

Validating a Titan Atmosphere Model Simulation with Specular Reflection Against Known Methane Lakes

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Others... (Shannon?)

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Abstract

**ABSTRACTION: this will be done last, as we need to know
the end from the beginning to properly do it.**

**[NOTE: Tense is exceptionally strange, go over and make sure it
matches at the end of writing this paper]**

1 Introduction

Titan’s surface is one of only two in the Solar System with bodies of stable liquid, the other being Earth’s (Hayes 2016). Unlike the seas we are familiar with, the ones on Titan are made primarily of liquid methane (Mastrogiuseppe et al. 2016). These seas pose a challenge to radiative transfer models of Titan’s atmosphere, for they exhibit behavior markedly different from conventional terrain. The vast majority of terrain, even extremely high albedo terrain, such as that on Enceladus (Li et al. 2023), reflects light in a diffuse or nearly “lambertian” manner. Liquids, meanwhile, arrange themselves with such a smooth surface that they can act as mirrors, producing bright “specular” reflections in a preferred direction. Direct specular reflections from the sun are a telltale sign that part of Titan’s surface is liquid, as no lambertian surface could ever produce them (Stephan et al. 2010). There are, however, indirect specular reflections as well, produced when sunlight scatters off somewhere in the atmosphere and proceeds to strike a specular surface at the appropriate angle (Vixie et al. 2015). Thus, specular reflections can alter the observed character of a surface dramatically from all angles when an atmosphere is present, which is the case on Titan.

Unfortunately, current radiative transfer models of Titan’s atmosphere assume a rough, lambertian surface, perhaps with variable albedo (Griffith et al. 2012, Xu et al. 2013, Corlies et al. 2021, Rannou et al. 2021, Es-sayeh et al.

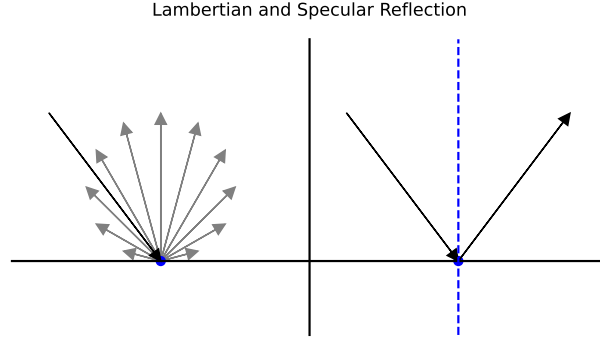


Figure 1: Lambertian and specular reflection diagram highlighting the difference between the two. Lambertian is left, specular is right. The ideal cases are pictured, real surfaces will deviate or even be a combination of the two. Our code assumes ideal behavior.

2023). Yet, the difference between specular and lambertian surfaces in radiative transfer is significant. In order to properly model Titan, this difference needs to be accounted for; not only to ensure that our understanding of Titan’s surface-atmosphere interaction is accurate, but also to assist in identifying unknown potentially-liquid terrain on Titan that has never had a favorable viewing geometry for direct specular reflections.

In this paper, we demonstrate a specular reflection routine for SRTC++ (Spherical Radiative Transfer in C++), a radiative transfer code tailored to model Titan in the infrared wavelengths available to Cassini’s VIMS (Visual and Infrared Mapping Spectrometer) instrument (Barnes, MacKenzie, et al. 2018). The new routine enables accurate simulation of liquid surfaces on Titan—in fact, as the properties of methane are well known, the accuracy for liquid surfaces is greater than that of the poorly-constrained land of Titan (Trainer et al. 2018). To demonstrate this routine, we begin with **Methods**, describing in brief the code and model we chose. **Results** examines the direct output of the completed simulation, and **Validation** compares those results to known lakes and seas on Titan. The implications of our simulation are considered in the **Discussion** before we end with a **Summary and Conclusion**.

[NOTE: Be sure to redo this last introduction paragraph when the paper is done.]

2 Methods

The primary code for our simulation, SRTC++, is described in detail elsewhere (Barnes, MacKenzie, et al. 2018). However, in order to describe the new rou-

tine, a brief overview is required. SRTC++ simulates radiative transfer in a Monte Carlo fashion, making it nondeterministic. Individual “photon packets” are launched toward Titan, with the results of every scattering event in the atmosphere determined randomly. The detector objects in SRTC++ do not detect these “photon packets”, but rather the result of their scattering events. Each scattering event has a certain probability of going any individual direction; SRTC++ finds the directions that go to the detectors and determines the intensity the detector would see from that event. Often, millions of “photon packets” are run for a single simulation, with each scattering event updating the detectors until a full picture of Titan forms at each detector.

