Model training

The split sample approach was employed; simulated data was split randomly into two complementary parts, a training set (50%) and a test set (50%) under the same event/censoring proportions. To tune the hyperparameters of ML algorithms, 5-fold cross validation was performed on the training part of a simulated dataset with 1000 synthetic patients according to the censoring rate of interest. Training data was divided into 5 folds. Each time 4 folds were used to train a model and the remaining fold was used to validate its performance and the procedure was repeated for all combination of folds. Tuning of the hyper-parameters was done using grid search. Performance of final models was assessed on the test sets (of each simulated dataset). Standard software of implementation was not available in R. Therefore, data transformation to longitudinal format was required. The time interval was added next to the other input features to estimate conditional hazard probabilities. Variables were presented in dummy coding - categorical variables as indicators and continuous variables standardized.

For PLANN original, the nnet package [1] of the R programming language was used. The choice of hyperparameters and their range (for the grid search) were based on reasoning from the original article by Biganzoli *et al.* [2]. Optimization was done via the BFGS method (quasi-Newton algorithm) of optim R function. Parameters tuned were i) size the number of nodes (units) in the hidden layer which determines the number of weights (values $2, 3, \cdots, 8$) and ii) decay a regularization technique applied to the error (loss) function which penalizes large weight values to avoid overfitting as $E^* = E + \lambda \sum w^2$ (values 0.001, 0.005, 0.01, 0.05, 0.1, 0.2, and 0.3). Having 6 inputs in total (5 prognostic variable levels in dummy coding + time interval variable) the optimal value for size is somewhere in the range 2-8. The best combination of the parameters on the training data was determined based on either the C-index [3] or the Integrated Brier Score (IBS) at 5 years (time-point of major clinical interest) - a measure that summarises the time-dependent Brier score estimated at different time points until 5 years in one value [4].

For PLANN extended, model tuning was performed in R with the package keras [5] which is an interface for the original state-of-the-art neural network library written in Python programming language. keras runs on top of tensorflow [6] which is a symbolic maths library used for ML. Two of the main advantages of this package are that it allows the use of distributed training of deep learning models on clusters of graphic processing units and the specification of many building blocks such as activation functions, layers, objectives, optimisers. Optimization was done with the stochastic gradient descent algorithm of keras. To narrow down the grid of point combinations, search for training data was performed on a 5-D space of some of the most fundamental hyper-parameters. Those are nodesize the size of nodes in the hidden layer (values 1, 4, 7, 10, 13, or 16), dropout rate that randomly selects the amount of nodes to be dropped-out with a given probability (values 0.1, 0.2 or 0.4), learning rate which is the step size of weight iteration (values 0.1, 0.2 or 0.4), momentum which helps to accelerate gradient vectors (values 0.8 or 0.9) and weak class weight that defines the weight of minority class (values 0.95, 1 or 1.05).

Nodesize defines the number of weights of the network and consequently the amount of its complexity. Having 13 inputs in total for the main analyses (5 prognostic variable levels in dummy coding +

8 yearly time intervals), the optimal nodesize was somewhere in the range 1 - 16. For supplementary analyses with 3-monthly or 6-monthly intervals, the optimal nodesize was in the range 10-40 (5 variables + 32 intervals) or 6-26 (5 variables + 16 intervals), respectively. Therefore, nodesize values were adjusted accordingly. Dropout rate is a technique used to control over-fitting [7]. Regarding the rest of the parameters, learning rate adjusts how fast the stochastic gradient descent iterative method uses stochastic approximation. momentum can accelerate the stochastic gradient vectors in the right directions and weak class weight can be used for re-weighting unbalanced classes (a small re-weighting adjustment was used). Additionally, we used early stopping to prevent overfitting (5 epochs tolerance). We specified 50 training epochs (an arbitrary large number) and terminated training once the performance stopped improving on the validation set. The best combinations of hyper-parameters were selected based on either the C-index or the Integrated Brier Score (IBS) at 5 years. Overall, training PLANN extended was more computationally intensive than PLANN original because of the increased number of hyperparameters and input features (the L non-overlapping intervals were treated as L separate variables). Moreover, please note that the implementation of PLANN extended with modern software does not necessarily imply a better performance than PLANN original regarding the numerical optimization.

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