

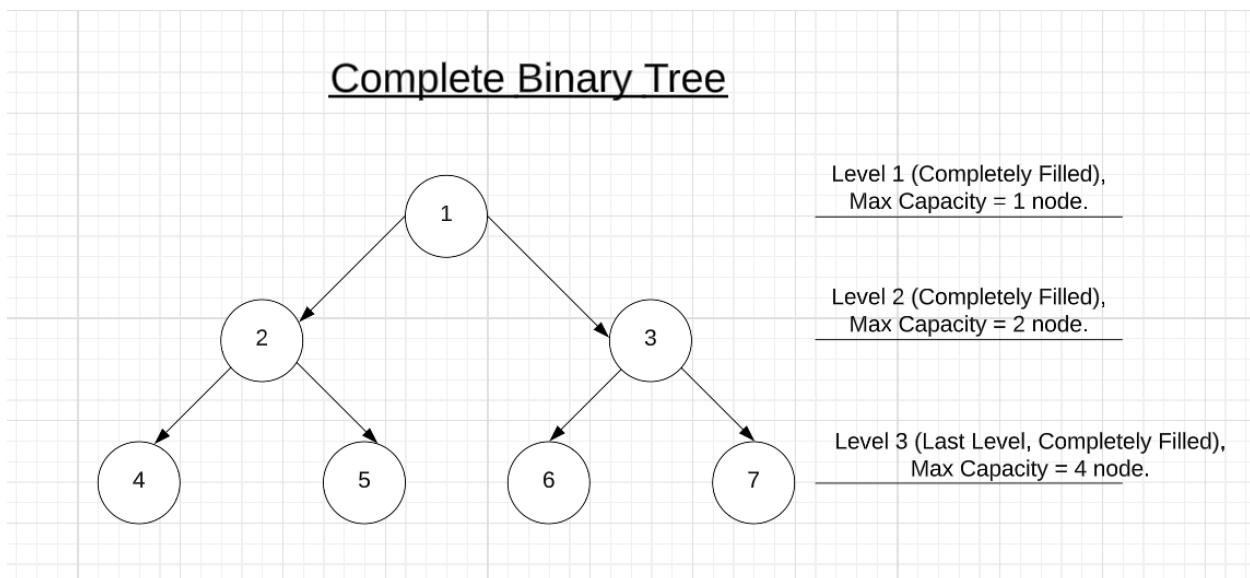
# Heap Data Structure

## What is Heap ?

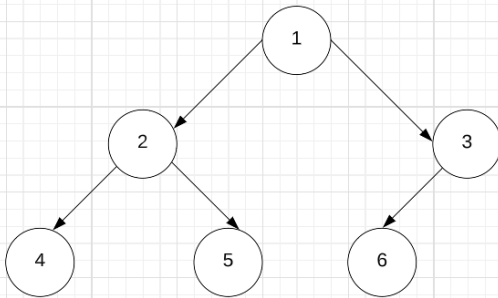
1. A Heap is a special **Tree-based** data structure in which the **tree is a complete binary tree**.
2. Heap comes with a special property called as **Heap Order property**.
3. In simple words, we can say that, A heap is a special tree-based data structure that satisfies the heap property and in which the tree is a Complete Binary Tree.

## What is Complete Binary Tree (AKA CBT) ?

1. A binary tree is called complete binary tree **when all the level of binary tree is completely filled except the last level (last level can be completely filled or cannot be completely filled)**.
2. A Complete Binary Tree is always filled from left to right. This means that if a node has two children, the left child will always be filled before the right child.
3. And if a node has only one child, then that child must be left child because of the order that we have just discussed in point 2.



## Complete Binary Tree

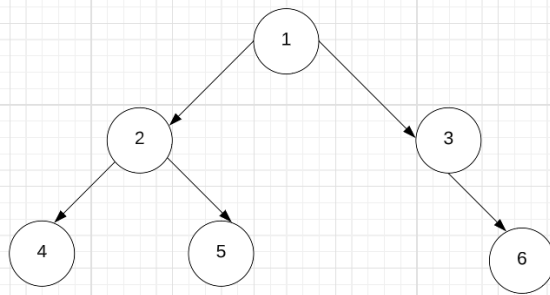


Level 1 (Completely Filled),  
Max Capacity = 1 node.

Level 2 (Completely Filled),  
Max Capacity = 2 nodes.

Level 3 (Last Level, Not Completely Filled),  
Max Capacity = 4 nodes, but only 3 nodes are there, but it is the last level so we can ignore it.

## Not a Complete Binary Tree



Level 1 (Completely Filled),  
Max Capacity = 1 node.

Level 2 (Completely Filled),  
Max Capacity = 2 nodes.

Level 3 (Last Level, Not Completely Filled),  
Max Capacity = 4 nodes, but only 3 nodes are there.

**Note:** If the last Level is not completely filled, we can ignore it but, Complete Binary Tree is always filled from left to right, this means that if a node has two children, the left child will always be filled before the right child and in this case left child of 3 is missing and if a node has only one child then it must be a left child.

