

Convert to base 5:

$$\begin{array}{r}
 5 \overline{) 21} \\
 \underline{5 \cdot 4} \phantom{1} \\
 0 \phantom{1} 4
 \end{array}
 \quad
 \begin{array}{r}
 .4375 \\
 \times 5 \\
 \hline
 2.1875 \\
 \times 5 \\
 \hline
 0.9375 \\
 \times 5 \\
 \hline
 4.6875 \\
 \times 5 \\
 \hline
 3.4375 \\
 \times 5 \\
 \hline
 2.1875 \text{ *repeats}
 \end{array}$$

$= (41.2043)_5$

### 1.3.3 Base $2^k$ Conversion

Each of the eight octal digits can be represented by a three-bit binary number. Similarly, each of the 16 hexadecimal digits can be represented by a four-bit binary number. In general, each digit of the base  $p$  number system, where  $p$  is an integral power  $k$  of 2, can be represented by a  $k$ -bit binary number.

In converting a base  $p$  number to base  $q$ , if  $p$  and  $q$  are both integral powers of 2, the base  $p$  number can first be converted to binary, and this in turn can be converted to base  $q$  by inspection. This conversion procedure is called the *base  $2^k$  conversion*.

#### Example 1.13

$$(42A56.F1)_{16} = (?)_8$$

$$p = 16 = 2^4, \quad q = 8 = 2^3$$

Therefore,

$$k_1 = 4, \quad k_2 = 3$$

1.3 Conversion 13

Start

$k_1 = 4$

Zero included  $\rightarrow$  0 0100 0010 1010 0101 0110 1111 0001 0

$k_2 = 3$

1 0 2 5 1 2 6 7 4 2

$= (1025126.742)_8$

#### Example 1.14

$$(AF5.2C)_{16} = (?)_4$$

base 16 =  $2^4$   $k_1 = 4$

base 4 =  $2^2$   $\therefore k_2 = 2$

2 2 3 3 1 1 0 2 3 0

$= (223311.0230)_4$

#### Example 1.15

$$(567.23)_8 = (?)_{16}$$

Zeros included 0 0 0 101 110 111 010 011 0 0

1 7 7 7 4 C

base 8  $\therefore k_1 = 3$

base 16  $\therefore k_2 = 4$

$= (177.4C)_{16}$

It is thus possible to represent binary numbers in a very compact form by using octal and hexadecimal systems. The conversion between these