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# HW 8

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read\_GPSbroadcast, broadcast2xv, adjust year, and read\_rinex functions provided from class are used in this home-work.

## Initialize

```
clearvars -except function_list pub_opt
close all
c = 2.99792458e8; %m/s
f_L1 = 1575.42; % MHz
f_L2 = 1227.60; % MHz

print_vec3 = @(x) ...
    fprintf(sprintf('%13.2f\n%13.2f\n%13.2f\n',x(1),x(2),x(3)));
print_vec4 = @(x) ...
    fprintf(sprintf('%13.2f\n%13.2f\n%13.2f\n%13.2f\n',x(1),x(2),x(3),x(4)));
```

## Read the data files

```
eph = read_GPSbroadcast('brdc2550.14n');
obs_data = read_rinex_obs('test.14o');
P1 = 6;
P2 = 7;
C1 = 8;
approx_rx_pos = [-1248596.2520 -4819428.2840 3976506.0340]'; % m
GPS_Week = eph(1,19);
GPS_TOD = [1 03 00];
TOW = eph(1,20)+GPS_TOD(1)*3600 + GPS_TOD(2)*60 + GPS_TOD(3);
fprintf('RINEX location:\n')
print_vec3(approx_rx_pos)
fprintf('\n')
```

```
Parsing RINEX file test.14o
Returning data for all PRNs
```

```
ans =
```

```
1049
```

```
13
```

```
Total epochs: 131
Finished.
```

```
RINEX location:
-1248596.25
-4819428.28
3976506.03
```

## Observations at the given epoch

```
obs_at_epoch = obs_data.data(obs_data.data(:,2) == TOW, :);
prn_list = obs_at_epoch(:,3);
num_sats = length(prn_list);

% Ionosphere
iono_free_pseudorange = ...
    (f_L1*f_L1*obs_at_epoch(:,P1) - f_L2*f_L2*obs_at_epoch(:,P2))./ ...
    (f_L1*f_L1-f_L2*f_L2);

% Geometric range, satellite clock correction, relativity correction
geo_range = zeros(num_sats,1);
relativityCorr = zeros(num_sats,1);
satClkCorr = zeros(num_sats,1);
r_sat = zeros(num_sats,3);
for ii = 1:num_sats
    [~, geo_range(ii), tmp] = compute_range(eph, prn_list(ii), TOW, approx_rx_pos)
    r_sat(ii,:) = tmp';
    [~,~,~,relativityCorr(ii),satClkCorr(ii)] = ...
        broadcast2xv(eph,[GPS_Week TOW],prn_list(ii));
end

% Azimuth, Elevation
GPSvec = [2014 09 12 1 03 00];
% navfilename = generate_GPSyuma_name(GPSvec);
[navfilename,statusflag] = download_GPSyuma(GPSvec);
durationhrs = 1;
dt_sec = 3601;
ant_enu = [0 0 1];
mask_min = 0; % deg
mask_max = 90; % deg
[latgd, lon, alt] = ECEF2ellipsoidal(approx_rx_pos);

[time_wntow, GPSdata] = ...
    ASEN5090_GPSvis(navfilename, 1, GPSvec,...
        durationhrs, dt_sec, latgd*180/pi, lon*180/pi, alt,...
        mask_min, mask_max, mask_min, ant_enu, 0, []);
% rearrange the data to be in the same order as prn list
prn_el = zeros(num_sats,1);
prn_az = zeros(num_sats,1);
for ii = 1:num_sats
    prn_el(ii) = GPSdata.topo_el(prn_list(ii));
```

```

prn_az(ii) = GPSdata.topo_az(prn_list(ii));
end

T = table(prn_list, iono_free_pseudorange, geo_range, satClkCorr, ...
    relativityCorr, prn_el, prn_az);
fprintf('PRNs and corrections (distances in meters, angles in degrees):\n')
disp(T)
fprintf('\n\n\n\n\n\n')

```

Downloading GPS YUMA file from: <http://www.celstrak.com/GPS/almanac/Yuma/>  
File name: yuma0785.405504.alm

PRNs and corrections (distances in meters, angles in degrees):

