



INDEX

Design and control of a DC electrical drive	2
Exercise text	2
Characteristics of machine	2
Development	4
Parameter Identification	4
Simulink Models	6
-Machine models	6
Mechanical model	6
-Control models	6
Current controller	6
Speed controller	8
Flux weakening	9
Excitation controller	9
-Complete scheme	11
Results	12
-Speed behaviour	12
Remark	12
-Excitation behaviour	13
Remark	13
-Torque behaviour	14
-Armature behaviour	15
Remark	15



EXERCISE 2

Design and control of a DC electrical drive

Exercise text

1. Find the design parameters of a DC independent excited motor that moves a tramway vehicle

Characteristics of machine

Quantity	Symbol	value	u.o.m
Motor rated voltage	V_n	600	V
Motor rated speed	ω_n	314	rad/s
Efficiency	η	0.9	
Armature circuit time constant	τ_a	10	ms
Excitation rated voltage	V_{en_n}	120	V
Excitation rated current	I_{en_n}	1	A
Excitation time constant	τ_e	1	s
Acceleration time	t_{acc}	25	s
Tramway mass	M_{tram}	10000	Kg
Reached speed	V_{reac}	60	km/h
Total people	peo_tot	80	/
People mass	M_{peo}	80	Kg

The tramway should accelerate from 0 to 60 km/h in 25 s. The tramway mass is 10 T and you should consider 200 people as the tramway trainload with a standard weight of 80 kg.



The friction force is proportional to the speed and at rated speed (60 km/h or 314 rad/s) is $\frac{1}{3}$ of traction force.

2. Design and simulate a DC electrical drive with speed and current control in order to cover a 10 km track considering the following data.

NB : the slope is defined as $s\% = 100 \cdot \tan \phi$

Track (km)	Slope %	Speed (Km/h)
0-1	0	35
1-3	0	60
3-4	5	60
4-6	0	75
6-8	0	60
8-9	-5	60
9-10	0	35



Development

Required specifics:

1. Armature time constant = 10 ms;
2. Excitation time constant = 1 s;
3. Acceleration to reach 60 Km/h from 0 Km/h in 25 seconds.

Parameter Identification

Considering the system and the energy balance is possible to define :

Name	Symbol	Equation	Computation	Value	U.O.M
Total mass	M _t	M _{tram} +M _{peo} *peo _{tot}	(100000 + 200*80)	26000	kg
Max Linear Speed	V _{max}		60/3.6	16.7	Km/h
Average acceleration	a _{ave}	V _{max} /t _{acc}	16.7/25	0.668	m/s ²
Traction force	F _{traction}	M _t *a _{ave}	26000*0.668	17333	N
Traction power	P _{traction}	F _{traction} *V _{max}	17333*16.7	288.9	kW
Friction Force	F _{friction}	F _{traction} /3	17333/3	5777.7	N
Friction power	P _{friction}	F _{friction} *V _{max}	5777.7*16.7	96.5	kW
Total Power	P _{tot}	P _{traction} +P _{friction}	288.9+96.5	385.4	kW
Armature Nominal current	I _{an_n}	P _{tot} /(η*V _n)	385.4/(0.9*600)	713.306	A
Nominal torque	T _n	P _{tot} /W _n	385.4/314	1226	N*M
Torque coefficient	K	T _n /(I _{an_n} *I _{en_n})	1226/(713.306*1)	1.7189	A
Armature Resistance	R _a	((1-η)*V _n)/I _{an_n}	(0.1*600)/713.306	0.084	Ω
Armature Inductance	L _a	R _a *τ _a	0.084*10	841	μH
Excitation Resistance	R _e	V _{en_n} /I _{en_n}	120/1	120	Ω
Excitation Inductance	L _e	R _e *τ _e	120/1	120	H



POLITECNICO DI MILANO
AUTOMATION AND CONTROL ENGINEERING

Ribolla Gabriele 10617369

5

Equivalent Inertia	Jeq	$M_t \cdot V_{\max}^2 / W_n^2$	$260000 \cdot 16.7^2 / 314^2$	73.174	Kgm ²
Conversion constant rad/s to m/s	C1	/	16.7/314	0.0531	(m/s)/(rad/s)
Conversion constant m/s to rad/s	C2	/	314/16.7	18.8039	(rad/s)/(m/s)
Conversion constant Km/h to rad/s	C3	/	314/60	5.2333	(rad/s)/(Km/h)
Anti Windup	ant_win	/	/	10	/

