

Basic Principles of Soil Mechanics

CI1-150 Geotechnics



Classification/Description

Why?

- To predict engineering performance
- Engineering properties Strength, stiffness and permeability will depend on both the *nature* and *state* of soil

Description

Describe what you see and how soil responds to simple tests.

Classification

Process of separating soils into broad groups that have similar behaviour or characteristics.

Nature and State

Nature;

The essential characteristics or basic qualities of the soil

State;

The physical condition in which the soil exists

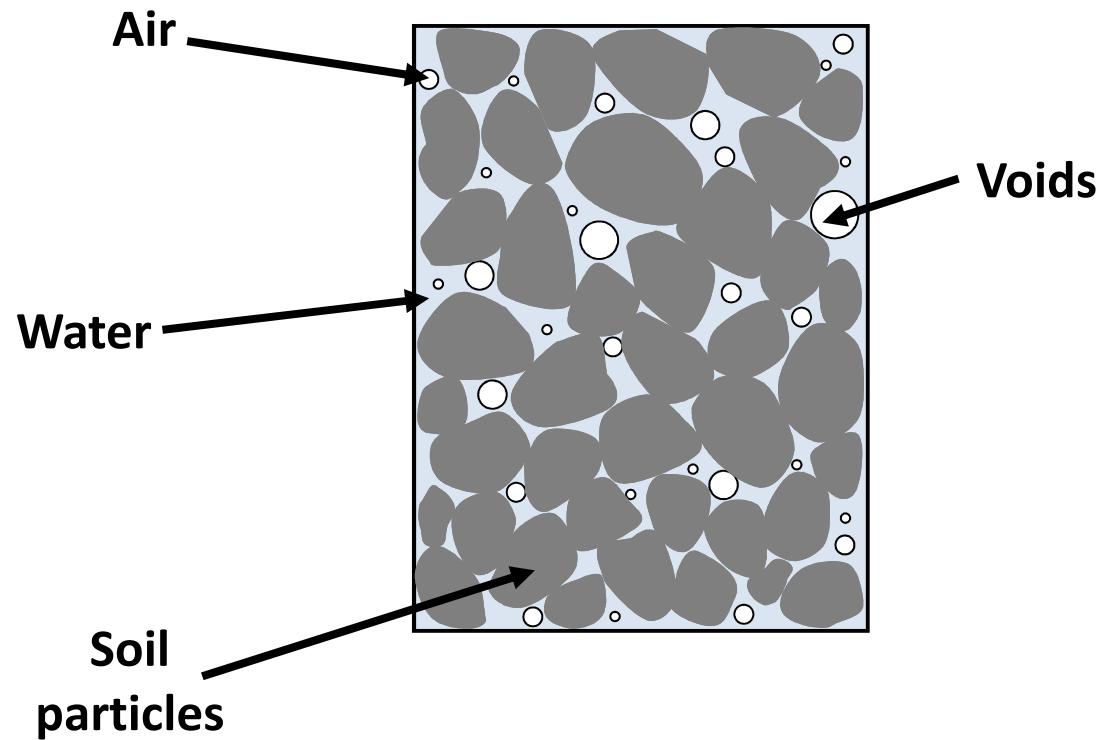


Nature

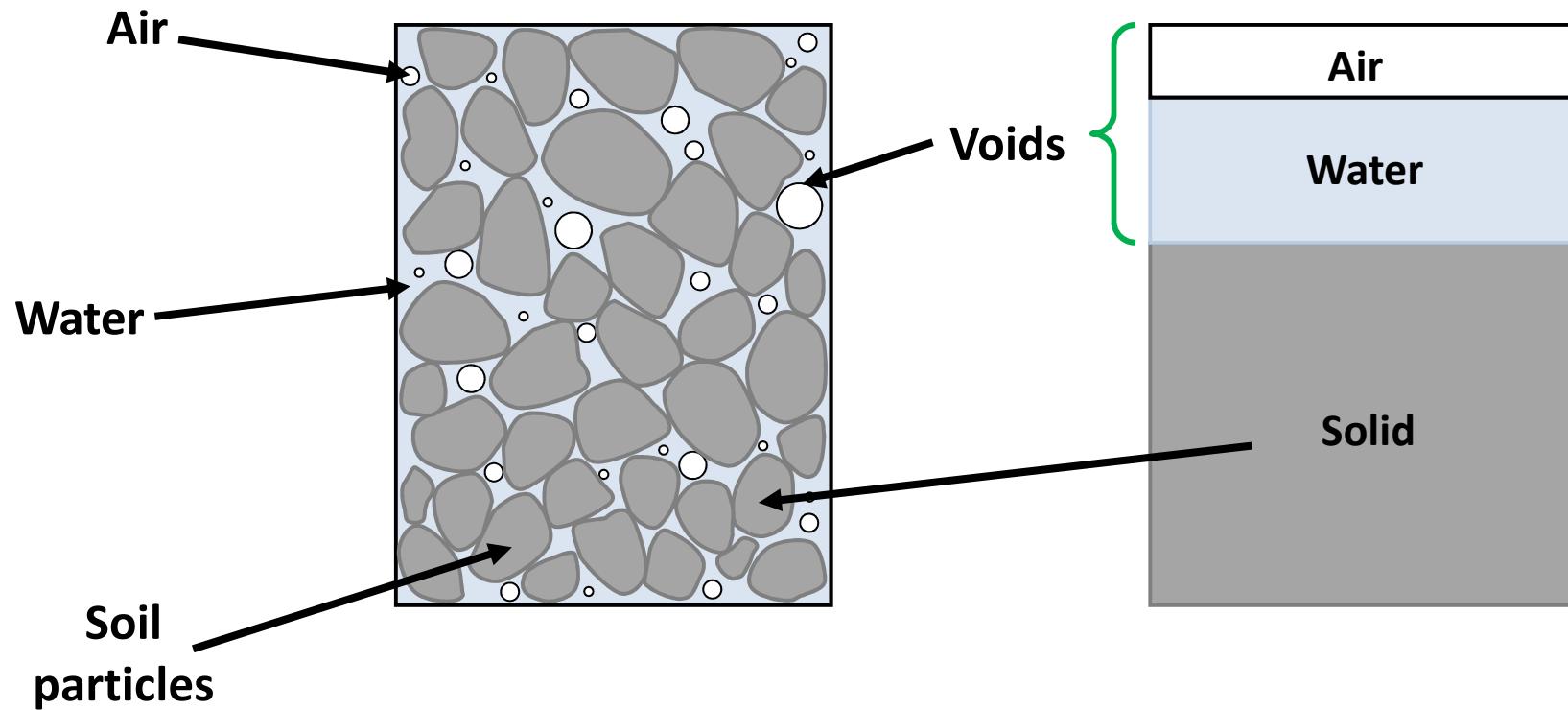
The essential characteristics or basic qualities of the soil



