

Untitled

me

2024-06-12

R Markdown

```
rm(list = ls())
```

We compute our Beta with respect to R_0 and our parameters

```
beta.calc <- function(Ro,mu=0.02/365.25,sigma=1/8,gamma=1/5){  
  Ro/((sigma/(mu+sigma))*(1/(mu+gamma)))  
}
```

We set up our SEIR model by including ν the birth rate and p the vaccination proportion. By adding the proportion of the new birth that were not vaccinated to the susceptible compartment and the vaccinated proportion to the Recovered compartment. We define the time (t) the number of years we are interested in simulating. We use linear ODE solver from R's deSolve to solve iteratively over the number of days in t and compute the value of all compartments at each iteration.

```
# Load necessary libraries  
library(deSolve) # for ode solving  
library(ggplot2) # for plotting  
library(glue)  
  
# Define SEIR model function with seasonal transmission rate  
SEIR_model <- function(time, state, parameters) {  
  with(as.list(c(state, parameters)), {  
    beta_t <- beta_0 * (1 + A * sin(2 * pi * time / T))  
    inc <- sigma * E  
    N <- S + E + I + R  
    dS_dt <- nu*(1-p) - ((beta_t * I) / N + mu) * S  
    dE_dt <- beta_t * S * I - (sigma + mu) * E  
    dI_dt <- sigma * E - (gamma + mu) * I  
    dR_dt <- (nu * p) + gamma * I - mu * R  
    return(list(c(dS_dt, dE_dt, dI_dt, dR_dt, inc)))  
  })  
}  
  
# Time points (in days)  
t <- seq(0, 7*365, 1)  
N0 <- 1
```

For study, we consider different values of ν and p and simulate with the model and observe the interaction of each compartment. The aim is to know what proportion of the new birth needs to be vaccinated in order to achieve a disease-free equilibrium.

```

# Initial conditions
initial_state <- c(S = NO * 0.95, E = NO * 0.05, I = NO * 0, R = NO * 0, inc = 0)

# Parameters
parameters <- list(
  beta_0 = beta.calc(2),
  A = 0.08,
  T = 365, # Period of one year in days
  sigma = 1/8,
  gamma = 1/5,
  nu = 0.09 * NO ,
  mu = 0.02,
  p = 0.9,
  N = NO
)

# Solve the SEIR equations
output <- ode(y = initial_state, times = t, func = SEIR_model, parms = parameters)

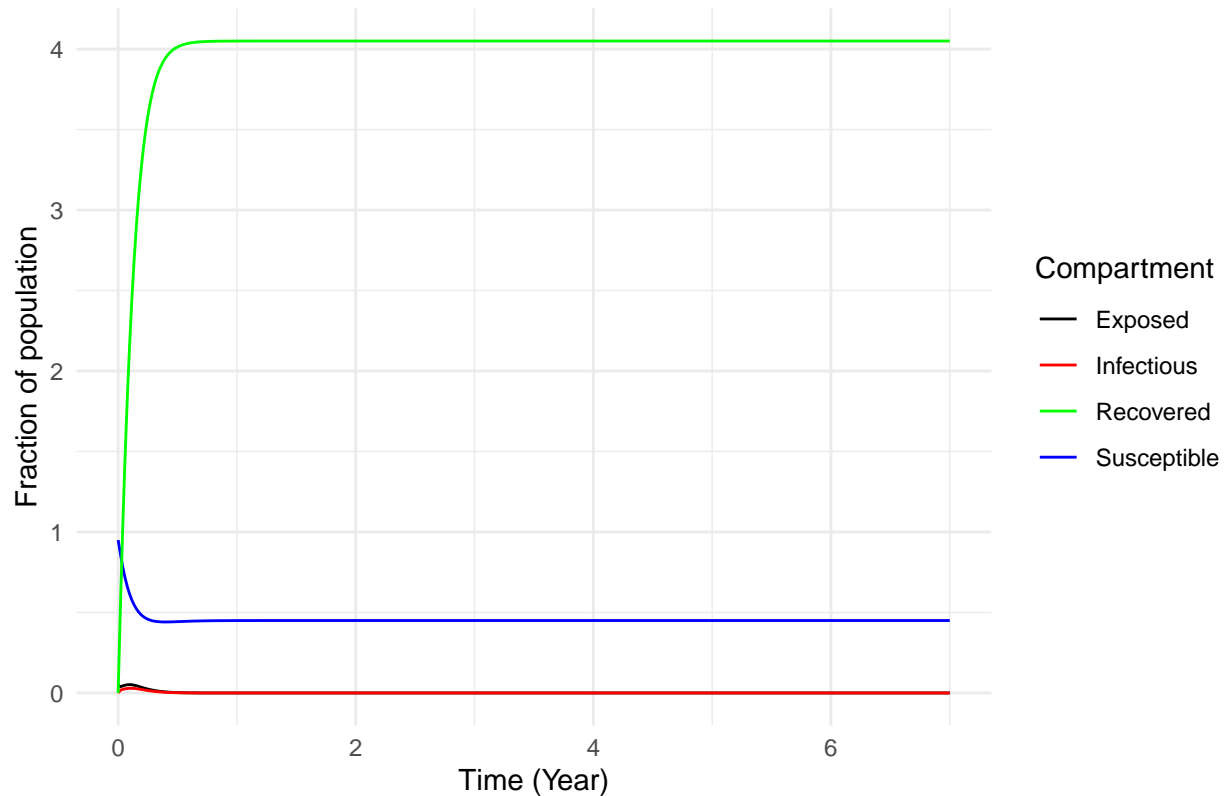
# Convert output to data frame for plotting
output_df <- as.data.frame(output)
weekly.report <- output_df[seq(1, nrow(output_df), by = 7),]

plot.param <- function(weekly.report){
  # Plotting using ggplot2
  ggplot(weekly.report, aes(x = time/365)) +
    geom_line(aes(y = S, color = "Susceptible")) +
    geom_line(aes(y = E, color = "Exposed")) +
    geom_line(aes(y = I, color = "Infectious")) +
    geom_line(aes(y = R, color = "Recovered")) +
    labs(x = "Time (Year)", y = "Fraction of population", color = "Compartment") +
    ggtitle(glue("SEIR Model at Nu = {parameters['nu']} and P = {parameters['p']}")) +
    theme_minimal() +
    scale_color_manual(values = c("Susceptible" = "blue", "Exposed" = "black", "Infectious" = "red", "Recovered" = "green"))
}

plot.param(weekly.report)

