

# Neutrino Properties



Adapted from Artwork by Sandbox Studio, Chicago with Ana Kova

**Elvio Lisi, INFN, Bari**

## Outline:

- **Pedagogical introduction**
- **Neutrino oscillations & their parameters**
- **Neutrino absolute mass observables**
- **[Neutrino properties in a wider picture]**

# Pedagogical introduction

Questions about fundamental  $\nu$  properties (mass, spinor d.o.f., charges, families) asked in the last century:

**1. How small is the neutrino mass?**

(Pauli, Fermi, '30s)

**2. Is the neutrino its own antiparticle?**

(Majorana, '30s)

**3. Do  $\nu$  of different flavors transform (“oscillate”) among them?**

(Pontecorvo, Maki-Nakagawa-Sakata, '60s)



Short answers →

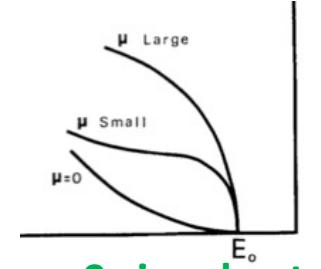
1

**Fermi:** In  $\beta$ -decay, when the  $\beta$  energy is near its max, the  $\nu$  energy is near its minimum (**nonrelativistic  $\nu$** ),

$$E \sim m + p^2/2m$$

→ the  $\beta$  energy spectrum tail kinematically probes  $m$ .

Dynamically:  $m$  is a source of gravity → cosmology. **No  $m>0$  signal yet.**



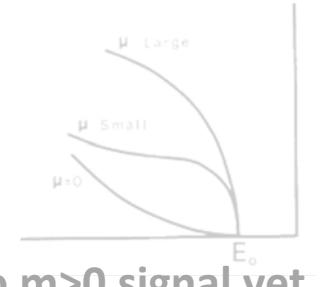
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2

More often one deals with  $\nu$  in the opposite limit (**ultrarelativistic  $\nu$** )

$$E \sim p + m^2/2E$$

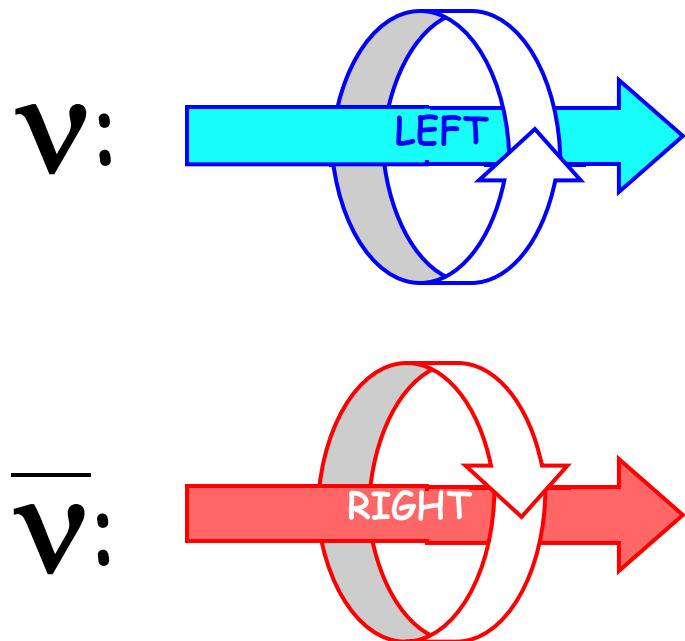
where **Majorana's hypothesis** involves rare flips of handedness

$$\text{LH} \leftrightarrow \text{RH} \sim O(m/E)$$

that may allow an otherwise forbidden decay ( $0\nu\beta\beta$ ). **No decay signal yet.**



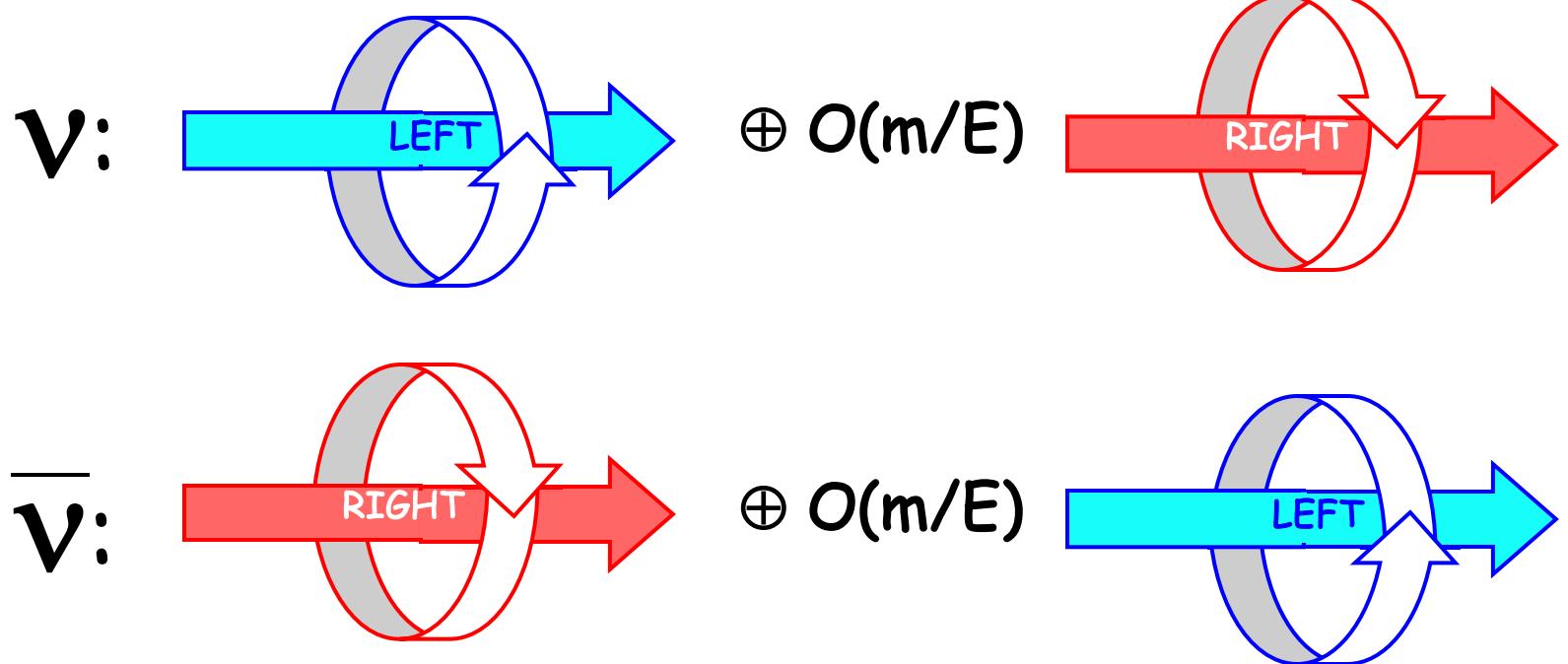
## Spinor d.o.f. for massless $\nu$ : handedness is a constant of motion



2 independent d.o.f.: massless (“Weyl”) 2-spinor

→ Weyl nu / antinu are different

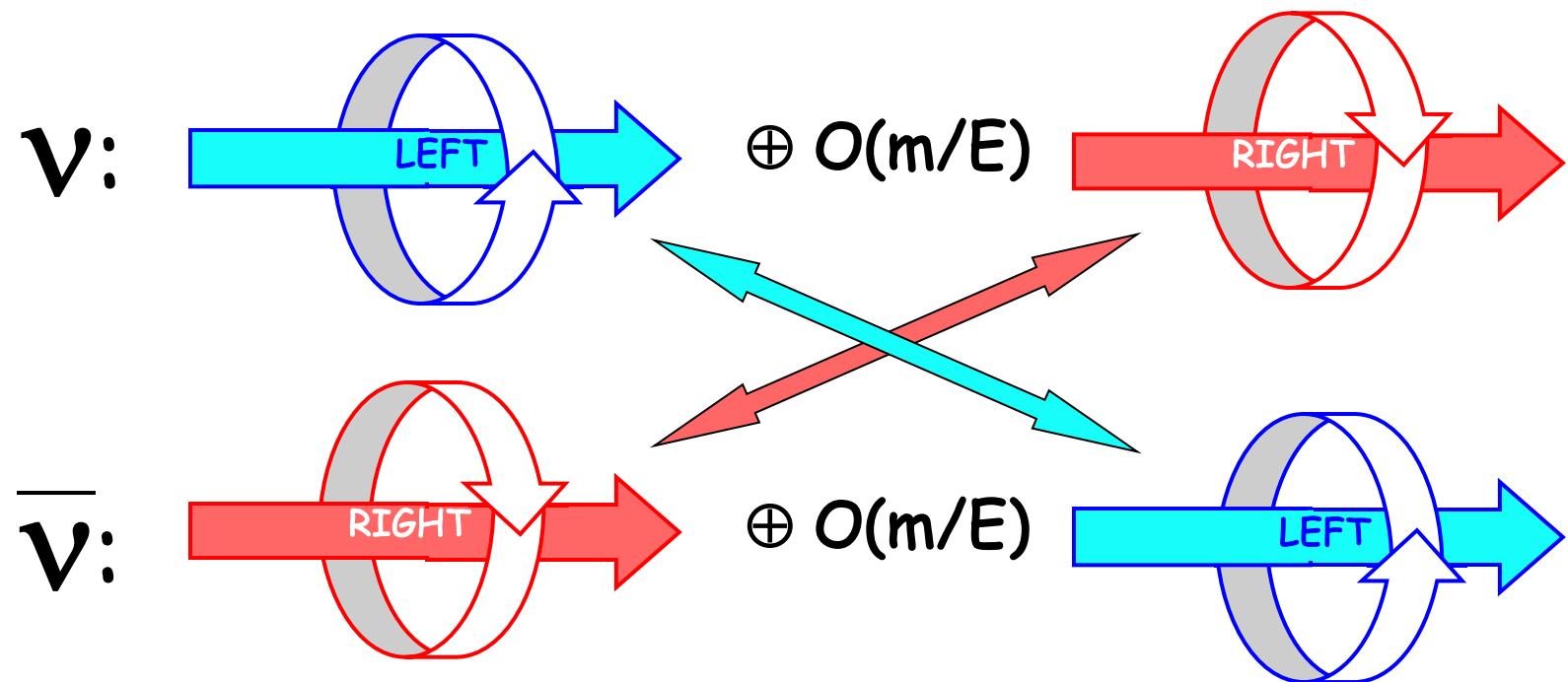
**Massive  $\nu$  can develop the “wrong” handedness at  $O(m/E)$**   
(Dirac equation mixes RH and LH states for  $m \neq 0$ ):



**If these 4 d.o.f. are independent: massive (“Dirac”) 4-spinor**

- Dirac nu / antinu are different, just as charged fermions.
- Can define a neutrino charge: their “lepton number”

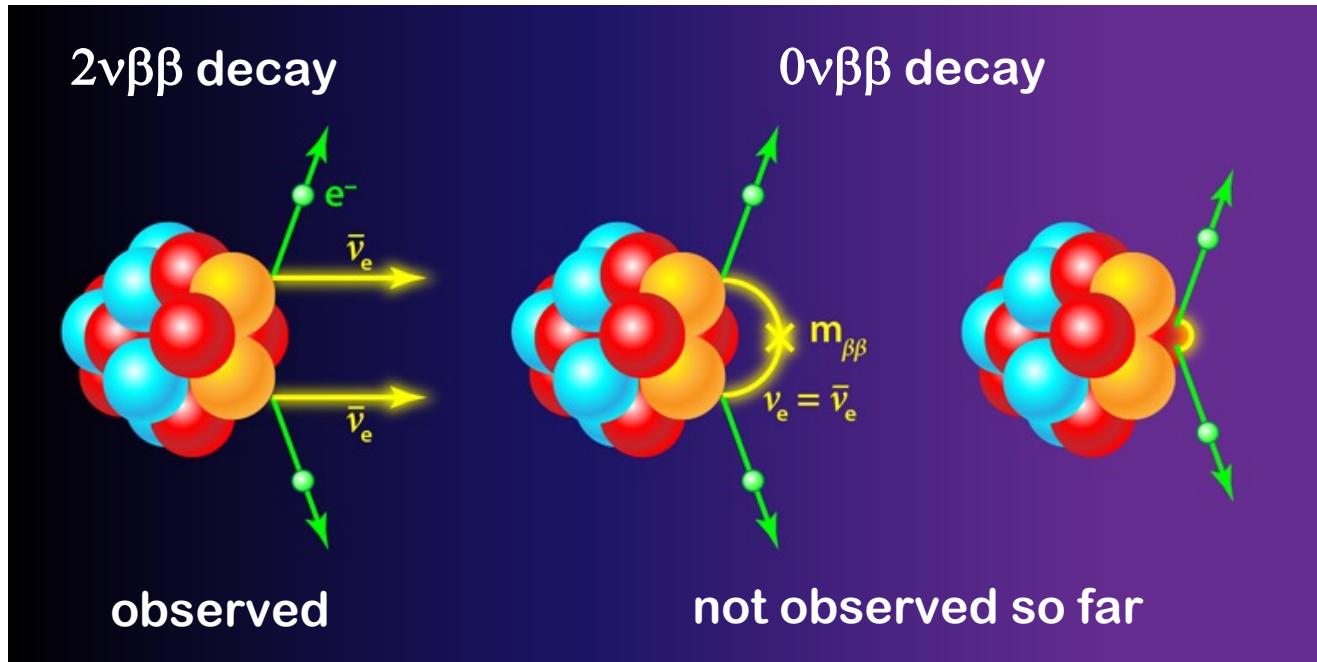
# Majorana: for neutral fermions, components might be paired!



**Massive (“Majorana”) 4-spinor with 2 independent d.o.f.  
the simplest massive fermion field, with no charge(s) at all**

- Fundamentally:  $\nu$  = antinu (up to a phase). Cannot define a lepton number
- $\nu$  and antinu remain “shorthand” for usual ultrarelativ. LH and RH  $\nu$  states

Only known realistic way to probe this option:  **$0\nu\beta\beta$  decay**  
**(occurring if and only if  $\nu$  are Majorana)**



A very rare (weak<sup>2</sup>) process that violates leptonic number and “creates matter” (\*)  
Worldwide searches in several candidate nuclei

(\*) see the review 2202.01787

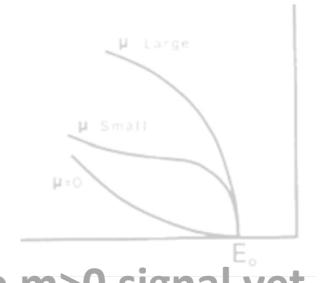
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3

Ultrarelativistic  $\nu$  of different mass accumulate phase differences over L

$$\Delta E \cdot L \sim (\Delta m^2/2E) \cdot L$$

that induce  $\nu_\alpha \rightarrow \nu_\beta$  oscillations if flavor and mass states are mixed

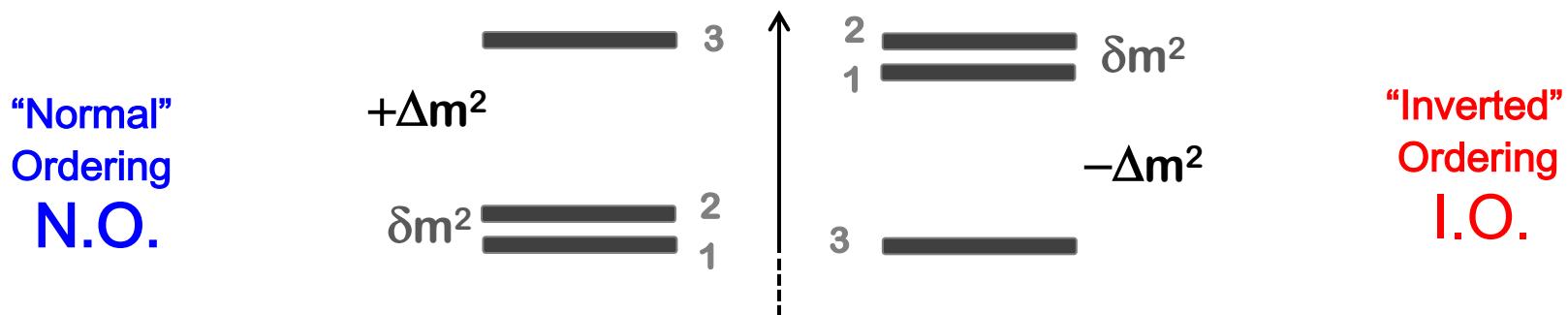
$$\nu_\alpha = U \nu_i$$

Sensitive to bkgd matter (MSW). **Oscillation signals in vac. & matter (>1998)**

# The standard 3v framework & oscillation parameters

Mixing matrix: CKM → PMNS [Pontecorvo-Maki-Nakagawa-Sakata]

## Mass [squared] spectrum)



$$\delta m^2 = \Delta m_{21}^2, \quad \Delta m^2 = (\Delta m_{32}^2 + \Delta m_{31}^2)/2$$

+ interaction energy in matter  $\rightarrow \sim G_F \cdot \text{density}$  (MSW effect, observed)  
 [Absolute v mass scale not tested in oscillations]