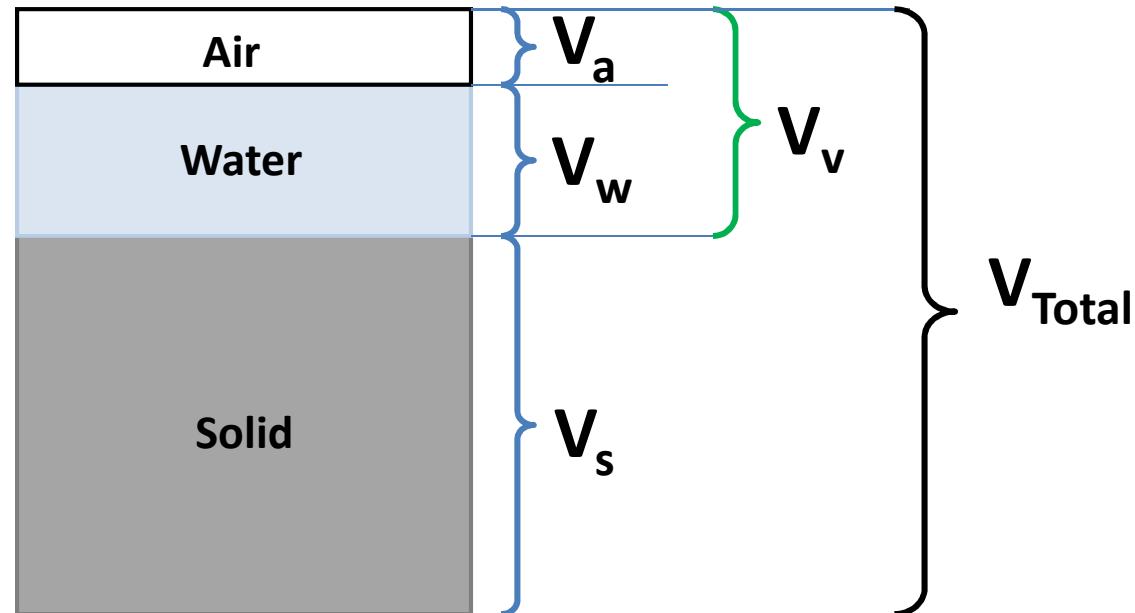
What is soil composed of?



