Integer Fraction 1256.932 Decimal point

10³10²10¹10⁰ . 10⁻¹10⁻²10⁻³ weights

Powers increase by 1. Powers decrease by 1

This number can also be represented as a polynomial:

$$1 \times 10^{3} + 2 \times 10^{2} + 5 \times 10^{1} + 6 \times 10^{0} + 9 \times 10^{-1} + 3 \times 10^{-2} + 2 \times 10^{-3}$$

tem. The general positional notation of a number N is We can thus generalize these two representations to any number sys-

$$N = (a_n \cdots a_3 a_2 a_1 a_0 \cdot a_{-1} a_{-2} a_{-3} \cdots a_{-m})_r \tag{1.1}$$

digits such that $0 \le a_i \le (r-1)$ for all i; a_n is the most significant digit (MSD), and a_{-n} is the least significant digit (LSD). The *polynomial* representation of the above number is where r is the radix of the number systems; a_{-1} , a_0 , a_1 , a_2 , and so on, are

$$N = \sum_{i=-m}^{n} a_i r^i {1.2}$$

There are n+1 integer digits and m fraction digits in the number shown

corresponds to each digit of the n-digit integer being equal to 0. When each digit corresponds in value to r=1, the highest digit in the number systems. We will discuss binary, octal, and hexadecimal systems next. system, the *n*-digit number attains the highest value in the range. This value is equal to $r^n = 1$. Table 1.1 lists the first few numbers in various represented by this integer. The smallest value in this range is 0 and Consider an integer with n digits. A finite range of values can be

1.2.1 Binary System

positional notation in the following example. digiT is abbreviated as BIT. A typical binary number is shown in the In this system, the radix is 2 and the two allowed digits are 0 and 1. BInary

Table 1.1 Number Systems 1.2 Number Systems 5

| | 0.0 | 3 - | 0 | | 1/ | i 5 | ; , | 7 | <u>, 7</u> | بد | 12 | Ξ | : = | 5 \ | 9 | 00 | 7 | 0 | | 4 . n | | ٠, ١ | | ۔ د | , | (r = 10) | 7 |
|---|-------|---------|-------|-------------|-------|-------------|----------------|------|------------|------|-----|------|------|------|------|------|---------|----------|-----|--------------|------|------|-----|-----|---------|----------------------|---|
| | 10100 | 10011 | 10011 | | 10001 | 10000 | 1111 | 1110 | | 1101 | 100 | 1011 | 0101 | 1001 | 1001 | 1000 | Ξ | 110 | 101 | | = | 0 | _ | 0 | | Binary $(r=2)$ | |
| | 202 | 107 | 100 | 300 | 122 | 121 | 120 | 1112 | = | - : | = | 102 | 101 | 100 | 100 | 23 | 21 | 20 | 12 | = | 0 | 2 | - | 0 | | Ternary $(r = 3)$ | |
| | =0 | 103 | 102 | | 101 | <u>1</u> 00 | 33 | 32 | 5 | 2 0 | 20 | 23 | 22 | 21 | | 30 | <u></u> | 12 | = | 10 | ų, | 2 | _ | 0 | | Quaternary $(r = 4)$ | |
| ! | 24 | 23 | 22 | <u>!</u> | 21 | 20 | 17 | 16 | 15 | 14 | | | 12 | = | 10 | | 7 | ς. | S | 4 | (L) | 2 | _ | 0 | 3 | Octal $(r = 8)$ | |
| 1 | Z ; | <u></u> | 12 | - | - 3 | <u>.</u> | মা | T. | D | C | 0 | ם ב | Δ, | 9 | 00 | ÷ ~ | 10 | , | л. | 4 | ا بر | ٠. | _ < | 0 | 0 - 10) | Hexadecimal | |

Example 1.2

In polynomial form, this number is

$$N = 1 \times 2^{4} + 1 \times 2^{3} + 0 \times 2^{2} + 1 \times 2^{1} + 0 \times 2^{0} + 1 \times 2^{-1} + 1 \times 2^{-2} + 0 \times 2^{-3} + 1 \times 2^{-4} = 16 + 8 + 0 + 2 + 0 + \frac{1}{2} + \frac{1}{4} + 0 + \frac{1}{16} \text{ (decimal)}$$

$$= 26 + \frac{1}{2} + \frac{1}{4} + \frac{1}{16} \text{ (decimal)}$$

$$= (26\frac{13}{6})_{10}$$