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# Simulation with PD control

```
fprintf('\n');
clearvars -except function_list pub_opt
close all
MRP0=[0.8;0.1;-0.1];%rad

fprintf('MRP vector:\n');
MRP = MRP0;
printVector(MRP, '');
omega_body0 = [0; 0; 0]; %rad/s
fprintf('Initial Body Rates:\n');
printVector(omega_body0, 'rad/s');
I_body=[10 0 0;0 20 0;0 0 30]; %kg*m2

%unit gains
P1=2*10/100;
K = P1*P1/10%0.004;
P = [P1 0 0; 0 sqrt(K*20) 0; 0 0 sqrt(K*30)]
cm_torque=[0;0;0];

delta_t = 0.01;
t_end = 600 - delta_t; % seconds

MRP = MRP0;
omega_body = omega_body0;
% Arrays for recording and plotting
t_mat = 0:delta_t:t_end+delta_t;
[rows, cols] = size(t_mat);
MRP_mat = zeros(3,cols);
omega_mat = zeros(3,cols);
EA_mat = zeros(3,cols);
mode_mat = zeros(3,cols);
CT_mat = zeros(3,cols);
MRP_mat(:,1) = MRP;
omega_mat(:,1) = omega_body;
mode_mat(:,1) = 0;
CT_MAT(:,1) = cm_torque;
idx = 2;

% RK4 integration
state = [MRP; omega_body];
control_int = 0;
linearization_mat = ...
    [zeros(3,3) 0.25*I_body; -K*inv(I_body) -inv(I_body)*P];
for t = 0:delta_t:t_end

    k1 = linearization_mat*state;
    k2 = linearization_mat*(state+delta_t*k1/2);
    k3 = linearization_mat*(state+delta_t*k2/2);
    k4 = linearization_mat*(state+delta_t*k3);