Phase Diagram



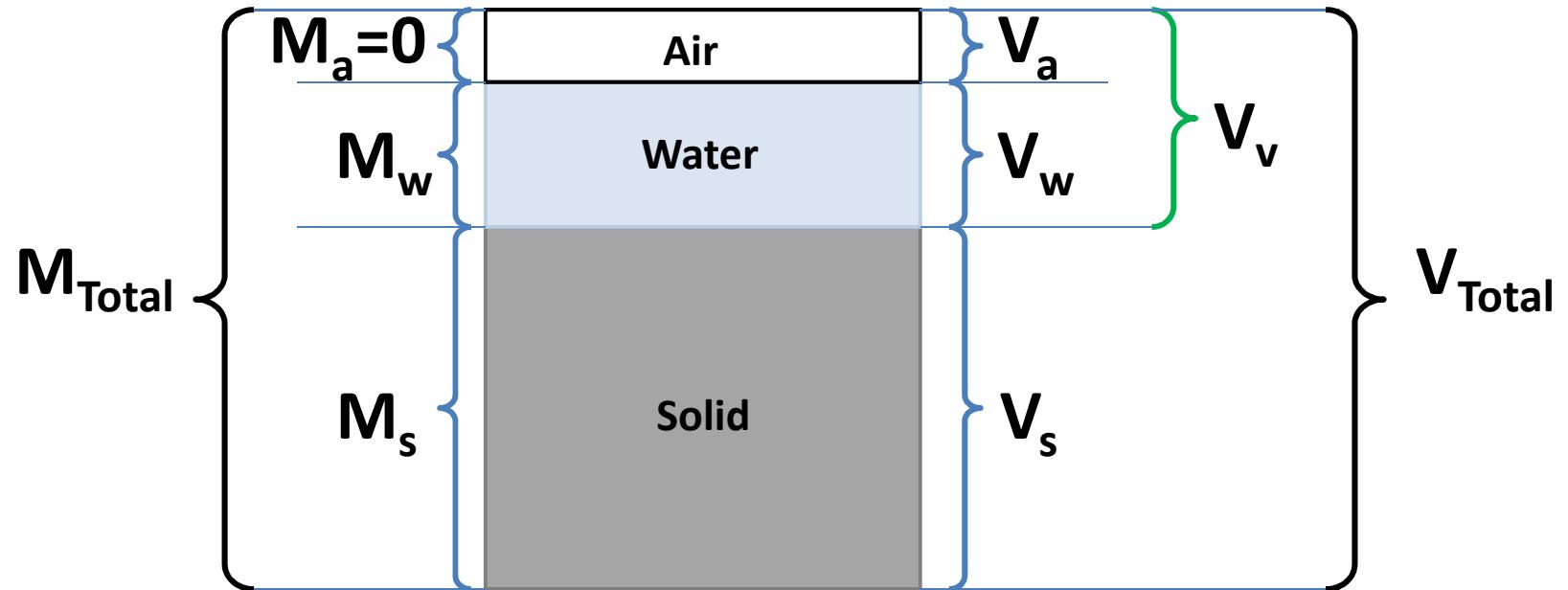
Volume



$$V_{Total} = V_v + V_s$$

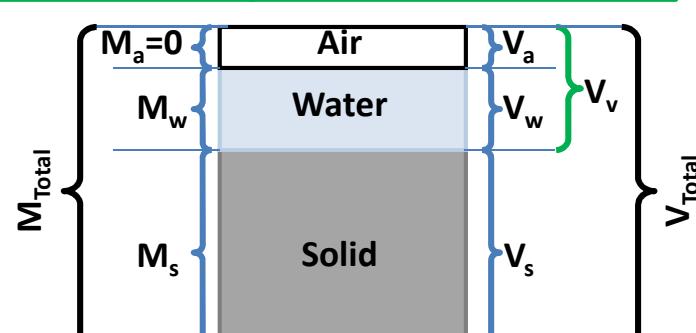
$$V_v = V_a + V_w$$

Mass



$$M_{Total} = M_w + M_s$$

Definitions

Density of water	$\rho_w = 1000$	kg/m ³	Specific Gravity	$G_s = \frac{\rho_s}{\rho_w}$
Water Content	$w = \frac{M_w}{M_s}$	[%]	Void Ratio	$e = \frac{V_v}{V_s}$
Degree of Saturation	$S_r = \frac{V_w}{V_v}$	[%]	Porosity	$n = \frac{V_v}{V_{Total}}$
Bulk Unit Weight	$\gamma_{bulk} = \frac{M_{Total} \cdot g}{V_{Total}}$	kN/m ³		

Barnes (2000) Soil Mechanics: Principles and Practice. 2nd Ed., Hounds mills, Palgrave: p33-34.

Knappett & Craig (2012) Craig's Soil Mechanics. 8th Ed, Abingdon, Spon Press: p22-25.

Proofs

In addition to:

$$v = e + 1$$

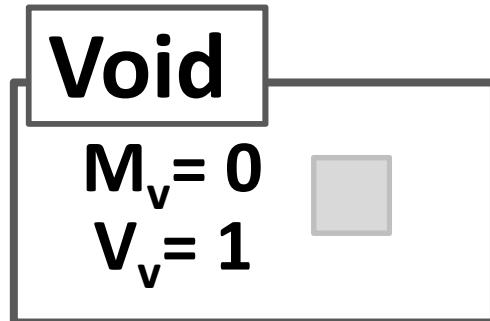
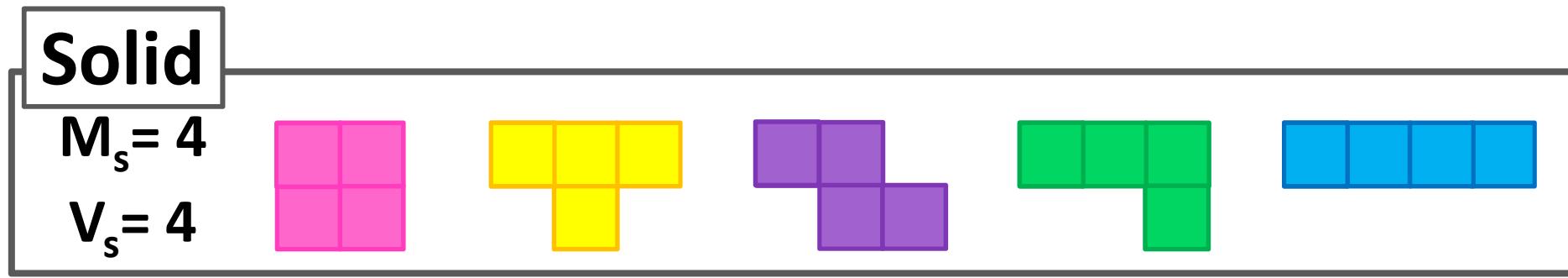
You should be able to prove:

$$e = \frac{n}{1-n}$$

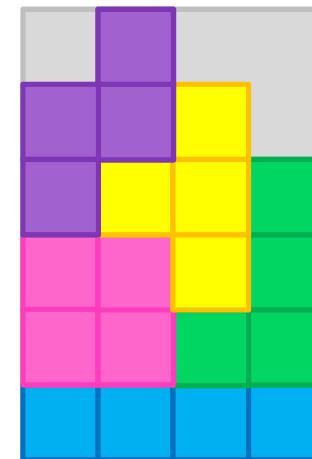
$$n = \frac{e}{1+e}$$

$$\rho = G_s \cdot \rho_w \cdot \left(\frac{1+w}{1+e} \right)$$

Packing Density

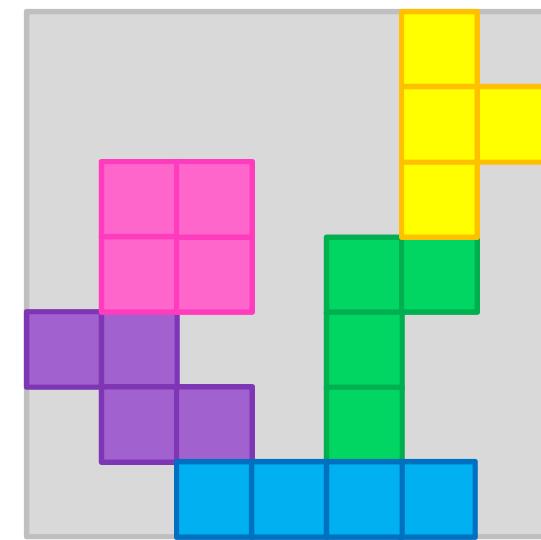


$$e = \frac{V_v}{V_s} = \frac{29}{20} = 1.45$$



Dense

$$e = 0.2$$

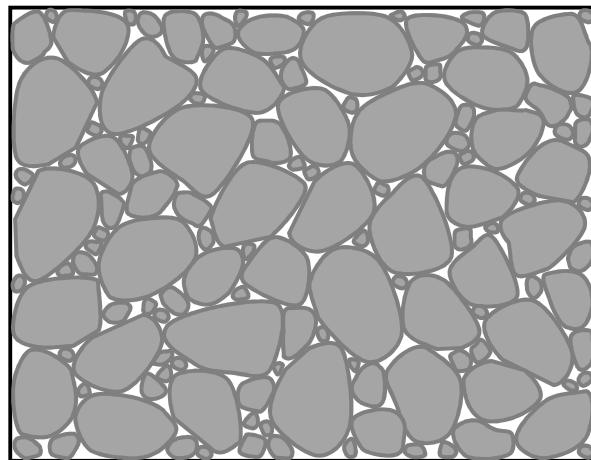


Loose

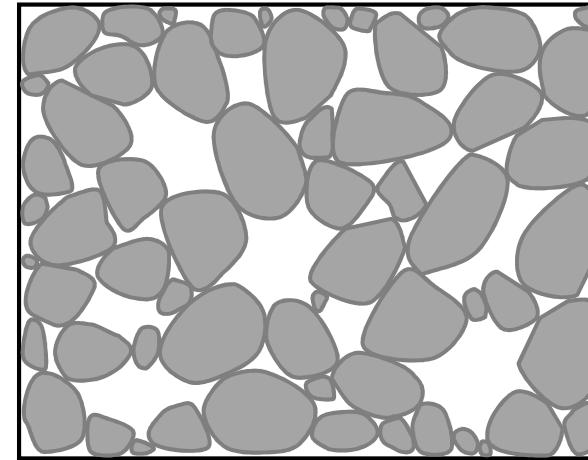
$$e = 1.45$$

Packing Density

... a similar situation in soils:



Dense



Loose

- **Min Void Ratio, e_{min}**

The densest pack possible for the soil

- **Max Void Ratio, e_{max}**

The loosest pack possible for the soil

Packing density

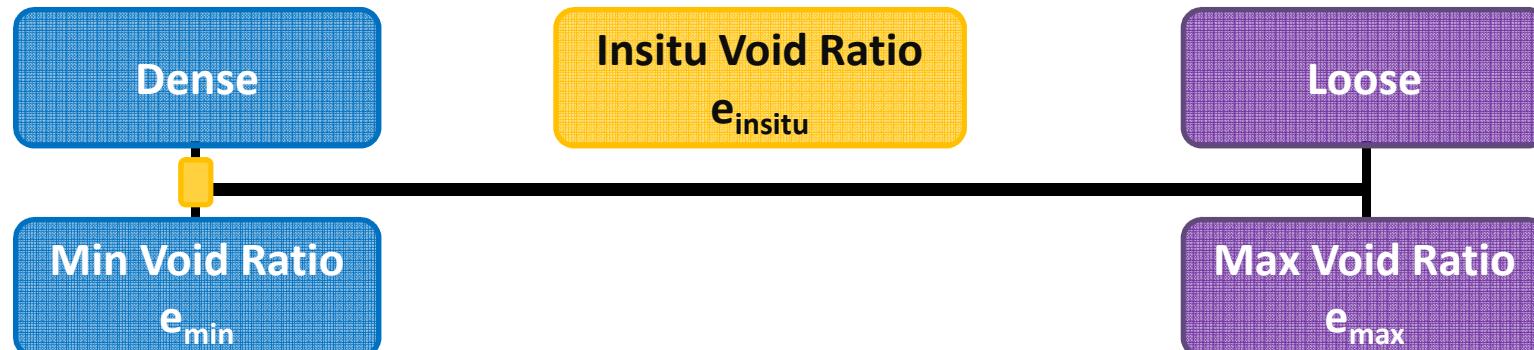
Relative Density, D_r

$$D_r = \frac{e_{\max} - e_{\text{insitu}}}{e_{\max} - e_{\min}}$$

1.0

■ *Insitu Void Ratio, e_{insitu}*

The void ratio of the soil on site, in its undisturbed/natural state.