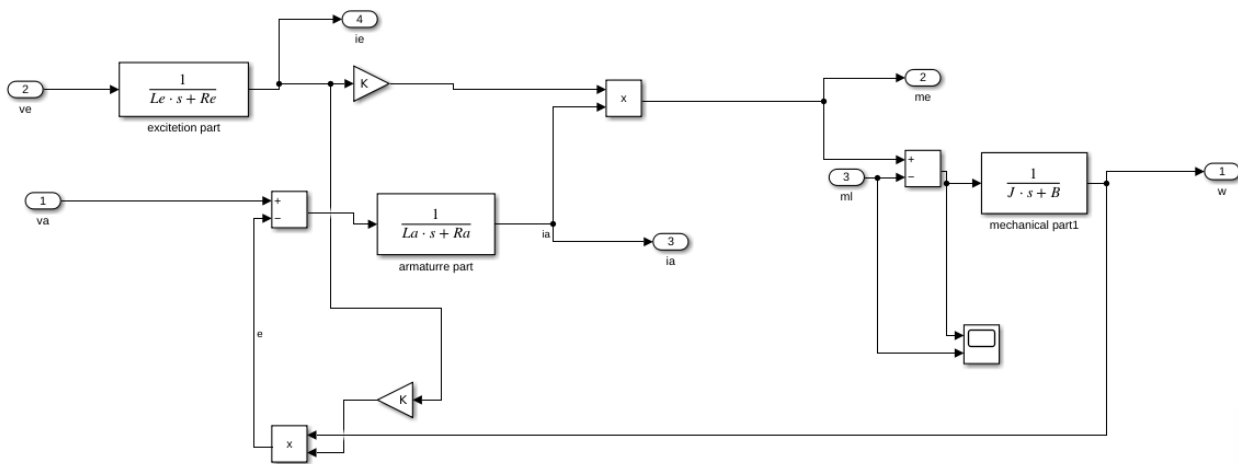


Simulink Models

-Machine models

They represent the dynamic model of the DC machine.

*Mechanical model



NB: B is used for the frictions

-Control models

The scope of the controller is to generate a control law to follow the system constraint required.

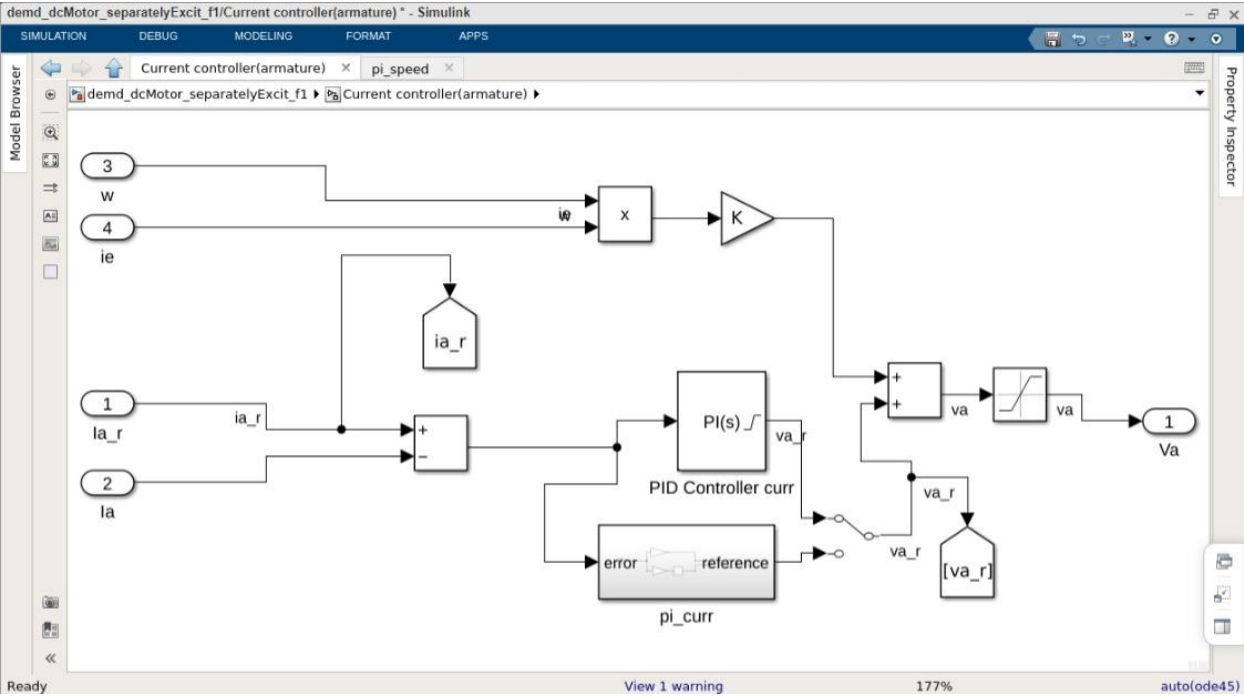
From the theory, it is known that the SE DC machine can be controlled using 2 decoupled regulators, one for the speed and one for the current.