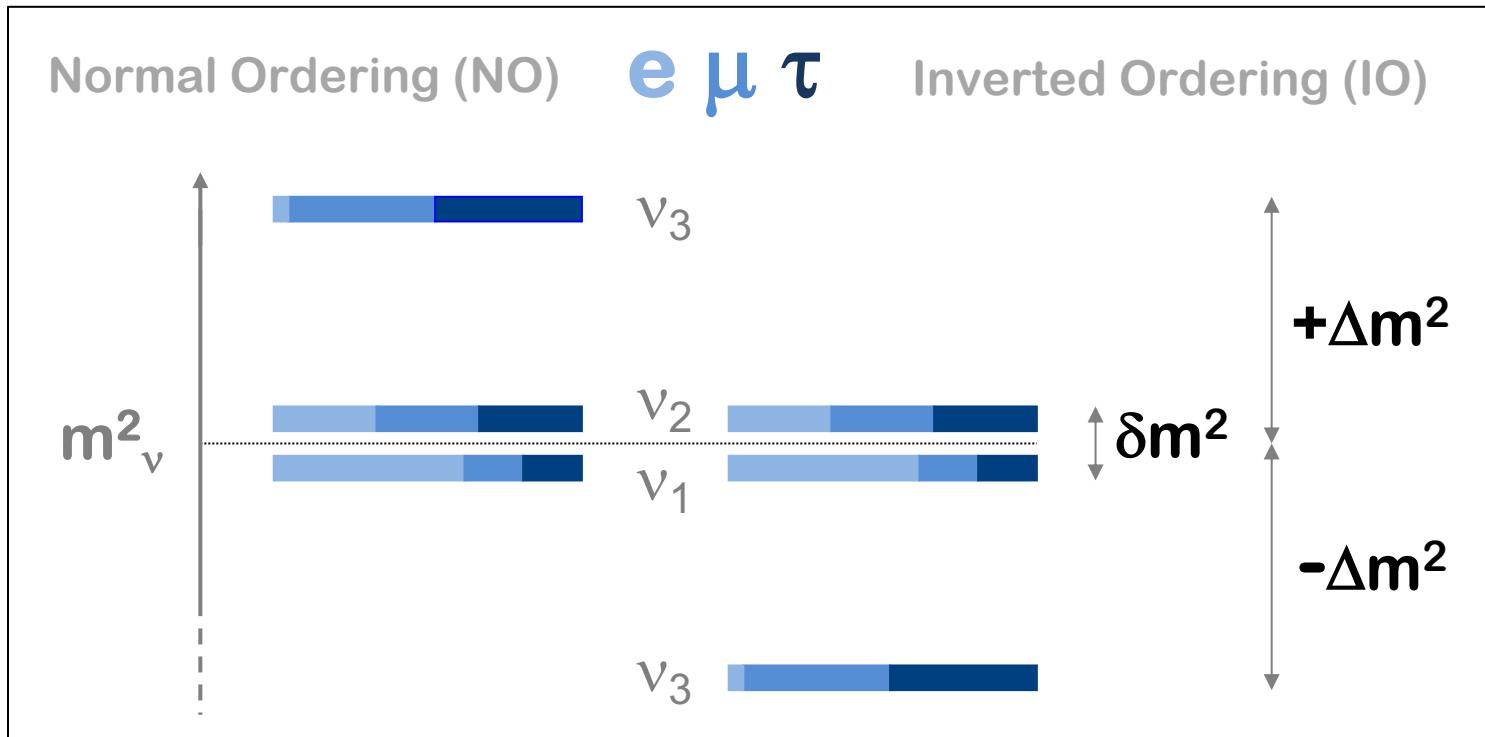
## Sketchy 3v overview

**5 knowns:**

$$\begin{array}{ll} \delta m^2 & \sim 8 \times 10^{-5} \text{ eV}^2 \\ |\Delta m^2| & \sim 2 \times 10^{-3} \text{ eV}^2 \\ \sin^2 \theta_{12} & \sim 0.3 \\ \sin^2 \theta_{23} & \sim 0.5 \\ \sin^2 \theta_{13} & \sim 0.02 \end{array}$$

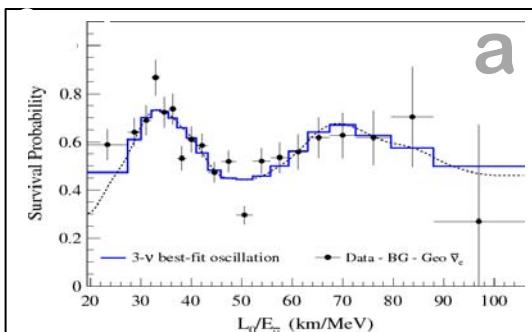
**5 unknowns:**

- Oscillations*
- $\delta$  CPV Dirac phase
  - $\text{sign}(\Delta m^2) \rightarrow \text{NO/IO}$
  - $\theta_{23}$  octant degeneracy
- Non-oscillat.*
- absolute mass scale
  - Dirac/Majorana nature

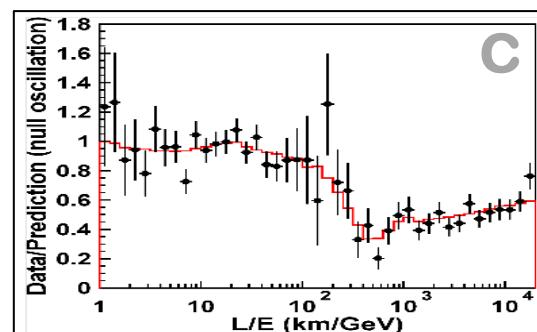


# 3ν oscillations probed by many experiments in different flavor channels...

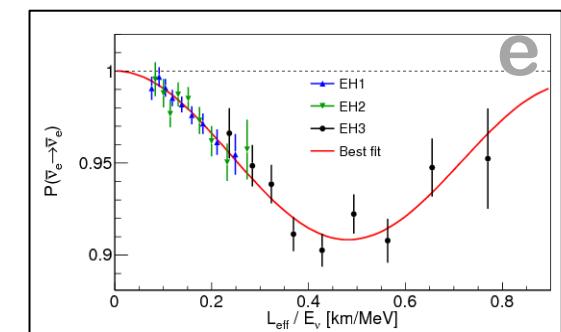
$e \rightarrow e$  (KamLAND, KL)



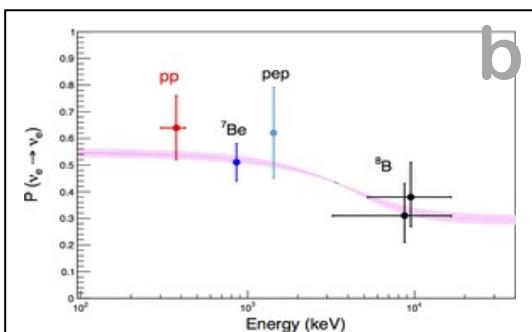
$\mu \rightarrow \mu$  (Atmospheric)



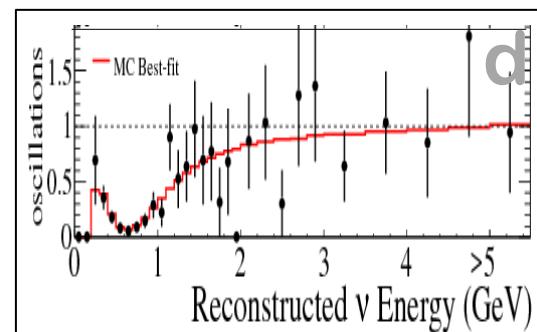
$e \rightarrow e$  (SBL Reac.)



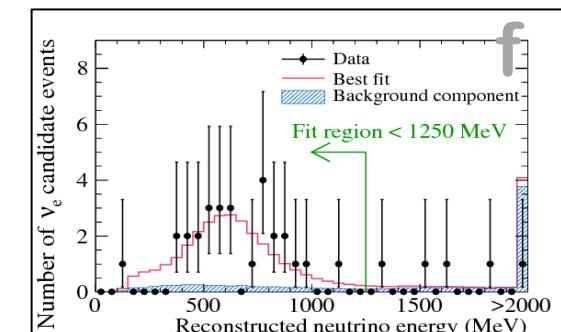
$e \rightarrow e$  (Solar)



$\mu \rightarrow \mu$  (LBL Accel.)



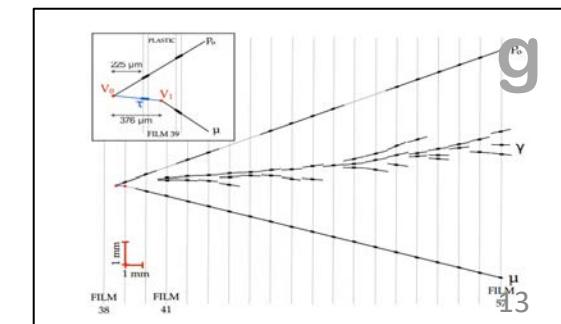
$\mu \rightarrow e$  (LBL Accel.)



LBL = Long baseline (few × 100 km); SBL = short baseline (~1 km)

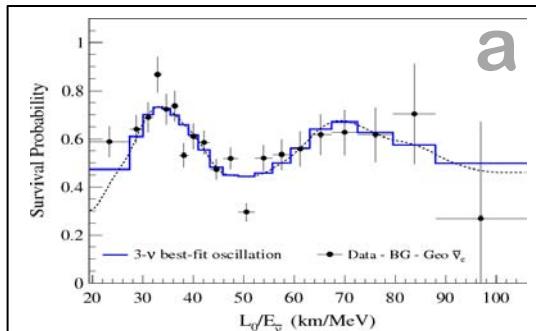
(a) KamLAND reactor [plot]; (b) Borexino [plot], Homestake, Super-K, SAGE, GALLEX/GNO, SNO; (c) Super-K atmosph. [plot], DeepCore, MACRO, MINOS etc.; (d) T2K (plot), NOvA, MINOS, K2K LBL accel.; (e) Daya Bay [plot], RENO, Double Chooz SBL reactor; (f) T2K [plot], MINOS, NOvA LBL accel.; (g) OPERA [plot] LBL accel., Super-K and IC-CD atmospheric.

$\mu \rightarrow \tau$  (OPERA, SK, DC)

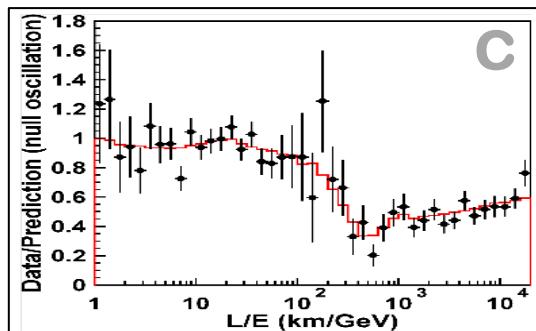


... with amplitude and frequency governed by 2 (or 3) leading parameters

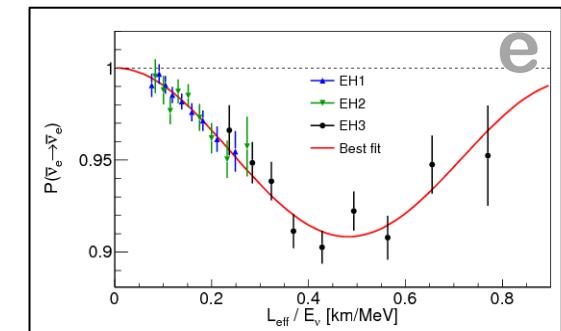
$e \rightarrow e$  ( $\delta m^2, \theta_{12}$ )



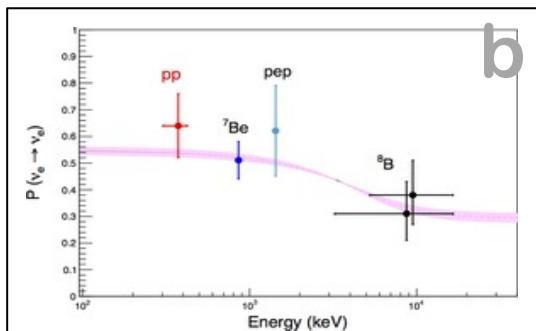
$\mu \rightarrow \mu$  ( $\Delta m^2, \theta_{23}$ )



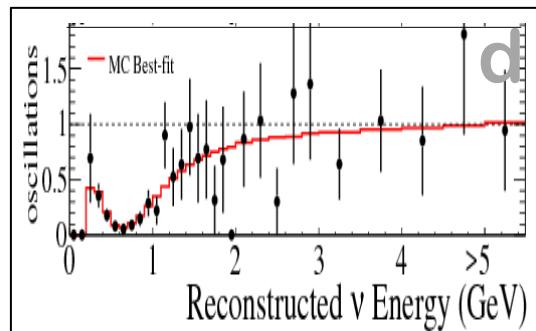
$e \rightarrow e$  ( $\Delta m^2, \theta_{13}$ )



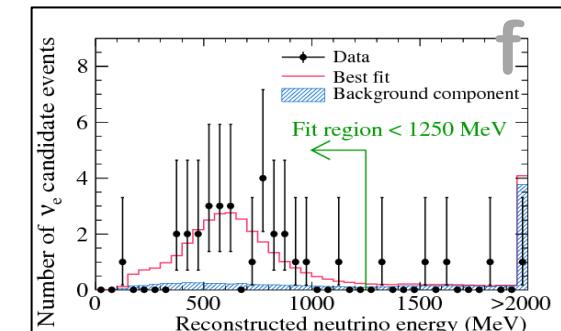
$e \rightarrow e$  ( $\delta m^2, \theta_{12}$ )



$\mu \rightarrow \mu$  ( $\Delta m^2, \theta_{23}$ )



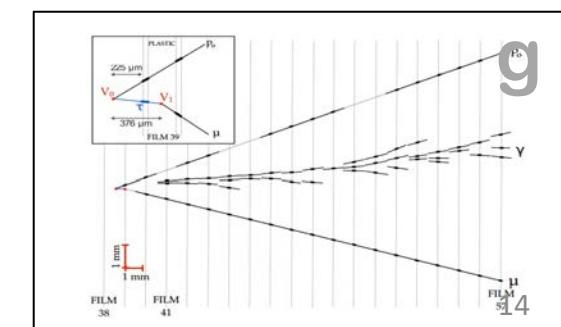
$\mu \rightarrow e$  ( $\Delta m^2, \theta_{13}, \theta_{23}$ )



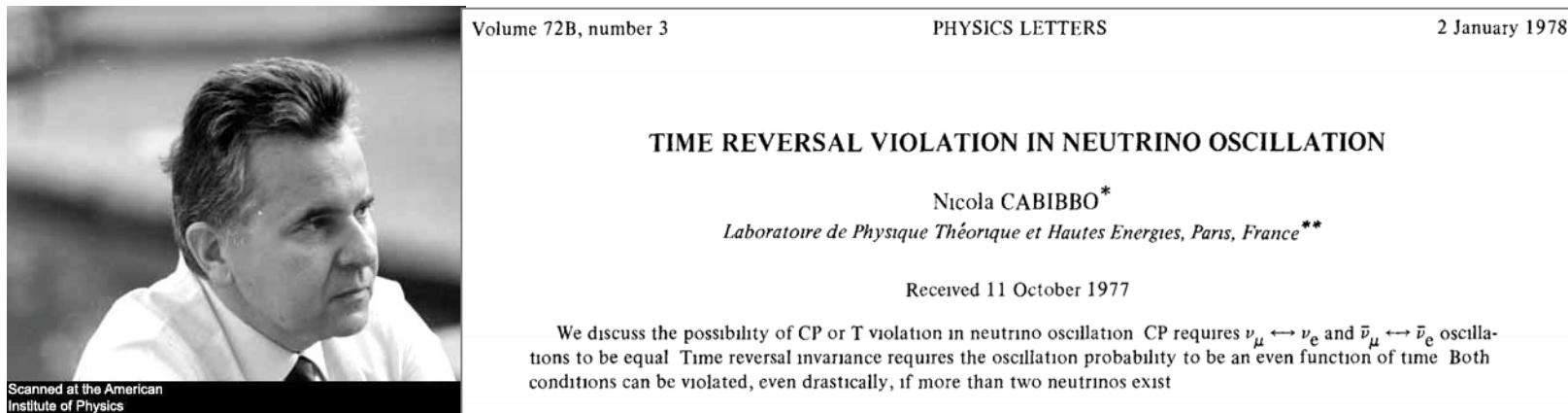
5 param.'s known & (over)constrained  $\rightarrow$  consistency

Currently: focus on unknown par. & subleading effects,  
especially CPV via  $\nu_\mu \rightarrow \nu_e$  in LBL accel. and atmos. expts  
and NO/IO mass spectrum via reactor + accel + atmos.

$\mu \rightarrow \tau$  ( $\Delta m^2, \theta_{23}$ )



# How do $\nu_\mu \rightarrow \nu_e$ oscillation searches probe CPV?



For two neutrinos, no CPV:

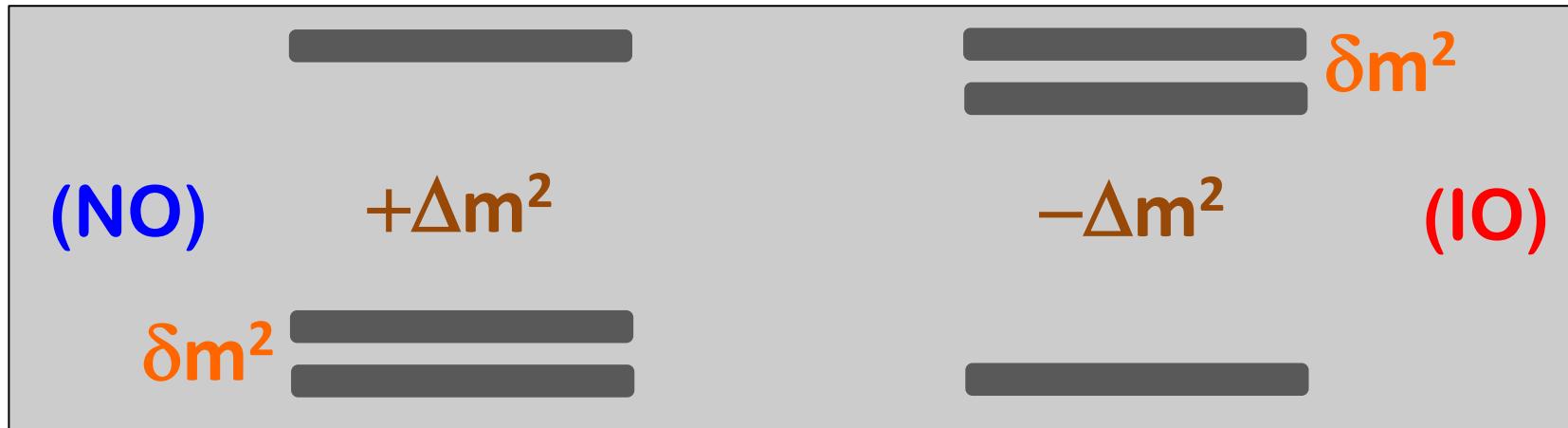
$$\stackrel{(-)}{\nu}_e = \cos\theta_{12} \nu_1 + \sin\theta_{12} \nu_2$$

For three neutrinos: possible CPV phase  $\delta$ , tested via  $\nu$  versus  $\stackrel{(-)}{\nu}$

$$\stackrel{(-)}{\nu}_e = \cos\theta_{13} (\cos\theta_{12} \nu_1 + \sin\theta_{12} \nu_2) + e^{\pm i\delta} \sin\theta_{13} \nu_3$$

CPV is a genuine  $3\nu$  effect →  
all oscillation parameters (known & unknown) are involved/entangled  
(currently tested in T2K, NOvA, Atmosph.)