Classification



Particle Size - Terminology

Clay

Silt

Sand

Gravel

Cobbles

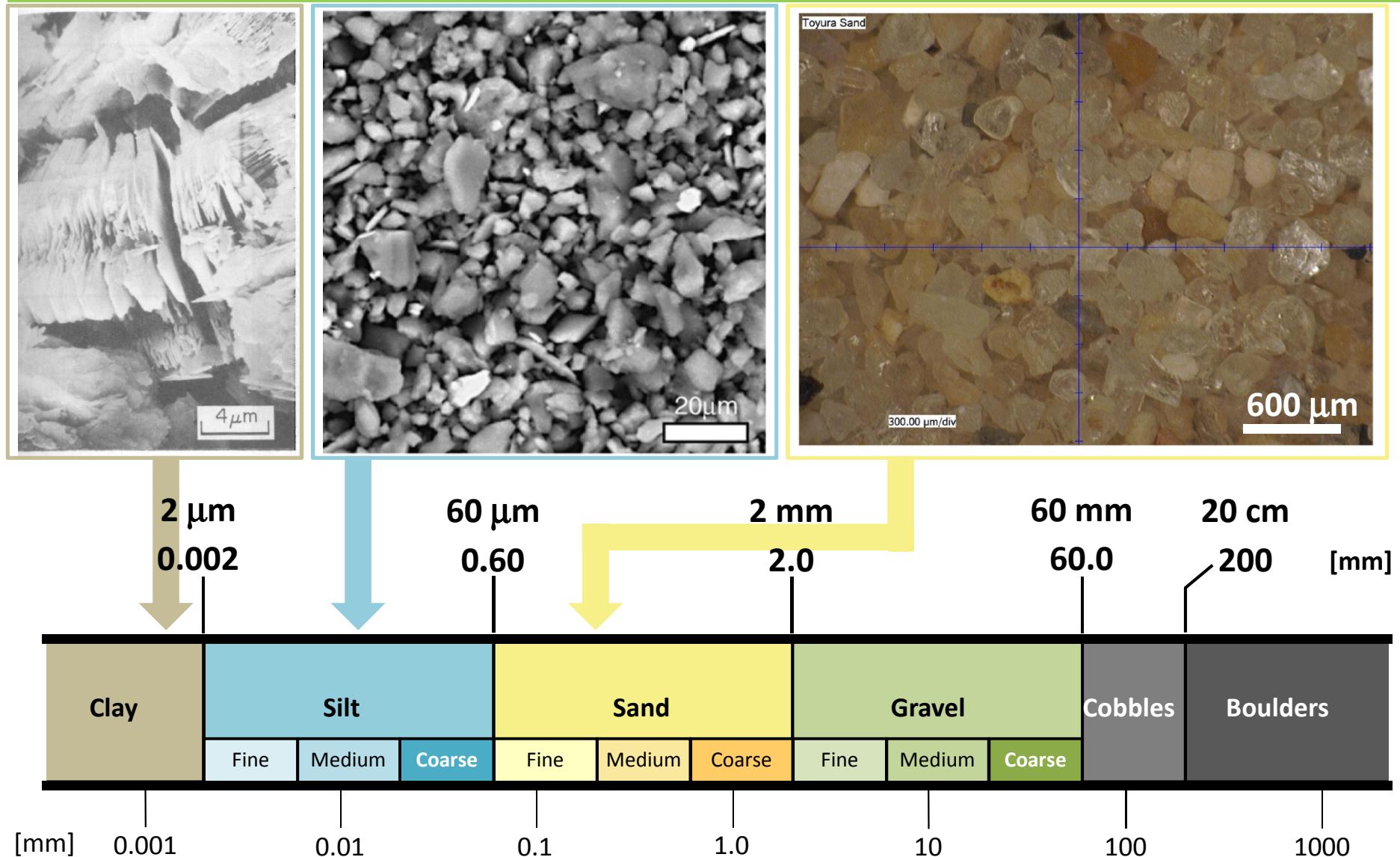
Boulders

Fine

Medium

Coarse

Particle Size - Definitions



Description



Consistency

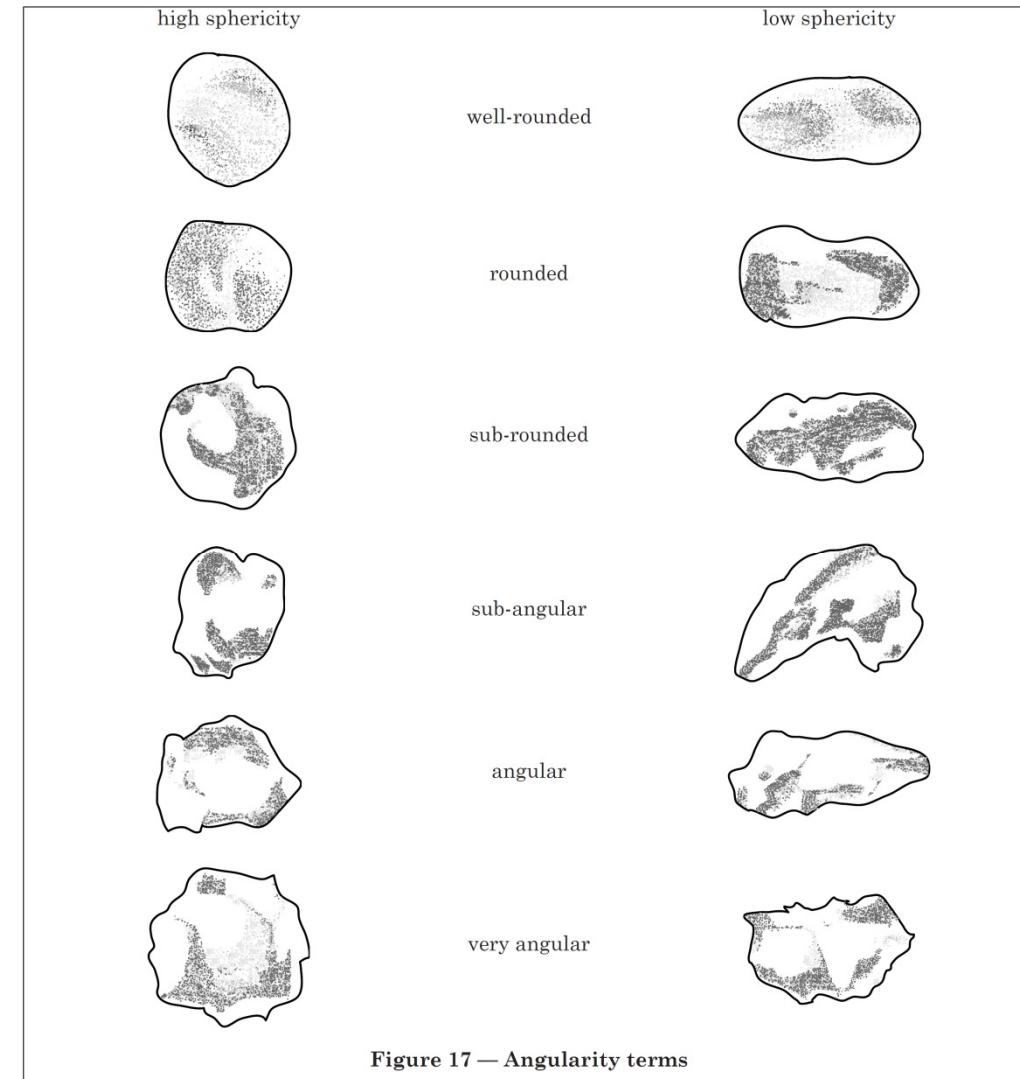
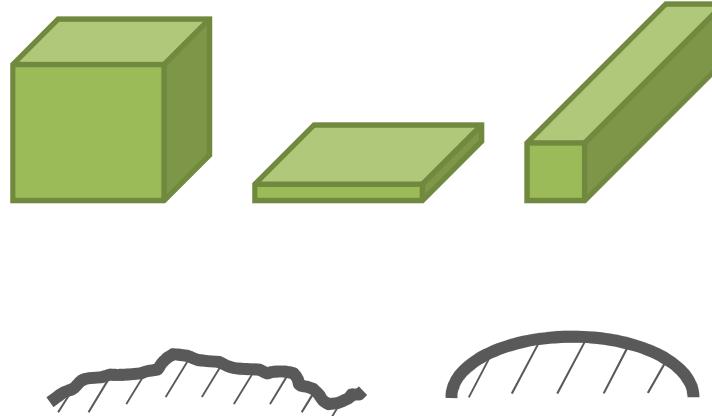
Term used for field description	Consistency description definition [after BS EN ISO 14688-1:2002, 5.14]
Very soft	Finger easily pushed in up to 25 mm. Exudes between fingers
Soft	Finger pushed in up to 10 mm. Moulds by light finger pressure
Firm	Thumb makes impression easily. Cannot be moulded by fingers, rolls in the hand to a 3 mm thick thread without breaking or crumbling
Stiff	Can be indented slightly by thumb. Crumbles in rolling a 3 mm thick thread, but can then be remoulded into a lump
Very stiff	Can be indented by thumb nail. Cannot be moulded but crumbles under pressure
Hard	Can be scratched by thumbnail