The 2 regulators have 2 different time constants, in particular the speed controller is slower with respect to the current one.

*Current controller

The Frequency transfer function controlled by this regulator is given by $1/(R_a + s \cdot L_a)$.

The values considered for the phase margin and the band frequency are:



Name	symbol	value	U.O.M
Frequency band	B_wia	200	rad/s
Phase_margin	M_phase_ia	75	degree

So, it is possible to define for the PI controller the following coefficients

Name	symbol	value	U.O.M
Proportional coefficient armature	kp_ia	0.1676	/
Integral coefficient armature	ki_ia	16.7598	/

Remembering that the PI structure is give by

$$PI = kp + ki/s$$

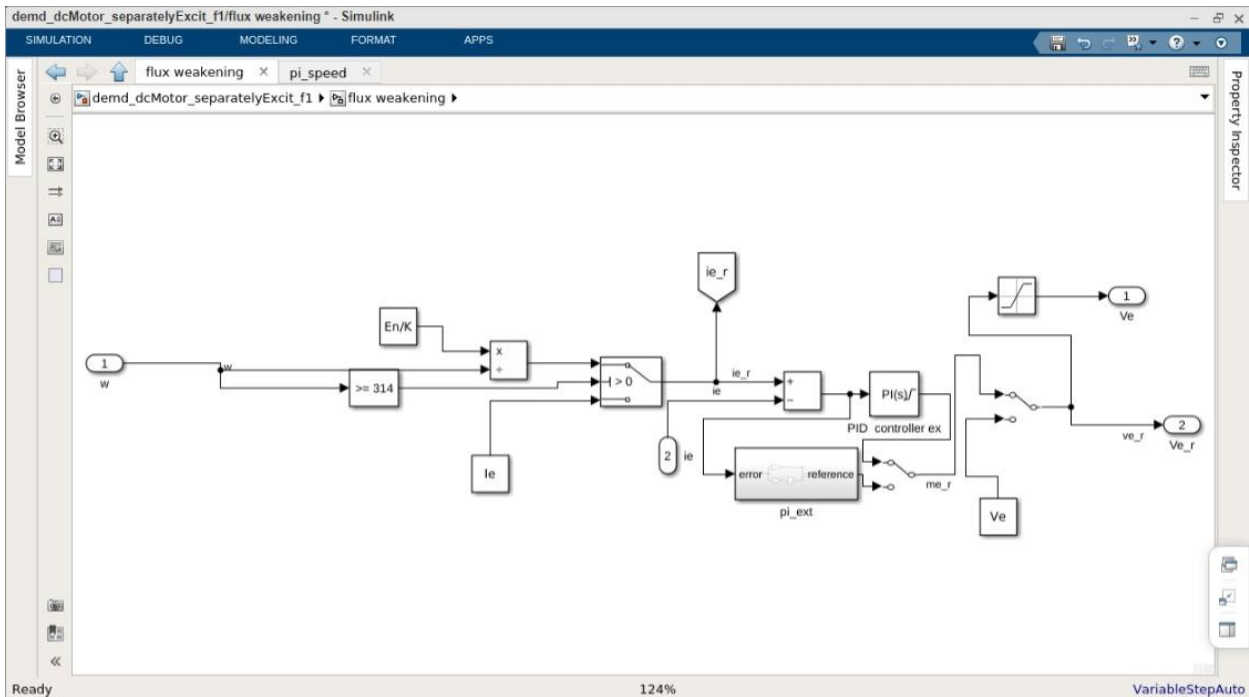


*Flux weakening

It helps us to go above the nominal speed of the machine (≈ 60 km/h). In particular the speed that the tram has to reach is equal to 75 km/h.