<i>prn_list</i>	<i>iono_free_pseudorange</i>	<i>geo_range</i>	<i>satClkCorr</i>
18	2.1011e+07	2.1114e+07	1.032e+05
15	2.0893e+07	2.0833e+07	-60652
16	2.4701e+07	2.4642e+07	-58603
26	2.2555e+07	2.254e+07	-15544
22	2.3265e+07	2.3345e+07	80061
21	2.1027e+07	2.0912e+07	-1.1497e+05
29	2.2088e+07	2.2256e+07	1.6781e+05
27	2.4188e+07	2.4192e+07	4115.5

<i>relativityCorr</i>	<i>prn_el</i>	<i>prn_az</i>
2.6998	63.304	-83.622
2.5463	57.302	79.488
3.994	11.896	-72.048
1.0851	26.304	46.523
3.645	25.315	-104.39
-9.2211	70.773	-26.078
-0.6098	37.032	174.32
0.94731	14.817	-40.155

## Observation/Geometry matrix

```

A = ones(num_sats, 4); % x, y, z, rx time error
for ii = 1:num_sats
    A(ii,1:3) = -(r_sat(ii,:)-approx_rx_pos')./geo_range(ii);
end
A

```

A =

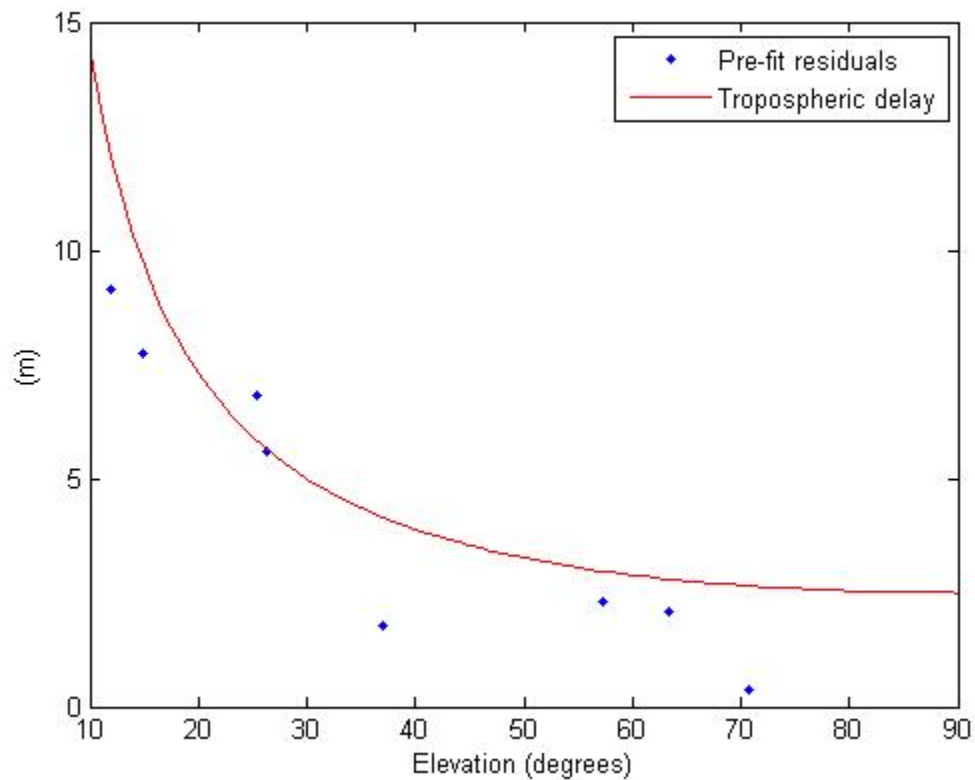
0.5998	0.5341	-0.5958	1.0000
-0.3648	0.7107	-0.6015	1.0000
0.8947	-0.2596	-0.3636	1.0000
-0.6398	0.1260	-0.7581	1.0000
0.9666	0.2398	-0.0904	1.0000
0.2792	0.4998	-0.8199	1.0000
0.1659	0.9550	0.2457	1.0000
0.5384	-0.4093	-0.7366	1.0000