Sands

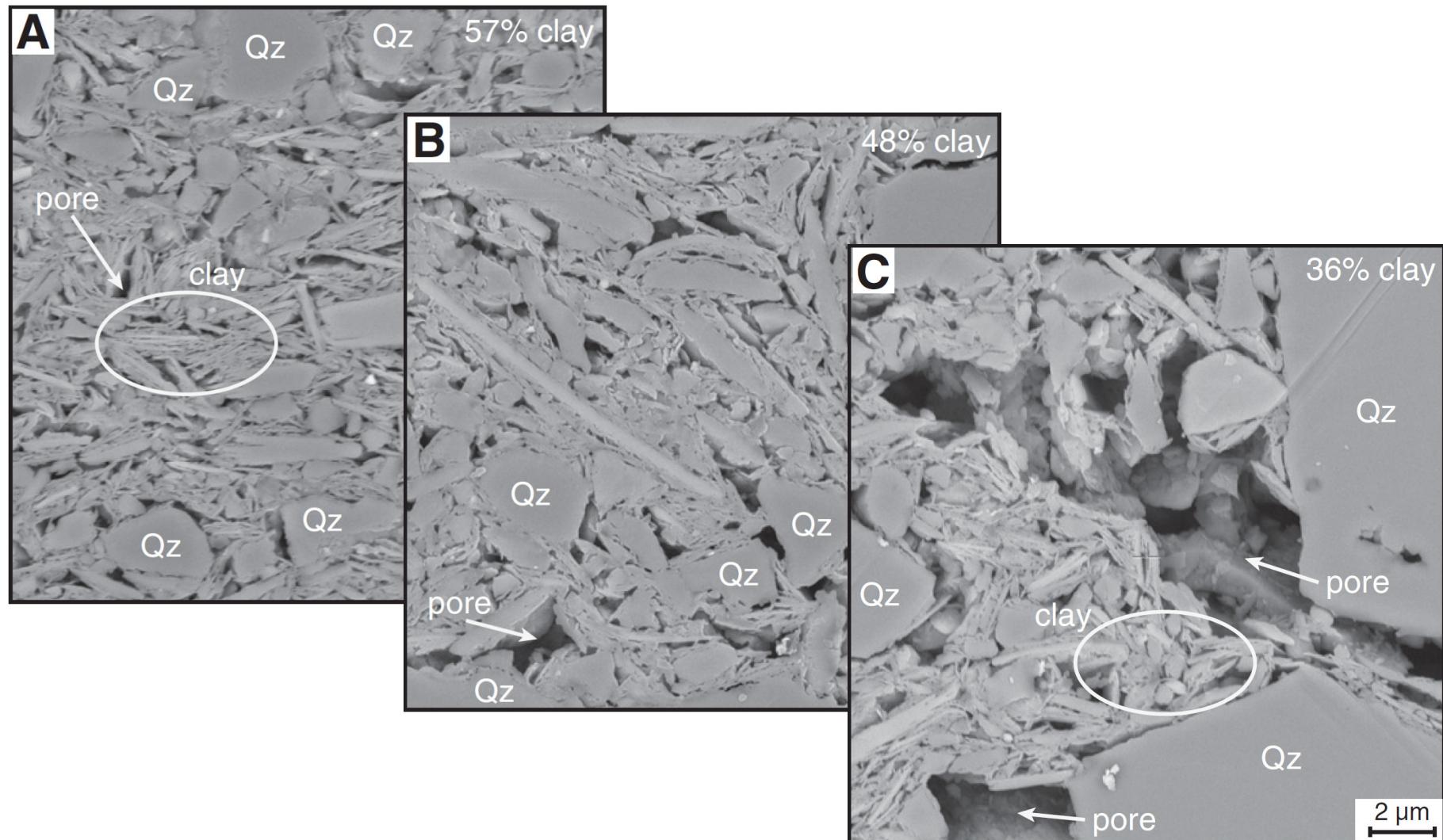
Granular (Discrete Grains) material

Describing shape

Angularity	very angular angular subangular subrounded rounded well rounded
Form	cubic flat (or tabular) elongate
Surface texture	rough smooth