So, to do that, for speed > 60 Km/h, the excitation current considered will be $E_n/(\Omega \cdot K)$, where $E_n = V_n \cdot \eta = 540$ V. Doing this the power for speed greater of 60 Km/h (Ω_b) the power remains constant equal to $T_e \cdot \Omega_m$, because T_e decreases proportional to $1/\Omega_m$. It is important for that point to add an excitation controller

*Excitation controller



The frequency transfer function that this controller has to control is given by $1/(R_e + s \cdot L_e)$.

The values considered for the phase margin and the band frequency are:

Name	symbol	value	U.O.M
Frequency band excitation	B_wie	1	rad/s
Phase_margin excitation	M_phase_ie	75	degree



So, it is possible to define for the PI controller the following coefficients

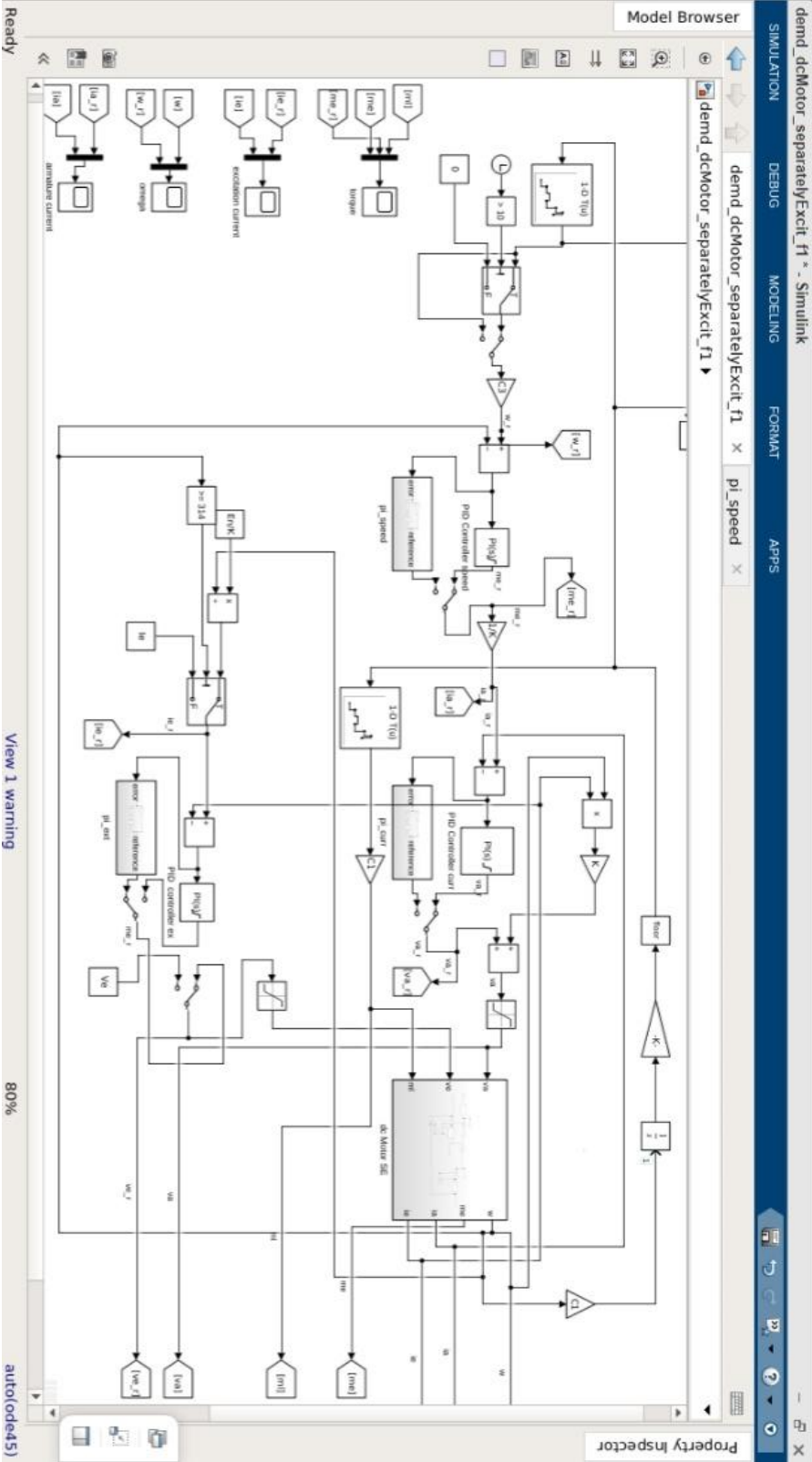
Name	symbol	value	U.O.M
Proportional coefficient excitation	kp_ie	2400	/
Integral coefficient excitation	ki_ie	2400	/