```

SEIR Model at $Nu = 0.09$ and $P = 0.9$



```
run.simu <- function(parameters){
  # Solve the SEIR equations
  output <- ode(y = initial_state, times = t, func = SEIR_model, parms = parameters)

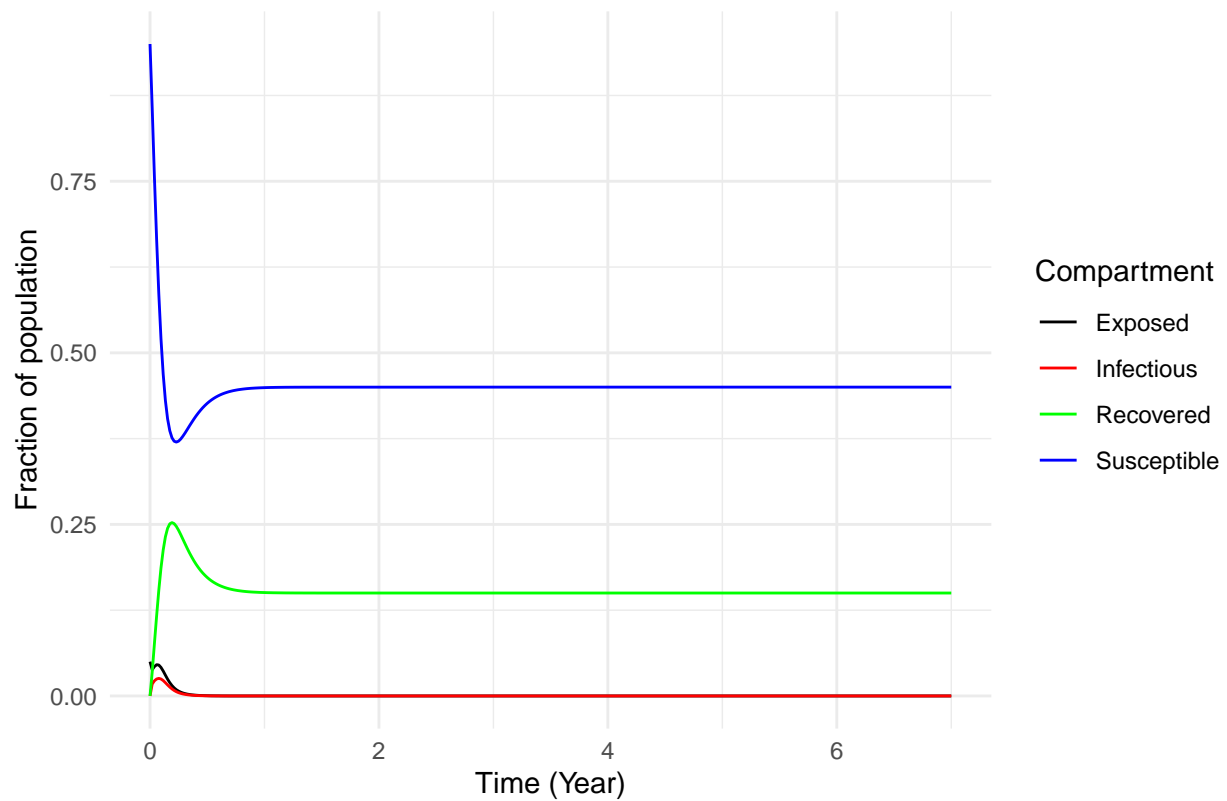
  # Convert output to data frame for plotting
  output_df <- as.data.frame(output)
  weekly.report <- output_df[seq(1, nrow(output_df), by = 7),]
  plot.param(weekly.report)
}
```

for $Nu = 0.12$ and 0.25

```
parameters["nu"] <- 0.012 * N0
parameters["p"] <- 0.25

run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.012$ and $P = 0.25$



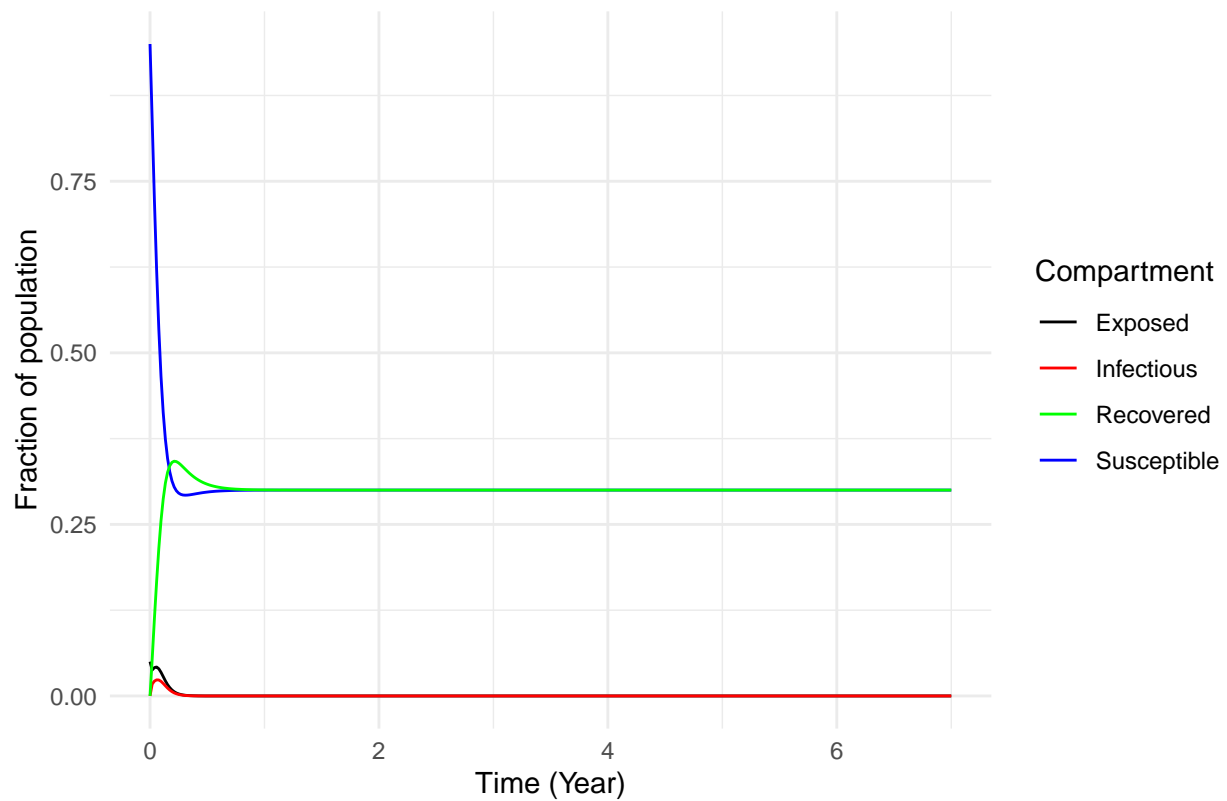
$Nu = 0.012$, $p = 0.5$

```
parameters["nu"] <- 0.012 * N0
```

```
parameters["p"] <- 0.5
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.012$ and $P = 0.5$