## Prefit residuals

Plotting the residuals and Lecture 15's simple Tropo model vs. elevation

```
dy = iono_free_pseudorange - geo_range + satClkCorr - relativityCorr;
```

```
plot(prn_el, dy, '.')
hold on
T_el = 10:90;
plot(T_el, 2.5./sin(T_el*pi/180), 'r')
ylabel('(m)')
xlabel('Elevation (degrees)')
legend('Pre-fit residuals', 'Tropospheric delay')
```



## Least squares solution for position deviation

Find the position deviation from the RINEX location, dx

```
est_deviation = (A'*A)\A'*dy;  
est_deviation_with_T = (A'*A)\A'*(dy - 2.5./sin(prn_el*pi/180));
```

```
fprintf('Estimated Deviation (m):\n')  
print_vec4(est_deviation)  
fprintf('Estimated Deviation with Troposphere model (m):\n')  
print_vec4(est_deviation_with_T)  
fprintf('\n')
```

```
Estimated Deviation (m):  
-0.99  
-7.87  
4.60  
9.28  
Estimated Deviation with Troposphere model (m):  
-0.31  
0.27  
-0.03  
-1.27
```

## Starting from incorrect location

Choosing the center of the earth as the initial guess.

```
approx_rx_pos = [0 0 0]'; % m  
b = 0;  
for iter = 1:5  
    for ii = 1:num_sats  
        [~, geo_range(ii), tmp] = ...  
            compute_range(eph, prn_list(ii), TOW, approx_rx_pos);  
        r_sat(ii,:) = tmp';  
        A(ii,1:3) = -(r_sat(ii,:)-approx_rx_pos')./geo_range(ii);  
    end  
    dy = iono_free_pseudorange - geo_range + satClkCorr - relativityCorr ;  
    est_deviation = (A'*A)\A'*dy;  
    approx_rx_pos = approx_rx_pos + est_deviation(1:3);  
    b = est_deviation(4) + b;  
    fprintf('Iteration %d\n',iter)  
    fprintf('Estimated Deviation (m):\n')  
    print_vec4(est_deviation)  
    fprintf('New Position (m, ECF):\n')  
    print_vec3(approx_rx_pos)  
    fprintf('\n')  
end
```

```
Iteration 1  
Estimated Deviation (m):  
-1551257.50  
-5743499.33
```

```
4823759.80
1337058.30
New Position (m, ECF):
-1551257.50
-5743499.33
4823759.80

Iteration 2
Estimated Deviation (m):
289790.62
895707.68
-816001.34
47666.39
New Position (m, ECF):
-1261466.88
-4847791.65
4007758.46

Iteration 3
Estimated Deviation (m):
12850.96
28321.67
-31206.10
68.62
New Position (m, ECF):
-1248615.92
-4819469.98
3976552.35

Iteration 4
Estimated Deviation (m):
18.67
33.83
-41.72
9.28
New Position (m, ECF):
-1248597.24
-4819436.16
3976510.63

Iteration 5
Estimated Deviation (m):
-0.00
0.00
0.00
9.28
New Position (m, ECF):
-1248597.24
-4819436.16
3976510.63
```