NB: The anti windup regulator has the saturation limits equal to:

Name	symbol	value	U.O.M
Minimum Excitation Voltage	Ve_min	0	V
Maximum Excitation Voltage	Ve_max	Ve_n	V



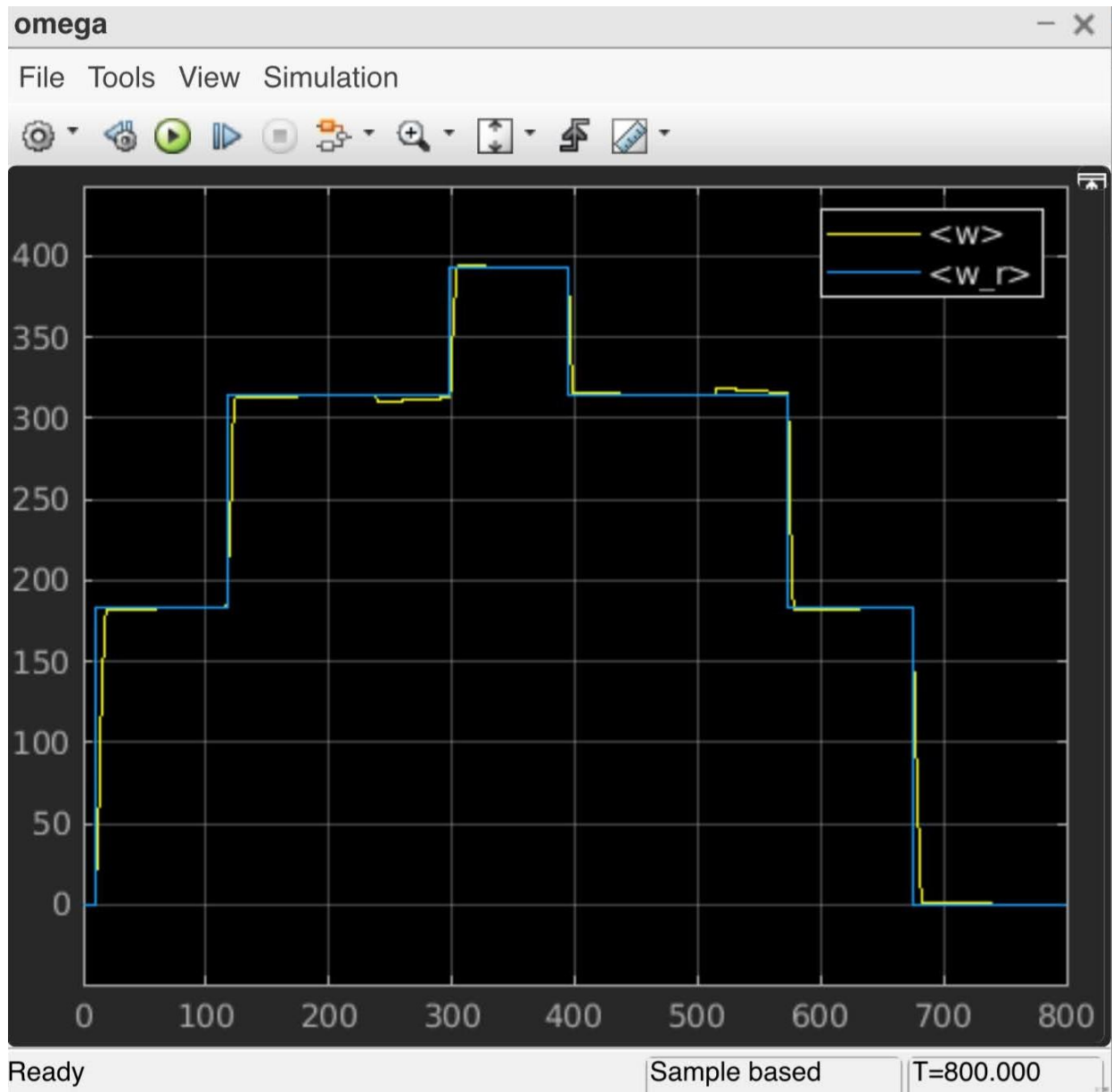
-Complete scheme





Results

-Speed behaviour

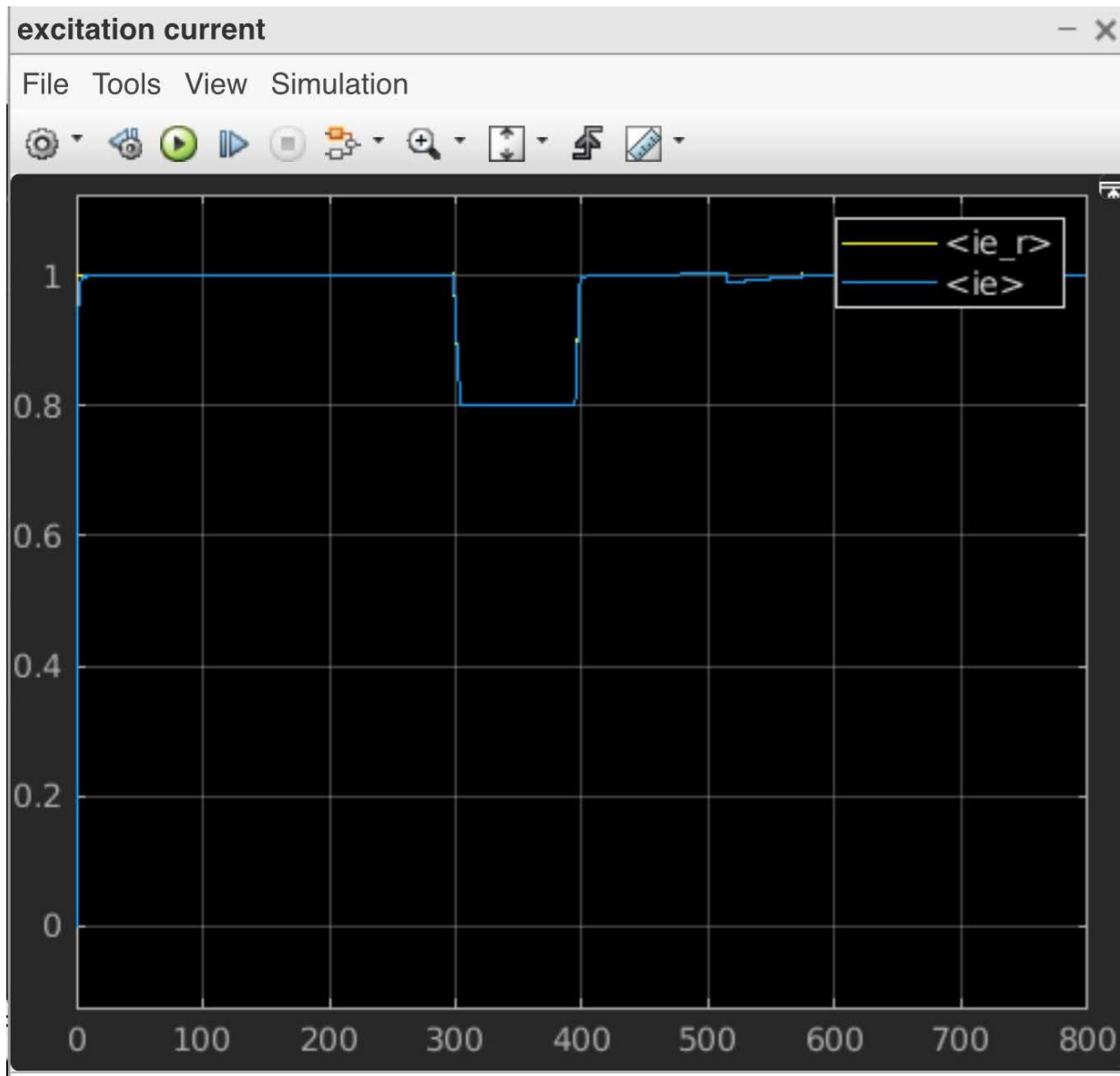


Remark

It is possible to notice that the control unit permits the machine to follow with a high accuracy the speed given as reference. The peak is reached thanks to the flux weakening because the value of the speed in that point is greater than the base speed.