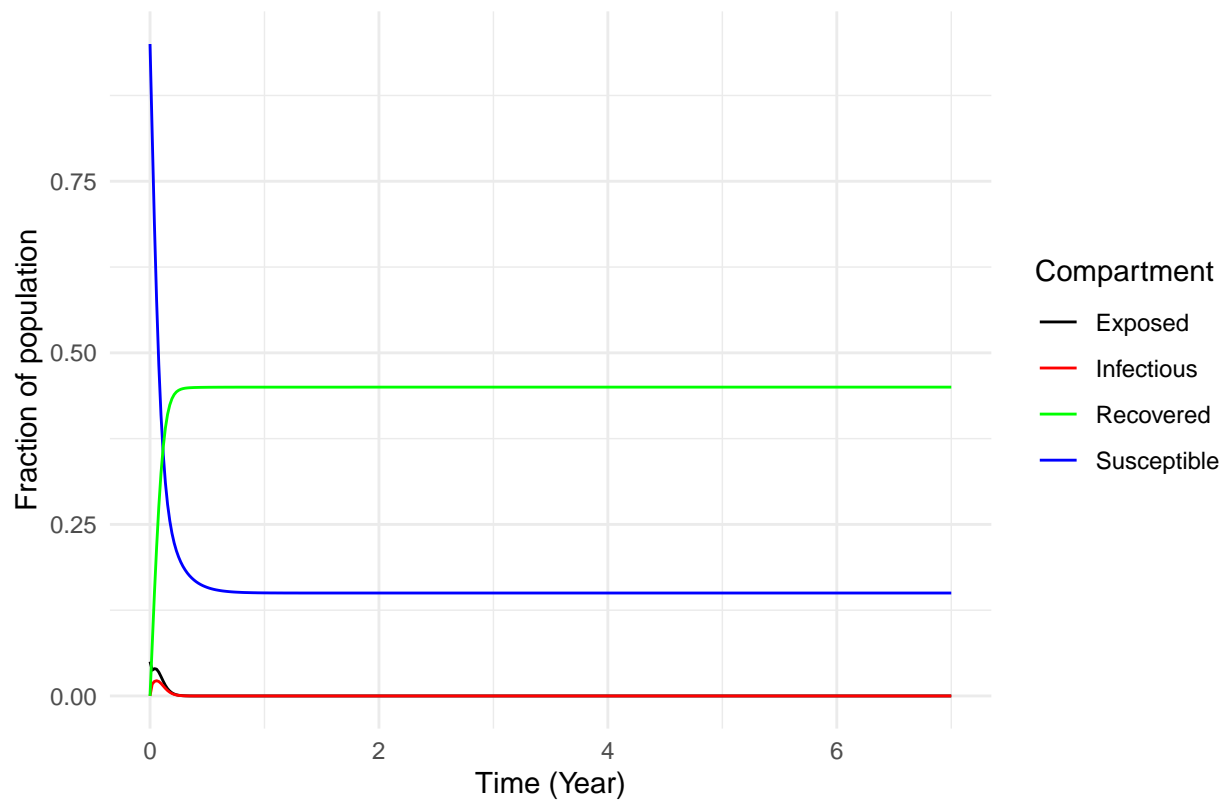


$Nu = 0.012$ $p = 0.75$

```
parameters["nu"] <- 0.012 * N0
parameters["p"] <- 0.75
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.012$ and $P = 0.75$

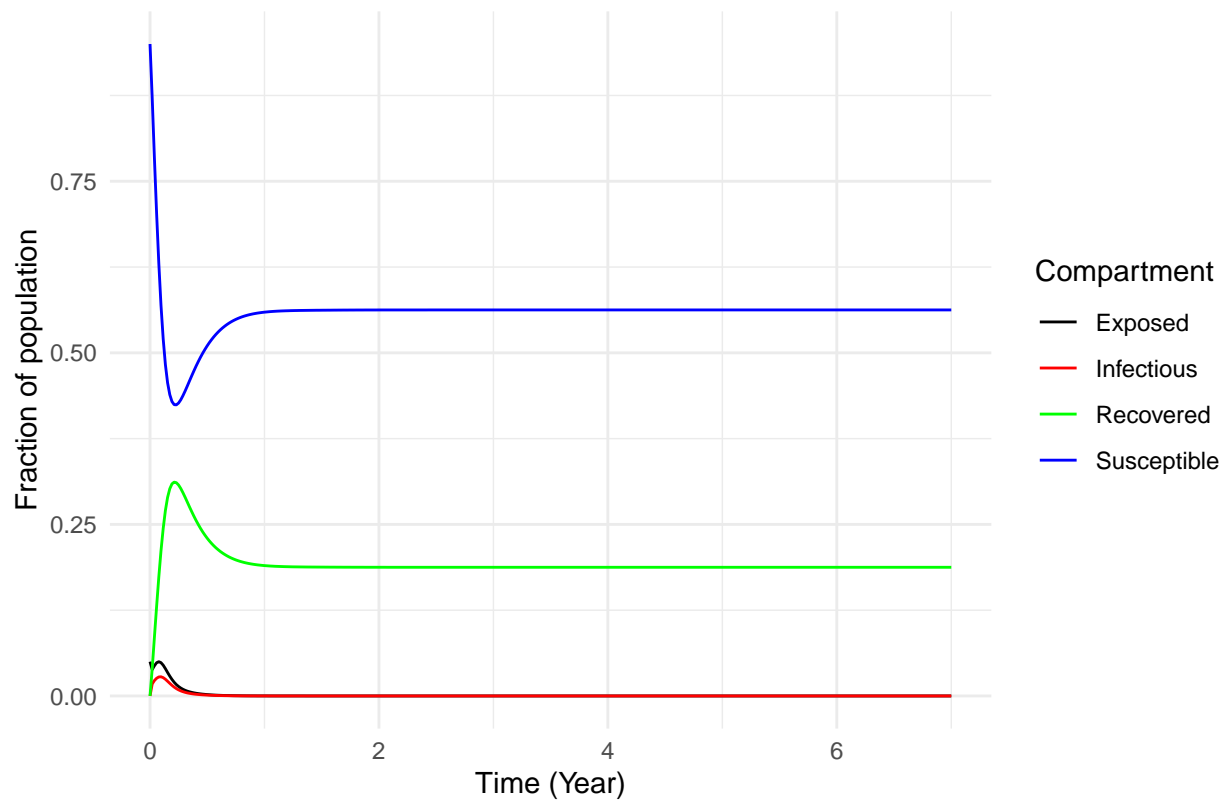


$Nu = 0.015$ $p = 0.25$

```
parameters["nu"] <- 0.015 * N0  
parameters["p"] <- 0.25
```

```
run.simu(parameters = parameters)
```

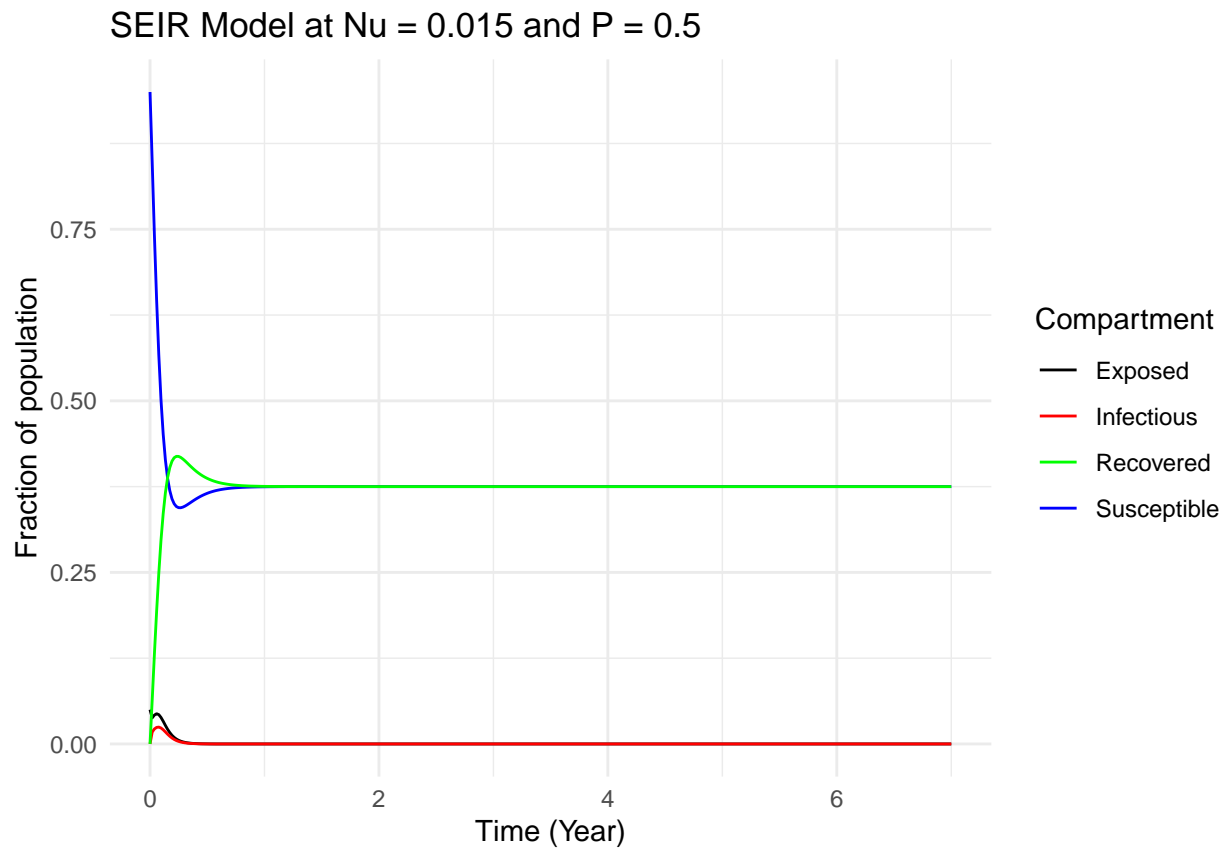
SEIR Model at $Nu = 0.015$ and $P = 0.25$



$Nu = 0.015$ $p = 0.5$