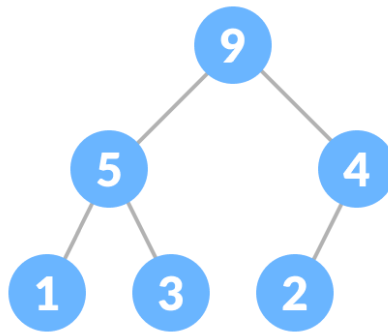
That's why it is not a complete binary tree.

## What is Heap Order Property ?

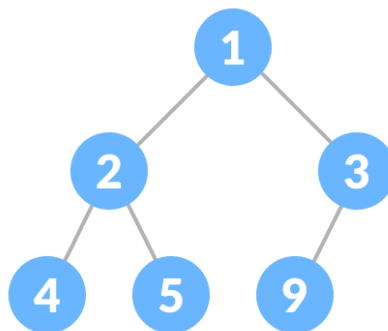
*The heap order property says that, for every node, the value of the root node or parent node must be ( $\geq$  or  $\leq$ ) than the value of its child nodes.*

**In Simple Words, Heap Order property is,**

1. For every node,
  - a. The value of root node or parent node  $\geq$  the value of its child nodes or,



- b. The value of root node or parent node  $\leq$  the value of its child nodes .

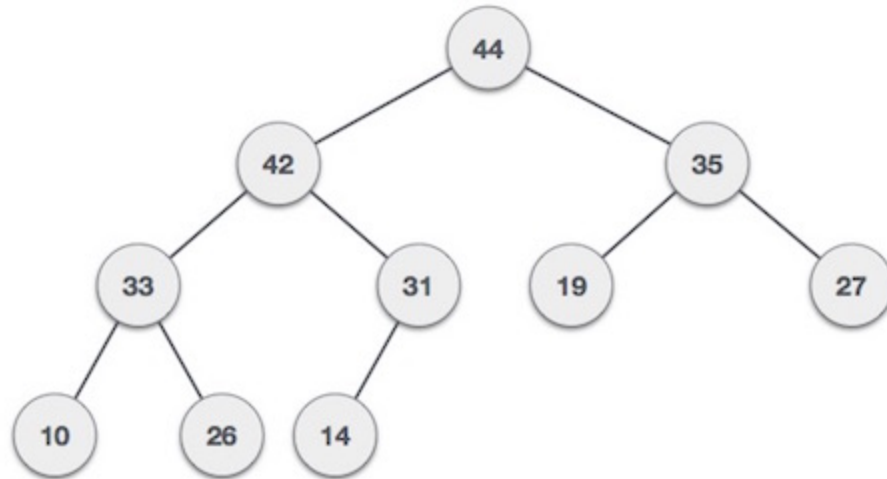


## Types of Heap ?

Based on the property of heap (Heap Order property), we can classify heaps into two types,

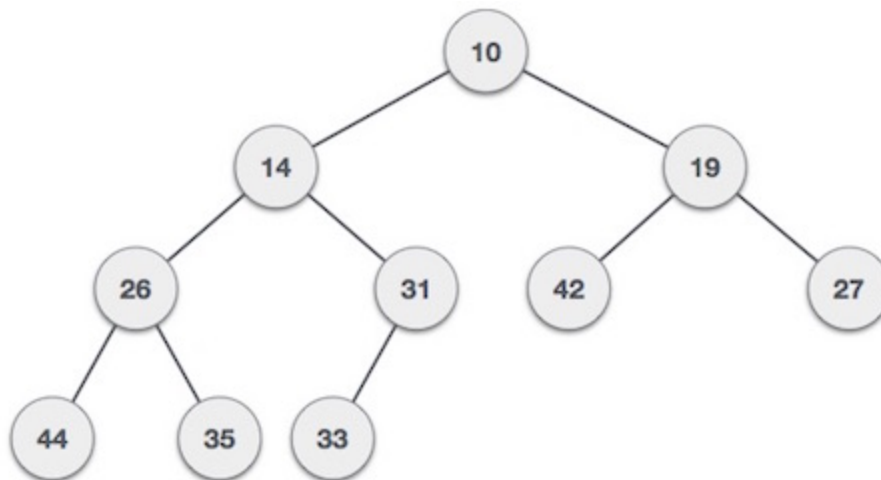
### 1. Max Heap

- a. The value of root node or parent node  $\geq$  the value of its child nodes.



## 2. Min Heap

- a. The value of root node or parent node  $\leq$  the value of its child nodes .



## How to implement Heap ?

Arrays are commonly used to implement heaps because heap are complete binary tree so there will be not wastage of memory.

In an array-based representation of a heap, the elements of the heap are stored in an array, where the root of the tree is located at index 0 and each child of a node at index  $i$  is located at indices  $2i+1$  and  $2i+2$ .

## **In Short,**

### **1. In 0-based Indexing**

- a. Left Child =  $2*i+1$
- b. Right Child =  $2*i+2$
- c. Parent Node =  $((i-1) / 2)$ .
- d. Leaf Nodes =  $[n/2, n-1]$ ,  $n$  is the size of array in integers.

### **2. In 1-based Indexing**

- a. Left Child =  $2*i$
- b. Right Child =  $2*i+1$
- c. Parent Node =  $(i / 2)$ .
- d. Leaf Nodes =  $[((n/2) + 1), n]$ ,  $n$  is the size of array in integers.