# How do oscillation searches probe mass ordering?



Observe **interference effects** of oscill. driven by  $\pm \Delta m^2$  with oscill. driven by another quantity  $Q$  with known sign. Options:

$$Q \sim \delta m^2$$

medium-baseline reactors

$$Q \sim G_F N_e E$$

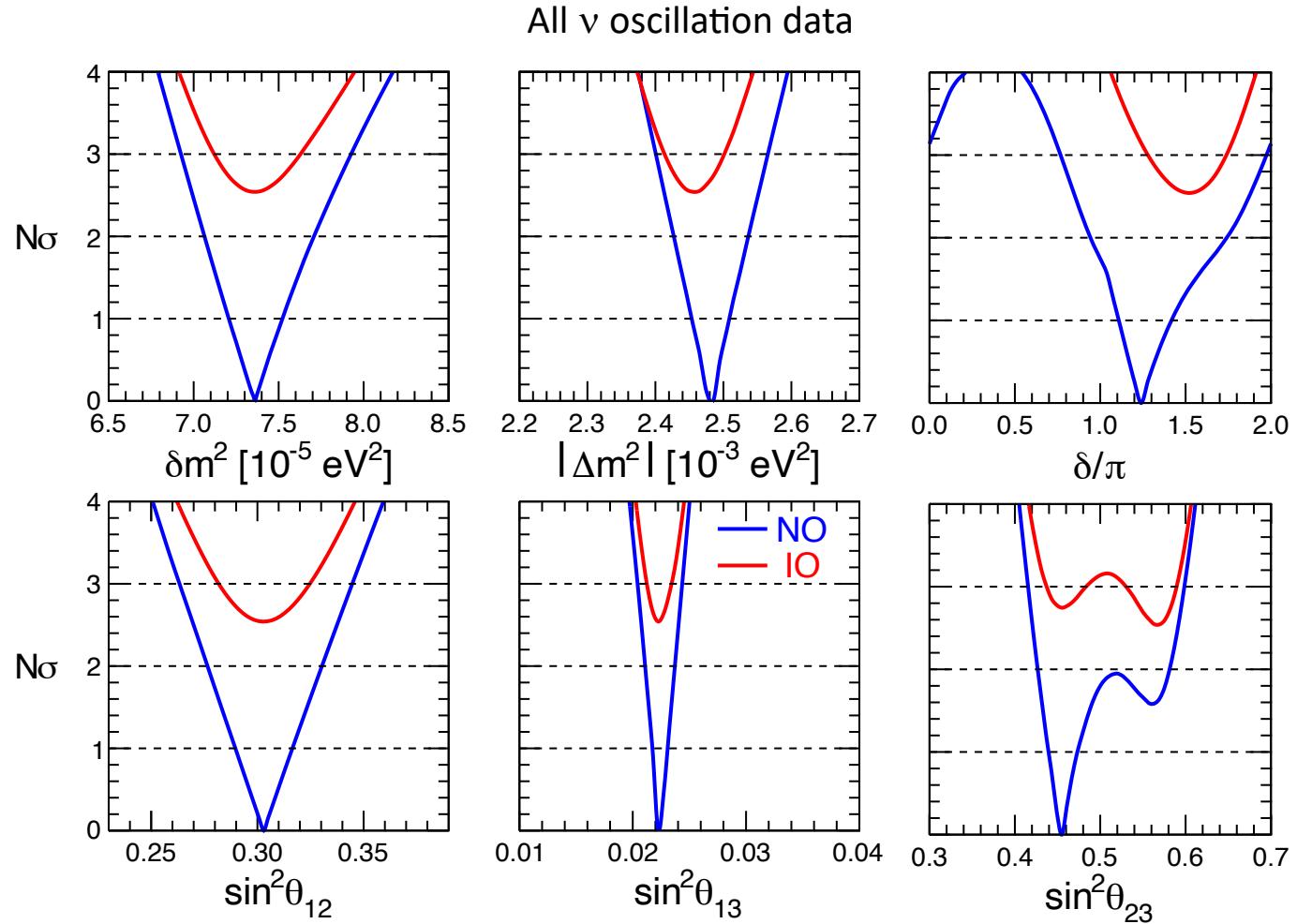
atmospheric & LBL accel. expts

$$[Q \sim G_F N_\nu E]$$

core-collapse SN via  $\nu-\nu$  collective effects]

Plus: synergy / complementarity of  $|\Delta m^2|$  data from different expts  
[should converge better in the true ordering than in the wrong one]

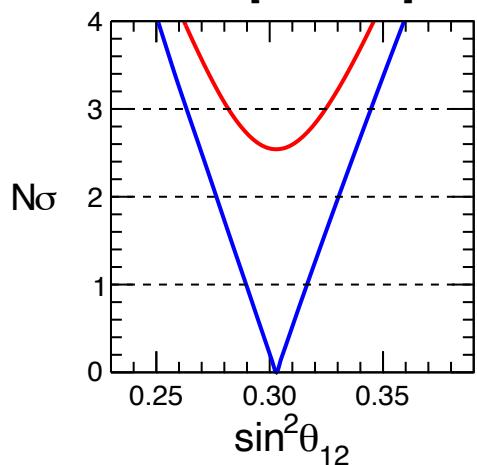
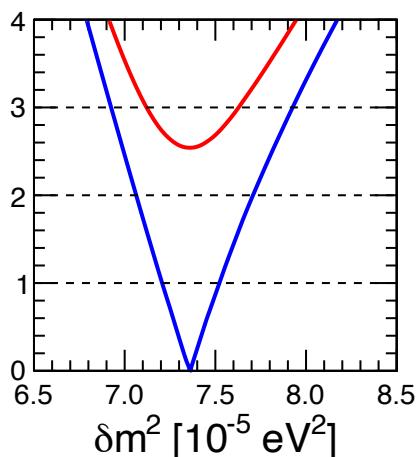
# Status of known and unknown 3ν oscillation parameters [from 2107.00532]



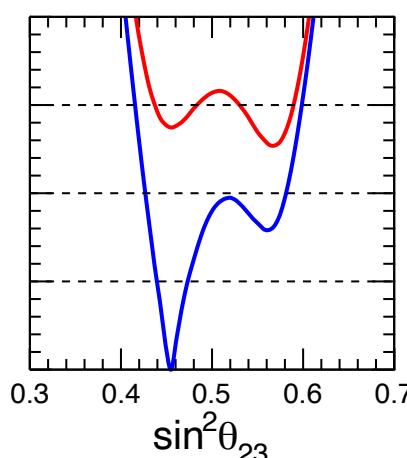
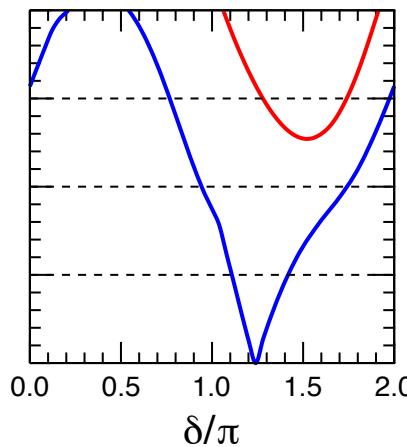
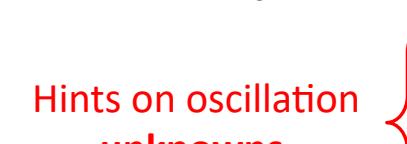
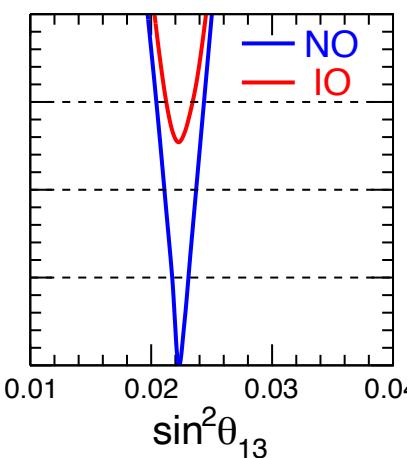
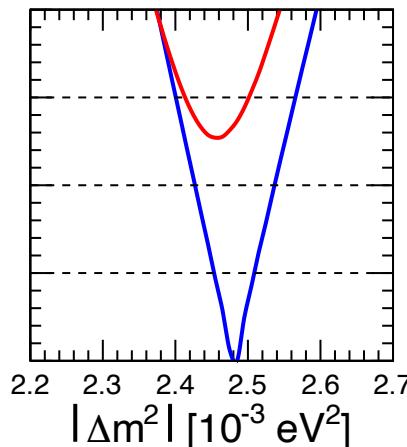
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**1 $\sigma$  error of known parameters**

$ \Delta m^2 $	1.1%
$\delta m^2$	2.3%
$\theta_{13}$	3.0%
$\theta_{12}$	4.5%
$\theta_{23}$	~ 6%



All ν oscillation data



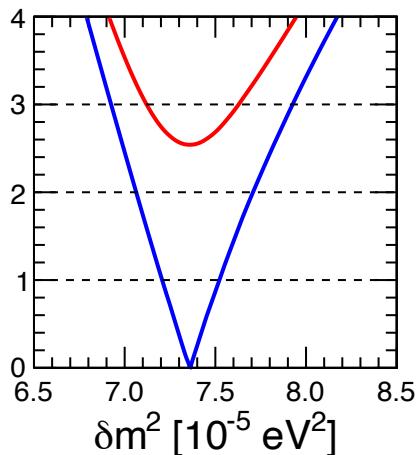
<b>NO</b>	~99% CL
$\sin \delta < 0$	~90% CL
$\theta_{23} < \pi/4$	~90% CL*

\*might flip to 2nd octant with recent data

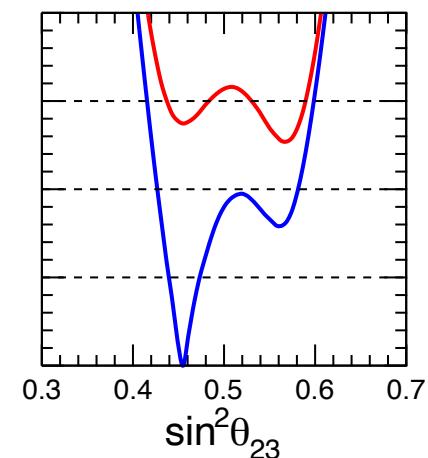
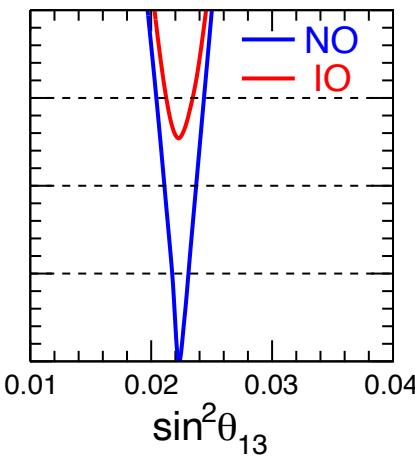
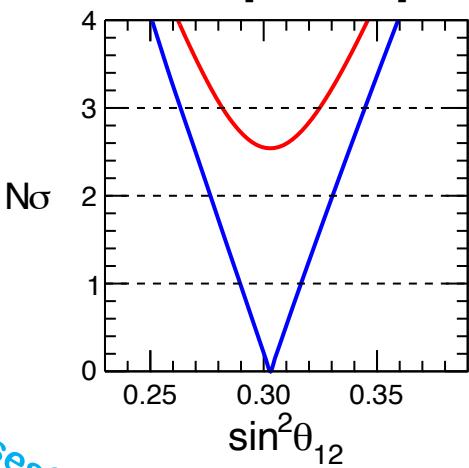
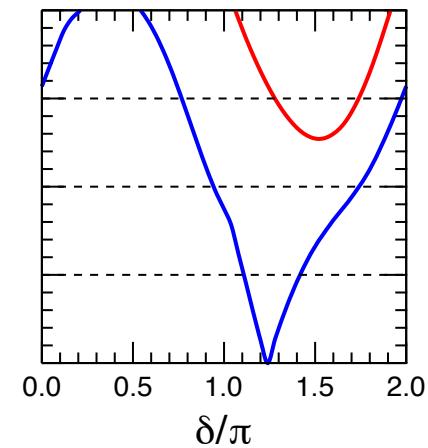
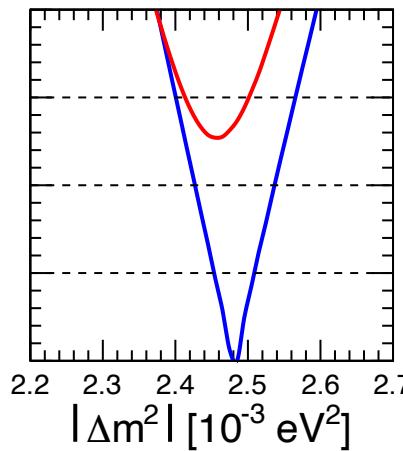
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All ν oscillation data



precision

(surprises?)

Frontiers

discovery

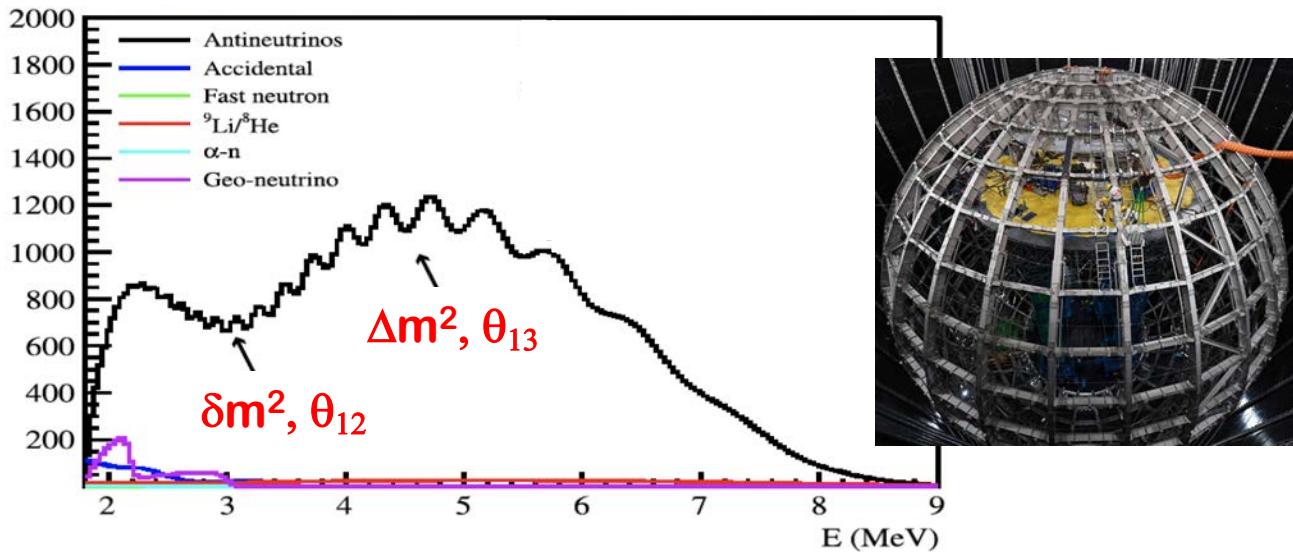
Hints on oscillation unknowns

- |                         |                        |
|-------------------------|------------------------|
| <b>NO</b>               | $\sim 99\% \text{ CL}$ |
| <b>sin</b> $\delta < 0$ | $\sim 90\% \text{ CL}$ |
| $\theta_{23} < \pi/4$   | $\sim 90\% \text{ CL}$ |

## E.g.: Frontiers for the JUNO reactor experiment [1507.05613]

At “medium” baseline  $\sim$ 50 km, will probe two oscillations in  $\sim$ vacuum

Main discovery goal: distinguish **NO vs IO** at  $3\text{-}4\sigma$  in 6y.



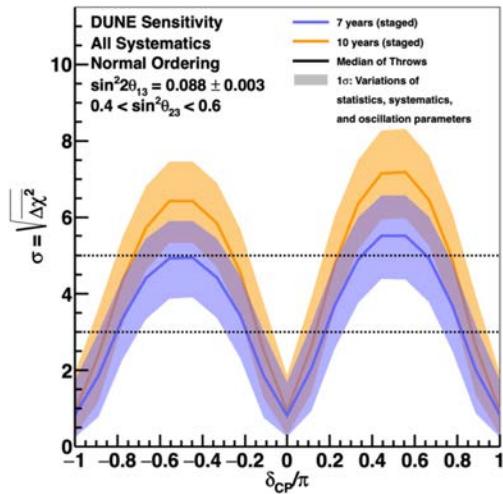
Significant better **precision** expected on 3 out of 4 oscillation parameters:

Parameter	$1\sigma$ , now	JUNO in $\sim$ 6y
$\delta m^2$	2.3 %	0.6 %
$\sin^2 \theta_{12}$	4.4 %	0.7 %
$\Delta m^2$	1.1 %	0.4 %
$\sin^2 \theta_{13}$	3.0 %	comparable

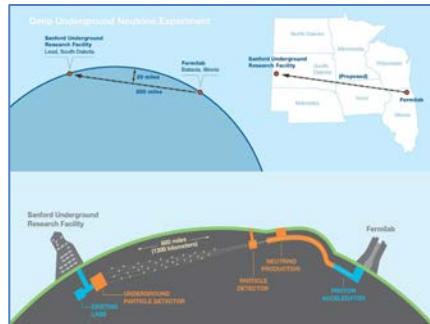
## E.g., frontiers for DUNE, LBL acceler. expt [2002.03005]

Disappearance + appearance, nu/antinu mode, matter effects at L~1300 km

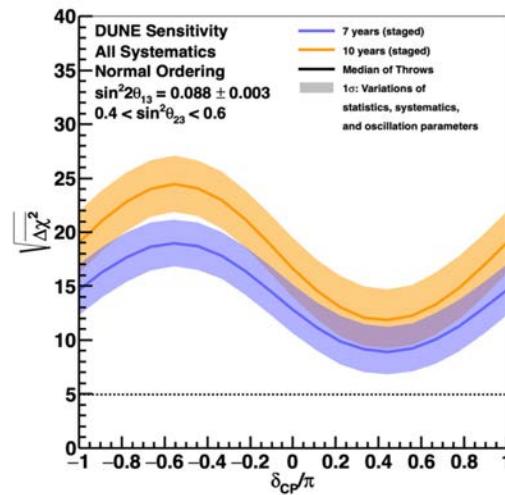
CPV



← Discovery goals →



NO vs IO



Precision frontier



Parameter

1σ, now

DUNE in ~10 y

$\Delta m^2$

1.1 %

factor ~1/4 reduction

$\sin^2 \theta_{23}$

~ 6 %

factor ~1/4 reduction

$\sin^2 \theta_{13}$

3.0 %

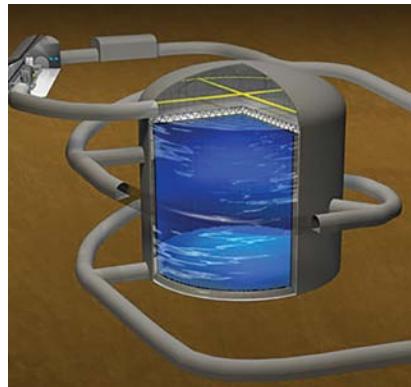
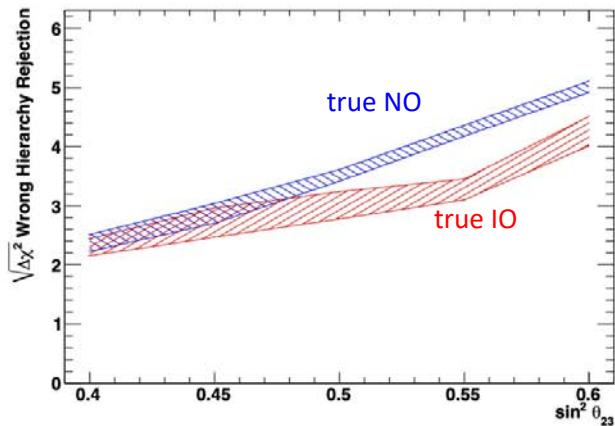
comparable

T2HK: same ballpark. DUNE & T2HK will need precise cross sections!