---

```

function [time_wntow, GPSdata, GLNSS, BOTH] = ASEN5090_GPSvis(navfilename, ephemtype, .
    gpsvecstart, durationhrs, dt_sec, latgd, lon, alt, topomaskmin, topomaskmax, ...
    antmask, ant_enu, junk1, junk2)

%=====
%=====
% [time_wntow, GPSdata, GLNSS, BOTH] = GPSvis(navfilename, ephemtype, ...
%     gpsvecstart, durationhrs, dt_sec, latgd, lon, alt, topomaskmin, topomaskmax, ...
%     antmask, ant_enu, glnss, tlefilename)
%
% Predicts the number of GPS and/or Glonass satellites that will be
% visible for a specific observation site and antenna. Either YUMA
% almanacs or broadcast ephemerides can be used to propagate GPS orbits.
% Two Line Elements (TLE) sets are used to propagate Glonass satellites.
% The default Glonass TLE filename that is used is Glonass.tle.
%
%
% Author: Ben K. Bradley
% date: 02/20/2011
% Modified to remove calculations for ASEN 5090 Class 9/12
%
%
% INPUT:                Description                Units
%
% navfilename           - filename of IGS broadcast ephemeris file to use      string
% ephemtype             - ephemeris type of navfilename:          1=YUMA, 2=Broadcast
% gpsvecstart           - GPS date/time vector to start analysis      [y m d h m s]
% durationhrs           - duration of analysis                      hours
% dt_sec                - time step                                  seconds
% lat_gd               - geodetic latitude of antenna site          [-90,90] deg
% lon                  - longitude of antenna site                  [-180,180] deg
% alt                  - WGS84 ellipsoidal height (altitude) of antenna    meters
% topomaskmin           - topographic minimum elevation (wrt horizon)      deg
% topomaskmax           - topographic maximum elevation (wrt horizon)      deg
% antmask               - antenna elevation mask (wrt antenna)          deg
% ant_enu               - boresight direction of antenna in east-north-up unit vector [E;
% glnss                 - boolean: 1=include Glonass, 0=don't include Glonass
% tlefilename           - filename of Glonass TLE file to use
%
%
% OUTPUT:
%
% NOTE: for outputs with 32 columns, the column number corresponds to
%       the PRN number of the GPS satellite (i.e. each row is a specific
%       time and each column is a specific satellite)
%
% time_wntow           - week number and tow for all computations [WN TOW] (nx2)
% GPSdata              - structure of GPS results. structure is below
% GLNSS                - structure of Glonass results. structure is below
% BOTH                 - structure of GPS/Glonass combined results
%
%

```

---

---

```

%      topo_numsats: number of satellites above topomask          (nx1)
%      topo_az: topocentric azimuth of satellites                (nx32)
%      topo_el: topocentric elevation of satellites              (nx32)
%      vis: flag for satellite visible (nx32)
%      ant_numsats: number of satellites above antenna mask      (nx1)
%      ant_el: satellite elevation wrt antenna                   (nx32)
%      DOP: structure containing DOPs:  .GDOP  .HDOP  each (nx1)
%                                           .VDOP  .PDOP
%                                           .TDOP
%
%
% Coupling:
%
%   lla2ecef      read_GPSbroadcast
%   gpsvec2gpstow broadcast2xva
%   ecef2azelrange2 sez2ecef
%   gpsvec2utc    utc2utc
%   init_EOP      get_EOP
%   alm2xv        read_TLE
%   tle2rv        teme2ecef
%
% References:
%
%   none
%
%=====
%=====

% Compute ECEF Position of Antenna Location =====
r_site = lla2ecef(latgd, lon, alt*0.001);

r_site = r_site' * 1000;  % [x y z] meters

% Compute boresight direction of antenna in ECEF =====
ant_ecef = sez2ecef(latgd,lon, [-ant_enu(2) ant_enu(1) ant_enu(3)]);

% Open GPS Ephemeris File and create ephemeris matrix =====

if (ephemtype == 1) % YUMA
    ephem_all = read_GPSyuma(navfilename);
elseif (ephemtype == 2) % Broadcast
    ephem_all = read_GPSbroadcast(navfilename);
end

% Create GPS time series =====

% Convert GPS date/time start to week number and time of week

```

---



---

```

[WN0, TOW0] = gpsvec2gpstow( gpsvecstart );

    % WN0  = week number count from 22Aug99
    % TOW0 = time of week, seconds

TOWseries = (TOW0: dt_sec : TOW0+durationhrs*3600)';
elapsed   = TOWseries - TOW0;

sz = length(TOWseries);

time_wntow = [WN0*ones(sz,1)    TOWseries];

    % time_wntow = [WN  TOW]  % Week numbers and Time of Weeks


% Initialize Variables =====

% GPS -----
prnlist = 1:32;

Xpos = zeros(sz,32) * NaN;
Ypos = Xpos;
Zpos = Xpos;

GPSdata = struct;

GPSdata.topo_numsats = zeros(sz,1);
GPSdata.topo_az      = zeros(sz,32) * NaN;
GPSdata.topo_el      = zeros(sz,32) * NaN;
GPSdata.ant_numsats  = zeros(sz,1);
GPSdata.ant_el       = zeros(sz,32) * NaN;
GPSdata.DOP.HDOP     = zeros(sz,1)  * NaN;
GPSdata.DOP.VDOP     = zeros(sz,1)  * NaN;
GPSdata.DOP.PDOP     = zeros(sz,1)  * NaN;
GPSdata.DOP.TDOP     = zeros(sz,1)  * NaN;
GPSdata.DOP.GDOP     = zeros(sz,1)  * NaN;
% -----

GLNSS = [];
BOTH  = [];


% Compute GPS Visibility =====
% =====

for nn = prnlist % Loop through satellite list -----

    if (ephemtype == 1) % YUMA
        [health,state] = alm2xv(ephem_all,time_wntow,nn);