```
parameters["nu"] <- 0.015 * N0  
parameters["p"] <- 0.5
```

```
run.simu(parameters = parameters)
```

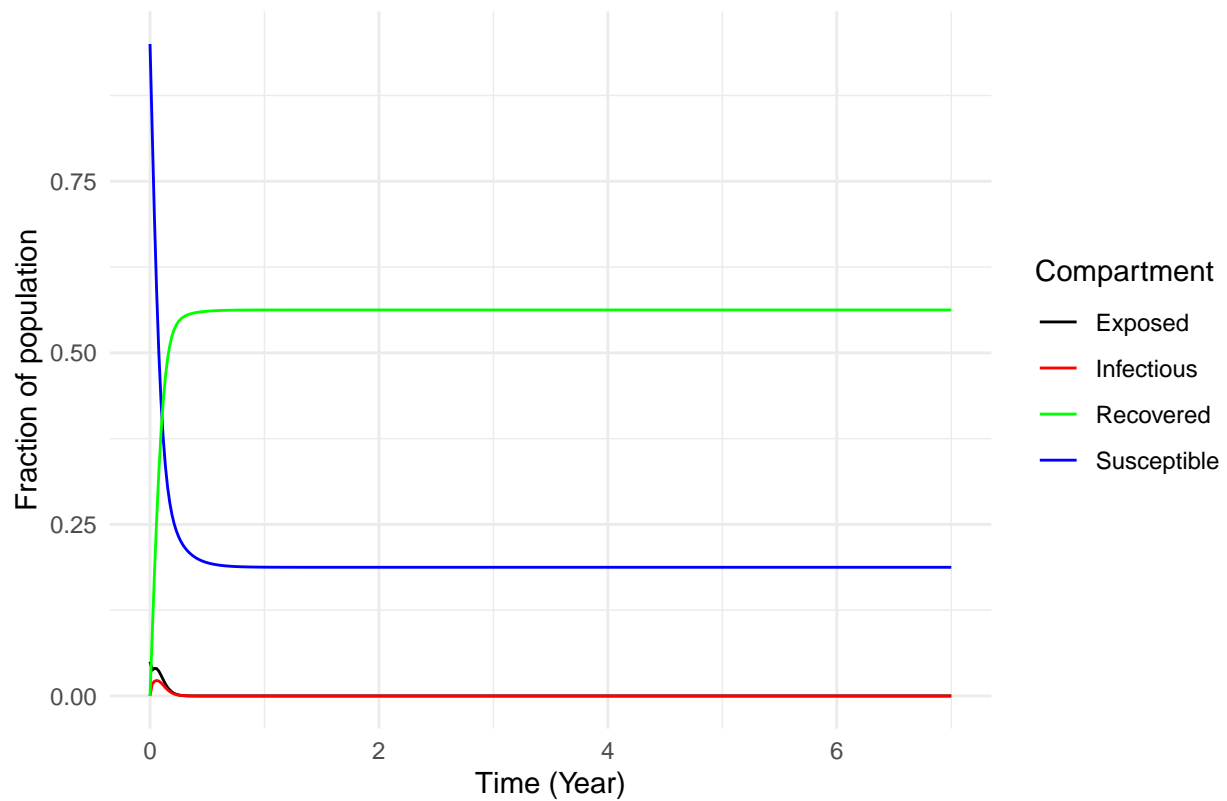


$Nu = 0.015$ $p = 0.75$

```
parameters["nu"] <- 0.015 * N0  
parameters["p"] <- 0.75
```

```
run.simu(parameters = parameters)
```


SEIR Model at $Nu = 0.015$ and $P = 0.75$

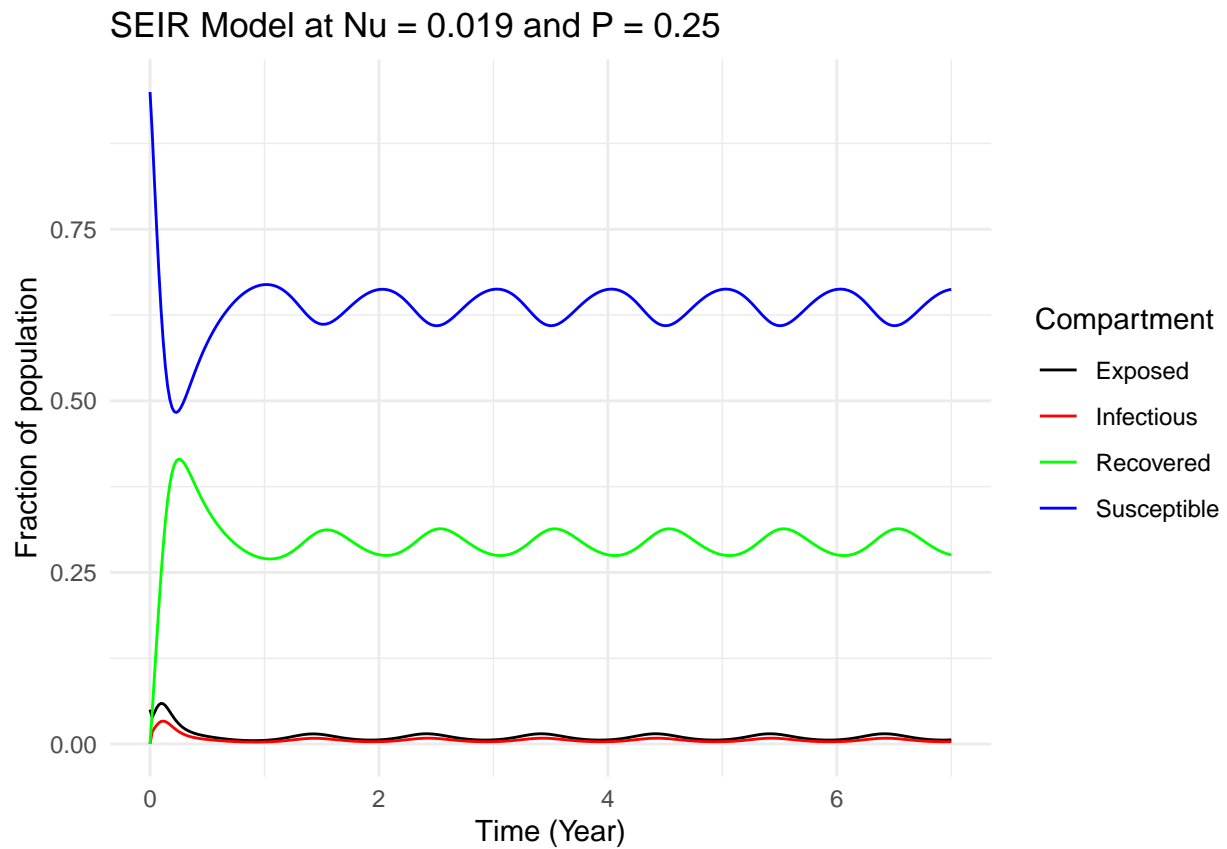


$Nu = 0.019$ $p = 0.25$

```
parameters["nu"] <- 0.019 * N0
```

```
parameters["p"] <- 0.25
```

```
run.simu(parameters = parameters)
```

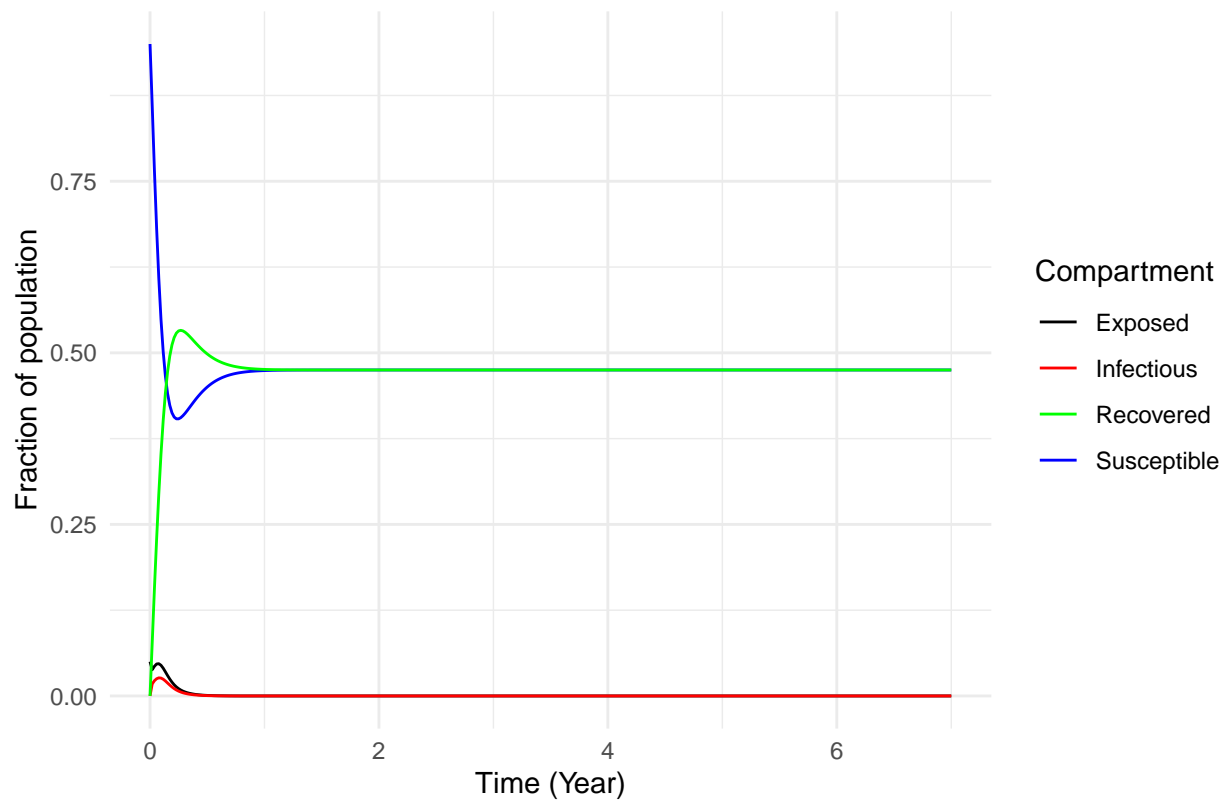


$Nu = 0.019$ $p = 0.5$

