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# Cryptography: Symmetric Key Establishment

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# Key management

- In a secured communication, users must setup the details of the cryptography
  - In some cases this may require sharing a symmetric key
  - In others it may require obtaining the other party's public key
- In both cases, an issue is how to securely distribute these keys
  - in case of symmetric key
    - must be exchanged over a secure communication channel
      - both confidentiality and data authentication must be guaranteed
  - in case of public key
    - keys can be openly exchanged (authenticated) over an insecure communications channel
      - only message authentication must be guaranteed
        - » the exchange is less troublesome
        - » for example, by using digital certificates
- Often secure systems fail due to a break in the key distribution

# Long-term vs Short-term Keys

- Cryptographic system and protocols usually deal with two types of keys with two different lifetimes:
  - **short-term keys**
    - also called as session keys
    - used to secure a communication
      - data confidentiality
      - data authentication and integrity
    - used only for a limited interval of time
    - setup through a proper KE protocol
  - **long-term keys**
    - also referred to as long-term secrets
    - can be used for
      - peer authentication
      - securing key exchanges

# (Secret) Key establishment

- Secret key establishment is a process or protocol whereby a shared secret becomes available to two or more parties, for subsequent cryptographic use
- Two approaches are possible:
  - **Key pre-distribution**
    - key establishment schemes whereby the resulting established keys are completely determined “a priori” by initial keying material
      - used mainly only for long-term secret keys
  - **Dynamic key establishment (or key exchange)**
    - those schemes whereby the key established by a pair (or group) of users varies on subsequent executions
    - subdivided into (see later):
      - key transport
      - key agreement

## Key establishment (cont.)

- Dynamic key establishment may be broadly subdivided into:
  - **key transport**
    - A key transport protocol or mechanism is a key establishment technique where one party creates or otherwise obtains a secret value, and securely transfers it to the other(s)
  - **key agreement**
    - A key agreement protocol or mechanism is a key establishment technique in which a shared secret is derived by two (or more) parties as a function of information contributed by, or associated with, each of these, (ideally) such that no party can predetermine the resulting value
- Additional variations exist, including various forms of key derivation and key update

# Use of trusted servers

- Some key establishment protocols involve a centralized or trusted party, for either or both:
  - **initial system setup**
  - **on-line actions (involving real-time participation)**
- This party is referred to by a variety of names depending on the role played
  - **generically called as trusted third party or trusted server**
- E.g.
  - **authentication server**
  - **key distribution center (KDC)**
  - **certification authority (CA)**

# Properties of key establishment

- Properties that a KE protocol may satisfy:
  - **Entity authentication**
    - a party in a key establishment protocol is able to determine the true identity of the other(s) which could possibly gain access to the resulting key
  - **Implicit Key authentication**
    - is the property whereby one party is assured that no other party aside from a specifically identified second party (and possibly additional identified trusted parties) may gain access to a particular secret key
      - the other protocol participant is the only other party that could possibly be in possession of the correct established key
  - **Key confirmation**
    - is the property whereby one party is assured that a second (possibly unidentified) party actually has possession of a particular secret key
  - **Explicit key authentication**
    - both implicit key authentication and key confirmation hold
      - an identified party is known to actually possess a specified key
- A KE protocol is usually called "Authenticated Key Exchange" (AKE) if both entity authentication and explicit key authentication are provided
- In addition:
  - **Key freshness assurance**
    - assurance that the exchanged key is new

# Forward secrecy and known-key attacks

- It is important to consider the potential impact of compromise of various types of keying material
  - **even if such compromise is not normally expected**
- In particular, the effect of the following is often considered:
  - **compromise of past session (established) keys**
  - **compromise of long-term secret (symmetric or asymmetric) keys**
- A protocol is said to be "resistant to a known-key attack" if compromise of past session keys doesn't allow an adversary to compromise future session key exchanges
- A protocol is said to have "(perfect) forward secrecy" if compromise of long-term keys does not compromise past session keys
  - **example: Diffie-Hellman key agreement, in some cases, may provide forward secrecy**



# Key transport and derivation using symmetric cryptography

# Point-to-point key transport and key derivation

- Key transport or derivation based on a long-term symmetric key  $K_{ab}$  shared “a priori” by two parties A and B
  - **the long-term key must be initially distributed over a secure channel or resulting from a key pre-distribution mechanism**
  - **the long-term key is used to establish new session keys  $K_s$** 
    - KE protocol (transport/derivation):  $K_{AB} \rightarrow K_S$
- Possible techniques:
  - **key transport based on symmetric encryption**
  - **key derivation based on non-reversible functions**
- Variants:
  - **key transport with one pass**
  - **key transport with challenge-response**