In SRTC++, the ground is normally modeled as just another scattering event, just one with different probabilities than an atmospheric scatter (Barnes, MacKenzie, et al. 2018). This works well for rough, lambertian surfaces, where the distribution is quite random at macro scales. However, specular surfaces do not fit this mold, as light reflecting off of them follows a deterministic path. The new routine takes advantage of this, calculating two different paths to the detector from every scattering event; one that goes directly to the scatter, and one that bounces off a specular surface first. This does leave a hole in the simulation: “photon packets” that pass through the atmosphere and strike the surface without scattering are missed. Fortunately, these missed packets would be at or near the point where the specular reflection is brightest and nowhere else, so minimal information about viewing geometry is lost. Furthermore, if recorded, those points would far outshine anything else in the resulting images, making them difficult to parse; just like real images of direct specular reflections on Titan, which are quite saturated (Barnes, Clark, et al. 2013).

SRTC++ Scatter With Specular Reflection

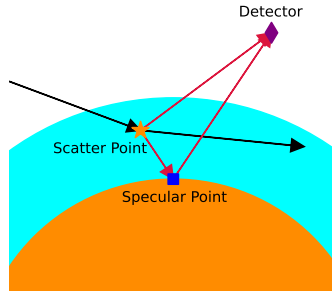


Figure 2: SRTC++ operation with specular point. Photon packet comes in from the left on a black arrow, hitting the scatter point. The code determines both paths to the detector, shown with red arrows. One path is direct, the other reflects off the specular point on the surface. The photon packet itself will continue along the black arrow, potentially to scatter again.

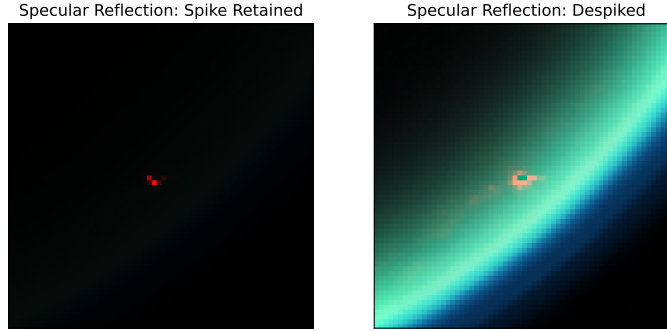


Figure 3: Cassini VIMS observation of specular reflection. CM_1721848119_1 on flyby T85. RGB map is to 5, 2, and $1.3\mu\text{m}$ without any artificial scaling of individual colors. Left: resulting image retaining the spike values as 1, the maximum. Right: resulting image with trimmed spike values, set to 1. The specular reflection’s spike is so dramatic it not only drowns out all other wavelengths, but it also outshines secondary reflections in the same wavelength, which contain valuable information. The hole in the center of the reflection is due to saturation of the VIMS instrument, indicating the real intensity of the direct specular reflection is beyond what we show here.

The angle of the second “photon packet” path is determined both by the curved geometry of Titan’s surface and the index of refraction of liquid methane. This new path can be ignored if the surface doesn’t have liquid at the required location, however we will not make use of this ability in this paper as our chosen model is a global methane ocean. This model does not accurately represent Titan, but it does not have to: when we model a global methane ocean, we see the surface from almost every possible viewing geometry. This will enable us to compare the specular results to a lambertian simulation, quantifying the differences, which can in turn be used to characterize real surface observations.

Titan is known to have at least some ethane in its seas (Mastrogiuseppe et al. 2016) but the indices of refraction of liquid methane and ethane are extremely similar (Kanjanasakul et al. 2020). We ran a simulation with ethane’s index and noticed no clear differences between it and the methane result, qualitatively justifying the use of a pure methane ocean model. This also justifies not modeling the change of index of refraction with wavelength and our using a value that, strictly speaking, is slightly too low for the environmental conditions on Titan (Martonchik and Orton 1994, Jennings et al. 2019). For a quantitative justification, we used the Fresnel equations to find the average reflection coefficient for water, ethane, and methane. Two methane values were examined, the one used in the code, and one sampled for more realistic Titan environmental conditions (Martonchik and Orton 1994). The results of this are seen in Figure 4. As

the maximum variation between the two values of methane is 2%, we deem the variation negligible. This also justifies not giving each tested wavelength of light a different index of refraction.