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state = state + delta_t/6*(k1 + 2*k2 + 2*k3 + k4);

% Enforce |MRP| <= 1, switch to shadow set if needed
if norm(state(1:3)) > 1
    state(1:3) = -state(1:3)/dot(state(1:3), state(1:3));
end

% Updating array

MRP_mat(:,idx) = state(1:3);
omega_mat(:,idx) = state(4:6);
idx = idx + 1;
end

font_size=8;
figure
plot(t_mat, MRP_mat);
mytitle = strcat('MRP Propagation - Linearized CLD');
title(mytitle,'FontSize',font_size)
xlabel('time(s)','FontSize',font_size)
ylabel('Element Magnitude','FontSize',font_size)
legend('\sigma_{1}', '\sigma_{2}', '\sigma_{3}')
grid on
set(gca,'FontSize',font_size)
fprintf('\n\n\n');

figure
plot(t_mat, omega_mat*180/pi);
mytitle = strcat('Body Rates - Linearized CLD');
title(mytitle,'FontSize',font_size)
xlabel('time(s)','FontSize',font_size)
ylabel('Element Magnitude (deg/s)','FontSize',font_size)
legend('\omega_{1}', '\omega_{2}', '\omega_{3}')
grid on
set(gca,'FontSize',font_size)
fprintf('\n\n\n');

MRP vector:
[0.800000; 0.100000; -0.100000]
Initial Body Rates:
[0.000000; 0.000000; 0.000000] rad/s

K =

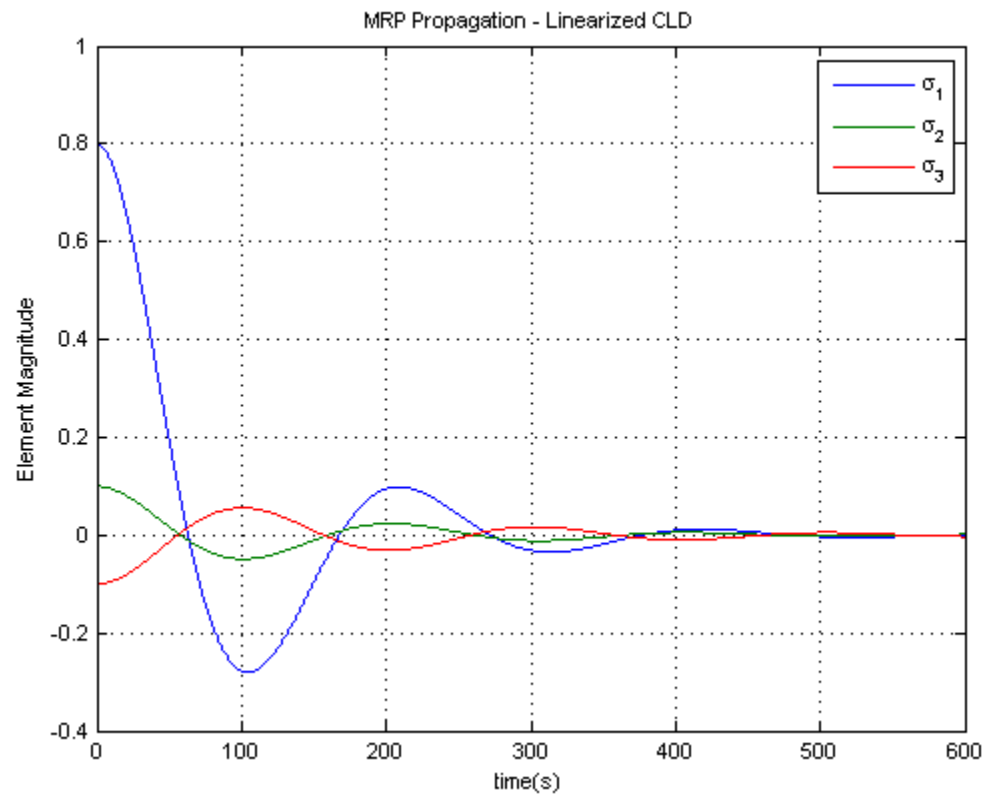
0.0040

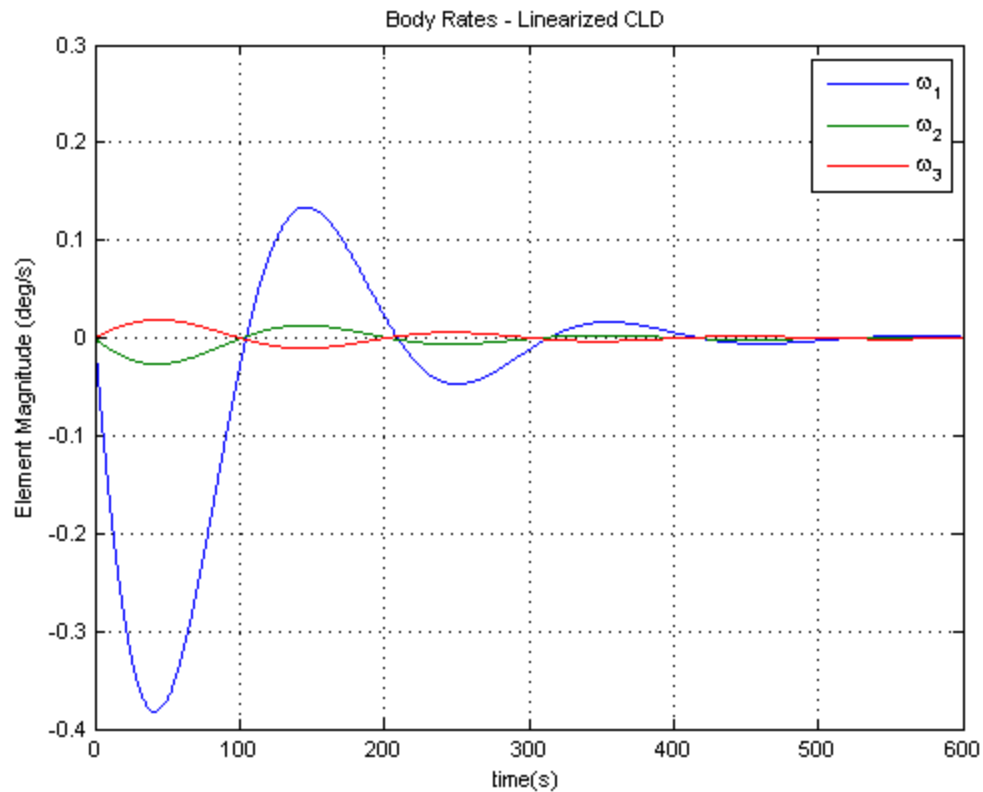
P =

0.2000    0    0
0    0.2828    0
0    0    0.3464