# Key transport

- Key transport with one pass:

$$A \rightarrow B : E_{Kab}(K_S)$$

- both A and B obtain implicit key authentication
- susceptible to known-key attacks through replay attack

- Additional optional fields might be transferred in the encrypted portion:

$$A \rightarrow B : E_{Kab}(K_S, t_A^*, B^*)$$

- field containing redundancy provides explicit key authentication to B and facilitates message modification detection
- timestamp (or sequence number) provides a sort of freshness guarantee to B
  - avoids replay attacks
- a destination identifier prevents message replay back on A
  - if a timestamp is present it provides also entity authentication to B

## Key transport (cont.)

- Key transport with challenge-response:
  - If anti-replay, explicit key authentication, and entity authentication are desired for B but reliance on timestamps added by A is not, a random value or sequence number  $n_B$  may be used
  - the cost is an additional message

$$A \leftarrow B : n_B$$

$$A \rightarrow B : E_{K_{ab}}(K_S, n_B, B^*)$$

- If it is required that the session key  $K_S$  be a function of inputs from both parties and mutual authentication:

$$A \leftarrow B : n_B$$

$$A \rightarrow B : E_{K_{ab}}(k_1, n_A, n_B, B^*)$$

$$A \leftarrow B : E_{K_{ab}}(k_2, n_B, n_A, A^*)$$

- $K_S = f(k_1, k_2)$

## Key transport (cont.)

- Vulnerabilities:
  - **Any previous exchange does not offer forward secrecy**
    - they fail if the long-term key  $K_{ab}$  is compromised
    - for this reason they may be inappropriate for many applications
- Note:
  - **Authentication protocols which employ encryption, including the above key exchange schemes, may require that the encryption function has a built-in data integrity mechanism to detect message modification**
    - i.e. Authenticated Encryption (AE)

# Key derivation

- Key exchange may be achieved also by dynamic key derivation where the derived session key is based on per-session random input provided by one party

$$A \rightarrow B : r_A$$

- **single message**
  - **the session key is computed as  $K_S = f_{Kab}(r_A)$** 
    - where  $f$  is a cryptographic function, like  $E_K()$  or  $MAC_K()$
  - **provides to both A and B implicit key authentication**
  - **susceptible to known-key attacks through replay attack**
- The random number  $r_A$  here may be replaced by other time-variant parameters
    - **e.g. a timestamp  $t_A$ , provides an implicit key freshness property**
      - avoids replay attack to B
      - avoids A can force a given key X

## Key derivation (cont.)

- In general is preferred a keyed one-way function (like  $\text{MAC}_K()$ ) for  $f_K()$ , in place of an encryption function  $E_K()$ 
  - **A cannot control the value of  $K_S$**
- The simple key derivation scheme can be further extended with two or three passes in order to provide:
  - **contribution of B to the creation of  $K_S$**
  - **mutual entity authentication**

# Example of authenticated key derivation protocol

- Authenticated Key Exchange Protocol AKEP2
  - provides mutual entity authentication, key freshness guarantee, and implicit key authentication
  - A and B exchange 3 messages
- *Setup:*
  - A and B share long-term symmetric keys  $K_{ab}$ 
    - $A \rightarrow B : r_A$
    - $A \leftarrow B : X_B = \{B, A, r_A, r_B\}, \text{MAC}_{K_{ab}}(X_B)$
    - $A \rightarrow B : X_A = \{A, r_B\}, \text{MAC}_{K_{ab}}(X_A)$
  - $K_S = f_{K'}(r_B)$ 
    - where  $f_{K'}()$  is a keyed one-way function or encryption function
    - $K'$  is the key used to derive  $K_S$ , usually obtained from  $K_{ab}$



# Key transport using asymmetric cryptography

# Key transport based on public-key encryption

- One party may choose a symmetric key and transfer it to a second, using that party's encryption public key

$$A \rightarrow B : \{ K_s \}_{KU_B}$$

- **this provides (implicit) key authentication to the originator (A)**
  - only the intended recipient has the private key allowing decryption
  - the originator (A) obtains neither entity authentication nor key confirmation
- **the second party (B) has no assurances regarding the source of the key and the timeliness**
  - even if A sends to B:  $\{K_s, A, T_A\}_{KU_B}$ , since  $KU_B$  is public
- **such additional assurances may be obtained through use of further techniques including:**
  - additional messages, with public-key encryption
    - using challenge-response like key transport based on symmetric key
  - digital signature