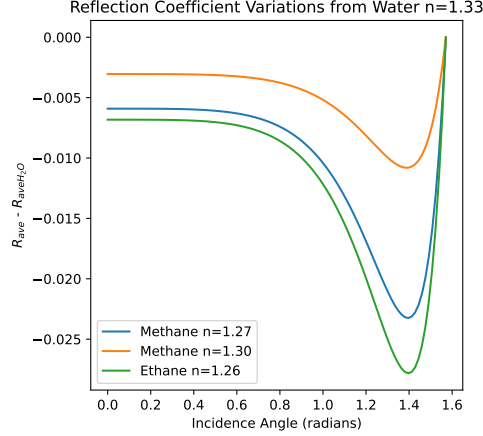


Figure 4: Average reflection coefficient differences from water with a 1.33 index of refraction. We do not plot the direct reflection coefficients since the differences between the various materials are largely indistinguishable. Methane 1.27 was used in the code, while methane 1.30 is more realistic. Note that the differences between the two are, across most angles, less than a percent, with a maximum difference of 2%. The mixture of ethane in Titan’s lakes and seas will likely lower this difference even further. At large angles the difference approaches zero as all reflection coefficients approach unity.

[NOTE: Perhaps all this justification would be better placed in an Appendix?]

No model of Titan is sufficient without an atmosphere. SRTC++ primarily uses Tomasko et al. 2008 for Titan’s atmosphere, and here we add corrections from Hirtzig et al. 2013 and Rodriguez et al. 2018. The version of SRTC++ used does not account for atmospheric absorption, but such effects are expected to be limited at the wavelengths we are simulating (Es-sayeh et al. 2023).

We compare our results lambertian simulation data taken from (Barnes, in preparation), also created using SRTC++. We made sure that the input parameters matched between the two simulations. There are 72 detectors placed every 5° around Titan’s equator at a distance of 1×10^6 km. Each detector sees 3500 km out from Titan’s center, chosen to be significantly larger than Titan’s 2575 km radius to avoid any edge artifacts.

Each simulation is run at eight different wavelengths that correspond to the eight atmospheric windows, areas of the electromagnetic spectrum that pierce through Titan’s atmosphere and allow characterization of the surface (Barnes, Brown, Soderblom, et al. 2007). Simulations could be run at other wavelengths, but they would mask any surface signals and be of minimal use for our current

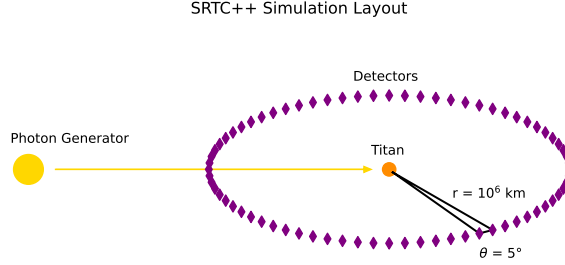


Figure 5: Layout of our SRTC++ simulations, identical for both the specular and lambertian case. Distances not to scale. Detectors all equidistant from Titan and angular separation is the same for each one. The yellow arrow represents “photon packets” being shot at Titan. Note that it does not interact with the detector it passes through.

purposes.

3 Results

In the above figure we have collected the results at 5, 2, and $1.3 \mu\text{m}$ mapped to red, green, and blue respectively in the same manner as Barnes, MacKenzie, et al. 2018’s “surface spectral diversity” color scheme. The most obvious distinction between real images of Titan and this simulation is the sharp, blue color. This is to be expected: pure methane’s index of refraction does not vary significantly through the tested wavelengths (Martonchik and Orton 1994), and so the atmosphere alone determines the color dependence. Since smaller wavelengths scatter more on Titan (Es-sayeh et al. 2023) the image appears bluer. This happens even in the lambertian simulation (Barnes, in preparation). **[WHY?? Not because we assume the surface is white, we apply different albedos to each one. Blue has a larger albedo than green, so blue will dominate, but why are those the values we’re using?]** However, while we expect the solid surface of Titan to be different from simulation, we do not expect that to be the case with pure liquid methane, so “relative blueness” is a possible identifier of surface liquid.