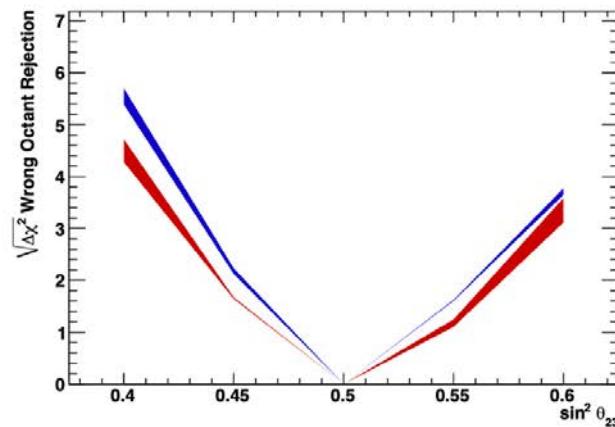
Worldwide activity to better understand nuclear response to ν probes

## E.g., frontiers for Hyper-Kamiokande atmosph. [2002.03005]

Mass ordering



Octant resolution



...surprises?

While advancing the precision and discovery frontiers, JUNO, DUNE, (T2)HK, ... might either converge on consistent discoveries and precision parameters, or find anomalous results → new neutrino states, nonstandard interactions?

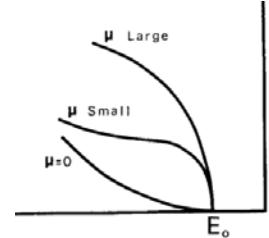
E.g., already in current data:

- Saga of possible indications of sterile (~RH) neutrino state(s) at O(eV) scale
- 4-fermion-like interactions  $\sim \varepsilon_{\alpha\beta} G_F$  weakly preferred by recent SK solar data

# Absolute neutrino mass observables: ( $m_\beta$ , $m_{\beta\beta}$ , $\Sigma$ )

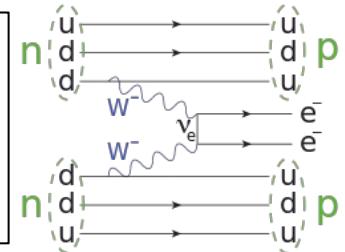
**$\beta$  decay**, sensitive to the “effective electron neutrino mass”:

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$



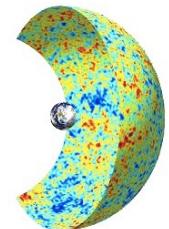
**$0\nu\beta\beta$  decay**: only if Majorana. “Effective Majorana mass” (+phases):

$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$



**Cosmology**: Dominantly sensitive to sum of neutrino masses:

$$\Sigma = m_1 + m_2 + m_3$$



Sensitive to absolute neutrino masses in different ways  
May provide additional handles to distinguish NO vs IO

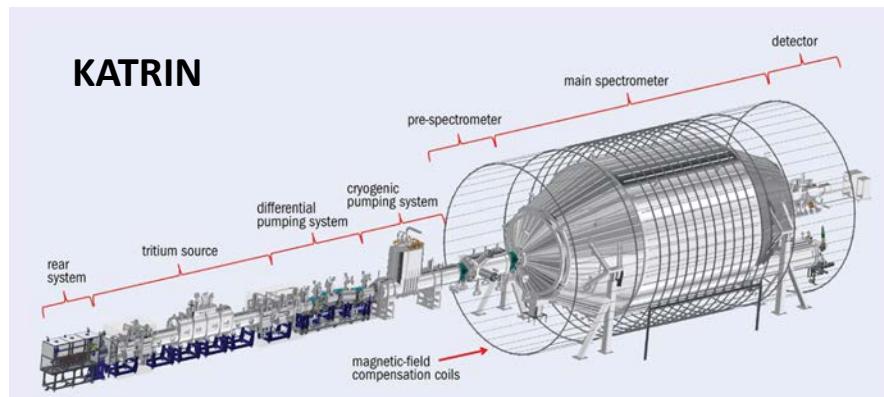
# Beta decay

$m_i^2 \neq 0$  can affect beta spectrum endpoint. For just one (electron) neutrino family: sensitivity to  $m^2(\nu_e)$  (obsolete)

For three neutrino families  $\nu_i$ , and individual masses experimentally unresolved in beta decay: sensitivity to the sum of  $m^2(\nu_i)$ , weighted by squared mixings  $|U_{ei}|^2$  with the electron neutrino. Observable:

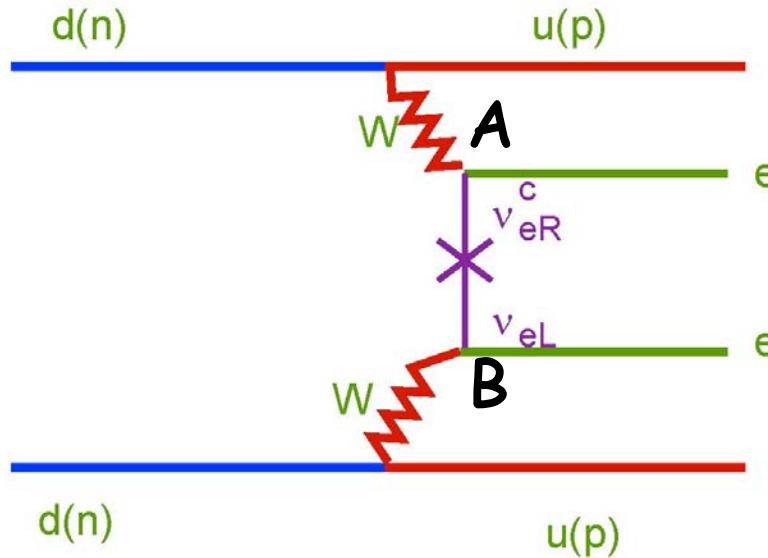
$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{\frac{1}{2}}$$

(so-called “**effective electron neutrino mass**”,  $c_{ij} = \cos \theta_{ij}$  etc.)



# Neutrinoless Double Beta Decay

Iff the  $\nu_e$  is a superposition of Majorana mass states  $\nu_i$ , then for each state the  $0\nu\beta\beta$  decay amplitude is proportional to:



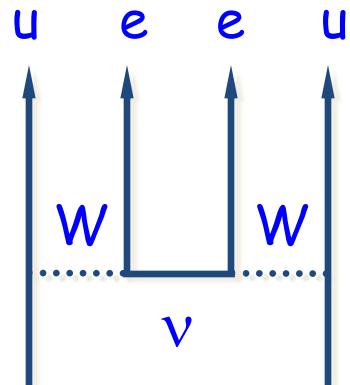
... mixing of  $\nu_e$  with  $\nu_i$   
... mass of  $\nu_i$  [ $O(m/E)$ ]  
... mixing of  $\nu_i$  with  $\nu_e$   
(times an unknown  $\nu_i$  phase)

Summing up for three massive neutrinos: Amplitude  $\sim$  “effective Majorana mass”

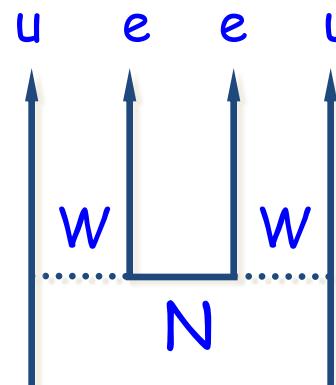
$$m_{\beta\beta} = |c_{13}^2 c_{12}^2 m_1 + c_{13}^2 s_{12}^2 m_2 e^{i\phi_2} + s_{13}^2 m_3 e^{i\phi_3}|$$

Searched in  $^{130}\text{Te}$  (**CUORE**),  $^{136}\text{Xe}$  (**KL-Zen, EXO**),  $^{76}\text{Ge}$  (**GERDA, MAJORANA**), ...  
currently probing  $T \sim O(10^{26}) \text{ y}$

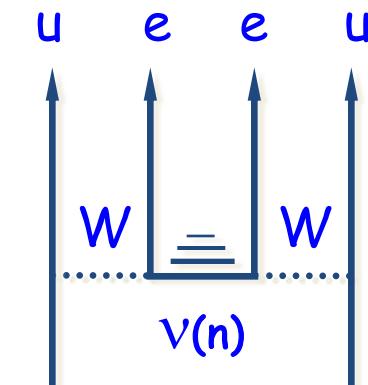
Warning:  $0\nu\beta\beta$  decays might also be induced by nonstandard physics



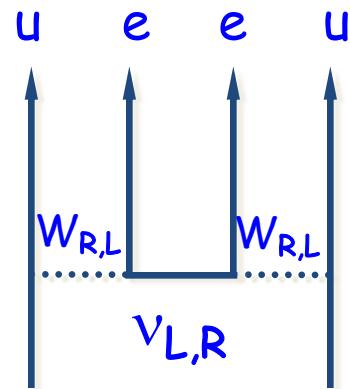
Standard



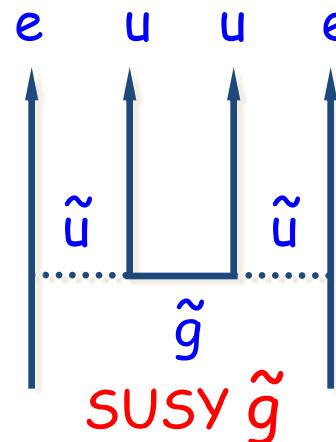
Heavy  $\nu$



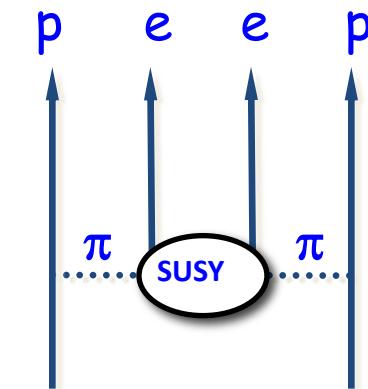
Kaluza-Klein  
(KK $\pm 1$  Brane:  $a=10^{-1}/\text{GeV}$ )



RHC  $\lambda, \eta$   
 $\lambda = \text{RH had}, \eta = \text{LH had}$

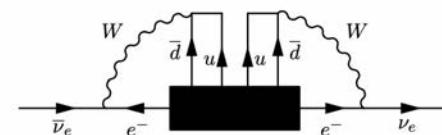


SUSY  $\tilde{g}$



SUSY  $\pi$

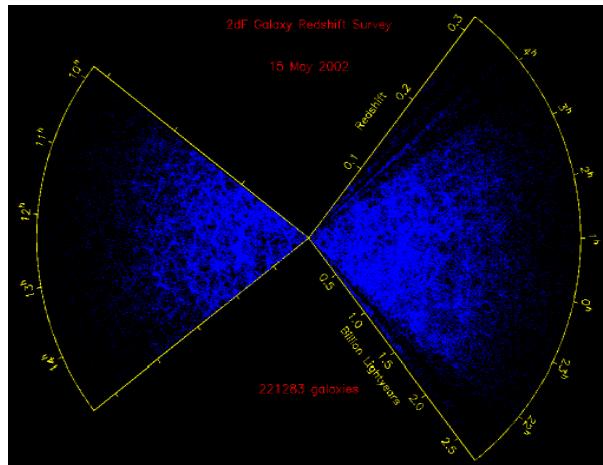
In any case,  $0\nu\beta\beta$  decay implies Majorana  $\nu$ :



# Precision Cosmology

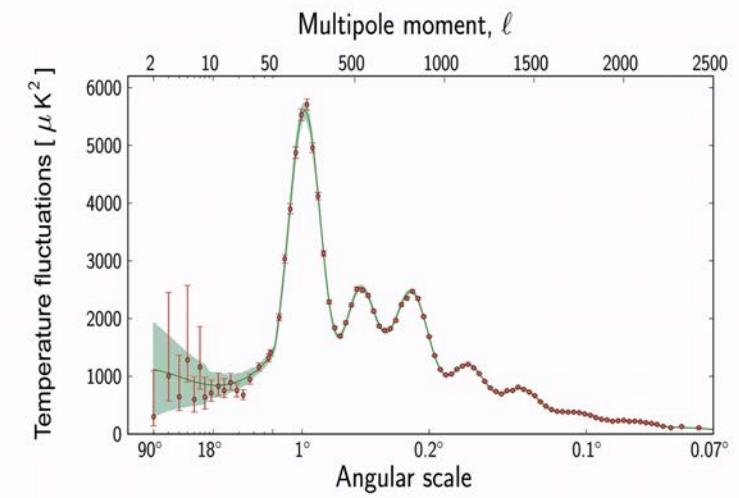
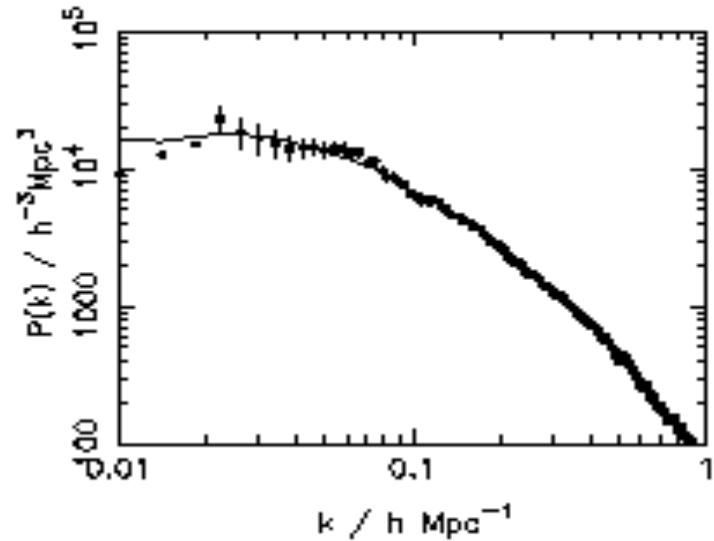
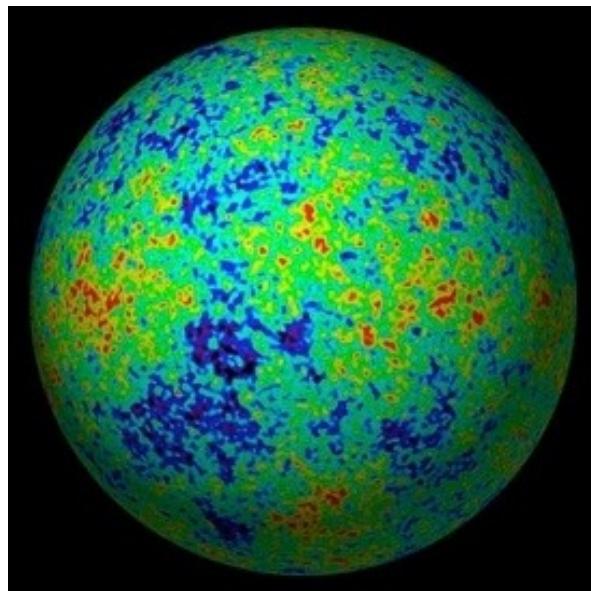
## Observations:

LSS



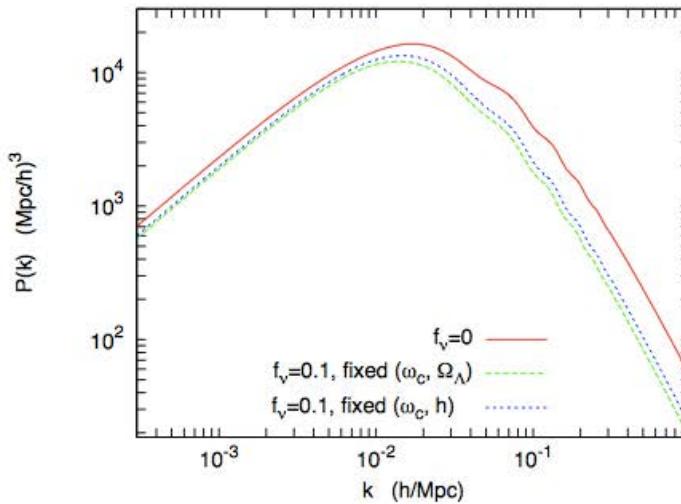
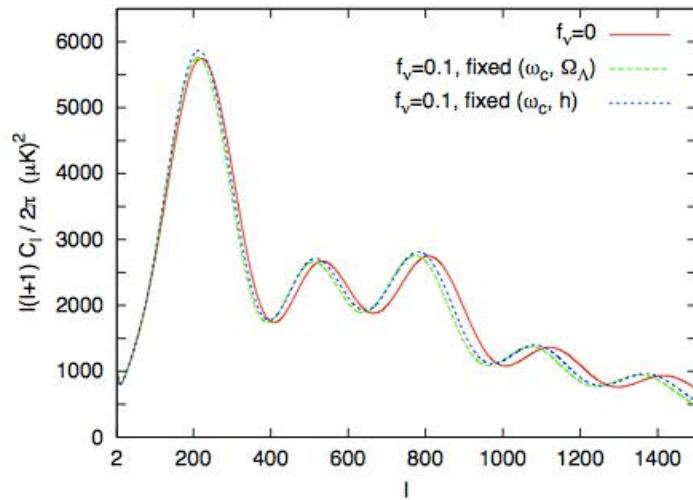
## Spectra:

CMB



Spectra depend mainly on “total gravit. charge”

$$\Sigma = m_1 + m_2 + m_3$$



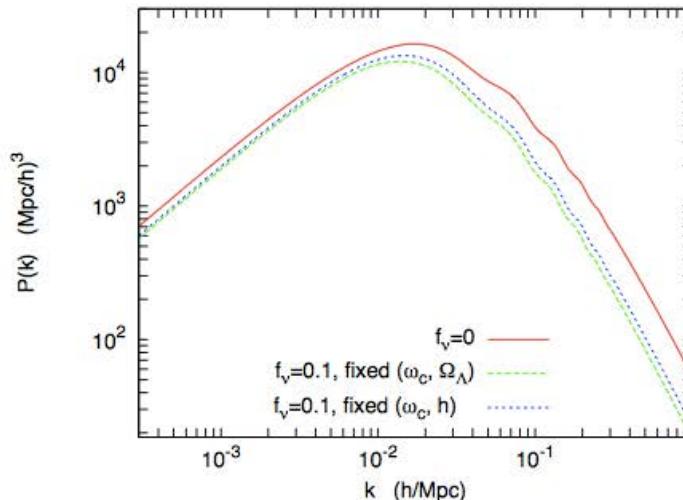
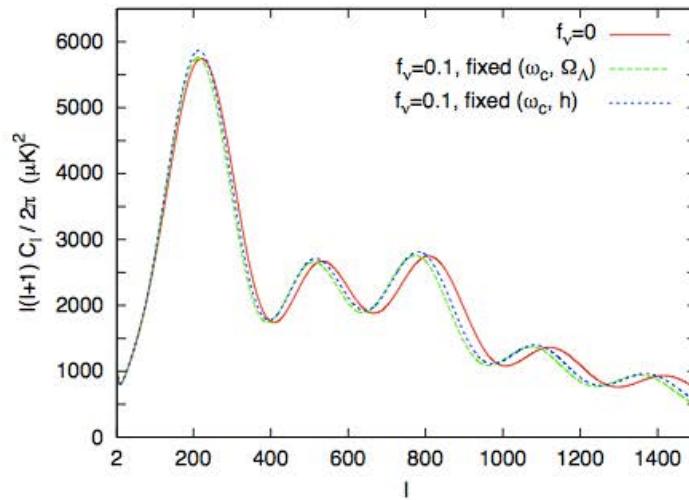
(e.g., from Lesgourgues & Pastor 2006)

Significant progress after Planck & recent galaxy surveys...