```

---

---

```

elseif (ephemtype == 2) % Broadcast
    [health,state] = broadcast2xva(ephem_all,time_wntow,nn);
end

Xpos(:,nn) = state(:,1); % column number = PRN number
Ypos(:,nn) = state(:,2); % meters ECEF
Zpos(:,nn) = state(:,3);

for tt = 1:sz % loop through all times -----

    if (health(tt) ~= 0) % satellite is unhealthy

        Xpos(tt,nn) = NaN; % get rid of unhealthy states
        Ypos(tt,nn) = NaN;
        Zpos(tt,nn) = NaN;

    else

        % Compute topocentric azimuth and elevation
        [GPSdata.topo_az(tt,nn),GPSdata.topo_el(tt,nn)] = ASEN5090_ecef2azelra

        % az,el = degrees
        % If the satellite is not visible, set the az and el to NaNs or zero h
        % CLOUSE: just NaN stuff with elevations below the min-mask
        GPSdata.topo_az(GPSdata.topo_el < topomaskmin) = NaN;
        GPSdata.topo_el(GPSdata.topo_el < topomaskmin) = NaN;

    end % END of satellite health

end % END of time loop -----

end % END of PRN loop -----

% PUT IN YOUR CALCULATIONS FOR VISIBLE SATELLITES HERE:

% =====
for tt = 1:sz

    % GPS -----

    % Number of Visible GPS Satellites
    % -----
    % Put in logic here to calculate the number visible
    % GPSdata.ant_numsats(tt) = ???;
    GPSdata.ant_numsats(tt) = sum(GPSdata.topo_el(tt, :)>topomaskmin);

```

---

---

end

%=====

## CLOUSE: sort the planes the PRNs are on,

```
planes = []; planes2prns = zeros(32,2); tol = 0.1; for prn=1:31 RAAN =  
ephem_all(prn,6); plane_found = 0; for plane = 1:length(planes) if planes(plane)-tol <  
RAAN < planes(plane)+tol plane_found = 1; planes2prns(ephem_all(prn,1),1)=RAAN*180/  
pi; planes2prns(ephem_all(prn,1),2)=ephem_all(prn,1); break end end if plane_found con-  
tinue end planes = [planes RAAN]; planes2prns(ephem_all(prn,1),1)=RAAN*180/pi;  
planes2prns(ephem_all(prn,1),2)=ephem_all(prn,1); end planes2prns sortrows(planes2prns,1)
```

%=====

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```
function [range0, range1, r_gps] = compute_range(eph, PRN, t, userpos)

fcnPrintQueue(mfilename('fullpath'))
c = 2.99792458e8; %m/s
w = 7292115.0e-11; %rad/s Earth spin rate

GPS_Week = eph(1,19);

% Get the GPS SV vector
[~, r_gps,~,~,~] = broadcast2xv(eph,[GPS_Week t],PRN);
r_gps = r_gps'; % Vertical vectors
R = norm(r_gps-userpos);
range0 = R; % Uncorrected

% Iterate to correct the range for TOF
tol = 1e-6;
oldR = R + 1;
while abs(R-oldR) > tol

Tt = t - R/c;

[~, r_gps_Tt,~,~,~] = broadcast2xv(eph,[GPS_Week Tt],PRN);
r_gps_Tt = r_gps_Tt'; % Vertical vectors

phi = w*(t-Tt);

C = [cos(phi) sin(phi) 0;
     -sin(phi) cos(phi) 0;
     0 0 1];

r_gps = C*r_gps_Tt;

oldR = R;

R = norm(r_gps-userpos);

end

range1 = R;
```

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