The other primary features of the simulation are expected. The bright central area is near the specular point, caused by “photon packets” that nearly passed through the atmosphere unhindered, and so did not get scattered far from the ideal path. The circular shape of this feature flattens as it approaches the limb of Titan, which is what should occur on a slanted reflective surface. The limb brightening effect is due to reflection coefficients rising as we approach 120° as seen in 4. Toward the terminator, Titan appears greener because shorter wavelengths scatter away more readily, leaving only green and red behind. The

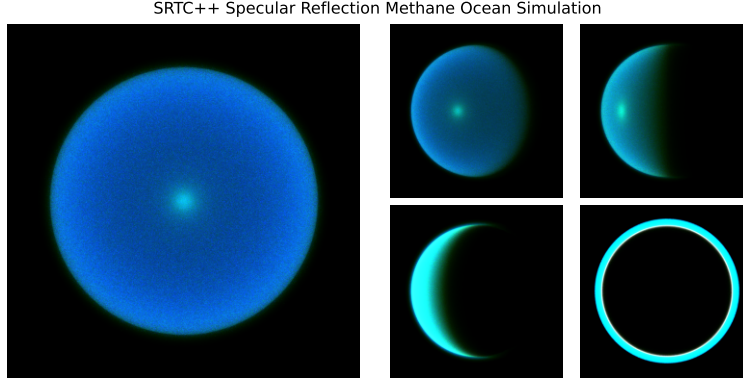


Figure 6: Simulation results for a methane ocean Titan, colored with 5, 2 and $1.3\mu\text{m}$ mapped to red, green, and blue respectively. Left image is viewed at 0° from the incidence angle. Right four images are at 35° , 90° , 120° , and 180° in left to right then top to bottom order. **[An animating version of the figure will exist in places that support it. The large left panel will hold the animating image, the right panels will remain static for comparisons]**

terminator sees no redness increase because the $5\mu\text{m}$ window is so much dimmer than the others it doesn't matter. **[Make sure to check this isn't due to titancolor2 not scaling it properly]**

The simulation also produces “eclipse views” of Titan backlit by the sun, but those show the atmosphere and not the surface, and so are beyond the scope of this paper. There is certainly worthwhile information to be gleaned here at a later date, though.

In truth, all eight of Titan's near-infrared atmospheric windows were simulated, not just the three used to create the color figures. 7 and 8 show a selection of monochromatic images for all the simulated wavelengths.

In general, shorter wavelengths are more intense than longer ones, giving the overall “blueness” noted in the color images. Shorter wavelengths are also noisier. Both of these facts have the same explanation: short wavelengths scatter more readily, making photons more likely to contribute to detectors while also scrambling information due to multiple scattering events on a single “photon packet.” This is also why the near-specular area is sharp in longer wavelengths, but blurred out in shorter.

The brightness pattern is not followed perfectly: $5\mu\text{m}$ is slightly brighter than $2.8\mu\text{m}$ while also having a fuzzier near-specular area. This is an atmospheric effect, as all wavelengths are treated the same in this model. At $5\mu\text{m}$ the atmosphere is known to have a very low optical depth; significantly lower than the other windows (Es-sayeh et al. 2023), but this should make it dimmer rather than brighter. The true difference lies in the difference in the phase function between $5\mu\text{m}$ and the other windows: both are forward scattering phase

