

# CSE 423 - Computer Graphics

## 2D Transformation



# Two dimensional transformation

- Translation



- Scaling

- Rotation

# Translation

- Moving object from one position to another position
- Change the position of objects
- Parameters for translation are:
  - $t_x$  - if we move the position with respect to  $x$  – axis
  - $t_y$  - If we move the position with respect to  $y$  – axis



# Calculate Translation

If we have –

- Original point is  $P(x, y)$
- Translated parameters are  $t_x$  and  $t_y$
- Object translated point is  $P'(x', y')$

## Matrix representation

$$[x' y'] = [x y] + [t_x t_y]$$

Or,

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$$

Then,

Translated  $x$  – axis is measured by  $x' = t_x + x$

Translated  $y$  – axis is measured by  $y' = t_y + y$

# Scaling

- Resizing the object
- Do maximizing and minimizing the object
- Parameters for scaling are:
  - $s_x$  - if we move the position with respect to  $x$  – axis
  - $s_y$  - If we move the position with respect to  $y$  – axis

Property	Result
In between 0 and 1	Point is closer to origin and size will be decreased
$s_x$ and $s_y$ are greater than 1	Point is away from origin and size will be increase
$s_x = s_y$	Uniformly increases or decreases

# Calculate Scaling

If we have –

- Original point is  $P(x, y)$
- Scaled parameters are  $s_x$  and  $s_y$
- Object scaled point is  $P'(x', y')$

Then,

Scaled  $x$  – axis is measured by  $x' = s_x \cdot x$

Scaled  $y$  – axis is measured by  $y' = s_y \cdot y$

## Matrix representation

$$\begin{bmatrix} x' & y' \end{bmatrix} = \begin{bmatrix} x & y \end{bmatrix} \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix}$$

# Rotation

- Rotate the object with a specific angle,  $\theta$
- Two types of rotation
  - Clockwise direction and
  - Anti clockwise direction

## Clockwise

$$[x' \quad y'] = [x \quad y] \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$$

Or,

$$x' = x \cos \theta + y \sin \theta$$

$$y' = y \cos \theta - x \sin \theta$$

## AntiClockwise

$$[x' \quad y'] = [x \quad y] \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix}$$

Or,

$$x' = x \cos \theta - y \sin \theta$$

$$y' = x \sin \theta + y \cos \theta$$

# Problem

**Q: (a)** Find the matrix that represents the rotation of an object by  $30^\circ$  by the origin.

**(b)** What's the new coordinate of the point  $P(2, -4)$  after the rotation?

## Solution

(a) The matrix  $R_{30^\circ} = \begin{bmatrix} \cos 30^\circ & -\sin 30^\circ \\ \sin 30^\circ & \cos 30^\circ \end{bmatrix}$

(b) New rotated points

$$[x' \quad y'] = [2 \quad -4] \begin{bmatrix} \cos 30^\circ & -\sin 30^\circ \\ \sin 30^\circ & \cos 30^\circ \end{bmatrix}$$



# Problem

**Q:** Transform  $(2, 1)$ ,  $(3, 4)$  and  $(5, 3)$  points using translation and scaling factors 6 along  $x$ -axis and 9 along  $y$ -axis.

**Solution:**

Translation for coordinates  $A(2, 1)$

The new coordinate will be  $A'(x', y')$

Translation factors are  $t_x = 6$  and  $t_y = 9$

Therefore,

$$x' = 6 + 2 = 8$$

$$y' = 9 + 1 = 10$$

Thus, the new coordinate for the point  $A(2, 1)$  is  $A'(8, 10)$

**Complete rest part of the problem yourself**