Upper bounds on  $\Sigma$  (well) below the eV scale

Spectra depend mainly on “total gravit. charge”

$$\Sigma = m_1 + m_2 + m_3$$

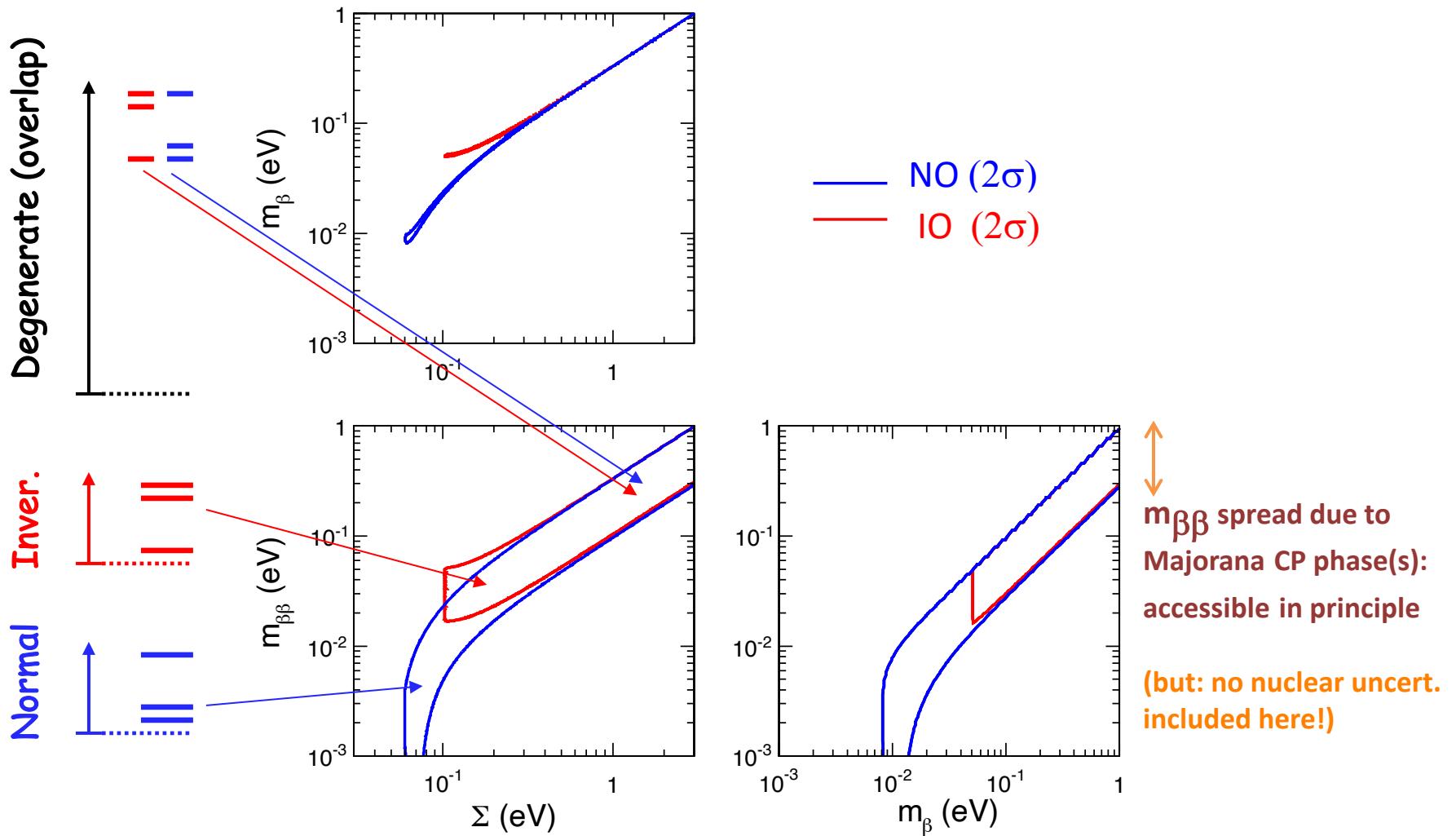


(e.g., from Lesgourgues & Pastor 2006)

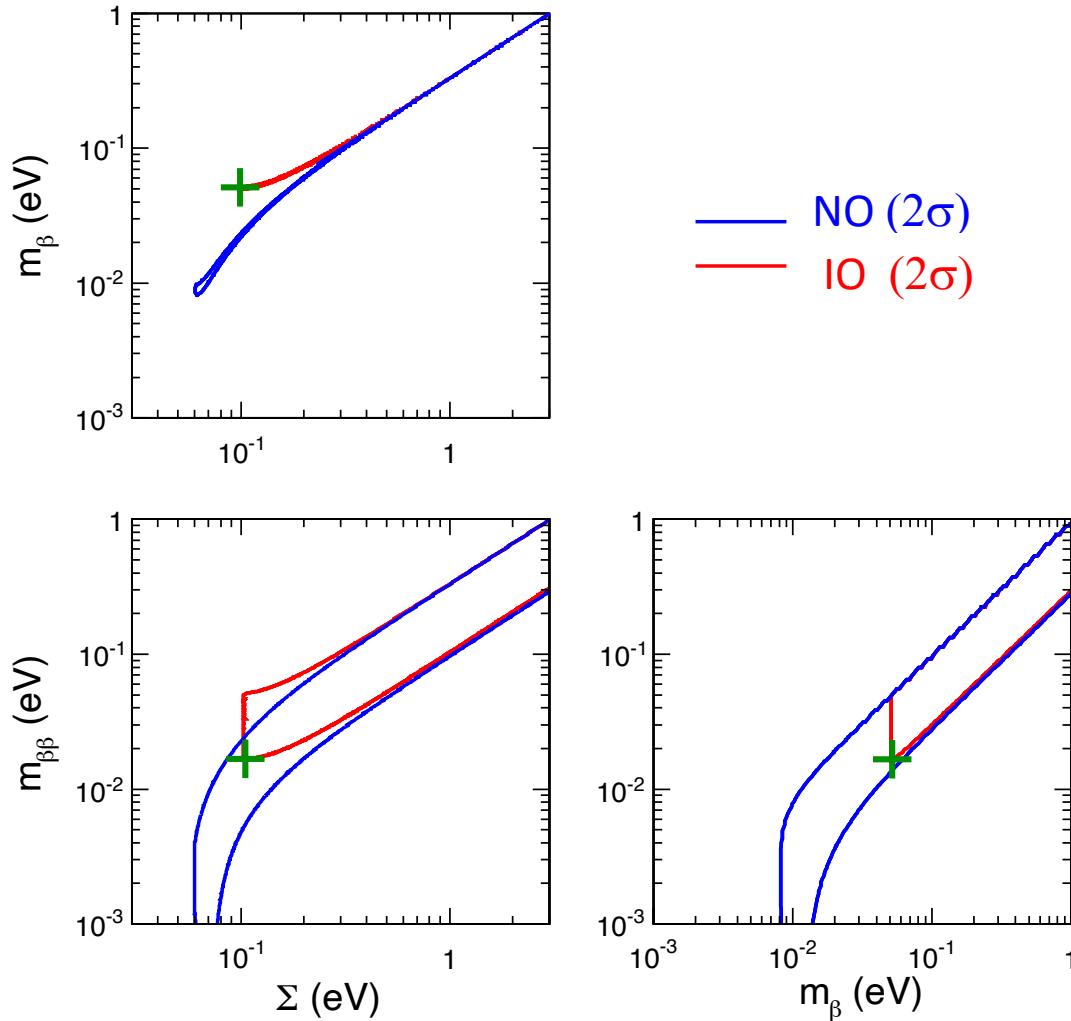
Significant progress after Planck & recent galaxy surveys...  
Upper bounds on  $\Sigma$  (well) below the eV scale

**Overview of  $(m_\beta, m_{\beta\beta}, \Sigma)$  observables →**

# Absolute mass observables: bands allowed by oscillations in NO/IO

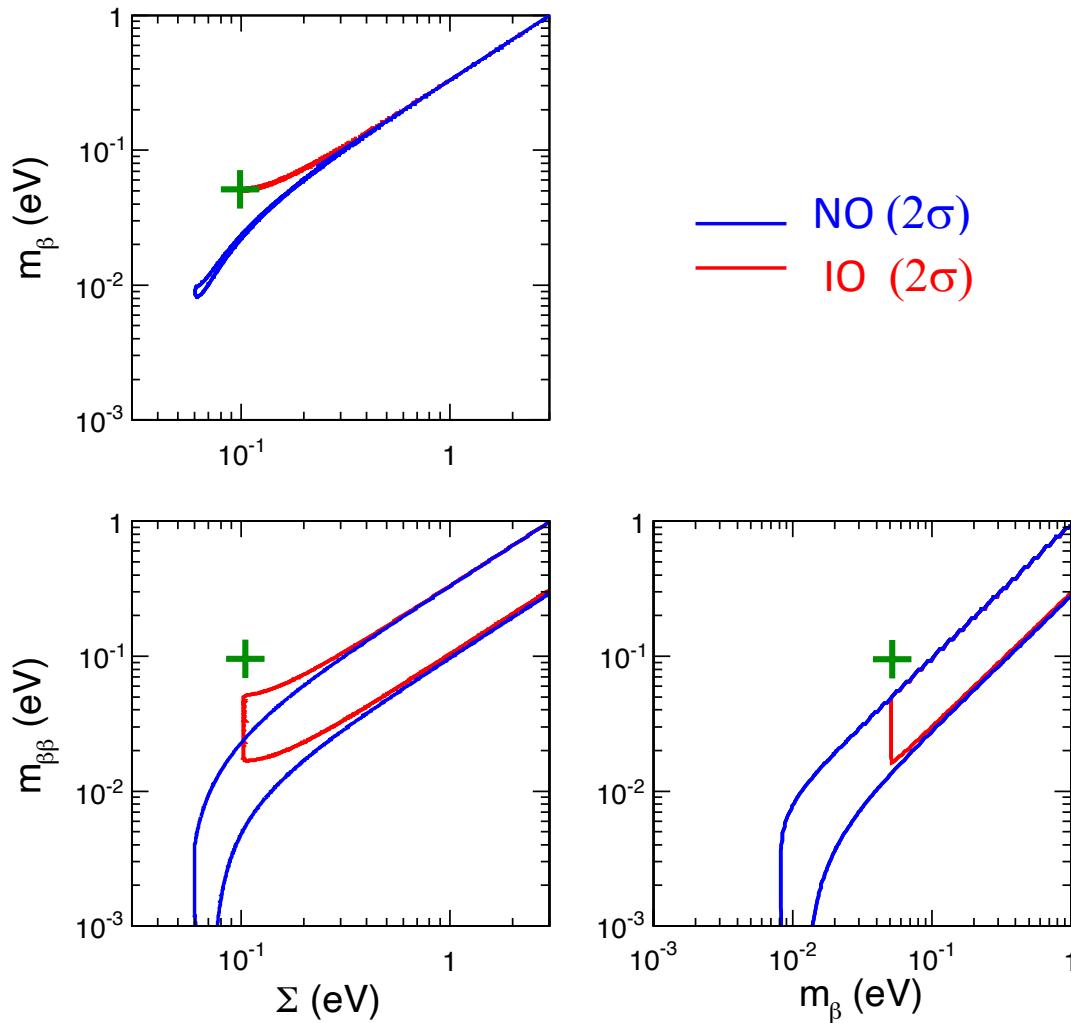


## Absolute mass observables: ...dreaming of far-future data ... +



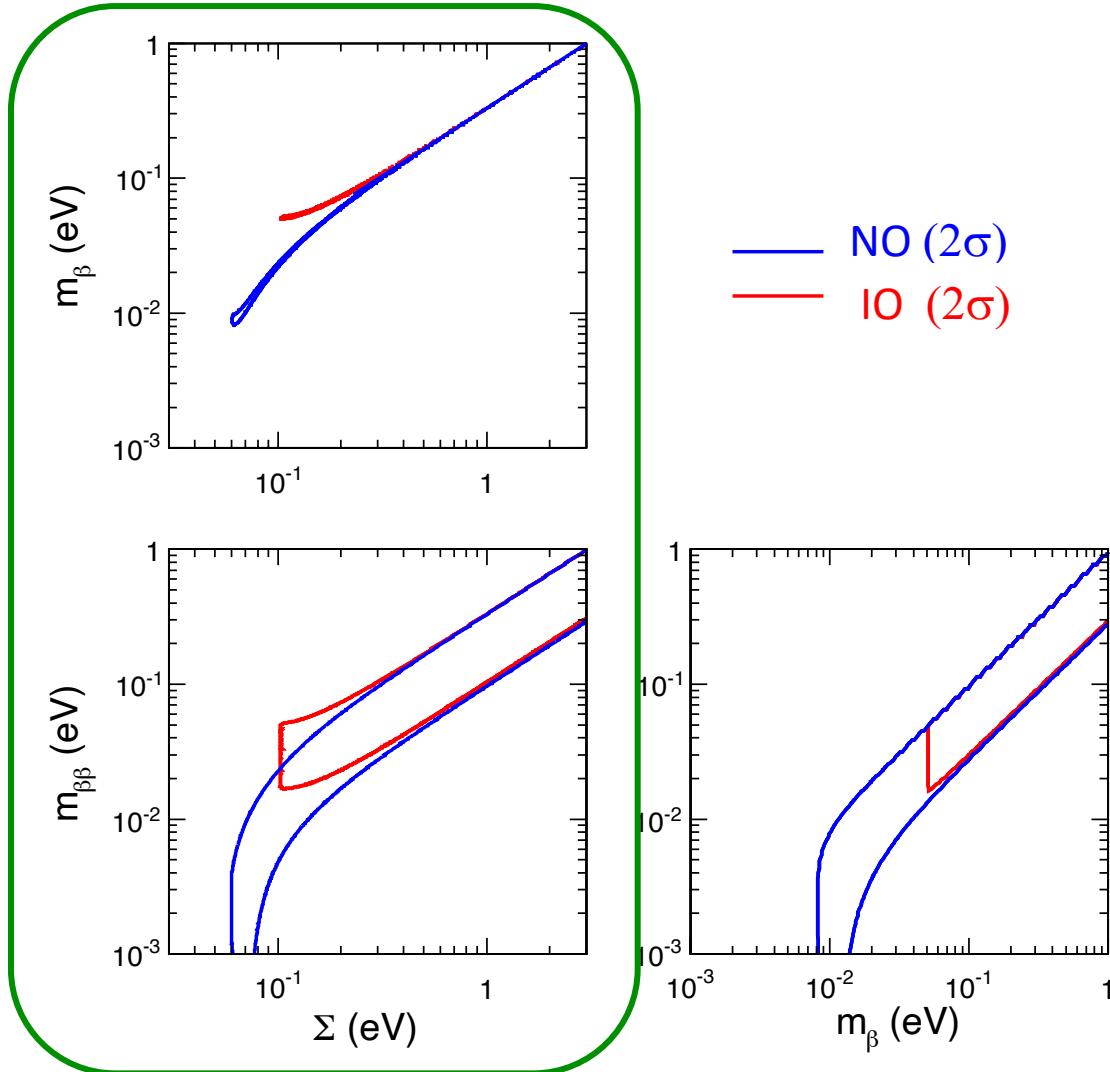
→ confirming the 3ν framework & discovering (some) current unknowns

## Absolute mass observables: ... finding some surprises ? ...

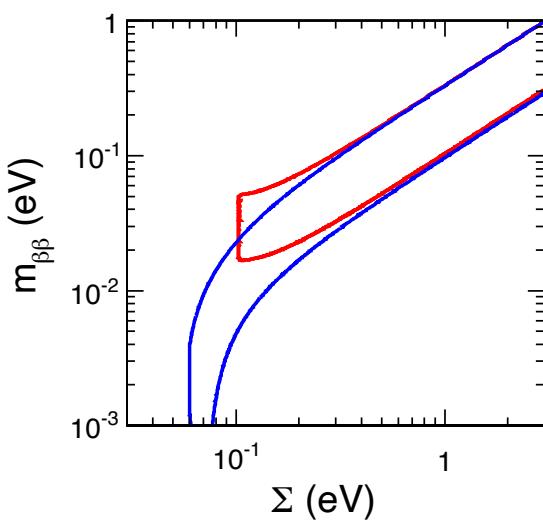
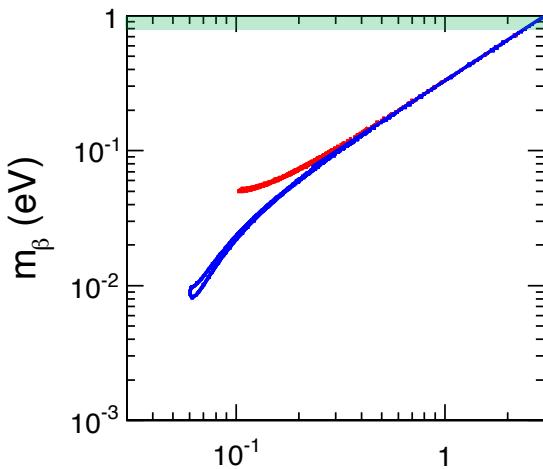


→ lack of convergence indicating new physics? (e.g., nonstandard  $0\nu\beta\beta$ )

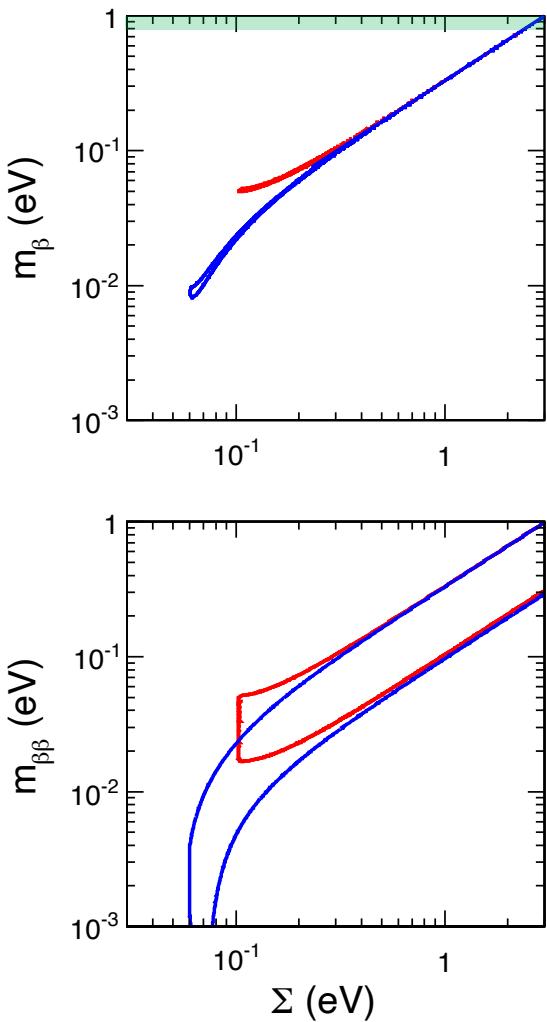
## Absolute mass observables: currently, only upper bounds!