# Key transport using public-key encryption and signature

- Encryption and signature primitives may be used to provide respectively:
  - **privacy of keying material**
  - **source authentication**
- Some possible approaches:
  - **sign the key and separately public-key encrypt the (unsigned) key**
  - **sign the key, then public-key encrypt the signed key**
  - **public-key encrypt the key, then sign the encrypted key**

# Key transport using public-key encryption and signature in one-pass

- Encrypting and signing separately:

- **An option is to sign the key and encrypt the key:**

$$A \rightarrow B: \{A, K_s, t_A^*\}KU_B, \text{Sign}_A(B, K_s, t_A^*)$$

- Encrypting signed keys:

- **A variation is to encrypt signed blocks:**

$$A \rightarrow B: \{A, K_s, t_A^*, \text{Sign}_A(B, K_s, t_A^*)\}KU_B$$

- Signing encrypted keys:

- **In contrast to encrypting signed keys, one may sign encrypted keys**

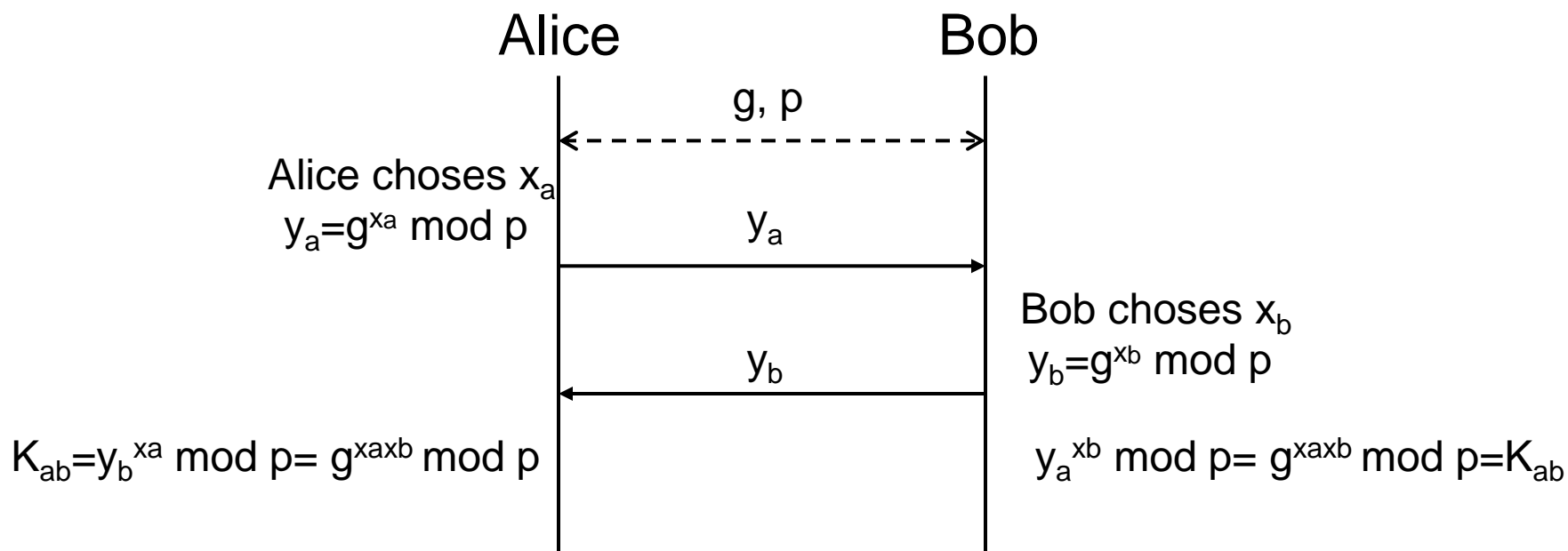
$$A \rightarrow B: t_A^*, Q, \text{Sign}_A(B, t_A^*, Q)$$

where  $Q = \{A, K_s\}KU_B$

# Key agreement using asymmetric cryptography

# Diffie-Hellman key exchange

- The first publicly known public-key agreement protocol was the Diffie-Hellman exponential key exchange

