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Bit position 1 requires a borrow from bit position 2 Because of this borrow, minuend bit 2 is a 0. The subtraction continue: through the

Example 1.18

are zeros, borrowing is from bit 6. In this process, the intermediate minuend bits 4 and 5 each attain a value of 1 (compare this with the Bit 2 requires a borrow from bit 3; after this borrow, minuend bit 3 is 0. Then, bit 3 requires a borrow. Because bits 4 and 5 of the minuend decimal subtraction). The subtraction continues through the MSB.

Multiplication Binary multiplication is similar to decimal multiplication. From Table 1.3(c), we can see that $0 \times 0 = 0$, $0 \times 1 = 0$, $1 \times 0 = 0$, and $1 \times 1 = 1$. An example follows.

In general, the product of two n-bit numbers is 2n bits long. In Example 1.19, there are two nonzero bits in the multiplier, one in position 2

two bits yield partial products whose values are simply that of the multiplicand shifted left two and three bits, respectively. The 0 bits in the multiplier contribute partial products with 0 values. Thus, the following corresponding to 22 and the other in position 3 corresponding to 23. These shift-and-add algorithm can be adopted to multiply two n-bit numbers A and B, where $B = (b_{n-1} \ b_{n-2} \cdots b_1 b_0)$.

- 1. Start with a 2n-bit product with a value of 0.
- 2. For each b_i ($0 \le i \le n 1$) $\ne 0$ shift A i positions to the left and add to the product.

This procedure reduces the multiplication to repeated shift and addition of the multiplicand.

Division The longhand (trial-and-error) procedure of decimal division can also be used in binary, as shown in Example 1.20.

Example 1.20

 $110101 \div 111 = ?$

 $q_1 = 0$ do not subtract $q_2 = 1$ subtract $q_3 = 1$ subtract $q_4 = 1$ subtract 110 < 111 1100 > 111 1011 > 111 1101 > 111remainder 0111 Quotient 110,101

dividend. The compare-and-subtract process is continued until the LSB of the dividend. The procedure is formalized in the following steps. is 0; otherwise, the quotient bit is 1, and the divisor is subtracted from the In this procedure, the divisor is compared with the dividend at each step. If the divisor is greater than the dividend, the corresponding quotient bit

1. Align the divisor (1) with the most significant end of the dividend. Let the portion of the dividend from its MSB to its bit aligned with