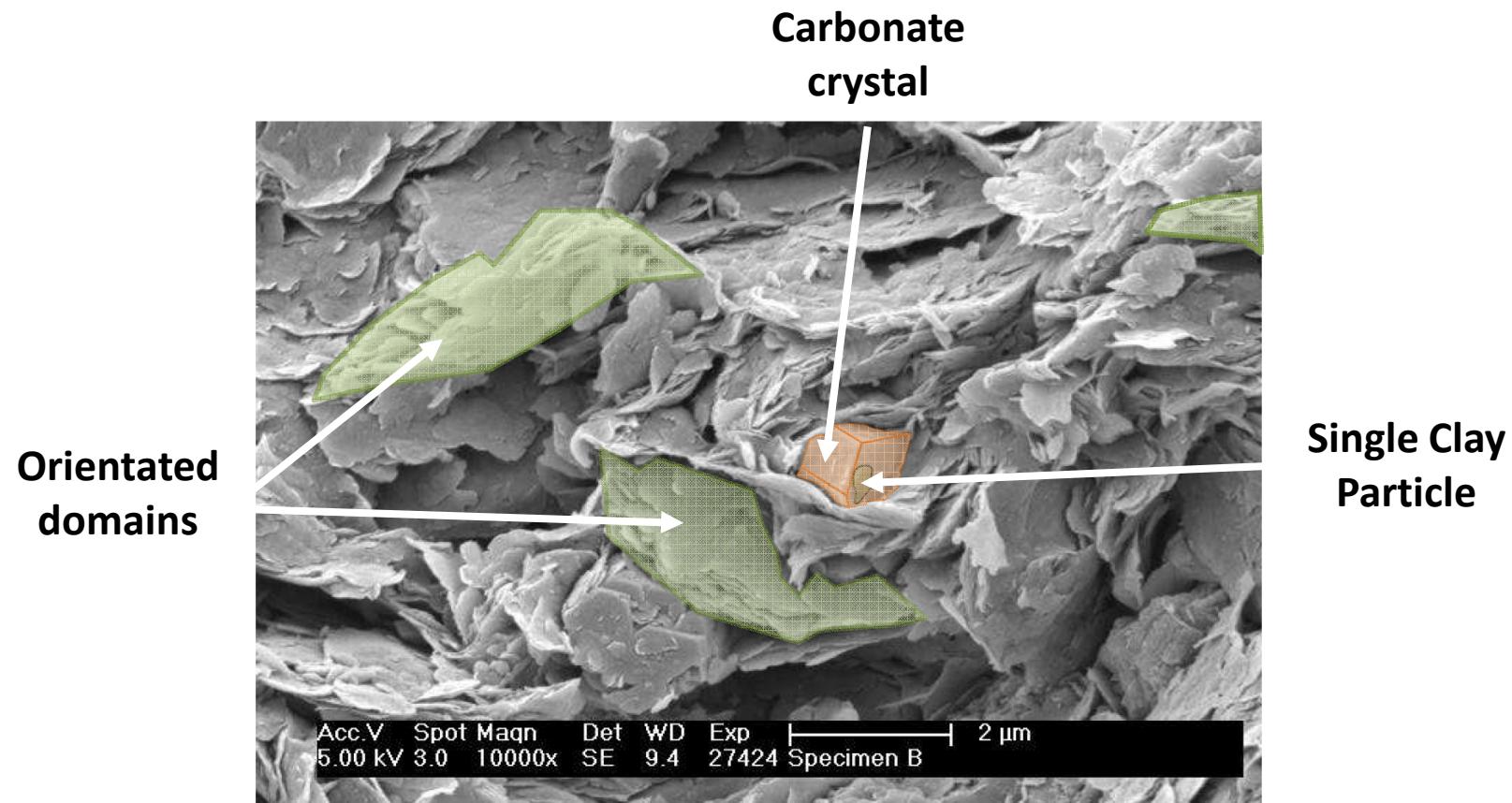


Clay Structure



Schneider et al. (2011) Insights into pore-scale controls on mudstone permeability through resedimentation experiments.
Geology **39** (11): 1011-1014.

Clay Structure



Classification of particle size



Particle Size Distribution [PSD]

Dry Sieving

Wet Sieving

Riffling

Aperture
Size

Percentage
Passing

Dispersing
Agent

Mass
Retained

Sedimentation

Hydrometer

Settling
Velocity

Pipette

Coarse fraction

Classification of particle size

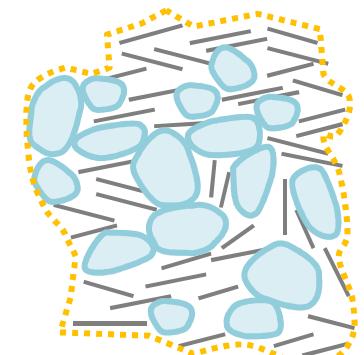
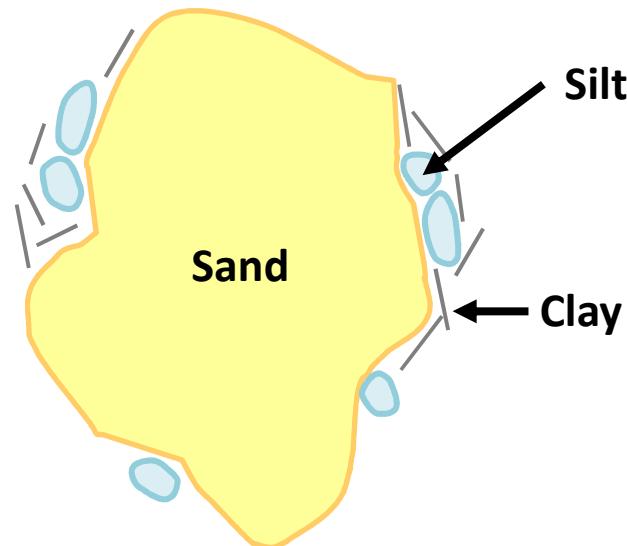
PSD - Coarse Fraction

Dry Sieving

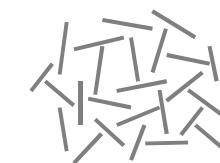
Suitable ONLY for soils containing *insignificant* quantities of silt and clay