```

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## Nonlinear CLD

Arrays for recording and plotting

```
t_mat = 0:delta_t:t_end+delta_t;
[rows, cols] = size(t_mat);
MRP_mat = zeros(3,cols);
omega_mat = zeros(3,cols);
EA_mat = zeros(3,cols);
mode_mat = zeros(3,cols);
CT_mat = zeros(3,cols);
MRP_mat(:,1) = MRP;
omega_mat(:,1) = omega_body;
mode_mat(:,1) = 0;
CT_MAT(:,1) = cm_torque;
idx = 2;
% RK4 integration
state = [MRP; omega_body];
for t = 0:delta_t:t_end

    k1 = [derivMRP(state(1:3), state(4:6)); ...
          inv(I_body)*(-P*state(4:6)-K*state(1:3))];
    k2 = [derivMRP(state(1:3) + delta_t*k1(1:3)/2, ...
          state(4:6) + delta_t*k1(4:6)/2); ...
          inv(I_body)*(-P*(state(4:6)+delta_t*k1(4:6)/2)-K*(state(1:3)+delta_t*k1(1:3))];
    k3 = [derivMRP(state(1:3) + delta_t*k2(1:3)/2, ...
```

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        state(4:6) + delta_t*k2(4:6)/2); ...
        inv(I_body)*(-P*(state(4:6)+delta_t*k1(4:6)/2)-K*(state(1:3)+delta_t*k2(1:3))
k4 = [derivMRP(state(1:3) + delta_t*k3(1:3), ...
        state(4:6) + delta_t*k3(4:6)); ...
        inv(I_body)*(-P*(state(4:6)+delta_t*k1(4:6)/2)-K*(state(1:3)+delta_t*k3(1:3))

state = state + delta_t/6*(k1 + 2*k2 + 2*k3 + k4);

% Enforce |MRP| <= 1, switch to shadow set if needed
if norm(state(1:3)) > 1
    state(1:3) = -state(1:3)/dot(state(1:3), state(1:3));
end