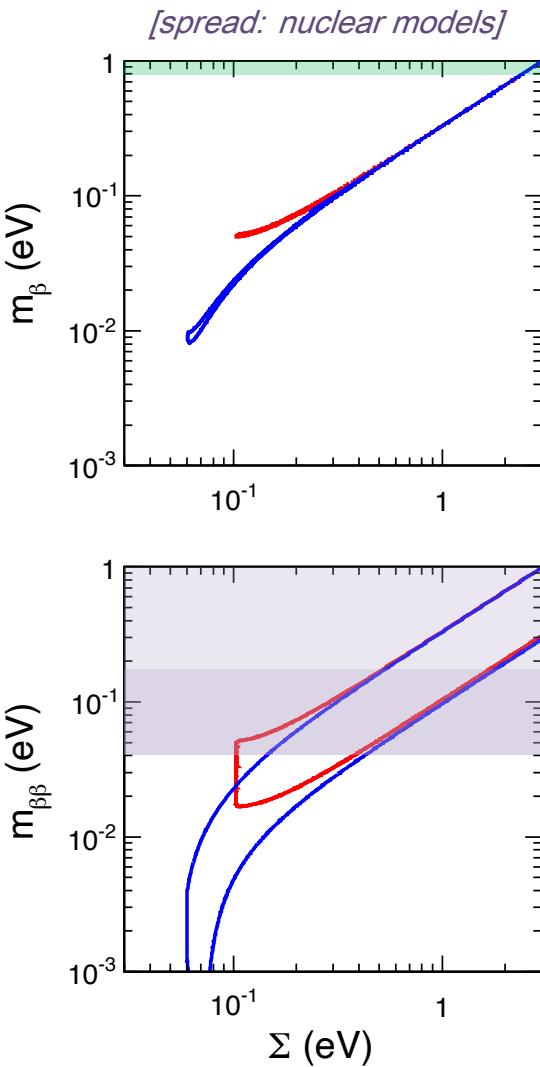
Focus on these planes



$\beta$  : KATRIN

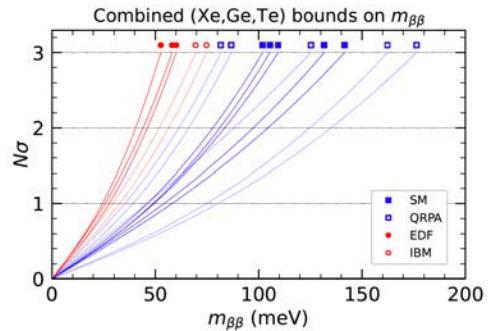


$0\nu\beta\beta$ : KL-Zen, Exo,  
GERDA, Cuore...

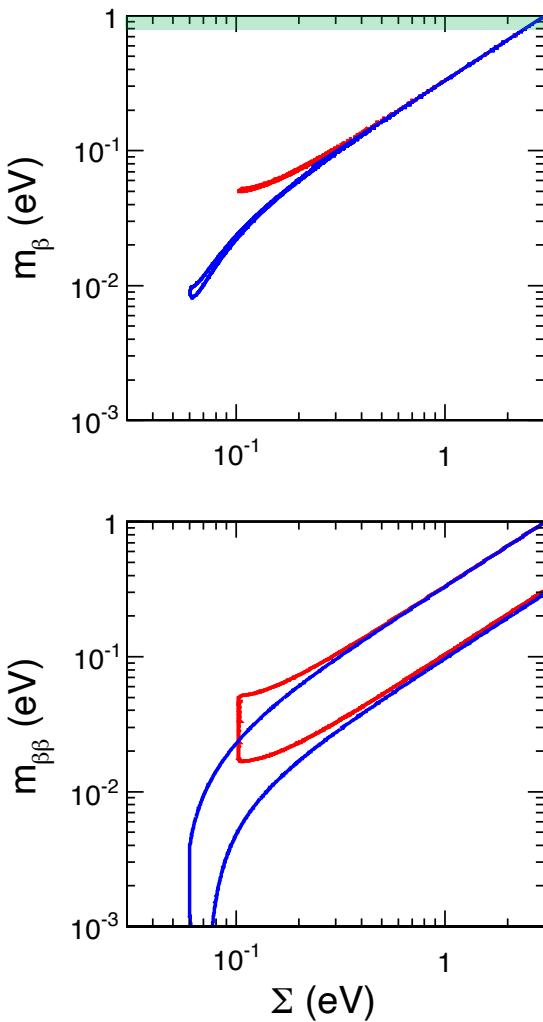


[spread: nuclear models]

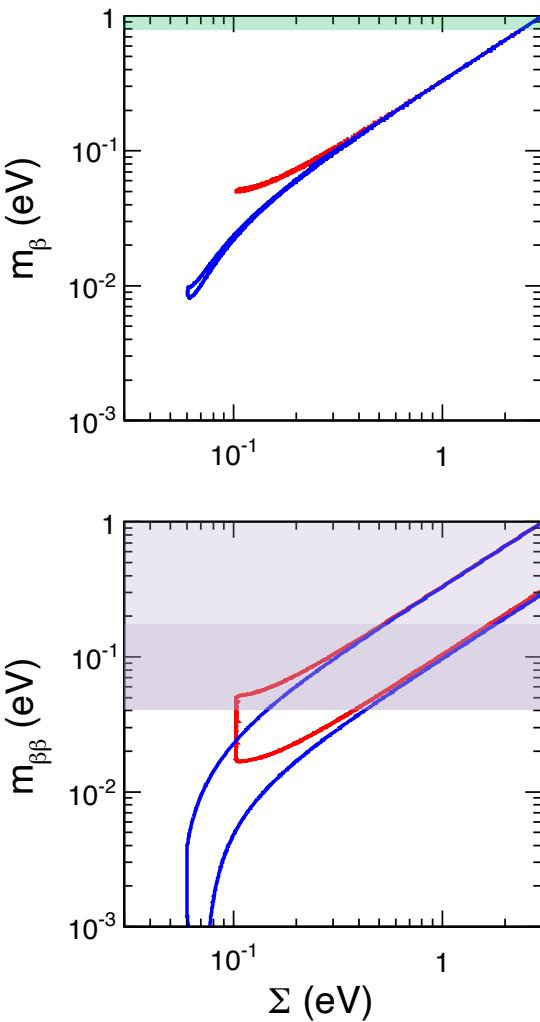
E.g., spread of upper bounds from Xe+Ge+Te data by using 15 nuclear matrix elements from 4 classes of nucl. models. e-print 2204.09569



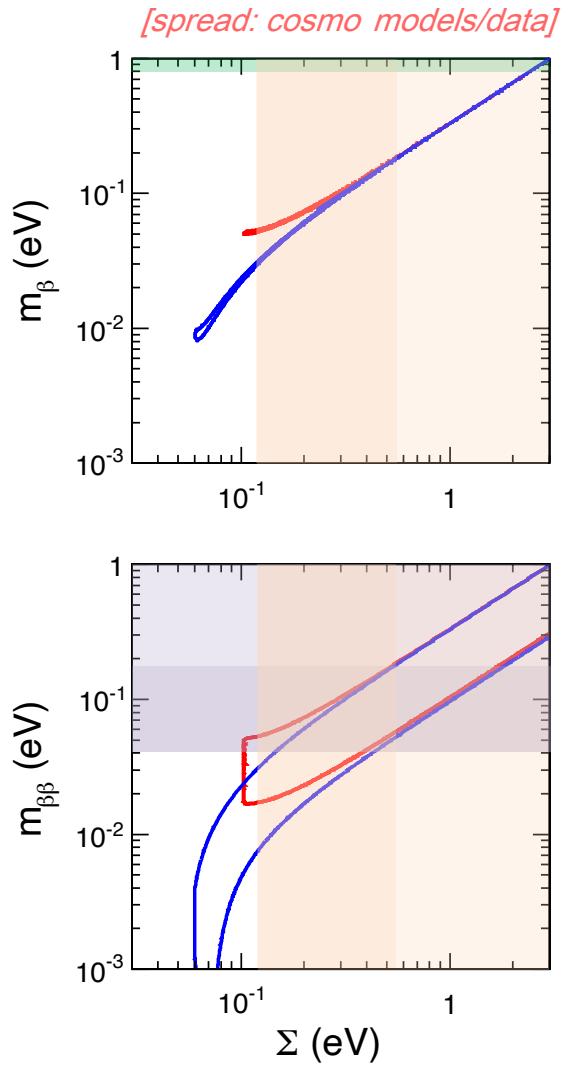
$\beta$  : KATRIN



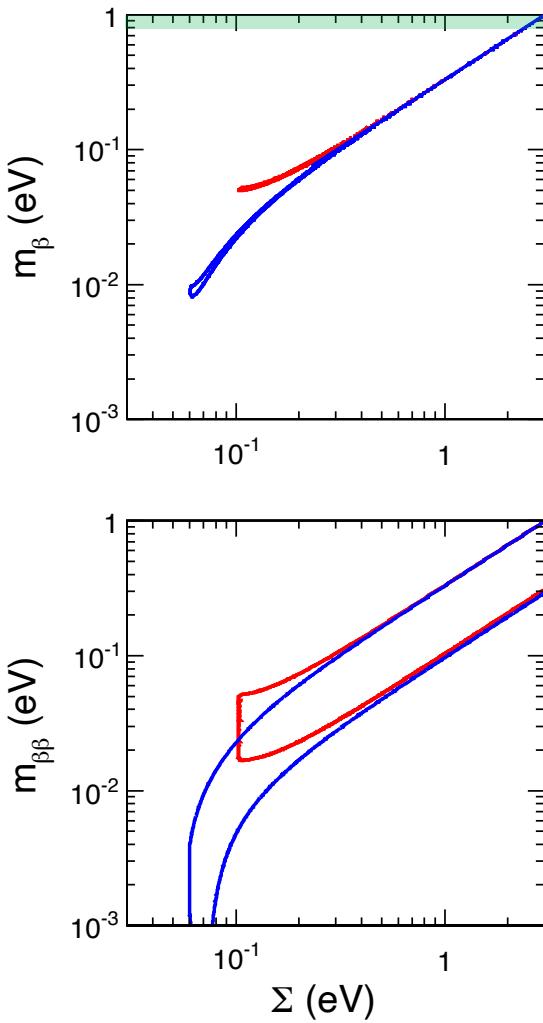
$0\nu\beta\beta$ : KL-Zen, Exo,  
GERDA, Cuore...



$\Sigma$ : Planck, BAO,  
lensing ...

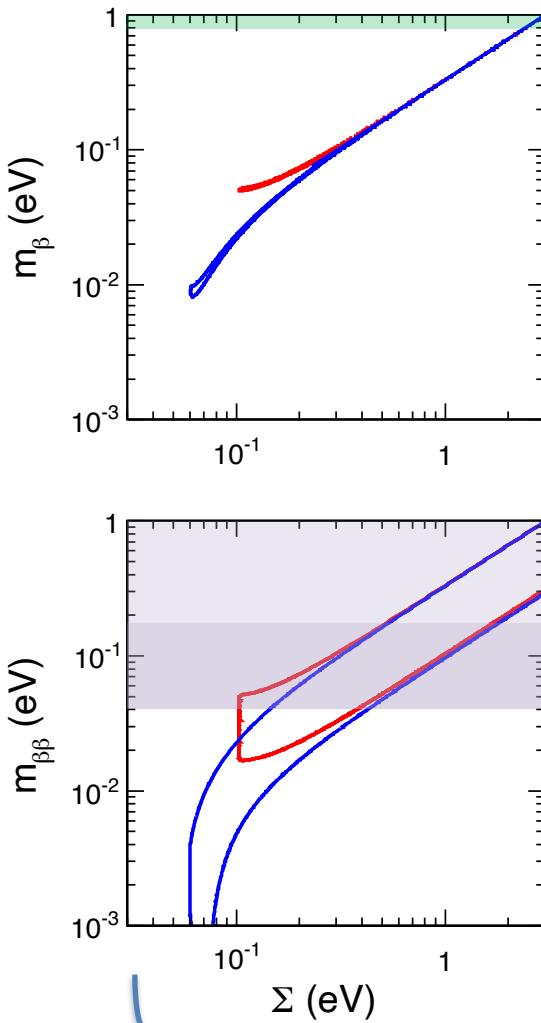


$\beta$ : KATRIN

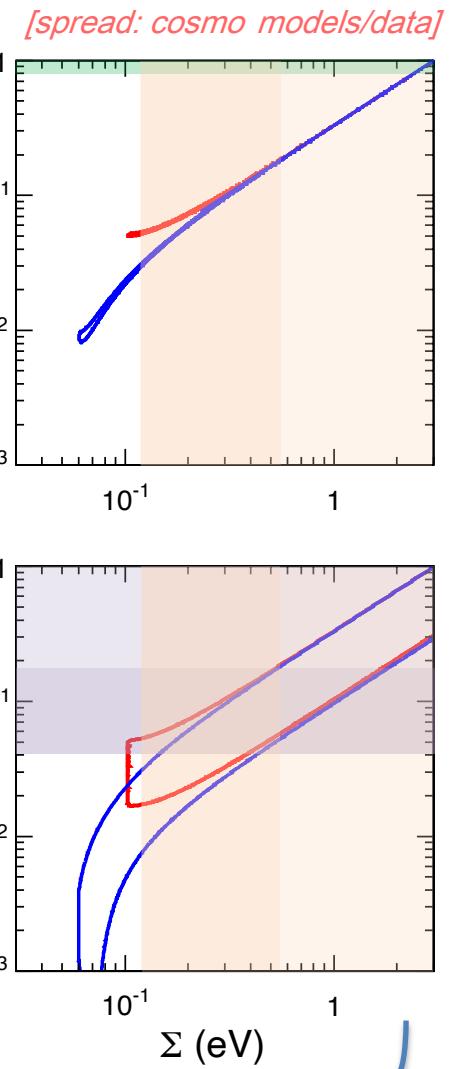


$0\nu\beta\beta$ : KL-Zen, Exo,  
GERDA, Cuore...

[spread: nuclear models]

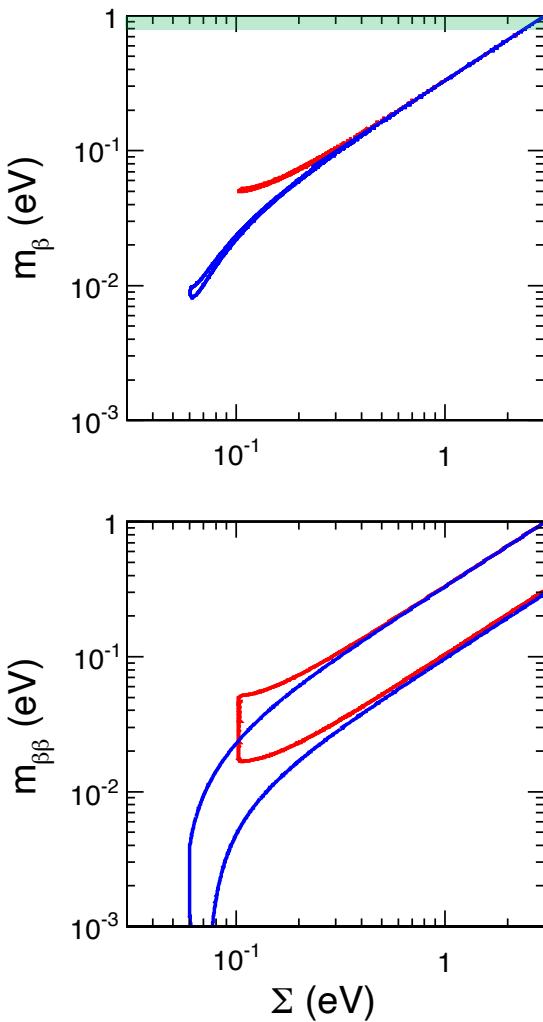


$\Sigma$ : Planck, BAO,  
lensing ...

