n bits in the divisor and 2*n* bits in the dividend. Let i = 0. the LSB of the divisor be denoted X. We will assume that there are

2. Compare X and Y. If $X \ge Y$, the quotient bit is 1: perform X - Y. If X < Y, the quotient bit is 0.

3. Set i = i + 1. If $i \ge n$, stop. Otherwise, shift Y one bit to the right

the divisor is 0, the procedure should be stopped since dividing by 0 integers. If the divisor is greater than the dividend, the quotient is 0, and if For the purposes of illustration, this procedure assumed the division of

tion and division that are more elegant than the ones described here.) the end of this chapter for books that describe procedures for multiplicamore complex operations in an economical manner. (See the references at in digital hardware technology, it is now possible to implement these and systems used such measures to reduce hardware costs. With the advances programmed to perform multiplication and division as well. Older digital hardware can perform shift, add, and subtract operations, it can be tions can be reduced to repeated shift and addition (or subtraction). If the As we can see from these examples, multiplication and division opera-

the vacant MSD position) generally is equivalent to dividing the number number by r. Shifting the number right by one position (inserting a 0 into inserting a 0 into the vacant LSD position) is equivalent to multiplying the Shifting Generally, shifting a base r number left by one position (and

right shift divides the number by 2, as shown in Example 1.21. In binary system, each left shift multiplies the number by 2, and each

Example 1.21

			N + 2	2 * Z	<
		Discard	Insert \ 000101.11[1]	10111.110 VInsert	Binary
retained.)	bit accuracy is	53 (Inaccurate,	231	112	Decimal

bits shifted out of the LSB position during a right shift are discarded, the and the 1 shifted out of the MSB position cannot be discarded. If nonzero number larger than the magnitude that can be accommodated in n bits-If the MSB of an n-bit number is not 0, shifting it left would result in a

accuracy is lost. Later in this chapter, we will discuss shifting in further

1.4.2 Octal Arithmetic

shown in the scratchpad. similarity to decimal arithmetic. (Table 1.4 can be used to look up the the result is converted into octal, before proceeding to the next stage, as following examples. The operation is first performed in decimal and then result at each stage in the arithmetic.) An alternate method is used in the ples that follow illustrate the four arithmetic operations in octal and their Table 1.4 shows the octal addition and multiplication tables. The exam-

Table 1.4 Octal Arithmetic

B	12	18					B] 2		10	
76543210	×	N	1	1 0		d. 6							(E)	L
	В									. 0	0		a) Addition	I
0000000	0	(b) Multiplication	-	0	· U	4 1	· w	2		0	0		on	I
765432-0	-	On	5	7	6	S	4	w	2	-	-			
0 2 4 4 10 11 11 16	2		=	10	7	6	S	4	w	2	2			
0 6 11 14 17 22 23	ω _A		12	=	10	7	6	S	4	w	w	A		
0 10 14 20 24 30	4		13	12	=	10	7	6	(A	4	4			22
0 5 12 17 17 24 31 36	5	_	4	13	12	=	<u>-</u>	7	0	(A	C,			
0 0 14 22 30 36 44	6		15	4	<u></u>	12	= ;	.	7	6	6			
61 23 43 43 43 43 43 43 43 43 43 43 43 43 43	7		16	<u>.</u>	<u>.</u>	ا بر ا	5 :	=	5,		7			