



Giovanni Bernardi and Hugo Férée

Academic background

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Studies in « Mathématiques Fondamentales » Université Paris Cité



⇒ Algebra, analysis, topology, probability, ...

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• Studies in « Mathématiques Fondamentales »



⇒ Algebra, analysis, topology, probability, ...

Studies in «Logique Mathématique et Fondements en Informatique »



>> Proof theory, calculability, formal proof, ...

Main scientific interest < but not only >

Quantum Computing and Quantum Information

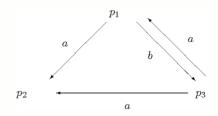


• Lambda Calculus

Process Calculus

• COQ

 $M := \lambda x.M \mid M_1 M_2 \mid x$



```
1   Inductive nat : Type :=
2   | 0 : nat
3   | S : nat -> nat.
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Main achievements

Elaboration of a quantum lambda calculus with measurement, normalization and confluence
 < supervised by Claudia Faggian and Benoît Valiron >



Formalization of CCS with Value Passing and Sequenciation in COQ





- + the Harmony Lemma in COQ
- Supervised by Giovanni Bernardi and Hugo Férée>
- Paper accepted at CSL 2025 :
 - « A Rewriting Theory for Quantum λ -Calculus » $\exists \mathbf{r}$
 - <with Claudia Faggian and Benoît Valiron>

What's the plan?

Study linear quantum CCS

<from Lorenzo Ceragioli, Fabio Gadducci, Giuseppe Lomurno and Gabriele Tedesch, 2023>

$$\frac{e \Downarrow tt}{\left\langle \rho, \text{if } e \text{ then } P \text{ else } Q \right\rangle \xrightarrow{\tau} \overline{\left\langle \rho, P \right\rangle}} \text{ ITET} \qquad \frac{e \Downarrow ff}{\left\langle \rho, \text{if } e \text{ then } P \text{ else } Q \right\rangle \xrightarrow{\tau} \overline{\left\langle \rho, Q \right\rangle}} \text{ ITEF}$$

$$\frac{e \Downarrow v}{\left\langle \rho, \tau.P \right\rangle \xrightarrow{\tau} \overline{\left\langle \rho, P \right\rangle}} \text{ TAU} \qquad \frac{e \Downarrow v}{\left\langle \rho, c!e.P \right\rangle} \text{ SEND} \qquad \frac{v \in \Sigma_{\rho}}{\left\langle \rho, c?x.P \right\rangle \xrightarrow{c?v} \overline{\left\langle \rho, P[v/x] \right\rangle}} \text{ RECEIVE}$$

$$\frac{\left\langle \rho, P \right\rangle \xrightarrow{\mu} \Delta}{\left\langle \rho, P + Q \right\rangle \xrightarrow{\mu} \Delta} \text{ SUML} \qquad \frac{\left\langle \rho, Q \right\rangle \xrightarrow{\mu} \Delta}{\left\langle \rho, P + Q \right\rangle \xrightarrow{\mu} \Delta} \text{ SUMR} \qquad \frac{\left\langle \rho, P \right\rangle \xrightarrow{\mu} \Delta}{\left\langle \rho, P \setminus c \right\rangle \xrightarrow{\mu} \Delta \setminus c} \text{ RESTRICT}$$

$$\frac{\rho_m = (M_m)_{\bar{q}}(\rho) \quad p_m = \text{tr}(\rho_m)}{\left\langle \rho, P \mid Q \right\rangle \xrightarrow{\tau} \overline{\left\langle E_{\bar{q}}(\rho), P \right\rangle}} \text{ QMEAS}$$

$$\frac{\left\langle \rho, P \right\rangle \xrightarrow{\mu} \Delta \quad \mu = c?v \Rightarrow v \notin \Sigma_Q}{\left\langle \rho, P \mid Q \right\rangle} \text{ PARL} \qquad \frac{\left\langle \rho, P \right\rangle \xrightarrow{c!v} \overline{\left\langle \rho, P' \right\rangle} \quad \left\langle \rho, Q \right\rangle \xrightarrow{c?v} \overline{\left\langle \rho, Q' \right\rangle}}{\left\langle \rho, P \mid Q \right\rangle \xrightarrow{\tau} \overline{\left\langle \rho, P' \mid Q' \right\rangle}} \text{ SYNL}$$

$$\frac{\left\langle \rho, Q \right\rangle \xrightarrow{\mu} \Delta \quad \mu = c?v \Rightarrow v \notin \Sigma_P}{\left\langle \rho, P \mid Q \right\rangle} \text{ PARR}} \qquad \frac{\left\langle \rho, P \right\rangle \xrightarrow{c!v} \overline{\left\langle \rho, P' \right\rangle} \quad \left\langle \rho, P \mid Q \right\rangle \xrightarrow{\tau} \overline{\left\langle \rho, Q' \right\rangle}}}{\left\langle \rho, P \mid Q \right\rangle \xrightarrow{\tau} \overline{\left\langle \rho, P' \mid Q' \right\rangle}} \text{ SYNR}$$



What's the plan?

• Study the MUST preorder with his characterization

Strom Giovanni Bernardi, Ilaria Castellani, Paul Laforgue, Léo Stefanesco, 2024

Definition We write

- $p \preccurlyeq_{\mathsf{cnv}} q \ whenever \ \forall s \in \mathsf{Act}^{\star}. \ p \Downarrow_{A} s \ implies \ q \Downarrow_{B} s,$
- $p \preccurlyeq_{\mathsf{AS}} q \text{ whenever } p \preccurlyeq_{\mathsf{cnv}} q \text{ and } p \preccurlyeq_{\mathsf{acc}} q.$

Theorem For every \mathcal{L}_A , $\mathcal{L}_B \in OF$ and $p \in A, q \in B$, $p \sqsubseteq_{MUST} q$ if and only if $FW(p) \preccurlyeq_{AS} FW(q)$.





What's the plan?

Supervised by Giovanni Bernardi and Hugo Férée:

- Study linear quantum CCS with a testing theory
 from Lorenzo Ceragioli, Fabio Gadducci, Giuseppe Lomurno and Gabriele Tedesch, 2023>
- Study the MUST preorder with his characterization
 <from Giovanni Bernardi, Ilaria Castellani, Paul Laforgue, Léo Stefanesco, 2024>
- Combine both to get wonderfull properties and/or new theories
- Formalize the results in COQ