-Excitation behaviour

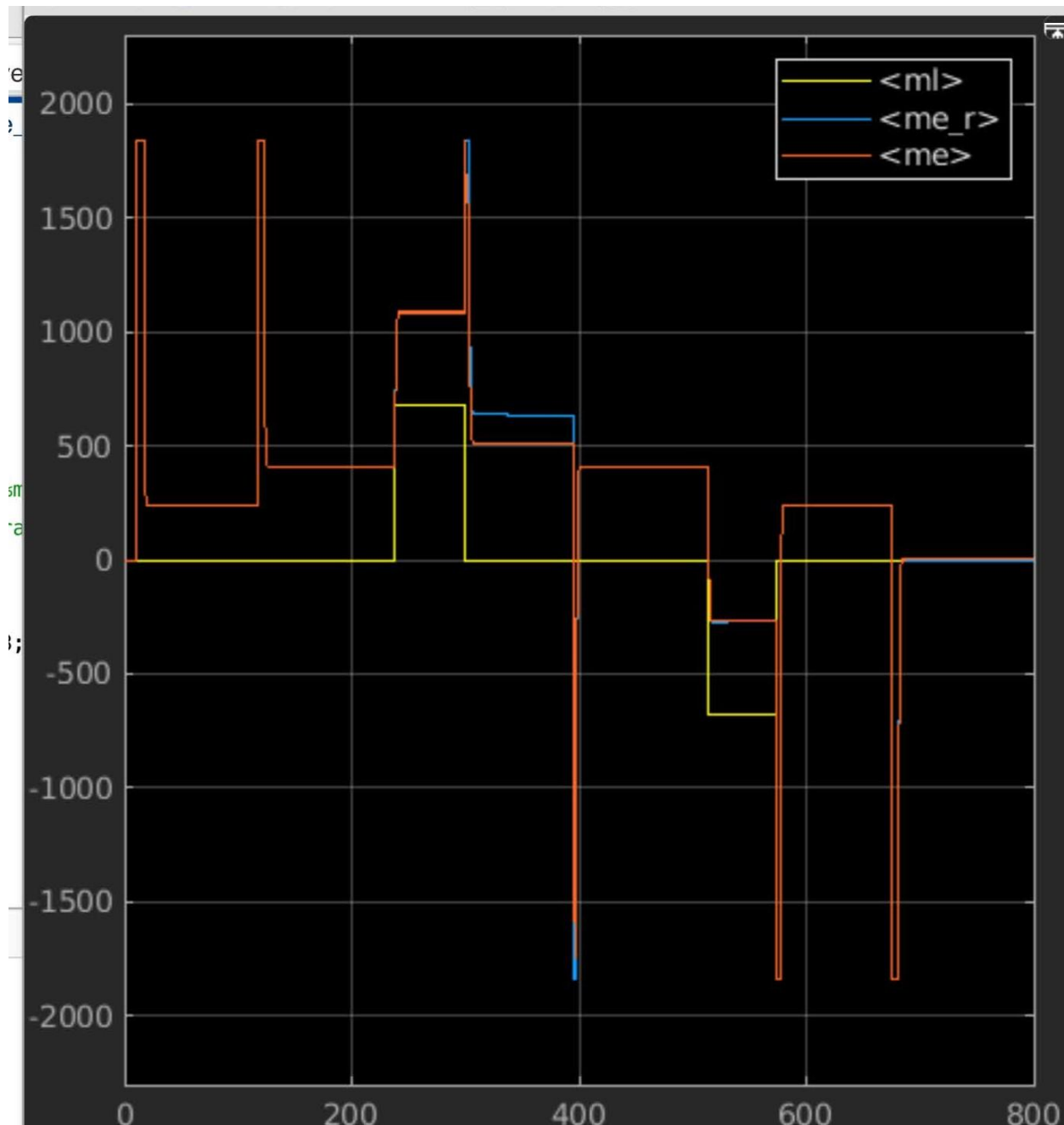


Remark

It is possible to notice a decrease of the excitation current due to the flux weakening, that helps to go above the base speed.