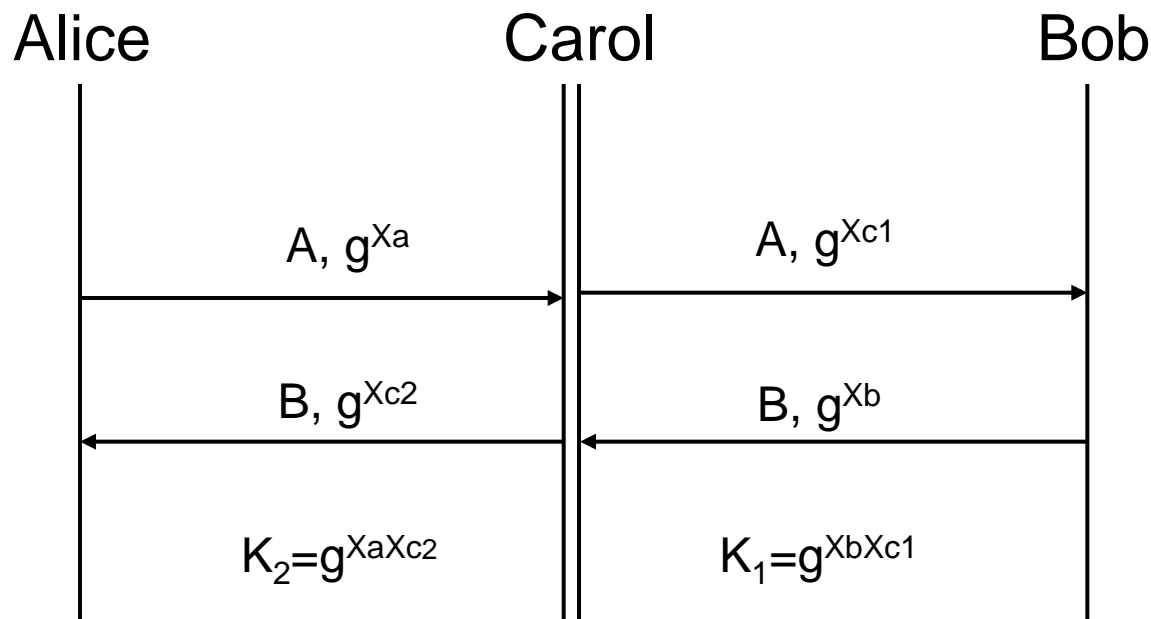


# DH modes

- Different ways of using DH:
  - **Fixed Diffie-Hellman**
    - each party already has the public part (DH public key) of the other entity
  - **Anonymous Diffie-Hellman**
    - DH exchange
    - susceptible to Man-in-the-Middle attacks
  - **Ephemeral Diffie-Hellman (EDH)**
    - authenticated DH exchange
- Elliptic Curve variant:
  - **Elliptic Curve DH (ECDH) uses elliptic curves instead of the multiplicative group of integers modulo  $p$**

# Diffie-Hellman Vulnerability (MITM attack)

- Anonymous Diffie-Hellman key exchange, does not provide authentication of the parties, and is thus vulnerable to Man-in-the-middle attacks
  - a third party C may run two separate exchanges with A and B, convincing the two peers that the exchange ended successfully between them



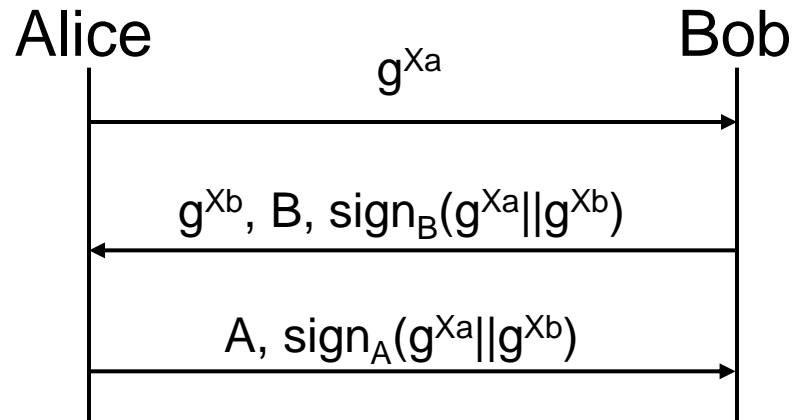


# Authenticated DH Exchange

- A wide variety of schemes and protocols have been developed to provide authenticated DH key agreement to prevent man-in-the-middle and related attacks
- These methods generally use:
  - **Public/private key pairs**
  - **Shared secrets**

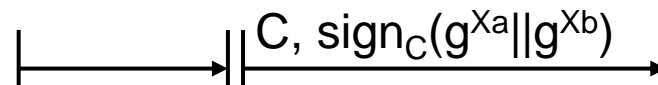
# Authenticated DH Exchange (cont.)