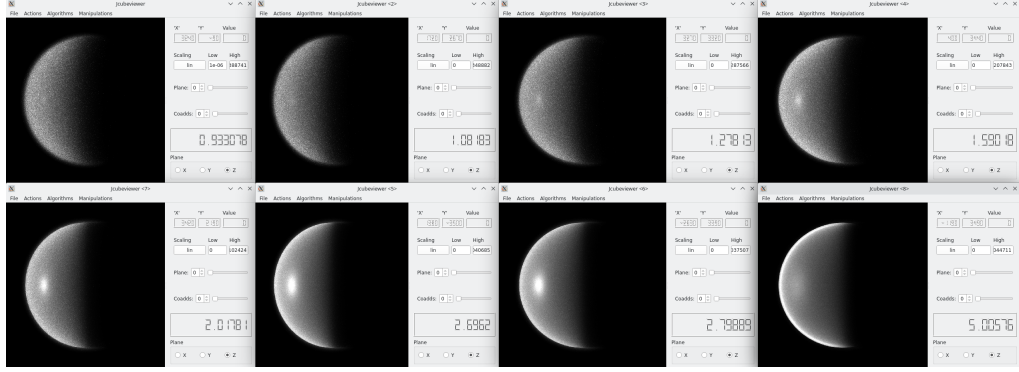


Figure 7: **PLACEHOLDER:** currently don't have access to the program to reprocess this

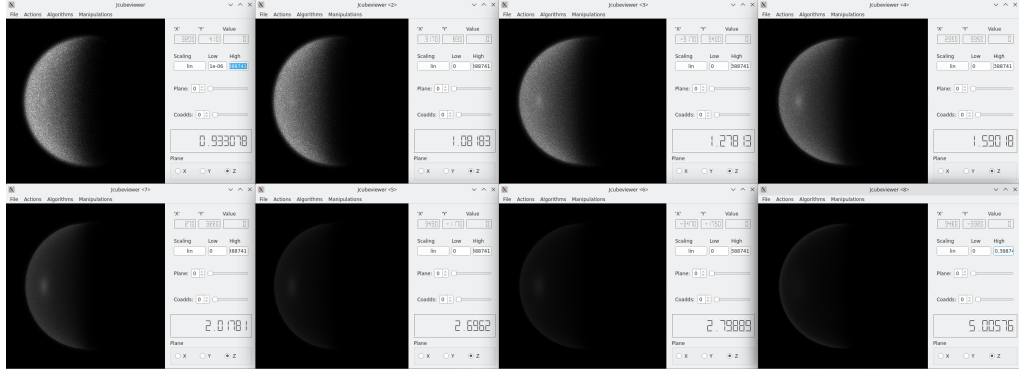


Figure 8: **PLACEHOLDER:** currently don't have access to the program to reprocess this

functions, but $5\text{ }\mu\text{m}$ is less so (Tomasko et al. 2008). This will force the light to take more distributed and indirect paths. Most visible paths in our images are from such viewing geometries, so with a significant difference in phase function, the overall appearance of the disc will increase in brightness. A side effect of this is that the viewing geometries that are close to direct forward scattering are going to be more diffuse than expected, which explains why the near-specular area at $5\text{ }\mu\text{m}$ isn't as bright or sharp as $2.8\text{ }\mu\text{m}$.

Direct comparisons between the specular and lambertian simulations reveal a few key differences. First, the lambertian simulation is brighter than the specular everywhere except near the specular point **[Check with actual intensity values to be sure]**. This was expected, each simulation's Titan is receiving the same amount of energy, but the specular Titan will preferentially focus its light in a single direction, while the lambertian will not, leading the specular point and areas near it to be bright in the specular simulation while everywhere

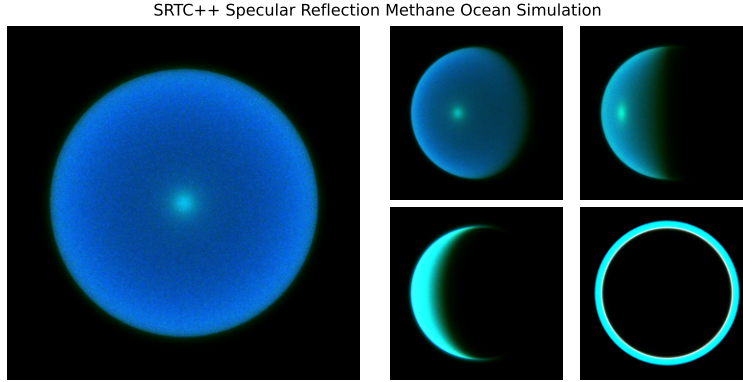


Figure 9: [FIGURE: show the lambertian version of the simulation, with the same structure as the specular figure above. Just need access to the data... which I don't have right now... yaaaay... have a repeat of the specular figure for now]

else is relatively dim.

Both simulations exhibit a “blue” color, though it is noticeably more intense for the specular case than the lambertian. [Hang on, WHY is it more intense? Might it have something to do with the abledos? Of course, we have to actually explain why the lambertian is blue first...]