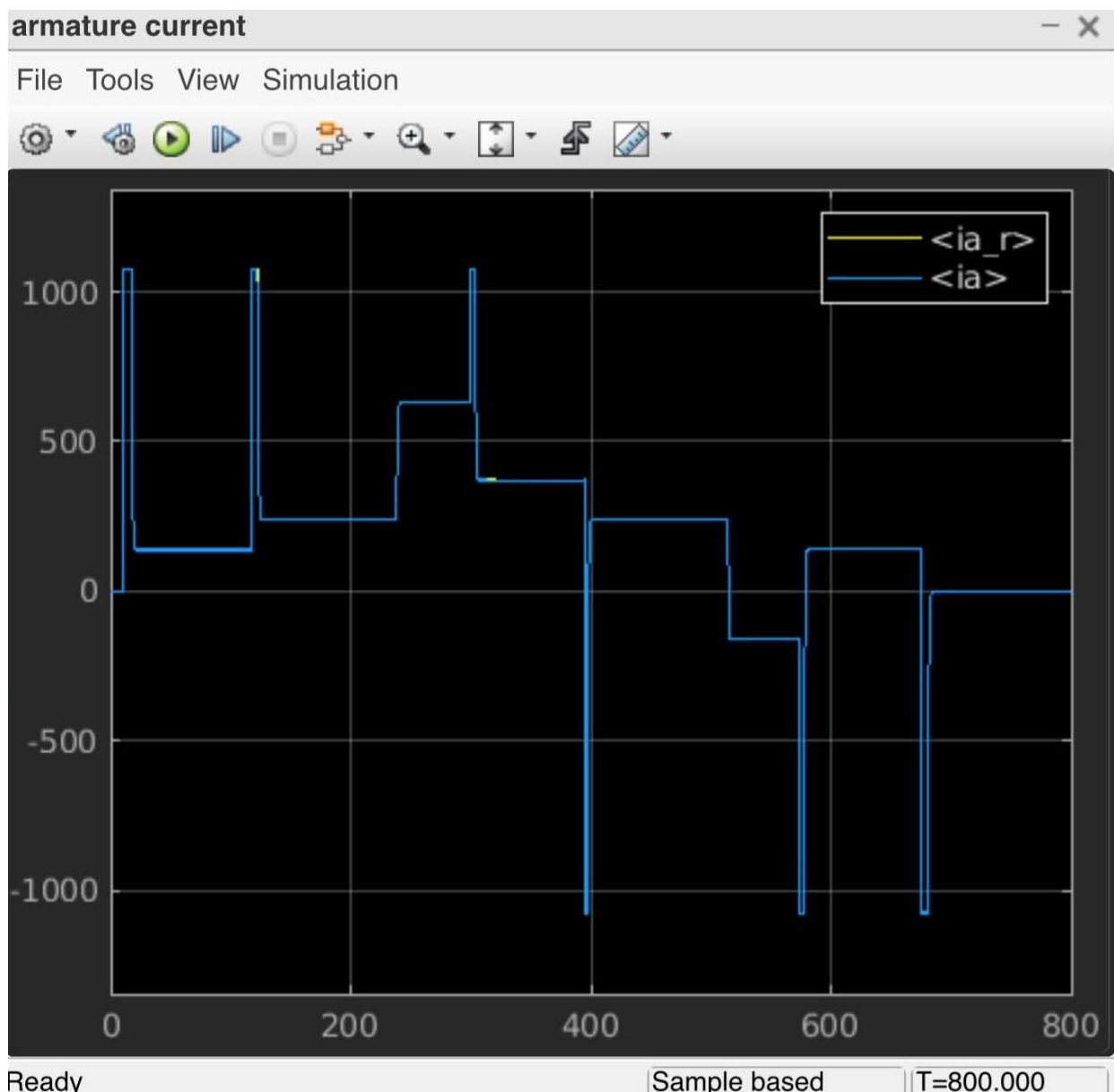


-Torque behaviour





-Armature behaviour



Remark

It is possible to notice that the torque and the armature current have the same behaviour, this is correct because the torque is directly depending on the armature current.

These quantities change with respect to the need of the machine to accelerate, maintain the same speed or decelerate.