```
parameters["nu"] <- 0.019 * N0  
parameters["p"] <- 0.5
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.019$ and $P = 0.5$

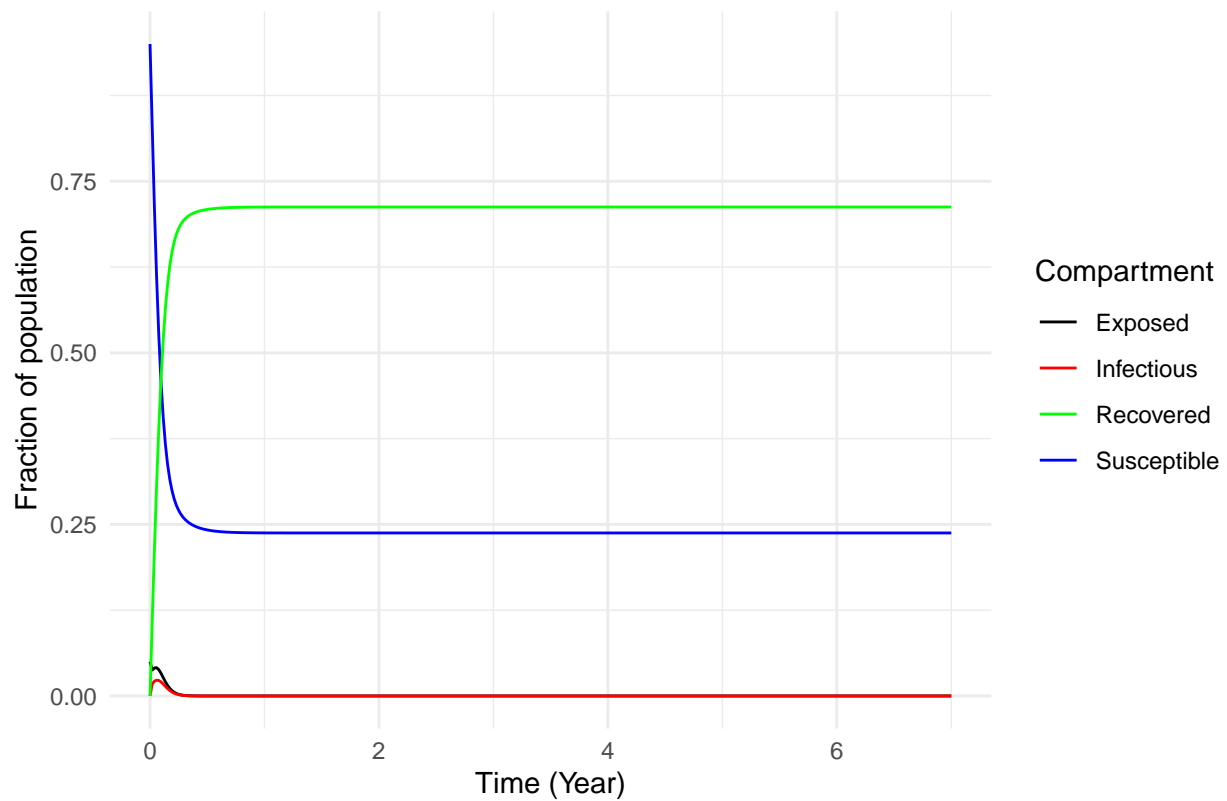


$Nu = 0.019$ $p = 0.75$

```
parameters["nu"] <- 0.019 * N0  
parameters["p"] <- 0.75
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.019$ and $P = 0.75$

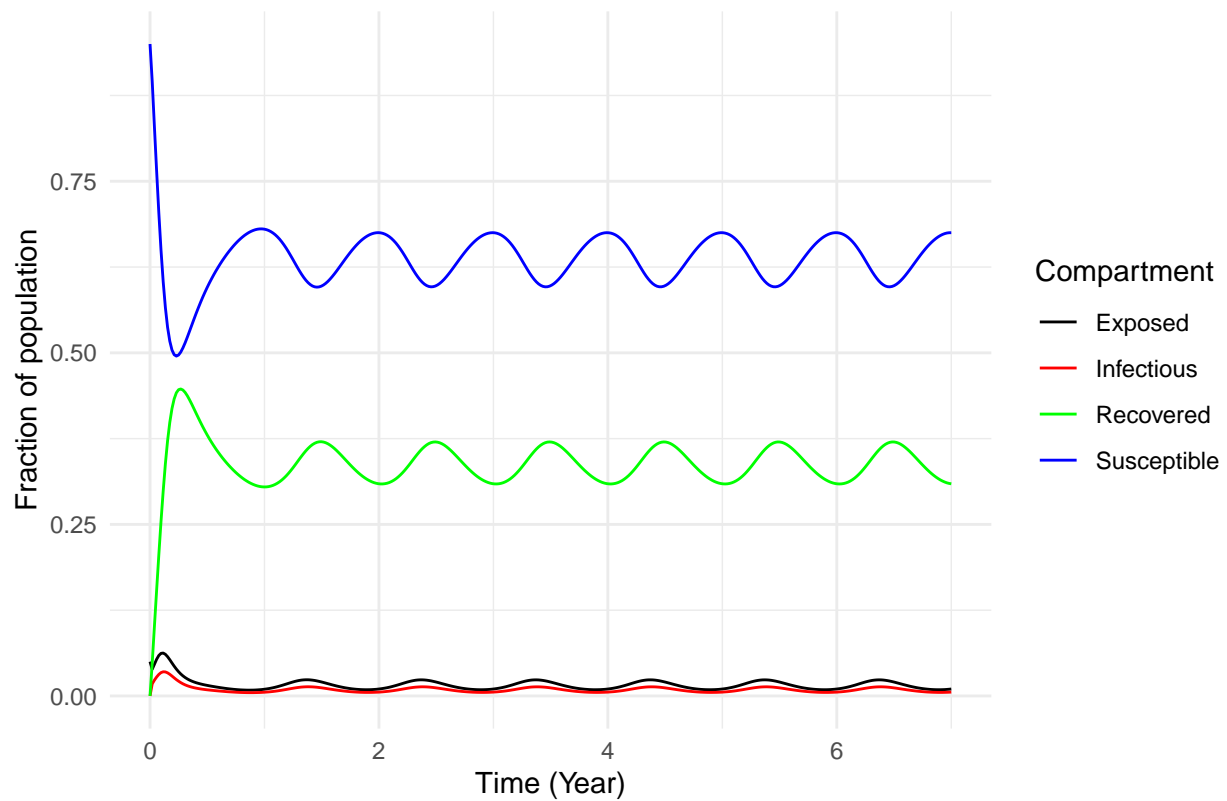


$Nu = 0.02$ $p = 0.25$