- The simplest way to authenticate the DH exchange could be to sign the DH exponentials



➤ **It does not guarantee implicit key authentication nor confirmation**

- the authenticated entity may be different from the peer that exchanged the secret key
  - a third party  $C$  can convince  $B$  that the exchange was run with  $C$ , by simply replacing the third message with:



- this attack does not result in a breach of secrecy of the key

# Authenticated DH Exchange (cont.)

- Solution: uses signature and Enc

- **variant of Station-to-Station (STS) protocol**

$A \rightarrow B: g^{Xa}$

$A \leftarrow B: g^{Xb}, E_{K_S}(B \parallel \text{Sign}_B(g^{Xa} \parallel g^{Xb}))$

$A \rightarrow B: E_{K_S}(A \parallel \text{Sign}_A(g^{Xa} \parallel g^{Xb}))$

- Solution: uses signature and MAC

- **SIGMA Protocol:**

- signatures authenticate the DH exponentials
- MACs bind the key to identities
  - MAC is performed with a key  $K_m$  derived by  $K_S = g^{XaXb}$

$A \rightarrow B: g^{Xa}$

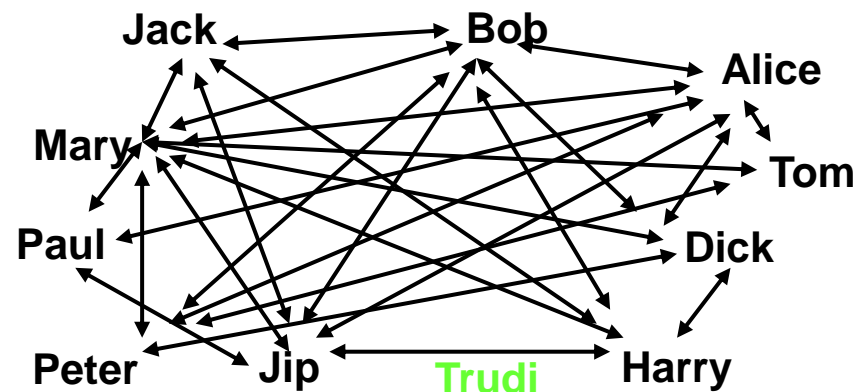
$A \leftarrow B: B, g^{Xb}, \text{Sign}_B(g^{Xa} \parallel g^{Xb}), \text{MAC}_{K_m}(B)$

$A \rightarrow B: A, \text{Sign}_A(g^{Xa} \parallel g^{Xb}), \text{MAC}_{K_m}(A)$