% Updating array

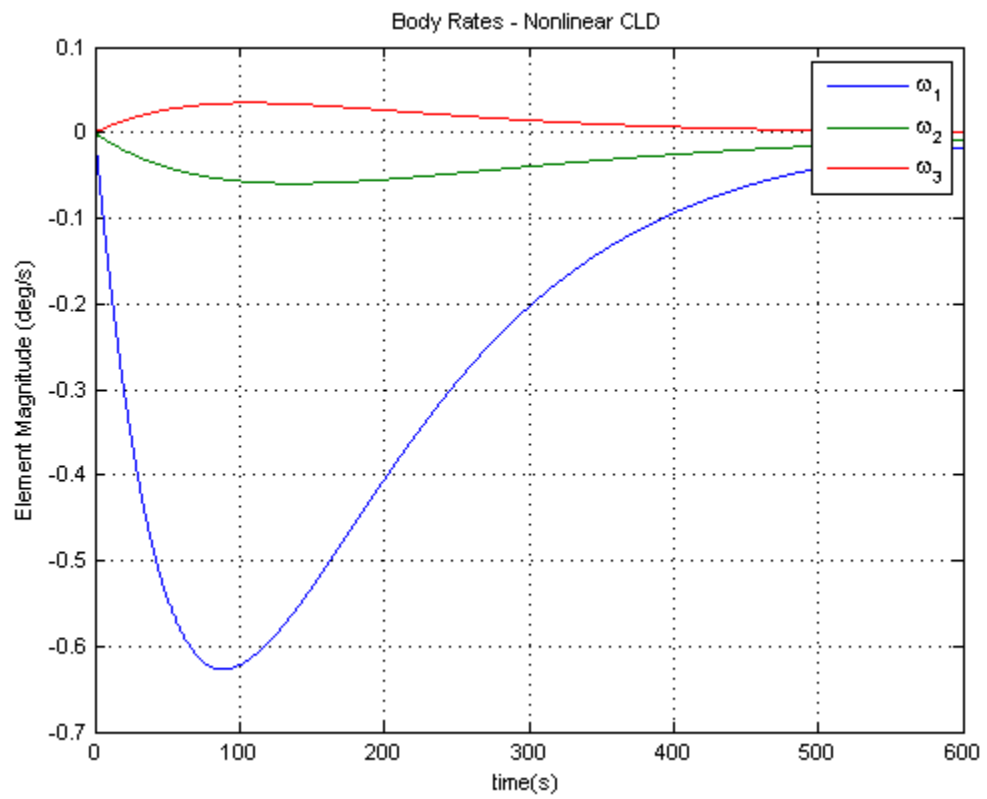
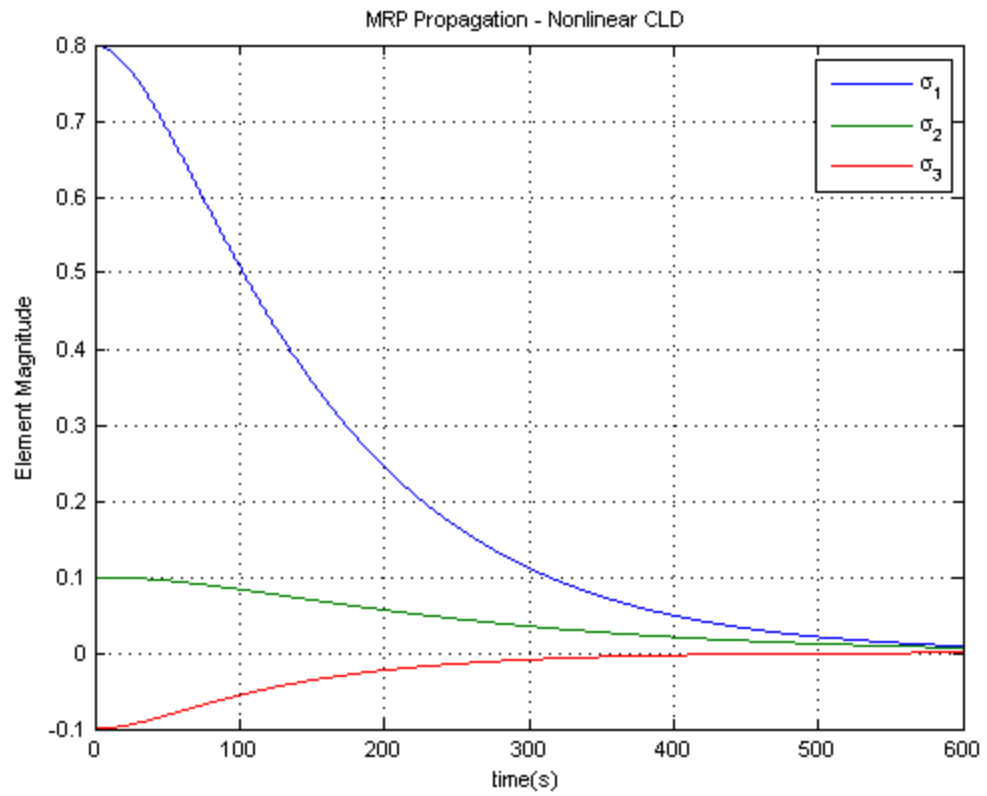
MRP_mat(:,idx) = state(1:3);
omega_mat(:,idx) = state(4:6);
% CT_mat(:,idx)=control_torque;
idx = idx + 1;
end

font_size=8;
figure
plot(t_mat, MRP_mat);
mytitle = strcat('MRP Propagation - Nonlinear CLD');
title(mytitle,'FontSize',font_size)
xlabel('time(s)','FontSize',font_size)
ylabel('Element Magnitude','FontSize',font_size)
legend('\sigma_{1}', '\sigma_{2}', '\sigma_{3}')
grid on
set(gca,'FontSize',font_size)
fprintf('\n\n\n');

figure
plot(t_mat, omega_mat*180/pi);
mytitle = strcat('Body Rates - Nonlinear CLD');
title(mytitle,'FontSize',font_size)
xlabel('time(s)','FontSize',font_size)
ylabel('Element Magnitude (deg/s)','FontSize',font_size)
legend('\omega_{1}', '\omega_{2}', '\omega_{3}')
grid on
set(gca,'FontSize',font_size)
fprintf('\n\n\n');

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