here, the positions containing a 0 do not contribute to the sum. To convert a binary number into decimal, we can simply accumulate the weights As we can see from the polynomial expansion and summation shown

corresponding to each nonzero bit of the number.

combinations possible for any n are obtained by starting with n 0s and counting in binary until the number with n 1s is reached. A more mechanvalue from 000 (0 in decimal) to 111 (7 in decimal). In general, with n bits it is possible to generate 2" combinations of 0s and 1s, and these combina-Table 1.2 shows some binary numbers for various values of n. The  $2^n$ Similarly, with three bits we can derive 23, or 8, combinations ranging in tions when viewed as binary numbers range in value from 0 to  $(2^{n}-1)$ . derive 22, or 4, combinations: 00, 01, 10, and 11. The decimal values of Each bit can take either of the two values: 0 or 1. With two bits, we can these combinations (binary numbers) are 0, 1, 2, and 3, respectively. ical method of generating these combinations is described herein.

to row. Similarly, the value of the bit in position 1 alternates every two 0-alternates in value between 0 and 1 every row, as we move from row rows (i.e., two 0s followed by two 1s). In general, the value of the bit in Table 1.2, the value of the least significant bit (LSB)-i.e., bit position The first combination has n 0s and the last has n 1s. As we can see from

position 3 2 1 0 ← Bit 100 0110 0100 1010 n = 38 010 8 Table 1.2 Binary Numbers 8

position i alternates every 21 rows starting from 0s. This observation can be utilized in generating all the 2" combinations.

1.3 Conversion

## 1.2.2 Octal System

In this system, r = 8, and the allowed digits are 0, 1, 2, 3, 4, 5, 6, and 7. A typical number is shown in positional notation in the following example.

### Example 1.3

```
= 4 \times 8^3 + 5 \times 8^2 + 2 \times 8^1 + 6 \times 8^0 + 2 \times 8^{-1}
                                                                                                                                             = 2048 + 320 + 16 + 6 + # + # (decimal)
                                                                                                       +3 \times 8^{-2} polynomial form
                                   = 8^{3}8^{2}8^{1}8^{0}.8^{-1}8^{-2} weights
N = (4526.23)_{R}
                                                                                                                                                                          = (2390 \frac{12}{10})_{10}
```

# 1.2.3 Hexadecimal System

A, B, C, D, E, and F. Digits A through F correspond to decimal values 10 through 15, respectively. A typical number is shown in the following In this system, r = 16, and the allowed digits are 0, 1, 2, 3, 4, 5, 6, 7, 8, 9,

#### Example 1.4

$$N = (A \ 1 \ F \ . \ 1 \ C)_{16}$$

$$16^{2} 16^{1} 16^{0} . 16^{-1} 16^{-2} \text{ weights}$$

$$= A \times 16^{2} + 1 \times 16^{1} + F \times 16^{0} + 1 \times 16^{-1}$$

$$+ C \times 16^{-2} \text{ polynomial form}$$

$$= 10 \times 16^{2} + 1 \times 16^{1} + 15 \times 16^{0} + 1 \times 16^{-1}$$

$$+ 12 \times 16^{-2} \text{ (decimal)}$$

$$= (259) \frac{34}{2} \frac{3}{6} \frac{1}{10}$$

### 1.3 Conversion

using decimal arithmetic, as shown in Examples 1.1 through 1.4. When a decimal number is converted to any other system, the integer and fraction portions of the number are handled separately. The radix divide technique expand the given number as a polynomial and evaluate the polynomial is used to convert the integer portion, and the radix multiply technique is To convert numbers from a nondecimal system to decimal, we simply used for the fraction portion.