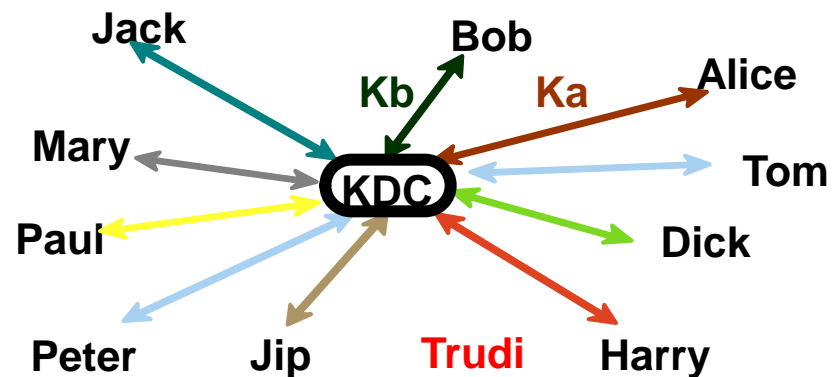
# Server-based Key Distribution

# Direct trust vs. Trusted intermediaries

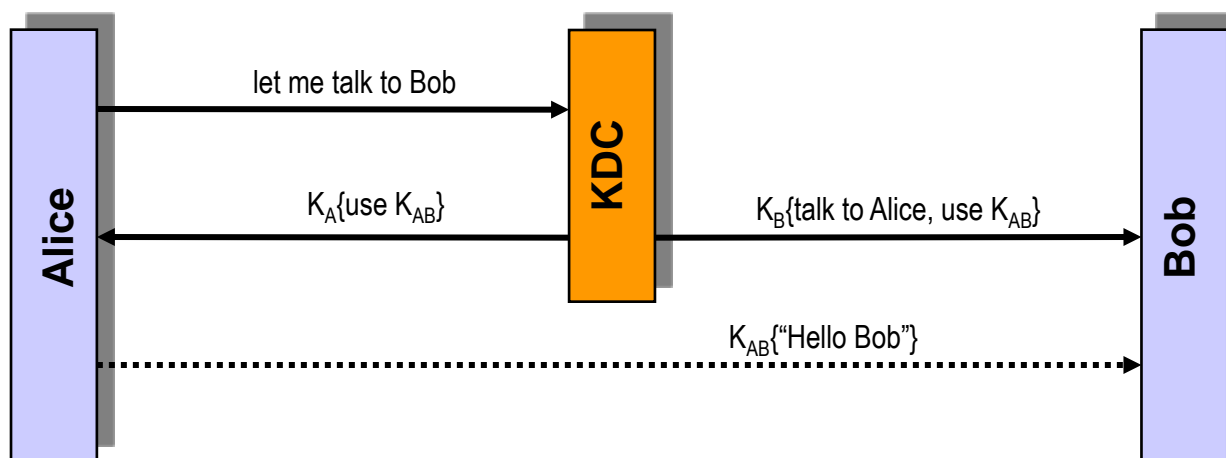
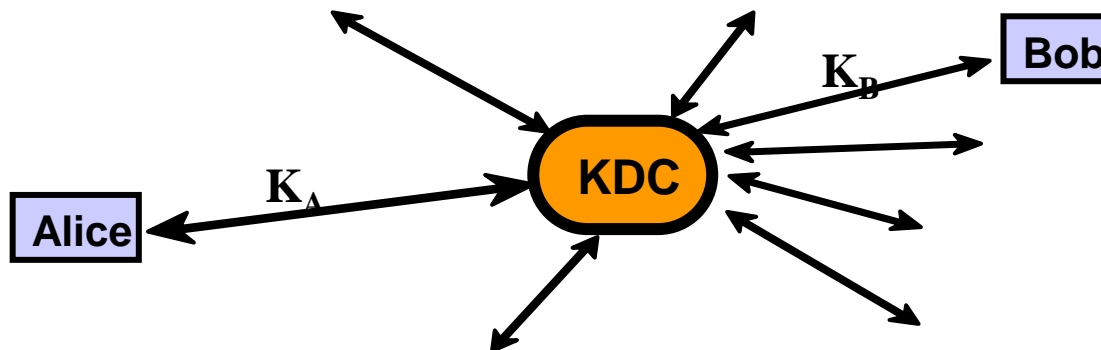
- With  $N$  nodes, each node must authenticate each other..  $N-1$  keys maintained by each node



