

HW1 Problem 4: Ground station observations

```
fprintf('\n');
clearvars -except function_list hw_pub toolsPath
close all

v = 50; %m/s
h = 100; %m
x0 = 250; %m

x = linspace(-x0, x0, x0*10);

range = sqrt(h*h + x.*x);
range_rate = x./range*v;
zenith = atan2(x,h);

h2 = 50; %m
range2 = sqrt(h2*h2 + x.*x);
range_rate2 = x./range2*v;
zenith2 = atan2(x,h2);

figure('OuterPosition', [0 50 hw_pub.figWidth hw_pub.figHeight])
subplot(3,1,1)
plot(x, range)
hold on
plot(x, range2, 'g')
title('Range')
xlabel('x position (m)')
ylabel('range (m)')
legend('h = 100 m', 'h = 50 m')
subplot(3,1,2)
plot(x, range_rate)
hold on
plot(x, range_rate2, 'g')
title('Range Rate')
xlabel('x position (m)')
ylabel('range rate (m/s)')
legend('h = 100 m', 'h = 50 m')
subplot(3,1,3)
plot(x, zenith*180/pi)
hold on
plot(x, zenith2*180/pi, 'g')
title('Zenith Angle')
xlabel('x position (m)')
ylabel('zenith (deg)')
legend('h = 100 m', 'h = 50 m')

fprintf(['range:\n',...
        '\tthe slope is steep away from the ground station, making the\n',...
        '\tmeasurement more sensitive to changes in x (more accurate)\n.',...
        '\tHowever, it loses accuracy directly above. There are also not\n',...
        '\tunique x/range pairings, so another method must be used to \n',...

```

```

'\tdetermine which side of the transmitter the receiver is on.\n',...
'\tLower values of h make the range measurement more accurate \n',...
'\tcloser to the transmitter\n',...
'range rate:\n',...
'\tThe slope is steep only near the transmitter, so it is not\n',...
'\taccurate at long distances.\n',...
'\tIt has unique x/range rate pairings, so you can tell which side\n',...
'\tof the transmitter the receiver is.\n',...
'\tLower values of h make the range rate measurement less accurate\n',...
'\tuntil the reciever is closest to the transmitter.\n',...
'Zenith angle:\n',...
'\tThe slope is steep only near the transmitter, so it is not\n',...
'\taccurate at long distances.\n',...
'\tIt has unique x/range rate pairings, so you can tell which side\n',...
'\tof the transmitter the receiver is.\n',...
'\tLower values of h make the range rate measurement less accurate\n',...
'\tuntil the reciever is closest to the transmitter.\n']])

```

range:

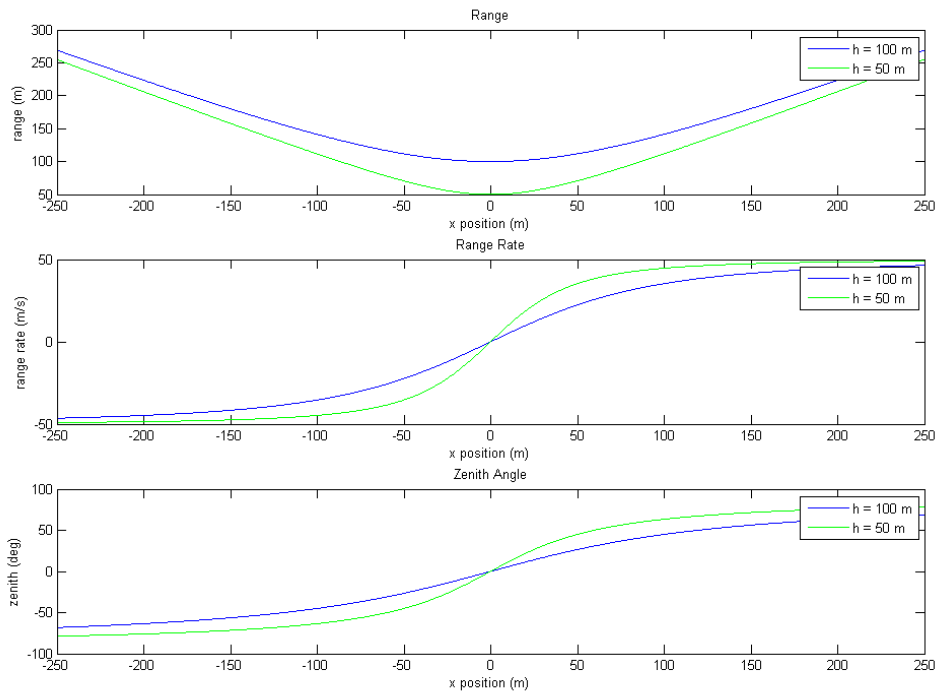
the slope is steep away from the ground station, making the measurement more sensitive to changes in x (more accurate). However, it loses accuracy directly above. There are also not unique x/range pairings, so another method must be used to determine which side of the transmitter the receiver is on. Lower values of h make the range measurement more accurate closer to the transmitter

range rate:

The slope is steep only near the transmitter, so it is not accurate at long distances. It has unique x/range rate pairings, so you can tell which side of the transmitter the receiver is. Lower values of h make the range rate measurement less accurate until the reciever is closest to the transmitter.