The lambertian simulation also lacks the stark limb brightening effect at low phase as it has no index of refraction. Some brightening can still be seen at other angles, but this is due to the atmosphere, and the specular simulation also showcases this increasing limb brightening with higher phase.

So far, we have only considered qualitative differences between the specular and lambertian geometries. For quantitative analysis, we chose to deconstruct the simulation data by viewing geometry. We took every single simulation pixel that showed the surface (as opposed to the atmosphere) and determined the incidence, emission, and azimuth angles. Any viewing geometries that were hit more than once were added together and then averaged. The result was a database in incidence, emission, azimuth, and wavelength that showed the intensity [I have GOT to nail down what the exact words and units are that we're simulating] at every possible geometry. We then subtracted the lambertian value from the specular one.

The broad behavior of the above figure is expected: we see that lambertian dominates in the negative (blue) areas, which take up most of the viewing geometries, matching what we saw visually. Specular dominantes in the positive (red) areas, which cluster around high emission and incidence angles and places where emission and incidence match. [Wait, hold on, investigate: the high angles of emission/incidence are due to the index of refraction. The actual specular point isn't generally there! Look closer.]. Notably,

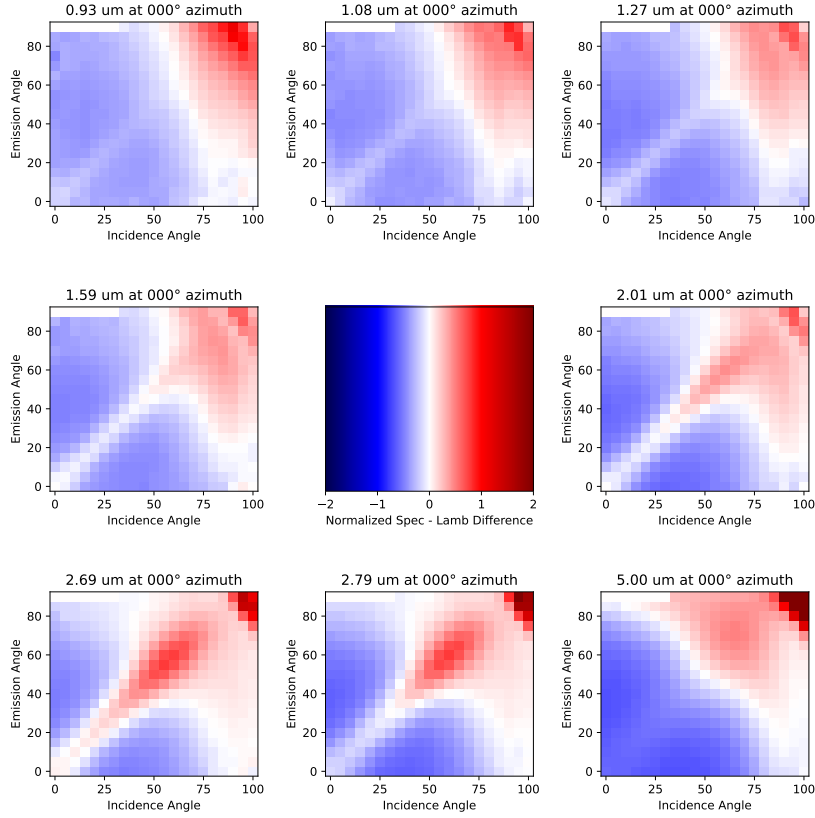


Figure 10: Comparison of specular and lambertian simulations based on viewing geometry. Each of the eight exterior plots are at one wavelength, with the horizontal and vertical axes plotting incidence and emission angle respectively. **[COMPLETE DESCRIPTION]**

the behavior of the 5 micron is distinctly different than the other windows, with a distinctly different shape and gradient across the azimuth. This is, in general, expected, as 5 microns is a much wider window separated from the other windows by a significant portion of the electromagnetic spectrum (). In fact this difference may be supremely helpful, as the behavior of the 5 micron window with respect to the others at different viewing angles could potentially be used as a test to identify liquid bodies.

In order to identify bodies... challenges from inaccuracy of lambertian versus accuracy of specular... need multiple reference points at different viewing angles... find the most dramatic viewing angle changes... maybe go based on viewing angles of location... generalize? Lots of unknowns.

