

The following equation describes steady state heat conduction with generation in two dimensions after non-dimensionalization:

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = q/k$$

where q and k are constants for heat generation and thermal conductivity. The system has the following boundary conditions:

$$T(x=0,y)=0$$

$$T(x=1,y)=1$$

$$\frac{\partial T}{\partial y} = 0 \text{ at } y=0$$

$$\frac{\partial T}{\partial y} = 0 \text{ at } y=1$$

Write a program that will calculate the Temperature profile using the finite difference method. Use central finite difference to express the second order derivatives. Try the following iterative solution methods Jacobian, Gauss-Seidal, SOR with different relaxation parameters $0 < \omega < 2$. Try meshes with 9x9, 17x17, 33x33 grid points for $q/k=100$. Plot the convergence history for the different iterative methods on the three different grids.