

Prove that $O(g(n)) \cap \omega(g(n))$ is the empty set.

A: \because at the definition of $O(g(n))$:

$$f(n) \leq c_1 \cdot g_1(n)$$

\because at the definition of $\omega(g(n))$:

$$f(n) > c_2 \cdot g_2(n)$$

$\therefore O(g(n))$ and $\omega(g(n))$ doesn't have any common elements

$\therefore O(g(n)) \cap \omega(g(n))$ is the empty set #