Of course, actually making use of the differences in specular and lambertian behavior depends on validation. We expect the specular model to be accurate

for large bodies of liquid methane, and we have plenty of viewing geometries from the Cassini mission to test.

4 Validation

Known lakes... perhaps also land next to the lakes... table of used flybys/locations... visual comparison first, then qualitative... really hope the validation confirms what we have... demonstrate “identification” of a lake using the data in the previous section...

[Validation procedure: compare with known lakes. Explain selection process for which images/flybys we used for this (not that I know what this procedure is yet, as we haven’t even started this part). Show a visual comparison first, then a quantitative comparison. (Structure: once per flyby used? Once per feature? Or do all visual comparisons and then all quantitative ones?) Compare the quantitative differences and assign some kind of confidence value as to how close our model is to reality. We HOPE that this validation is confirmed. If it is not we presumably need to go back to the drawing board and figure out what went wrong rather than publishing this paper. (if it goes wrong it’s possibly a lack of absorption or some other feature.)]]

5 Discussion

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[So we don’t know what to put here really since we haven’t done the full experiment. Most of the observations I currently know of are best put in Results as they are observations about the results directly rather than any real new knowledge. If validation flies, we do have one piece of knowledge: to find lakes look for fully illuminated disks and find the BLUE in Jason Color. Other possible discussion points: deviations from reality, noise at five microns, error quantifications if we can get them, other potential signs of lakes.]

6 Summary and Conclusion

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[Conclude based on how confident we are in the simulation, and summarize points of new science and potential indications of how to identify future lakes. Keep it simple and short, but make sure to include relevant details, such as precise values that can be used to detect lakes. Summary of most important points is simply helpful to readers]]

Acknowledgements

Data availability? Would like to make it clear that we'll give all the information after just being asked...

[Not sure who needs to be put here who won't be put on the author list. Though there is going to be funding recognition here.]

References

- Barnes, Jason W., Robert H. Brown, Laurence Soderblom, et al. (2007). "Global-scale Surface Spectral Variations on Titan seen from Cassini/VIMS". In: *Icarus* 186.1, pp. 242–258. DOI: [10.1016/j.icarus.2006.08.021](https://doi.org/10.1016/j.icarus.2006.08.021).
- Barnes, Jason W., Robert H. Brown, Elizabeth P. Turtle, et al. (2005). "A 5-Micron-Bright Spot on Titan: Evidence for Surface Diversity". In: *Science* 310.5745, pp. 92–95. DOI: [10.1126/science.1117075](https://doi.org/10.1126/science.1117075).
- Barnes, Jason W., Roger N. Clark, et al. (2013). "A Transmission Spectrum of Titan's North Polar Atmosphere from a Specular Reflection of the Sun". In: *The Astrophysical Journal* 777, p. 161. DOI: [10.1088/0004-637X/777/2/161](https://doi.org/10.1088/0004-637X/777/2/161).
- Barnes, Jason W., Shannon M. MacKenzie, et al. (2018). "Spherical Radiative Transfer in C++ (SRTC++): A Parallel Monte Carlo Radiative Transfer Model for Titan". In: *The Astrophysical Journal* 155, p. 264. DOI: [10.3847/1538-3881/aac2db](https://doi.org/10.3847/1538-3881/aac2db).
- Corlies, Paul et al. (2021). "Modeling Transmission Windows in Titan's Lower Troposphere: Implications for Infrared Spectrometers Aboard Future Aerial and Surface Missions". In: *Icarus* 357, p. 114228. DOI: [10.1016/j.icarus.2020.114228](https://doi.org/10.1016/j.icarus.2020.114228).
- Griffith, Caitlin A et al. (2012). "Radiative Transfer Analyses of Titan's Tropical Atmosphere". In: *Icarus* 218, pp. 975–988. DOI: [10.1016/j.icarus.2011.11.034](https://doi.org/10.1016/j.icarus.2011.11.034).
- Hayes, Alexander G. (2016). "The Lakes and Seas of Titan". In: *Annual Review of Earth and Planetary Sciences* 44, pp. 57–83. DOI: [10.1146/annurev-earth-060115-012247](https://doi.org/10.1146/annurev-earth-060115-012247).