```
parameters["nu"] <- 0.02 * N0  
parameters["p"] <- 0.25
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.02$ and $P = 0.25$

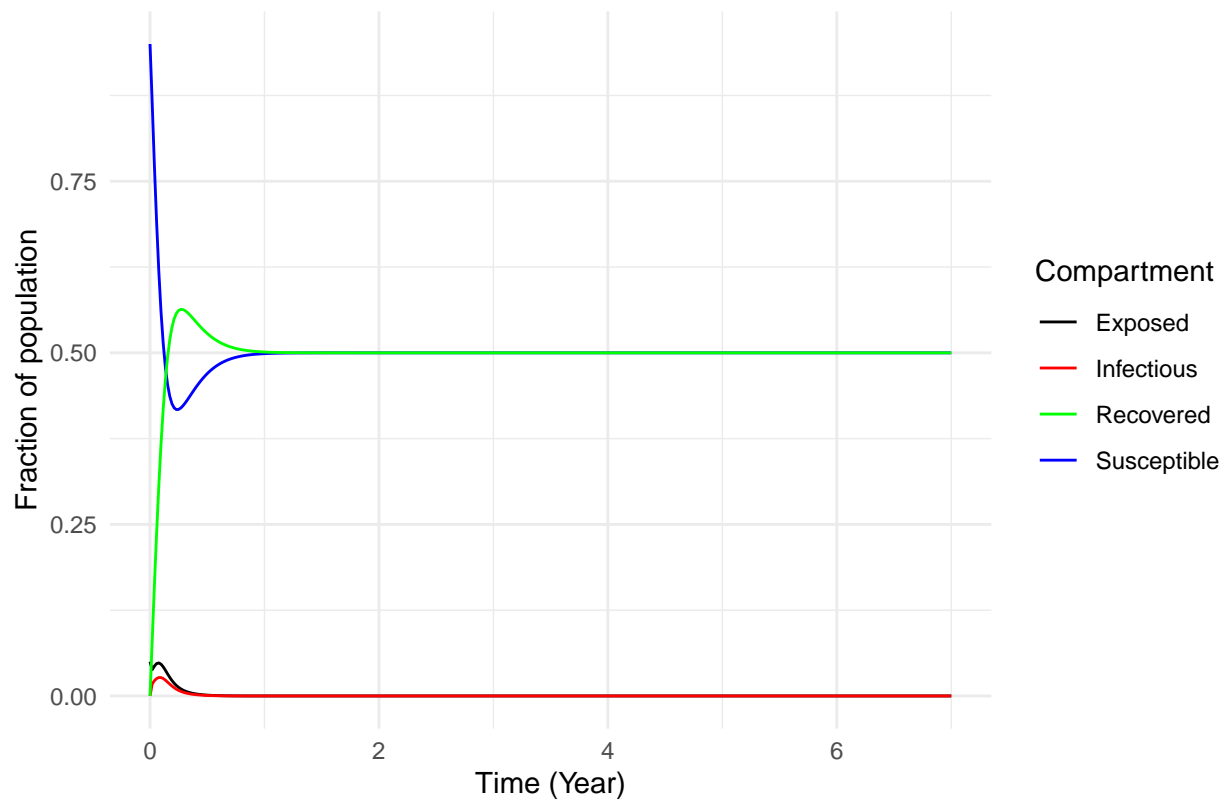


$Nu = 0.02$ $p = 0.5$

```
parameters["nu"] <- 0.02 * N0  
parameters["p"] <- 0.5
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.02$ and $P = 0.5$

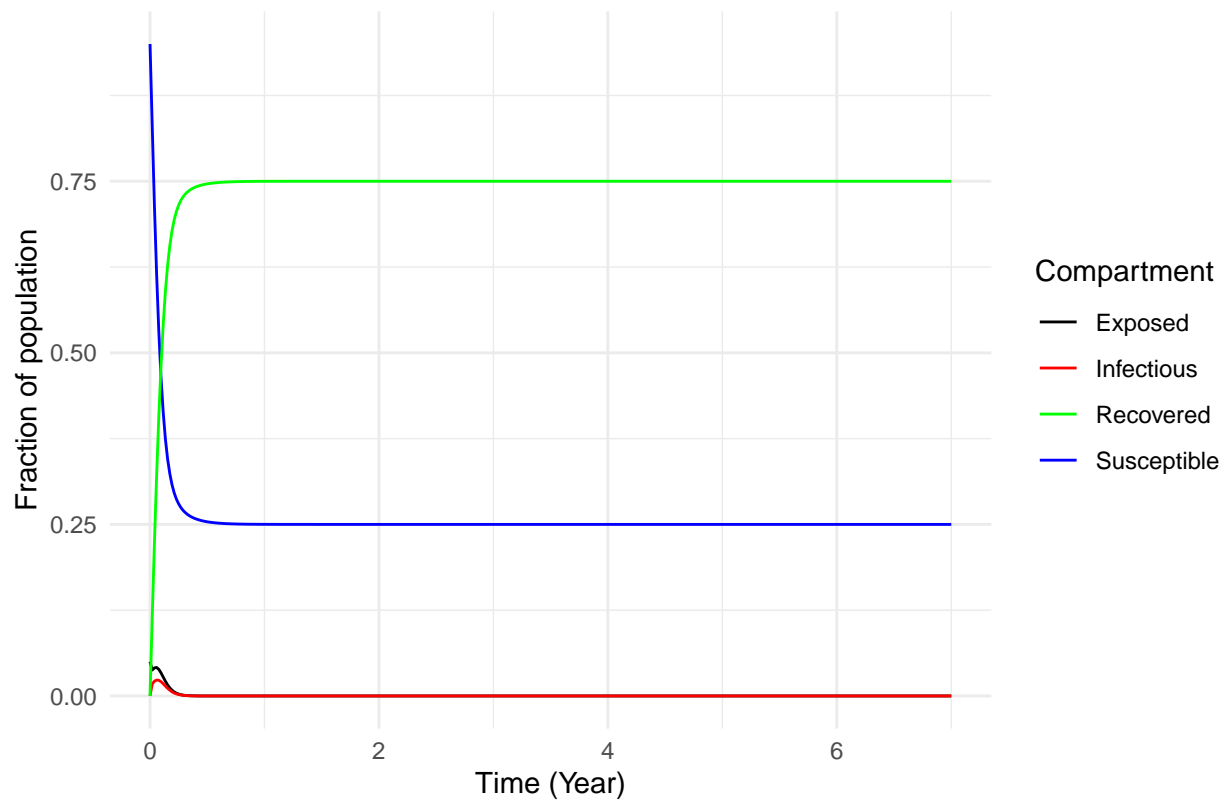


$Nu = 0.02$ $p = 0.75$

```
parameters["nu"] <- 0.02 * N0  
parameters["p"] <- 0.75
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.02$ and $P = 0.75$