Zenith angle:

The slope is steep only near the transmitter, so it is not accurate at long distances. It has unique x/range rate pairings, so you can tell which side of the transmitter the receiver is. Lower values of h make the range rate measurement less accurate until the reciever is closest to the transmitter.



Hyperbolic multilateration

```
figure
hold on
color_opts = ['b'; 'g'; 'r'];
counter = 1;
for ground_station_spacing = [50 100];
    x1 = -ground_station_spacing/2; %m
    x2 = ground_station_spacing/2; %m
    r1 = sqrt((x1-x).*(x1-x) + h*h);
    r2 = sqrt((x2-x).*(x2-x) + h*h);
    d21 = r2 - r1;
    d21_dot = -(x2-x)./r2*v - -(x1-x)./r1*v;
    subplot(2,1,1)
    hold on
    plot(x, d21, color_opts(counter))
    title('Range Difference')
    xlabel('x position (m)')
    ylabel('\Delta range (m)')
    legend('50 m tx distance', '100 m tx distance')
    subplot(2,1,2)
    hold on
    plot(x, d21_dot, color_opts(counter))
    title('Range Difference Rate')
    xlabel('x position (m)')
    ylabel('\Delta range rate (m/s)')
    legend('50 m tx distance', '100 m tx distance')
    counter = counter + 1;
end
```

```

end
fprintf(['delta range:\n',...
        '\tthe slope is steep closer to the ground station, making the\n',...
        '\tmeasurement more sensitive to changes in x when it approaches \n',...
        '\tthe first transmitter.\n',...
        '\tThere are also unique x/delta-range pairings, so it is known\n',...
        '\twhere the receiver is wrt the transmitters\n',...
        '\tLarger transmitter distances result in more accuracy both between\n',...
        '\tand slightly beyond the transmitters\n',...
        'delta range rate:\n',...
        '\tThe slope is steep just as it approaches the transmitters.\n',...
        '\tIt does not have unique x/delta range rate pairings, so you cannot\n',...
        '\ttell which side of the midpoint the receiver is located.\n',...
        'Delta Range measurement seems most sufficient in this case\n'])

```

Warning: Ignoring extra legend entries.

Warning: Ignoring extra legend entries.

delta range:

the slope is steep closer to the ground station, making the measurement more sensitive to changes in x when it approaches the first transmitter.

There are also unique x/delta-range pairings, so it is known where the receiver is wrt the transmitters

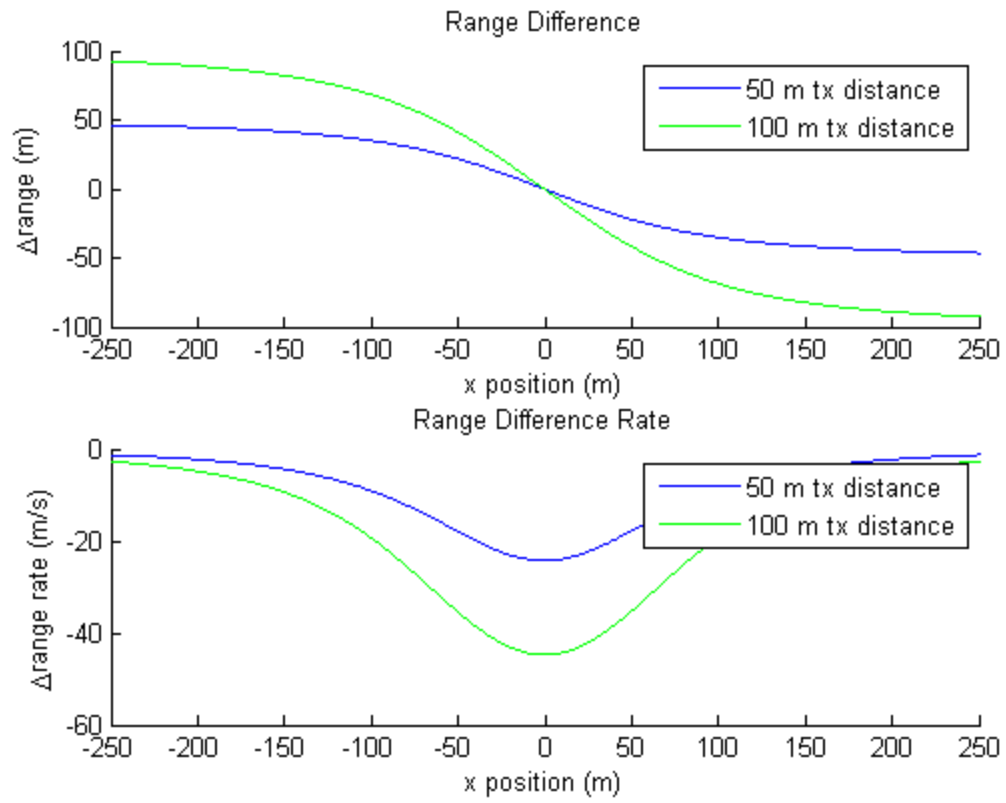
Larger transmitter distances result in more accuracy both between and slightly beyond the transmitters

delta range rate:

The slope is steep just as it approaches the transmitters.

It does not have unique x/delta range rate pairings, so you cannot tell which side of the midpoint the receiver is located.

Delta Range measurement seems most sufficient in this case



Published with MATLAB® R2013b