

4.5 Precipitation(A) :- Raining(A) ; Snowing(A).
Snowing(A,B) :- (Freezing(A), Precipitation(B)).
Raining(A,B) :- (not(Freezing(A)), Precipitation(B)).
Precipitation(Snowing).

?- Freezing(A)

no

?- Raining(A)

no

The only fact that it is Snowing can be deduced
therefore Freezing & Raining are false. The clauses
can't be rearranged for better answers.

4.7 $\text{gcd}(u, v, w) :- \text{min}(u, v, x), \text{divisor}(u, v, x, w)$

$\text{min}(u, v, u) :- u < v.$

$\text{min}(u, v, v) :- u \geq v.$

$\text{divisor}(u, v, x, x) :- \text{divides}(u, x), \text{divides}(v, x), !.$

$\text{divisor}(u, v, x, w) :- \text{divisor}(u, v, y, w).$

$\text{divides}(u, x) :- \text{divisor}(u, x, y, 0).$

Euclid's efficiency is $O(\log(\min(a, b)))$ whereas this is less efficient at $O(n)$

4.19 $\text{member}(x, [x1-])$.

$\text{member}(x, [-1L]) :- \text{member}(x, L).$

2- $\text{member}(x, [2, 3])$

if $x == 2$ or $x == 3$ return true

$\text{member}(2, L) \rightarrow \text{if } 2 \in L \ \& \ \text{return result}$

$\swarrow \quad \searrow$
 $[2 \neq 2] \quad [2 \in L]$
false true

$\text{member}(x, [2, 3])$
 $\swarrow \quad \searrow$
 $[x \neq 2] \quad [x = 2]$
 $[x \neq 3] \quad [x = 3]$
false true

4.29 Sort is a built in list operation that would throw an error if overloaded. The predicate must avoid names of current built in predicates in order to implement.