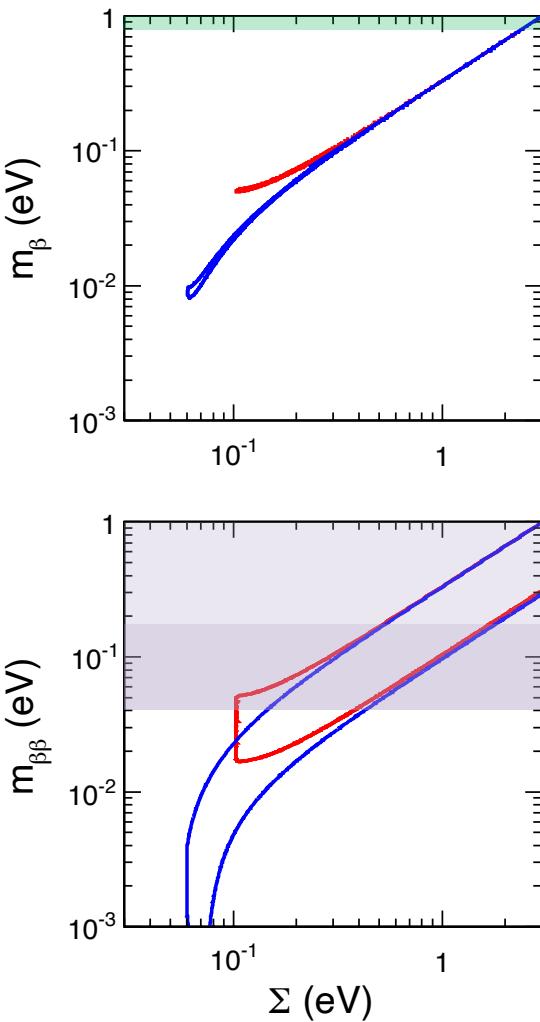


IO “under pressure” but not excluded yet  
[IO disfavored at  $\sim 3\sigma$  by osc+nonosc data]

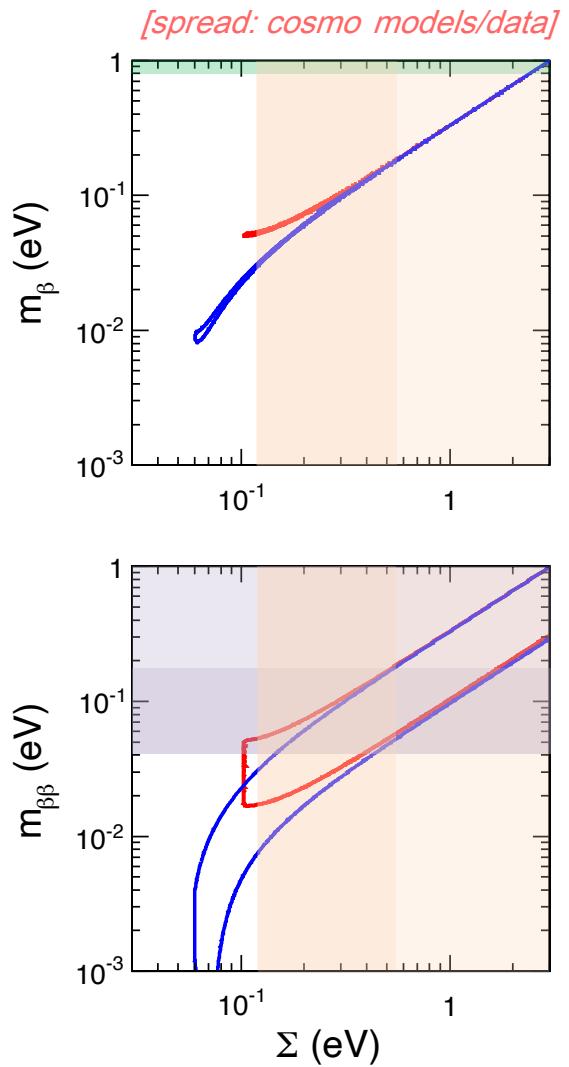
$\beta$ : KATRIN



$0\nu\beta\beta$ : KL-Zen, Exo,  
GERDA, Cuore...

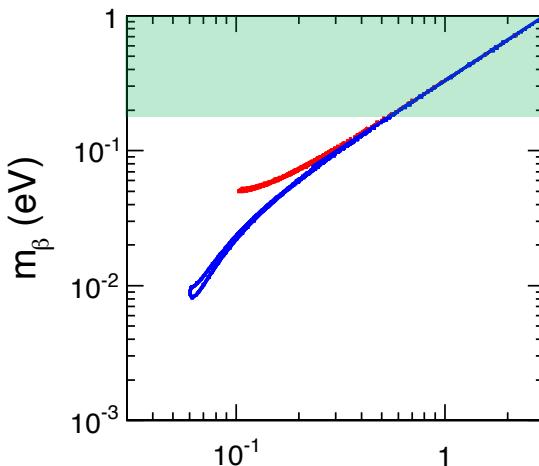


$\Sigma$ : Planck, BAO,  
lensing ...

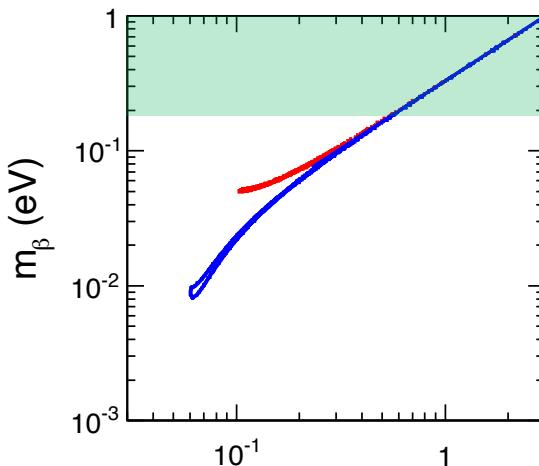


Frontiers for the next ~10-20 yrs →

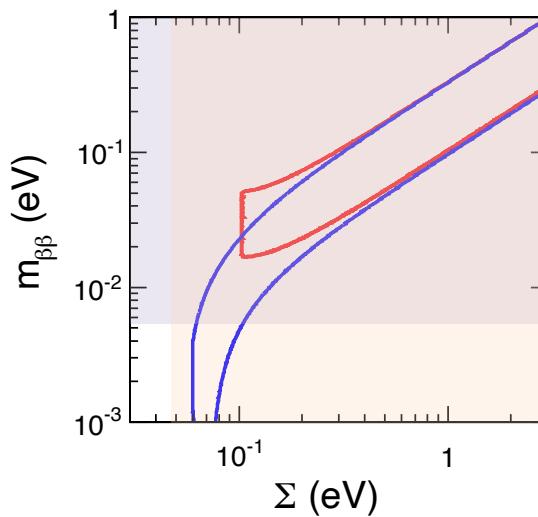
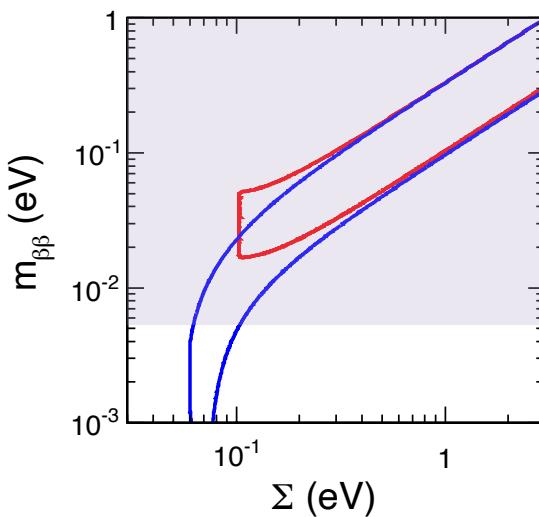
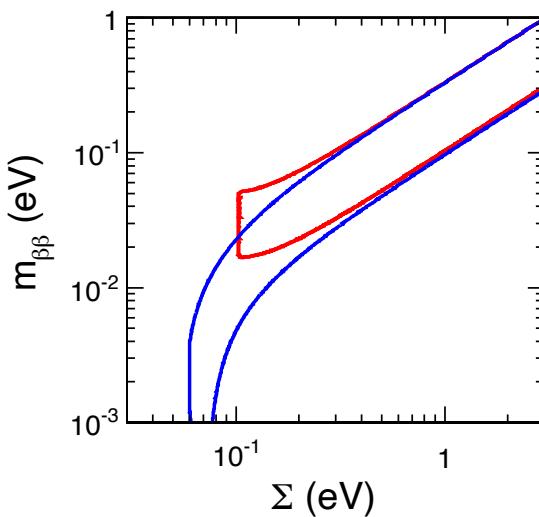
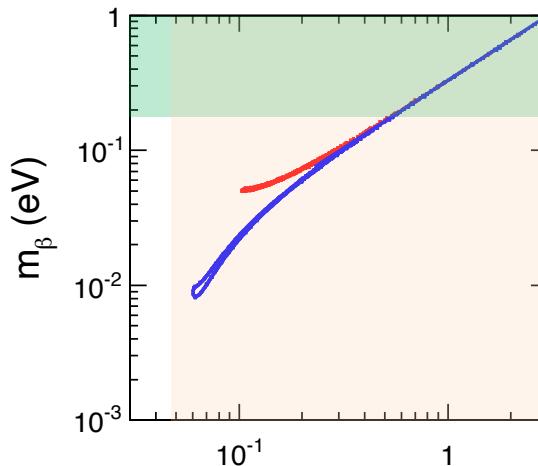
$\beta$ : ~0.2 eV sensitivity  
(difficult to go beyond KATRIN afterwards)



   $0\nu\beta\beta$ : Well below IO limit at ton scale (LEGEND, NEXO, CUPID...) w/ improved NME



   $\Sigma$ : complete covering seems possible if cosmo model globally confirmed.



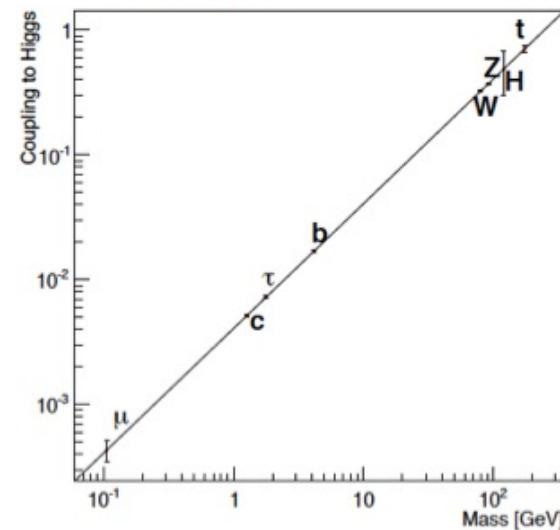
See e.g. review talks at Neutrino 2022 and NOW 2022 + Snowmass 2022 Reports

Large phase space for possible signal discoveries

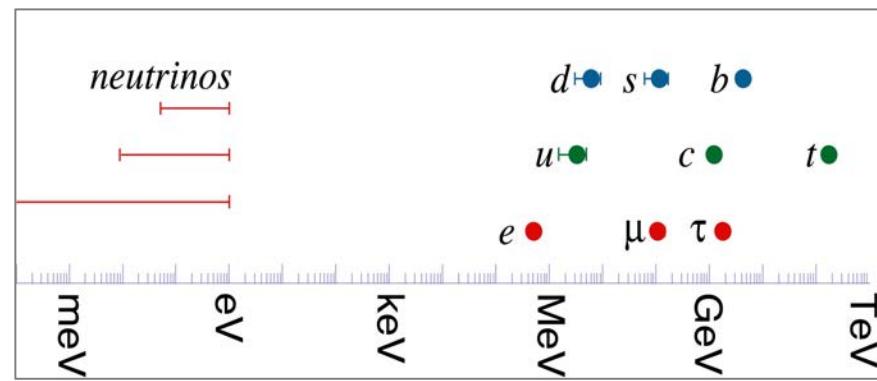
First claims about absolute neutrino mass are likely to come from cosmology!

# Neutrino mass and Dirac/Majorana nature: Linking two research programs

## 1. Test Higgs sector

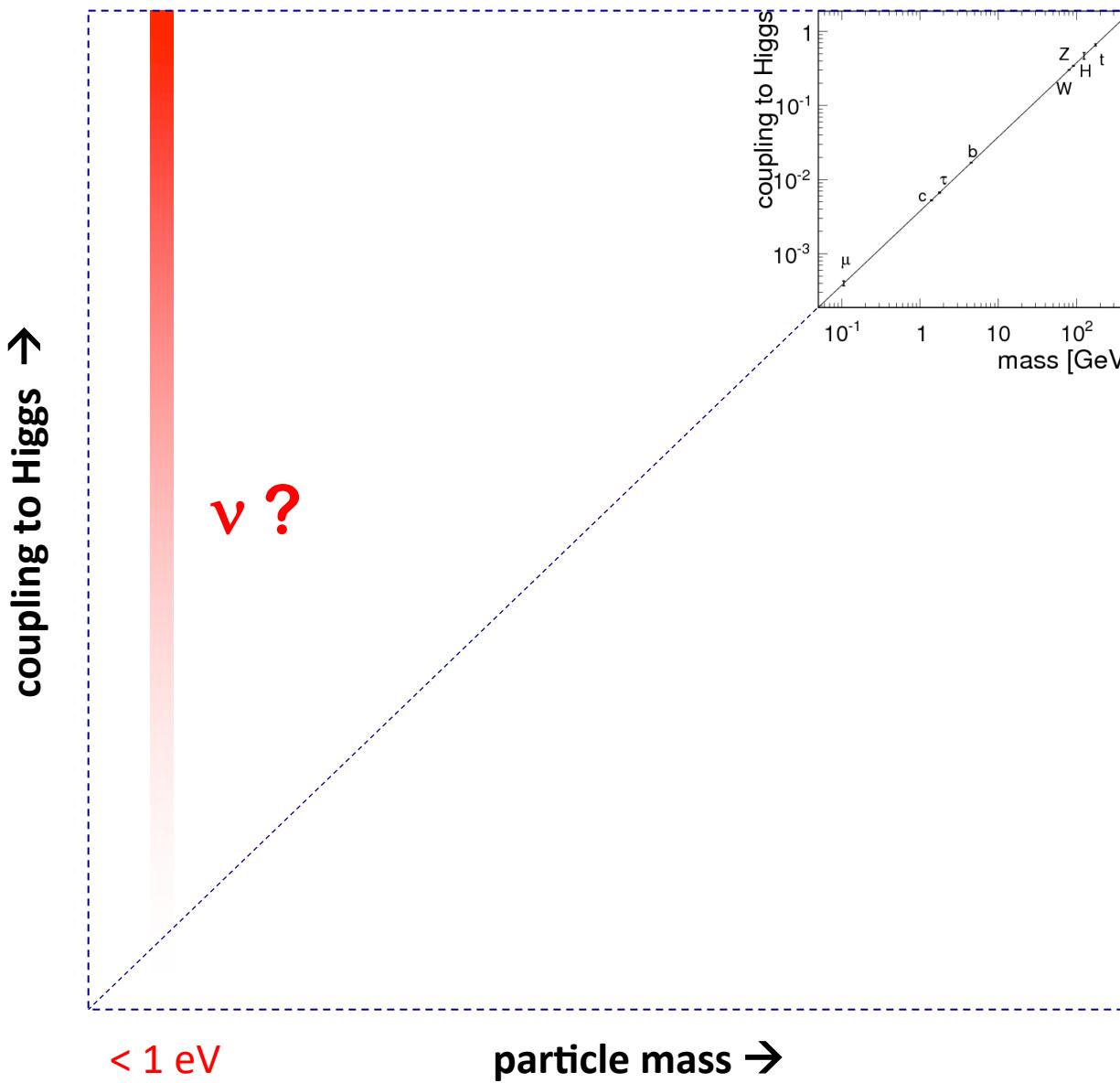


## 2. Find $\nu$ masses



**1 + 2**

Where are the  $\nu$ 's on this plot? Why are they so light?



