

## Quiz 4

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### Q1

Solve  $T(n) = 4T(\frac{n}{2}) + n$  using the master theorem:

1.  $a = ?$

**Answer: 4**

2.  $b = ?$

**Answer: 2**

3.  $f(n) = ?$

**Answer:  $n$**

4. To make  $f(n) = O(n^{(\log_b a) - \epsilon})$ , the largest possible value for  $\epsilon$  is ?

**Answer: 1**

### Q2

Solve  $T(n) = 3T(\frac{n}{2}) + n$  using the master theorem. Which of the following is true?

1.  $f(n) = O(n^{(\log_b a) - \epsilon})$
2.  $f(n) = \Theta(n^{\log_b a})$
3.  $f(n) = \Omega(n^{(\log_b a) + \epsilon})$
4. None of the above is true

**Answer: Option 1**

### Q3

Solve  $T(n) = 9T(\frac{n}{3}) + n^2$  using the master theorem. Which of the following is true?

1.  $f(n) = O(n^{(\log_b a) - \epsilon})$
2.  $f(n) = \Theta(n^{\log_b a})$
3.  $f(n) = \Omega(n^{(\log_b a) + \epsilon})$
4. None of the above is true

**Answer: Option 2**

### Q4

Solve  $T(n) = 9T(\frac{n}{3}) + n^3 \log n$  using the master theorem. Which of the following is true?

1.  $f(n) = O(n^{(\log_b a) - \epsilon})$
2.  $f(n) = \Theta(n^{\log_b a})$

3.  $f(n) = \Omega(n^{(\log_b a) + \epsilon})$
4. None of the above is true

**Answer: Option 3**

**Q5**

Solve  $T(n) = 9T(\frac{n}{3}) + n^2 \log n$  using the master theorem. Which of the following is true?

1.  $f(n) = O(n^{(\log_b a) - \epsilon})$
2.  $f(n) = \Theta(n^{\log_b a})$
3.  $f(n) = \Omega(n^{(\log_b a) + \epsilon})$
4. None of the above is true

**Answer: Option 4**

**Q6**

When using the master theorem to solve a recurrence, after we find a constant  $\epsilon > 0$  such that  $f(n) = \Omega(n^{(\log_b a) + \epsilon})$ , what is the name of the condition we also need to check?

**Answer: regularity**