

Statistics 305: Introduction to Biostatistical Methods for Health Sciences

Summary of Review Material

Jinko Graham

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Ch8-10: Inference of a Population Mean

- ▶ A statistic is computed from data on a sample; e.g. \bar{X} , the sample average.
- ▶ By contrast, a parameter is a population quantity; e.g. μ , the population average.
- ▶ Statistical inference: Learning about parameters from statistics that are subject to random variation.
 - ▶ e.g. Hypothesize about parameters such as μ .
 - ▶ Test $H_0 : \mu = 0$ vs. $H_a : \mu \neq 0$.

- ▶ Key point: Even though the population mean, μ , and the population SD, σ , are unknown, we know the (approximate) distribution of the pivotal quantity

$$\frac{\bar{X} - \mu}{s/\sqrt{n}},$$

regardless of the shape of the population distribution for X .

- ▶ This result relies on the CLT, which tells us that (large) sample averages such as \bar{X} are approximately normally distributed.
- ▶ Many of the statistics we will study are based on averages, so inference of a population mean is a useful template.
- ▶ Knowing the distribution of the pivotal quantity allows us to construct confidence intervals, calculate p -values, test statistical hypotheses, calculate power, etc.

Ch11: Inference for a Difference of Population Means

- ▶ Inference for the difference between two population means is based on either the pivotal quantity Z (SDs known) or T (SDs unknown).
- ▶ CIs are of the form estimate \pm margin of error
 - ▶ the margin of error is a critical value (z^* for Z , t^* for T) times the SE for the estimate.
- ▶ To test the null hypothesis $H_0 : \mu_1 - \mu_2 = 0$ against an alternative H_a we compute a test statistic t (or z if SDs known) from our sample of data and use it to get the p -value.
 - ▶ can compare p -value to a significance level α to obtain a test of H_0 against H_a .
- ▶ Inference is considered reliable when the parent populations are normal, or when rules-of-thumb about sample sizes are satisfied.

Ch14: Inference for Proportions

- ▶ Inference for the difference $p_1 - p_2$ between two population proportions is based on a pivotal quantity, also called Z .
- ▶ CIs are estimate \pm margin of error, where
 - ▶ estimate is the difference between sample means, and
 - ▶ margin of error is a critical value (z^*) times the SE of the difference in sample proportions.
- ▶ To test the null hypothesis $H_0 : p_1 - p_2 = 0$ against an alternative H_a we calculate a test statistic, z , from our sample of data and use it to get the p -value.
 - ▶ The p -value is the chance of seeing a value of the test statistic as or more extreme than the value that was observed, under H_0 .
 - ▶ Compare the p -value to a significance level α to obtain a test of H_0 against H_a .
- ▶ Inference is considered reliable when:
 - ▶ the population is at least $10\times$ larger than the size of the sample
 - ▶ there are sufficient numbers of successes and failures in each sample.

Ch6: Probability

- ▶ Discussed the basic definitions and rules of probability, including the definition of conditional probability.
- ▶ Use Bayes' Theorem to relate $P(A | B)$ to
 - ▶ $P(B | A)$, $P(A)$ and $P(B)$.
- ▶ Public-health and medical practitioners work with many conditional probabilities every day; e.g.,
 - ▶ diagnostic test sensitivity and specificity
 - ▶ relative risks and odds ratios
- ▶ Case-control data
 - ▶ Disease probabilities or risks in the exposure groups cannot be estimated, owing to oversampling of the cases in the study design.
 - ▶ However, exposure probabilities in the disease groups can be estimated, allowing us to estimate odds-ratios.
 - ▶ For a rare disease, the odds-ratio approximates the relative risk.