a predictive one with additional data and the use of machine learning algorithms. The tactical decision to split the N into several soil or foliar applications will also require additional modeling effort using more detailed meteorological information from stations closest to the field.

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## 982 SUPPLEMENTARY MATERIAL

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- 983 *Supplementary material 1. R code and data archive at [https://github.com/essicolo/site-specific-multilevel-](https://github.com/essicolo/site-specific-multilevel-modeling-of-potato-response-to-nitrogen-fertilization)*  
984 *modeling-of-potato-response-to-nitrogen-fertilization*
- 985 *Supplementary material 2. Mean, standard errors and covariance of coefficients of the Nitrogen multilevel*  
986 *model.*