Regressogram Implementation & Analysis

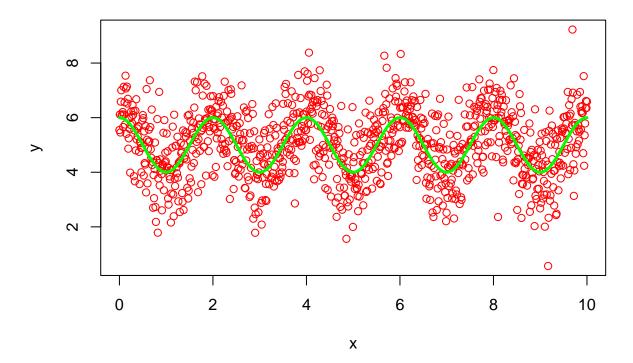
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Let us assume the function (on which we want to perform regression) as $5+\cos(pi^*x)+$ noise and the domain to be [0,10]

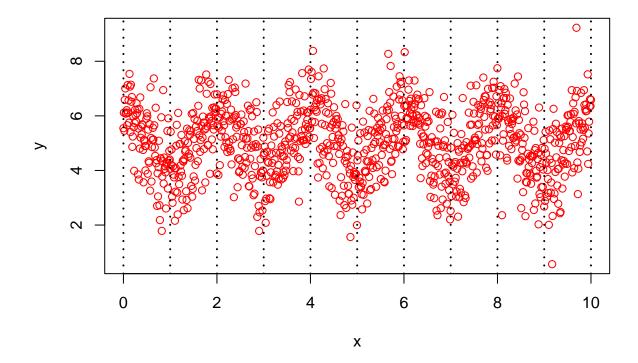
```
n = 1000
x = seq(0,10,length.out=n)
y = 5 + cos(pi*x) + rnorm(n)
#y = 5 + cos(pi*x)
plot(x,y,col="red",main="Regressogram")
curve(5+cos(pi*x),min(x),max(x),n,add=TRUE,col="green",lwd=3)
```

Regressogram



Let's say the number of bins we want is 10.We plot the bin boundaries as well using vertical lines, splitting the x axis into 10 different rectangles/bins.

```
m = 11
bins = 0:10
plot(x,y,col="red")
abline(v = bins,lty = 3,lwd=2)
```

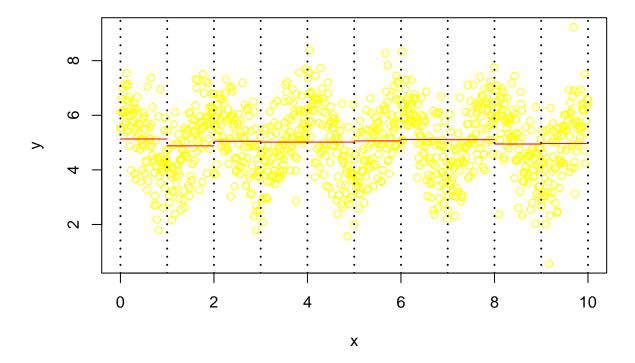


We initialize all the estimates for the m different Y's to 0.We then evaluate the estimates as the mean of all the y values in a particular bin. For the last bin, we calculate the mean separately as both the bin endpoints are included. We then plot horizontal lines, across each bin width, representing the mean calculated (i.e the y estimate).

```
y.hat=rep(0,m-1)
for (i in 1:(m-2)){
    # y.hat[i] <- mean(y[which((x<bins[i+1]) & (x>=bins[i]))])
    y.hat[i] <- mean(y[which((bins[i]<=x)&(x<bins[i+1]))])
}

#for the last bin
y.hat[m-1] = mean(y[which((x<=bins[m]) & (x>= bins[m-1]))])

plot(x,y,col="yellow")
abline(v = bins,lty = 3,lwd=2)
for (i in 1:(m-1)){
    lines(bins[i:(i+1)],rep(y.hat[i],2),col="red")
}
```



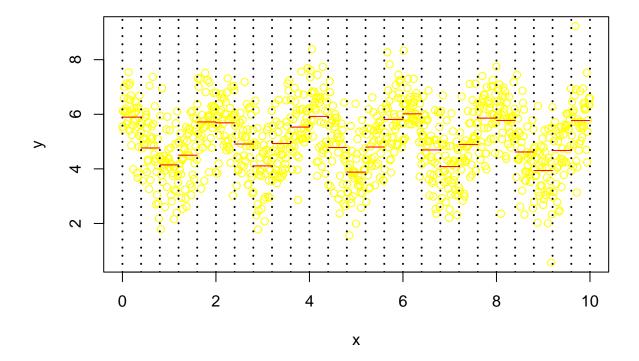
Let's now say the number of bins we want is 26 and repeat the same procedure.

```
m = 26
bins = seq(0,10,by=0.4)

y.hat=rep(0,m-1)
for (i in 1:(m-2)){
    # y.hat[i] <- mean(y[which((x<bins[i+1]) & (x>=bins[i]))])
    y.hat[i] <- mean(y[which((bins[i]<=x)&(x<bins[i+1]))])
}

#for the last bin
y.hat[m-1] = mean(y[which((x<=bins[m]) & (x>= bins[m-1]))])

plot(x,y,col="yellow")
abline(v = bins,lty = 3,lwd=2)
for (i in 1:(m-1)){
    lines(bins[i:(i+1)],rep(y.hat[i],2),col="red")
}
```



We can thus conclude that increasing the number of bins gives us a better overall fit that matches the true shape of the function (in question) in a much improved manner. The advantage is that we do this without assuming the functional form for the true original function.