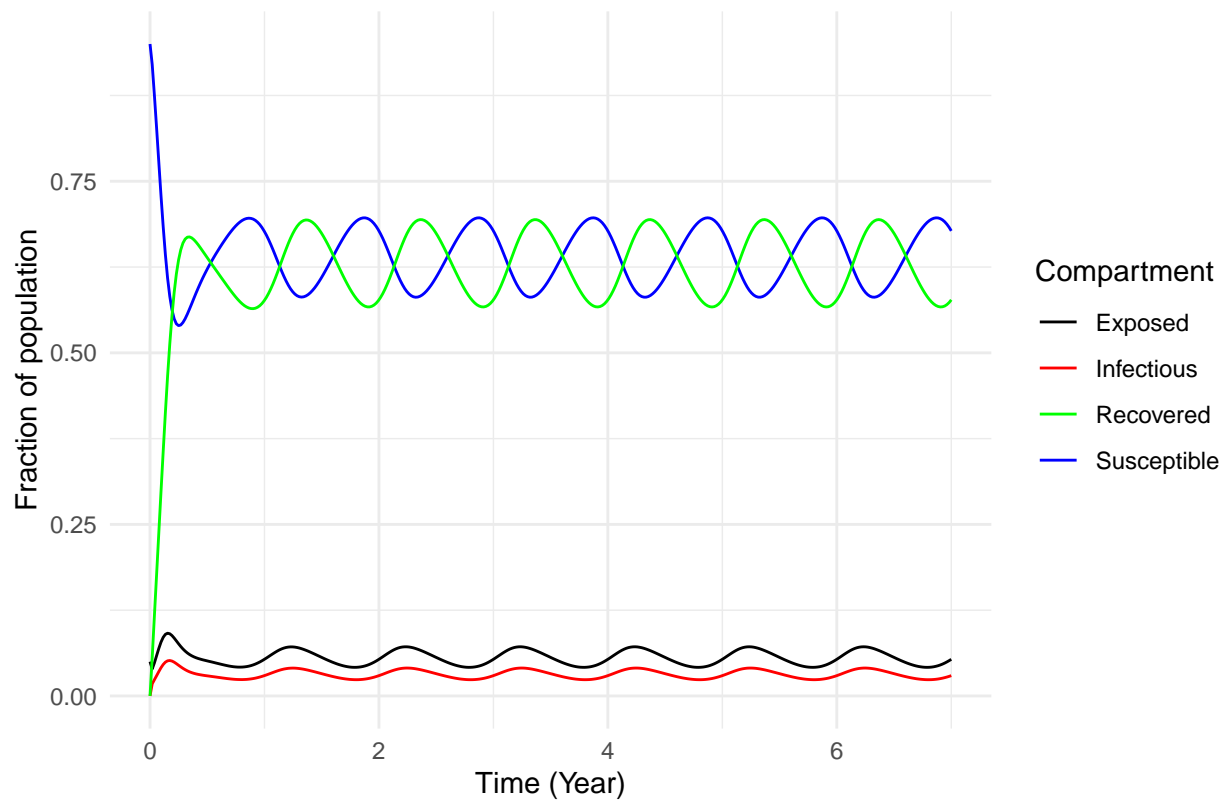


$Nu = 0.025$ $p = 0.25$

```
parameters["nu"] <- 0.025 * N0  
parameters["p"] <- 0.25
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.025$ and $P = 0.25$

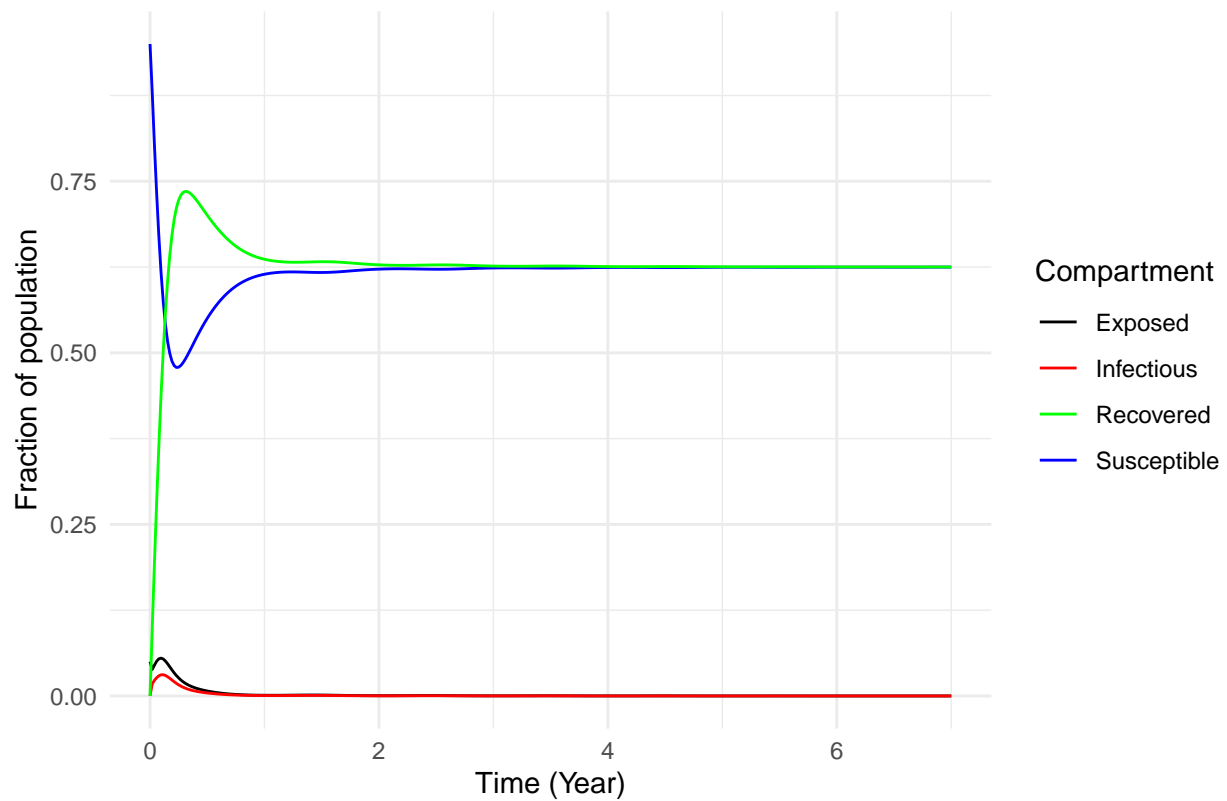


$Nu = 0.025$ $p = 0.5$

```
parameters["nu"] <- 0.025 * N0  
parameters["p"] <- 0.5
```

```
run.simu(parameters = parameters)
```


SEIR Model at $Nu = 0.025$ and $P = 0.5$

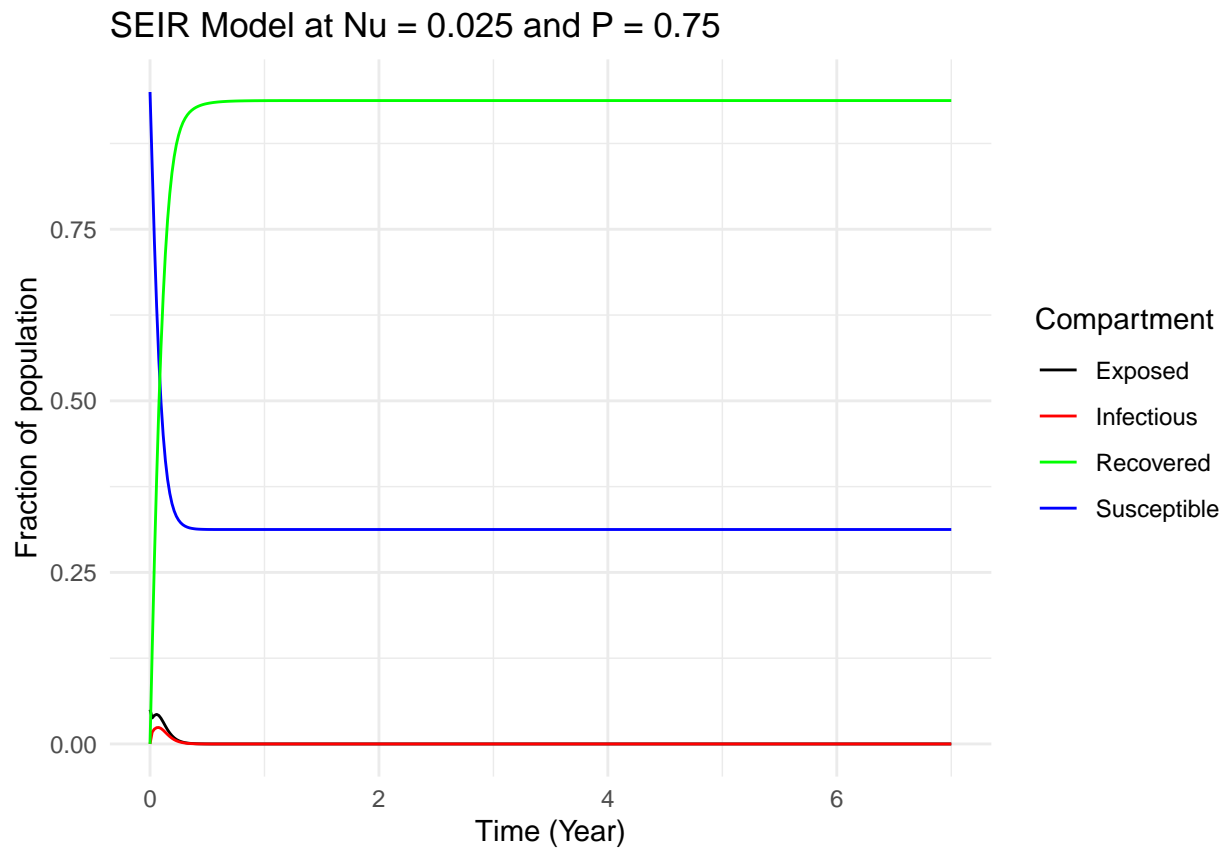


$Nu = 0.025$ $p = 0.75$