- Hirtzig, M. et al. (2013). “Titan’s Surface and Atmosphere from Cassini/VIMS Data with Updated Methane Opacity”. In: *Icarus* 226.1, pp. 470–486. DOI: [10.1016/j.icarus.2013.05.033](https://doi.org/10.1016/j.icarus.2013.05.033).
- Jennings, D. E. et al. (2019). “Titan Surface Temperatures During the Cassini Mission”. In: *The Astrophysical Journal Letters* 887, p. L8. DOI: [10.3847/2041-8213/ab1f91](https://doi.org/10.3847/2041-8213/ab1f91).
- Kanjanasakul, Chanisa et al. (2020). “Optical Characterization of Ethane Droplets in the Vicinity of Critical Pressure”. In: *Oil Gas Sci. Technol. – Rev. IFP Energies nouvelles* 75. DOI: [10.2516/ogst/2020039](https://doi.org/10.2516/ogst/2020039).
- Li, Liming et al. (2023). “The Bolometric Bond Albedo of Enceladus”. In: *Icarus* 394, p. 115429. DOI: [10.1016/j.icarus.2023.115429](https://doi.org/10.1016/j.icarus.2023.115429).
- Martonchik, John V. and Glen S. Orton (1994). “Optical Constants of Liquid and Solid Methane”. In: *Applied Optics* 33.36. DOI: [10.1364/AO.33.008306](https://doi.org/10.1364/AO.33.008306).
- Mastrogiuseppe, Marco et al. (2016). “Radar Sounding Using the Cassini Altimeter: Waveform Modeling and Monte Carlo Approach for Data Inversion of Observations of Titan’s Seas”. In: *IEEE Transactions on Geoscience and Remote Sensing* 54.10, pp. 5646–5656. DOI: [10.1109/TGRS.2016.2563426](https://doi.org/10.1109/TGRS.2016.2563426).
- Rannou, P. et al. (2021). “Convection Behind the Humidification of Titan’s Stratosphere”. In: *The Astrophysical Journal* 922.239. DOI: [10.3847/1538-4357/ac2904](https://doi.org/10.3847/1538-4357/ac2904).
- Rodriguez, S. et al. (2018). “Observational Evidence for Active Dust Storms on Titan at Equinox”. In: *Nature Geoscience* 11, pp. 727–732. DOI: [10.1038/s41561-018-0233-2](https://doi.org/10.1038/s41561-018-0233-2).
- Es-sayeh, Mael et al. (2023). “Updated Radiative Transfer Model for Titan in the Near-infrared Wavelength Range: Validation AGainst Huygens Atmospheric and Surface Measurements and Application to the Cassini/VIMS Observations of the Dragonfly Landing Area.” In: *The Planetary Science Journal* 4.44. DOI: [10.3847/PSJ/acbd37](https://doi.org/10.3847/PSJ/acbd37).
- Stephan, Katrin et al. (2010). “Specular Reflection on Titan: Liquids in Kraken Mare”. In: *Geophysical Research Letters* 37.7. DOI: [10.1029/2009GL042312](https://doi.org/10.1029/2009GL042312).
- Tomasko, M. G. et al. (2008). “A Model of Titan’s Aerosols Based on Measurements Made Inside the Atmosphere”. In: *Planetary and Space Science* 56.5, pp. 669–707. DOI: [10.1016/j.pss.2007.11.019](https://doi.org/10.1016/j.pss.2007.11.019).
- Trainer, M. G. et al. (2018). “Dragonfly: Investigating the Surface Composition of Titan”. In: *49th Lunar and Planetary Science Conference* (The Woodlands, United States), pp.LPI Contribution No. 2083, id.2586. insu-04513182.
- Vixie, Graham et al. (2015). “Possible Temperate Lakes on Titan”. In: *Icarus* 257, pp. 313–323. DOI: [10.1016/j.icarus.2015.05.009](https://doi.org/10.1016/j.icarus.2015.05.009).
- Xu, Feng et al. (2013). “A Hybrid Method for Modeling Polarized Radiative Transfer in a Spherical-shell Planetary Atmosphere”. In: *Journal of Quantitative Spectroscopy and Radiative Transfer* 117, pp. 59–70. DOI: [10.1016/j.jqsrt.2012.10.013](https://doi.org/10.1016/j.jqsrt.2012.10.013).