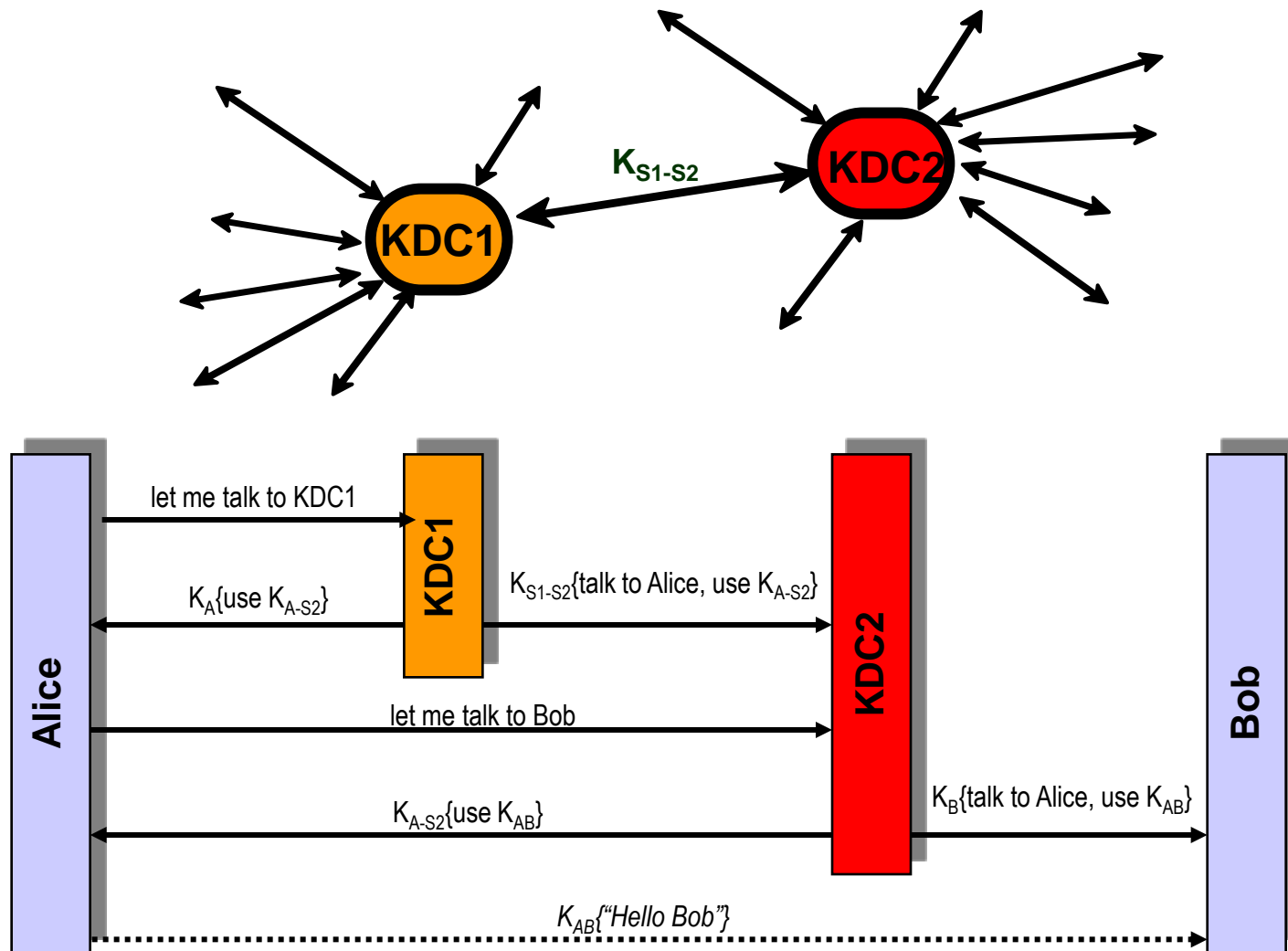
- Possible solution: Trusted intermediate party
  - **Key Distribution Center (KDC) or Key Translation Center (KTC)**
  - similar to CAs for public-key cryptography



# Key distribution with a trusted intermediary

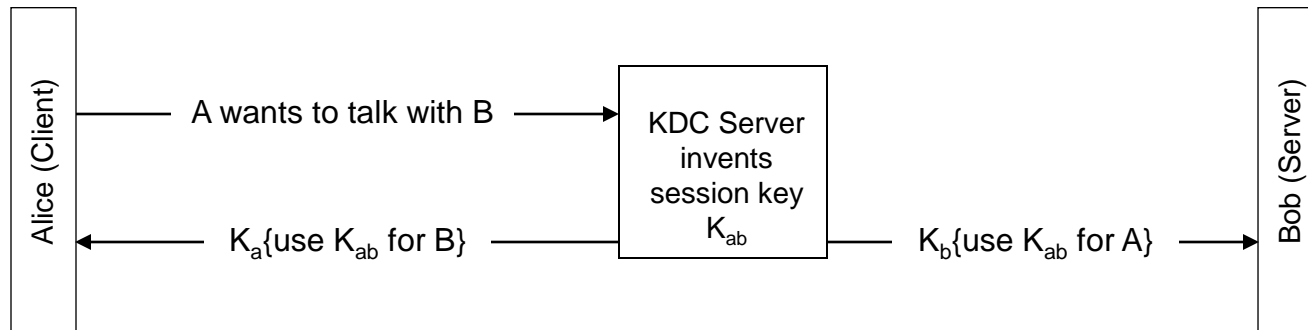


# Key distribution with multiple trusted intermediaries



# Key Distribution in practice

- Key Distribution in theory (Client-Server)



- Key Distribution in practice (Client-Server)

➤ e.g. used by Kerberos protocol