# Options:

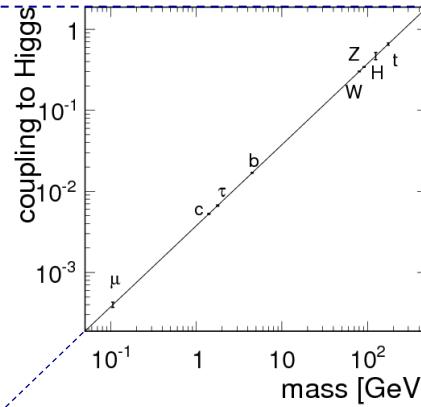
coupling to Higgs →

< 1 eV

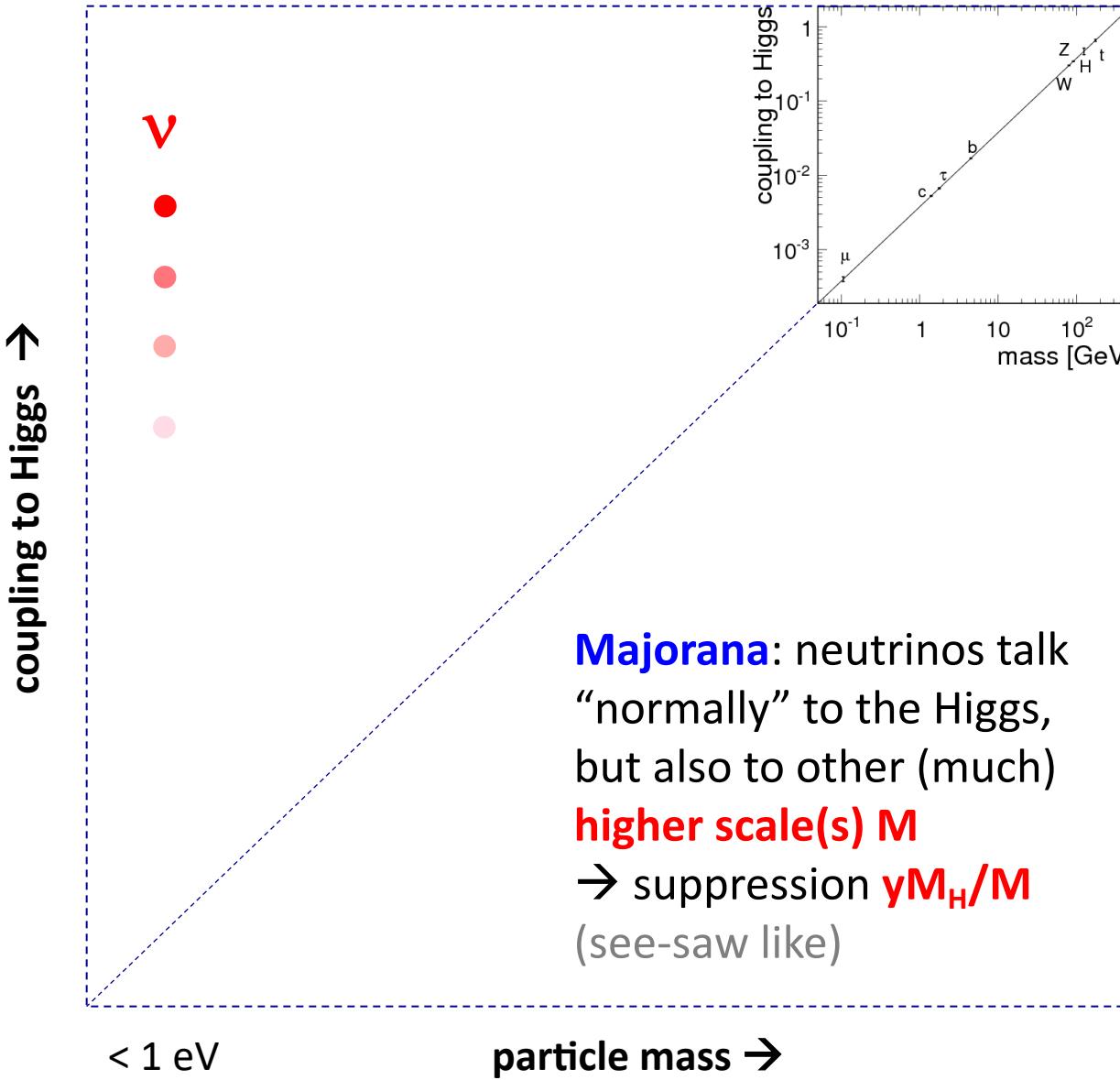
particle mass →

**Dirac:** neutrinos “talk”  
very weakly to the  
Higgs boson,  $y < 10^{-12}$   
for unknown reasons...

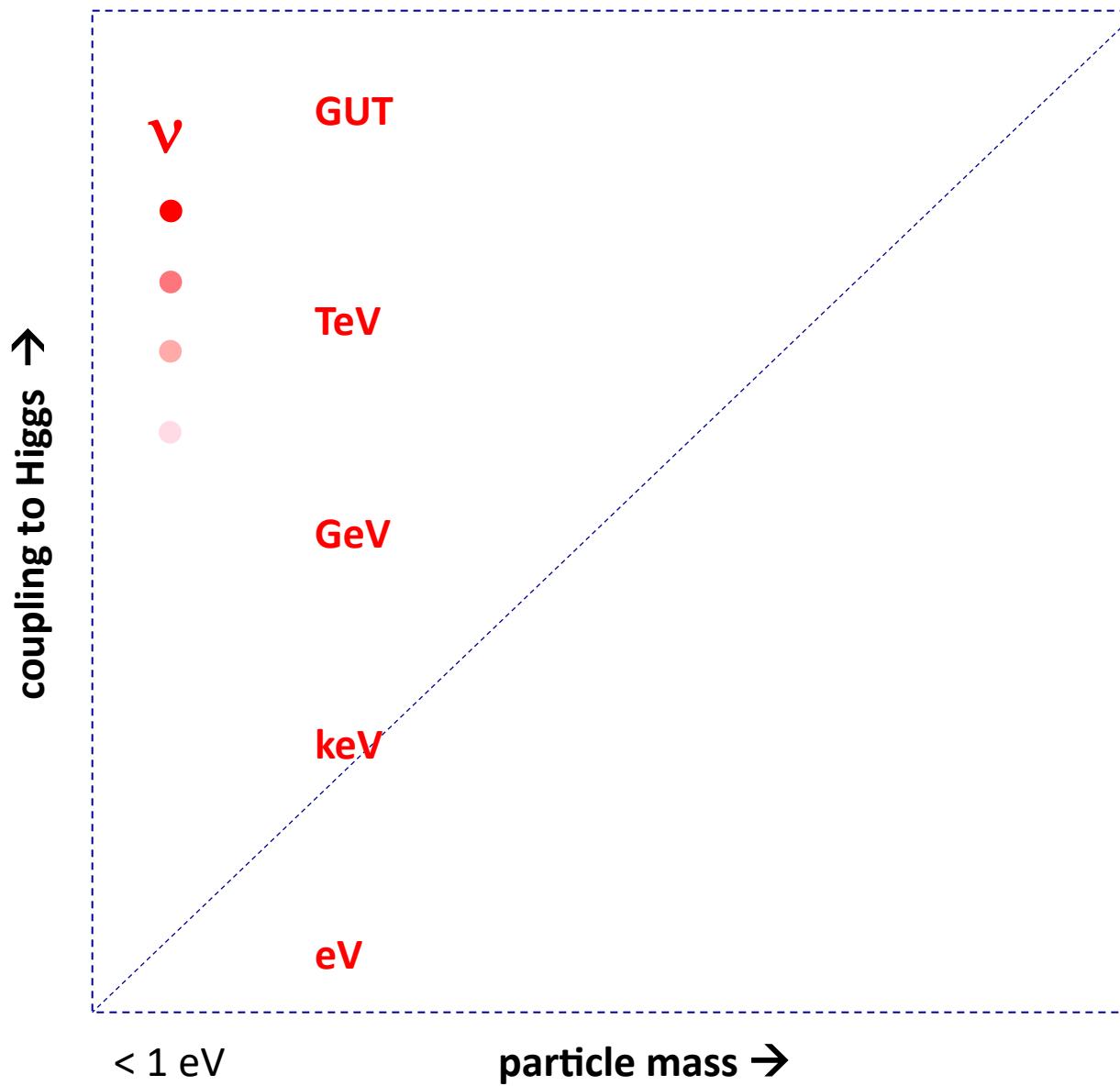
$\nu$



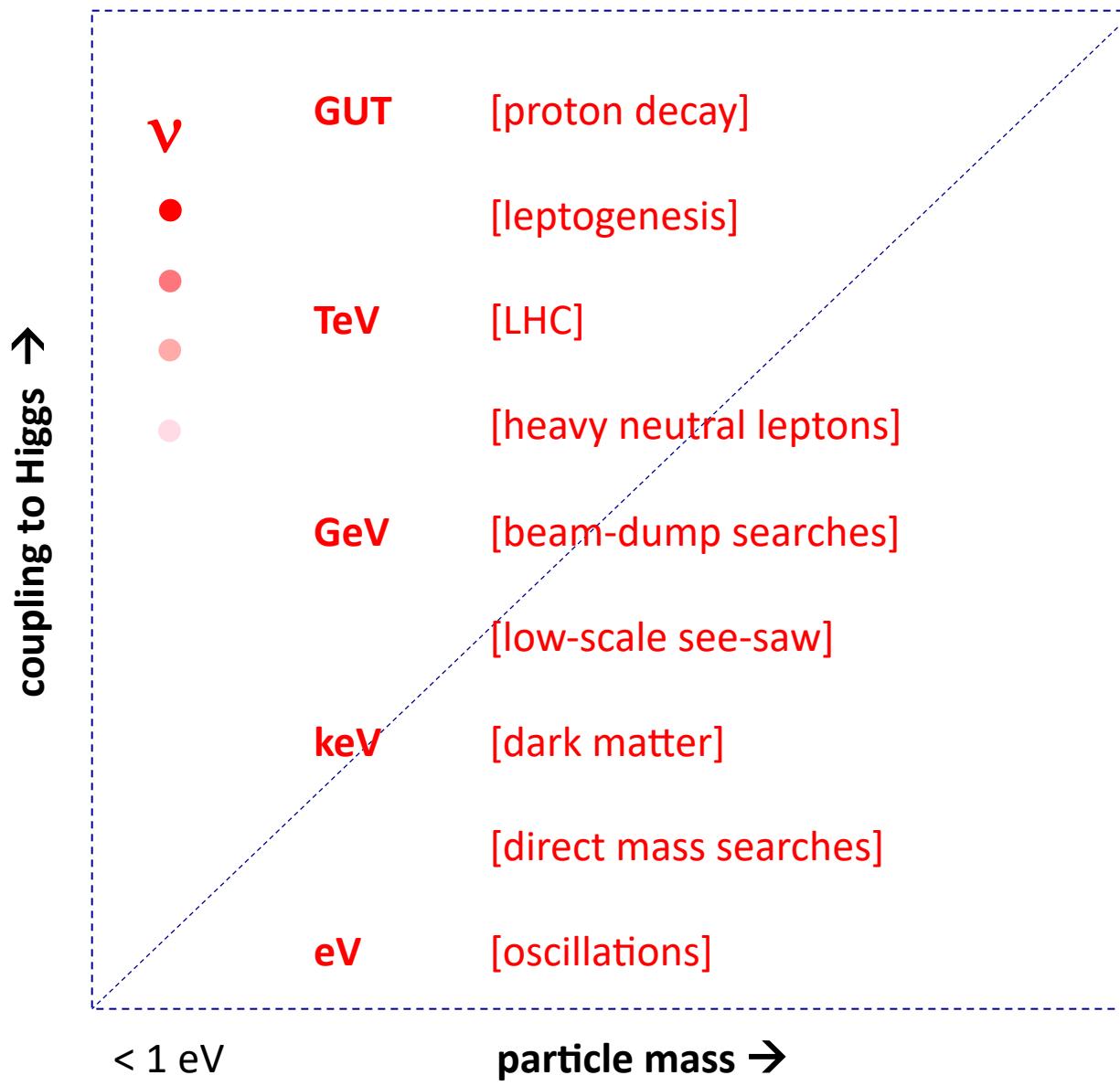
# Options:



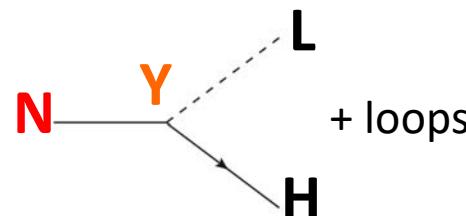
...New  $\nu$  mass states could emerge at one or more scales ...



... and contribute to a wide research program with HE/LE links...



**E.g. Leptogenesis:** C, CP, L-violating and out-of-equilib. decays of heavy N at  $T \sim M_N$  can generate lepton asymmetry  $\Delta L \rightarrow$  non-perturb.  $\rightarrow \Delta B$  (BAU)



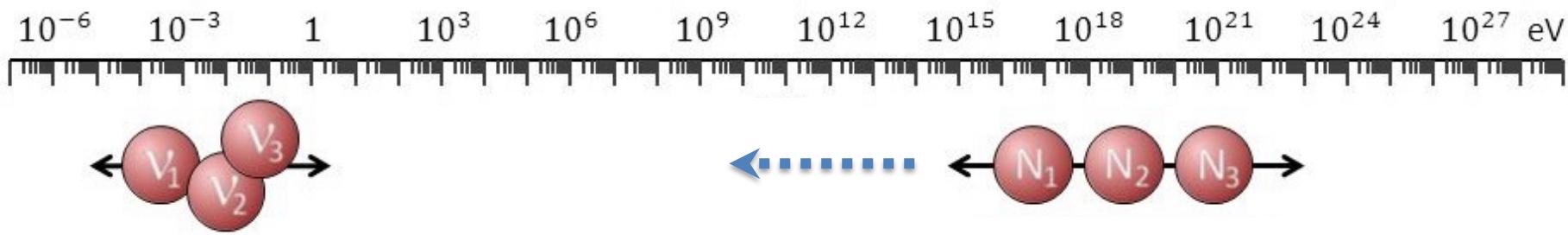
with:  $\Gamma(N \rightarrow L) \neq \Gamma(N \rightarrow \bar{L}) \rightarrow \Delta L$

via:  $Y \sim U_\nu \ m_\nu^{1/2} \ \frac{1}{v} \ U_N \ M_N^{1/2}$

Involves masses, mixing, phases at both low ( $v$ ) and high ( $N$ ) scales.

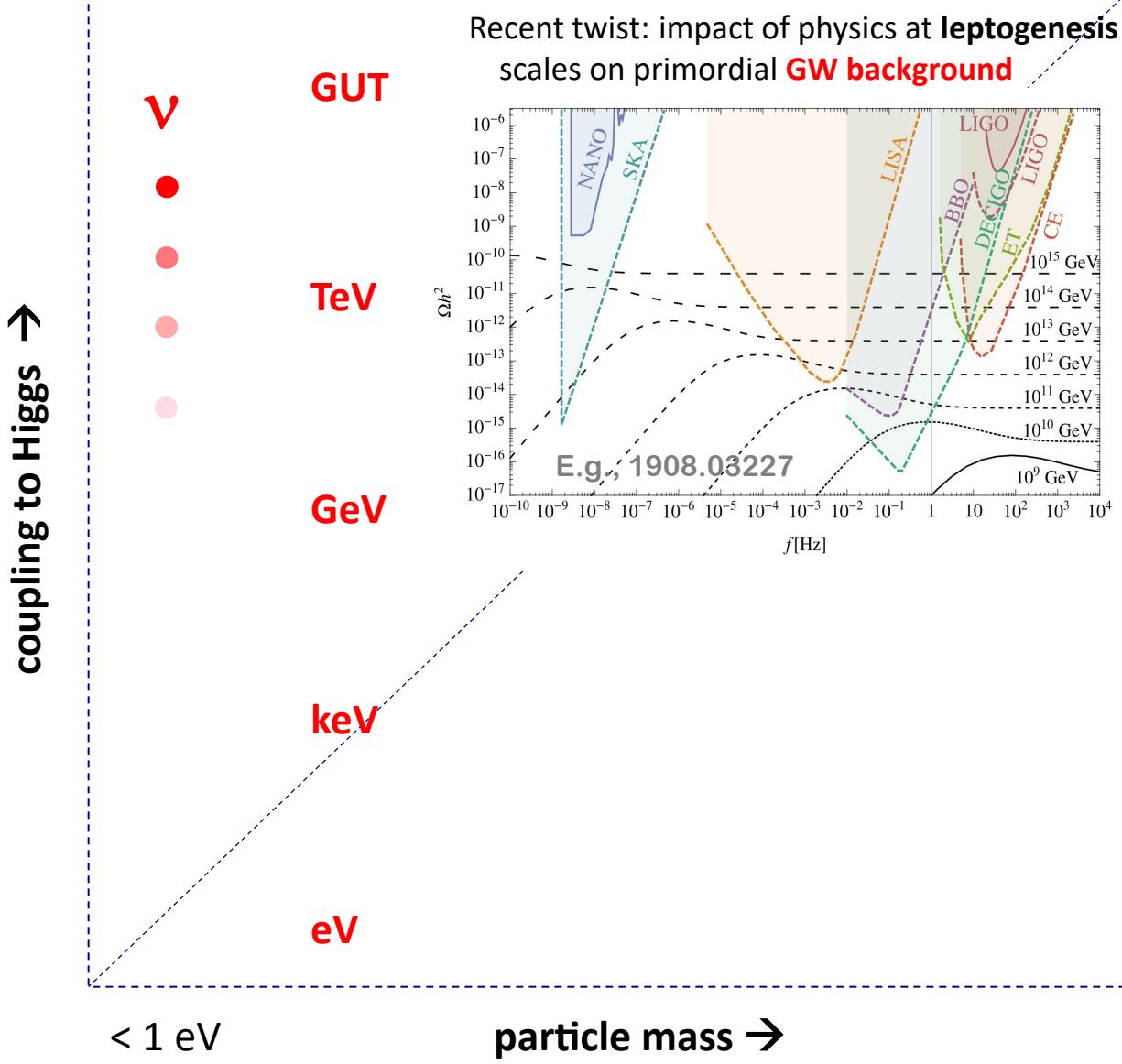
Involves (non)equilibrium evolution in an expanding & cooling universe.

Significant work to assess/extend ranges of  $M$  (and  $T$ ) of successful models



At low scale: contact with low-energy CPV and  $0\nu\beta\beta$  decay

At high scale: contact with heavy N searches and other HE processes



# Summary

Knowns:

$\delta m^2$ ,  $|\Delta m^2|$ ,  $\theta_{13}$ ,  $\theta_{12}$  and  $\theta_{23}$  (up to octant)

→ worldwide precision physics program

Unknowns:

NO/IO, CPV, abs. mass, Majorana/Dirac

→ ongoing searches aiming at discoveries

Be open to:

New  $\nu$  states and interactions, HE/LE links

→ diversity of expt/theo approaches

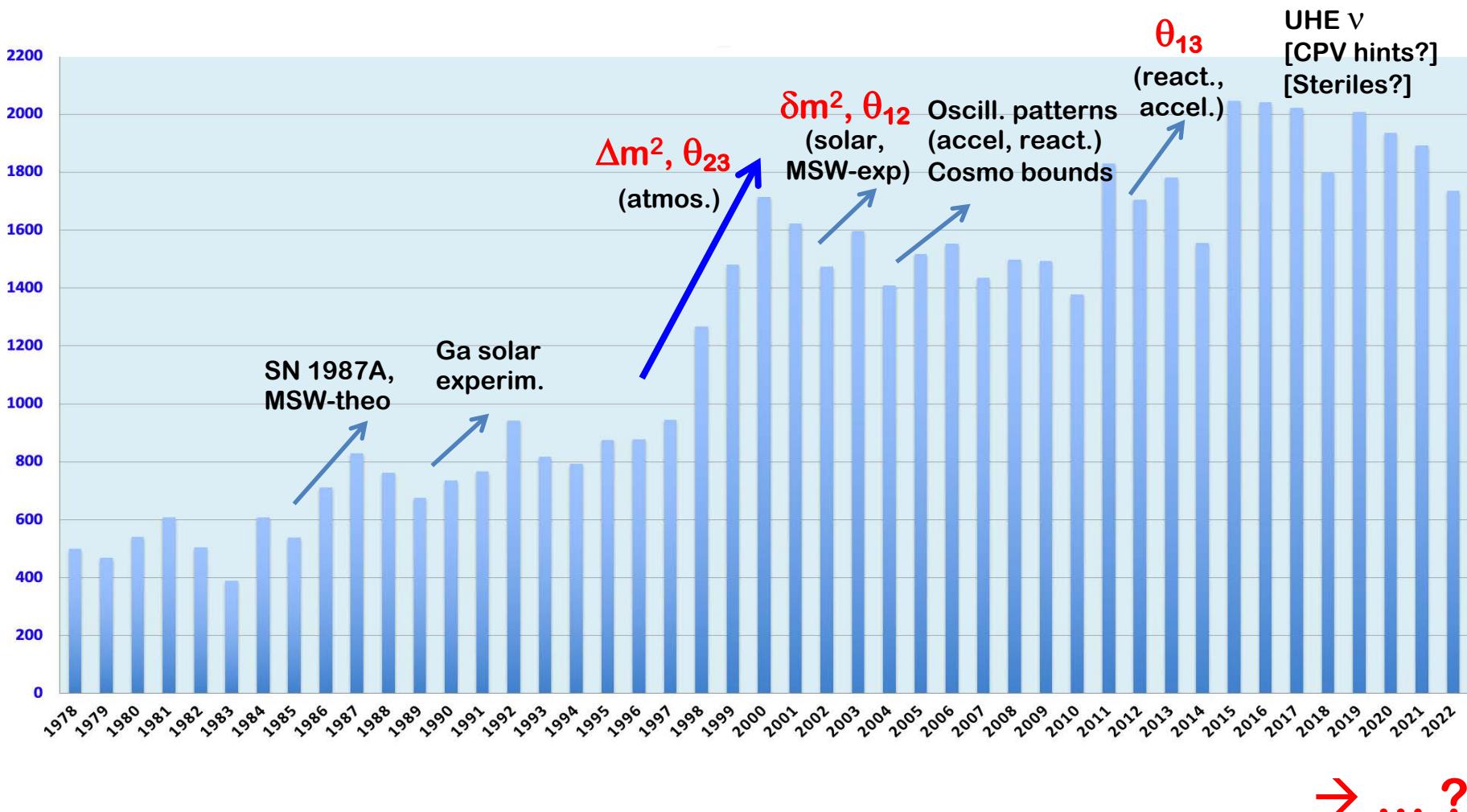
Be part of this adventure!

While answering old questions...

→ new questions will emerge!



# Papers with \*neutrino\* in the title, yearly trend from iNSPIRE



→ ... ?