```
parameters["nu"] <- 0.025 * N0
```

```
parameters["p"] <- 0.75
```

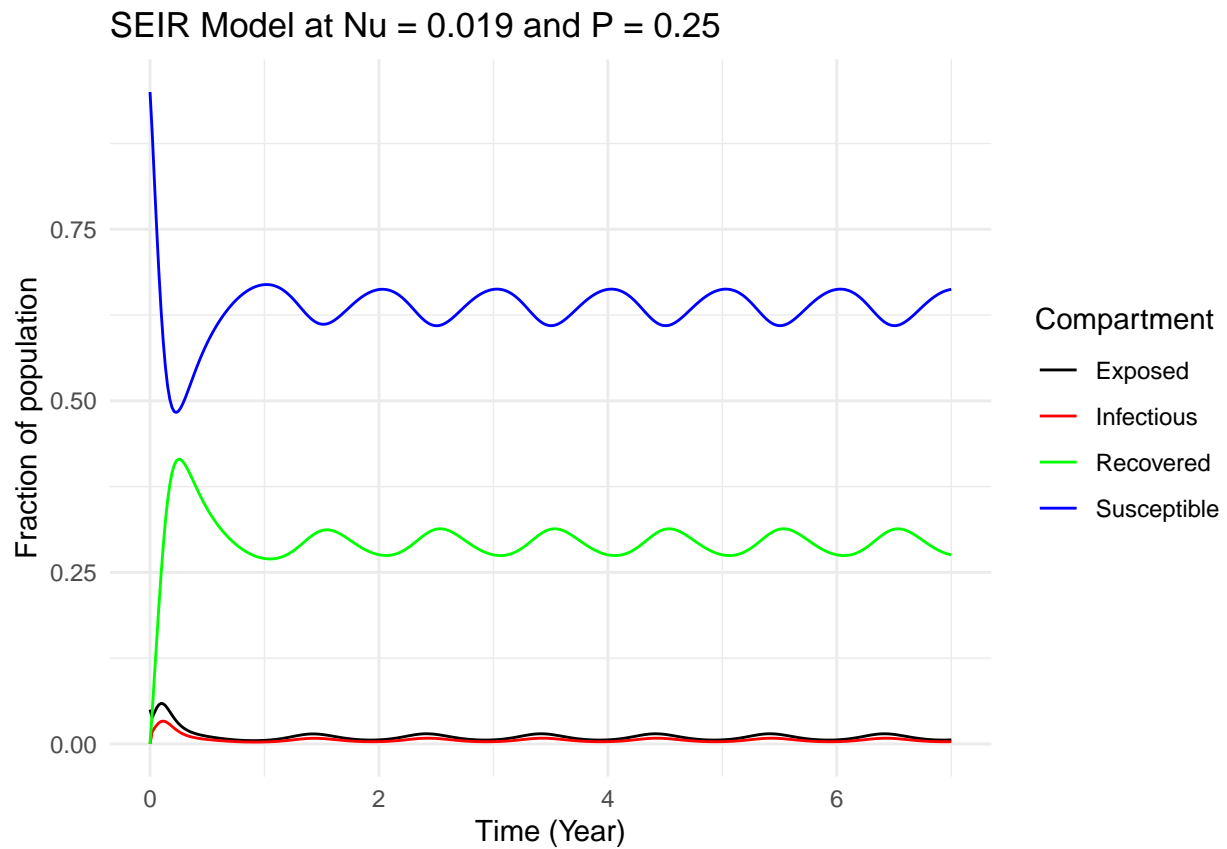
```
run.simu(parameters = parameters)
```



$Nu = 0.03$ $p = 0.5$

```
parameters["nu"] <- 0.019 * N0  
parameters["p"] <- 0.25
```

```
run.simu(parameters = parameters)
```

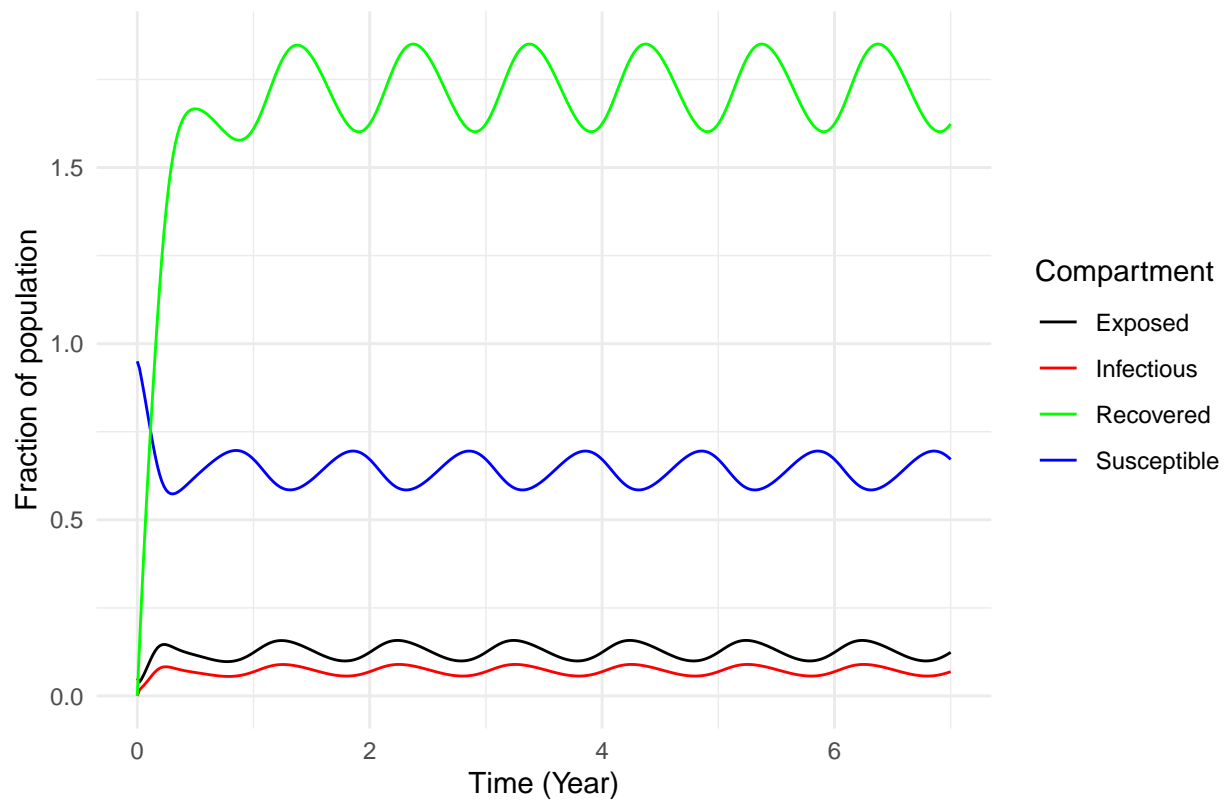


$Nu = 0.05$ $p = 0.5$

```
parameters["nu"] <- 0.04 * N0  
parameters["p"] <- 0.5
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.04$ and $P = 0.5$



$Nu = 0.09$ $p = 0.5$

```
parameters["nu"] <- 0.09 * N0
```

```
parameters["p"] <- 0.75
```

```
run.simu(parameters = parameters)
```

SEIR Model at $Nu = 0.09$ and $P = 0.75$

