

mid term 2

Q1

1) Compatible activity with latest start time
assume there is an optimal solution in S_{oi} ($o_i \in OPT$)

$$S \subseteq a_0, a_1, a_2$$

$$S_{a_0} = \{a_1, a_2\}$$

pick $i=0$, $S_{a_0} = \{a_2, a_1\}$

$$OPT - \{a_0\} = \{a_2\}$$

Proof by contradiction (need to prove B is an optimal sol)

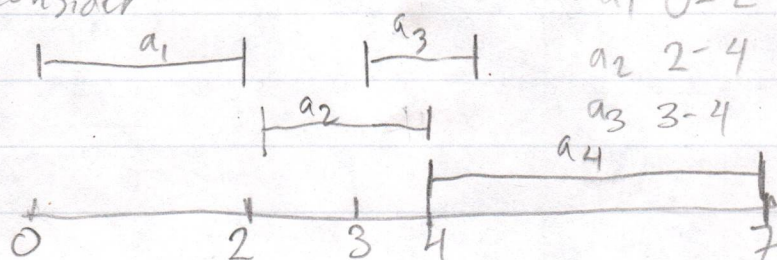
$$|B'| > |B|$$

$$o_i \notin S_{oi}$$

$$B' \supset B$$

$$|B' + \{o_i\}| > |B + \{o_i\}| \rightarrow B' \subset S_{oi} \text{ but } B \text{ is } OPT$$

2) Consider



not all compatible, discard a_4

$$\text{greedy sol } \{a_3\} \quad OPT \subseteq \{a_1, a_2, a_4\}$$

a_4 discarded then $a_1 \rightarrow$ then a_2

Q2

1) Largest = 10 Second largest = 9

2) i) [10, 5]

ii) [9, 8]

iii) Compare largest A_1 with 2nd A_2 &

Largest A_2 with 2nd A_1

if Save values of both conditions

Compare both updated values

3) max val ($A[0 \dots n-1]$)

lenarr =

if $i = \text{len}(A[0 \dots n-1])$ # when end of arr

len($A[i \dots n-1]$)

return i

else

Temp1 = maxVal ($(i \dots \text{lenarr})/2$)

Temp2 = maxVal (~~$(i+1 \dots \text{lenarr})$~~)

$\left(\frac{i+j}{2} + 1 \dots \text{lenarr}\right)$

Ans

if $A[\text{temp1}] \geq A[\text{temp2}]$

return $A[\text{temp1}]$

else return $A[\text{temp2}]$

array [0 1 2 3...]
↑ ↑
j i

Q3 value
 $V = [1, 10, 15, 20]$
 $W = [1, 2, 3, 4]$
 weight

Capacity
 $J \leq 8$
 $i \leq 4$ items

		w					
		0	1	2	3	4	5
obj	0	0	0	0	0	0	0
	1	0	1	10	1	1	1
	2	0	1	10	11	11	11
	3	0	1	10	15	16	25
	4	0	1	10	15	20	21

$F = 25$ 3, 15