Wet Sieving

Used on essentially *cohesionless* soils



Agglomeration of
silt and clay

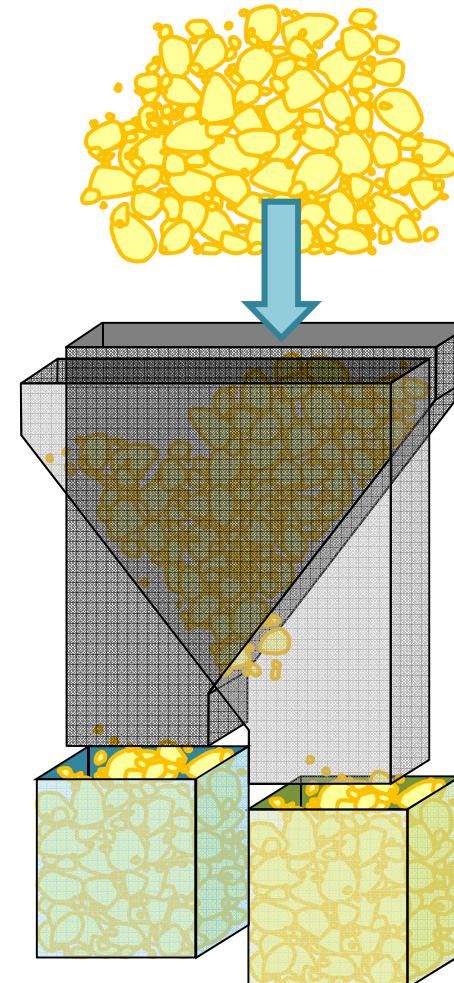


Clay floc

PSD - Coarse Fraction

Riffling

Splitting the soil sample into smaller (or appropriate) representative units

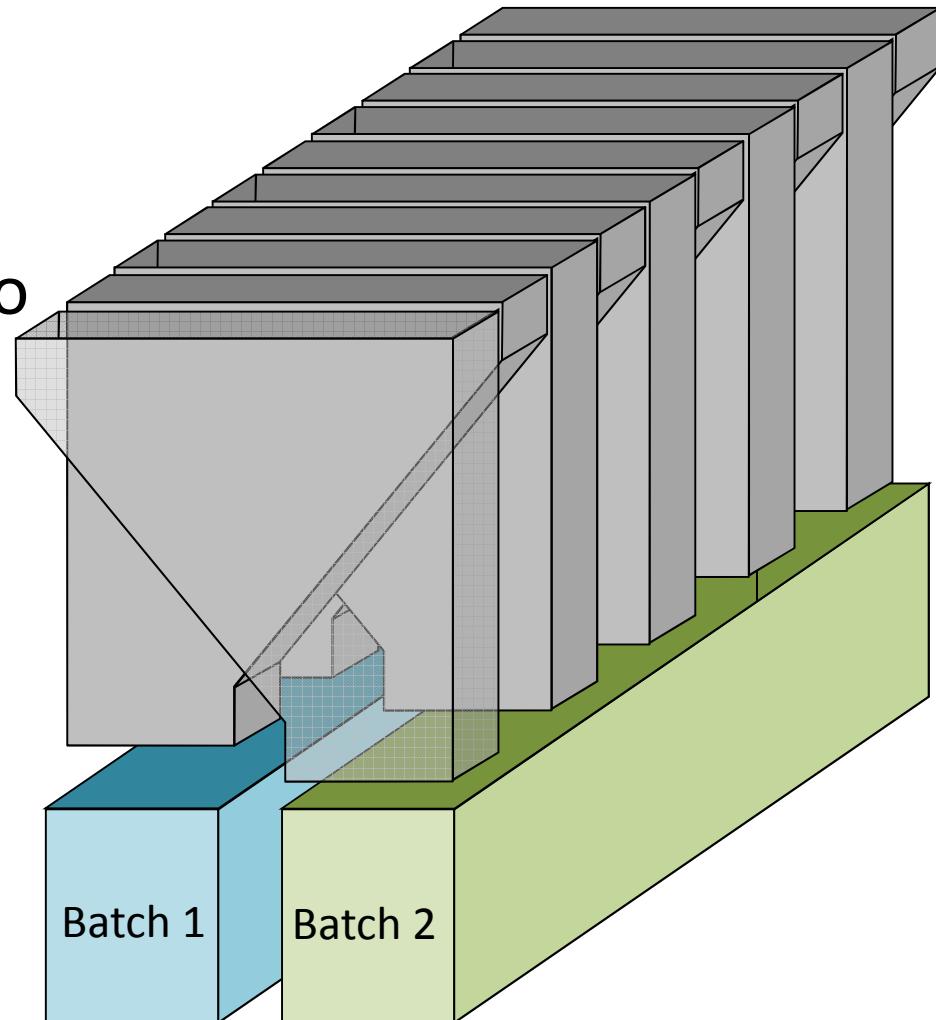


[1] vjtech (2013) VJT0017 - Riffle Box (Slot Width 13 mm, 12 Slots) [Online], Available from: http://www.vjtech.co.uk/Products/SoilRock/ClassificationTesting/tabcid/205/ProdID/402/CatID/83/Riffle_Boxes.aspx [Accessed: 9th Aug 2013].

PSD - Coarse Fraction

Riffling

Splitting the soil sample into smaller (or appropriate) representative units



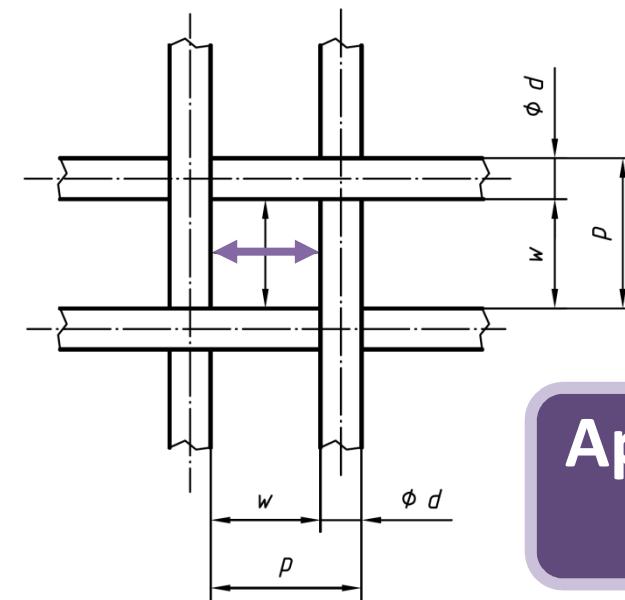
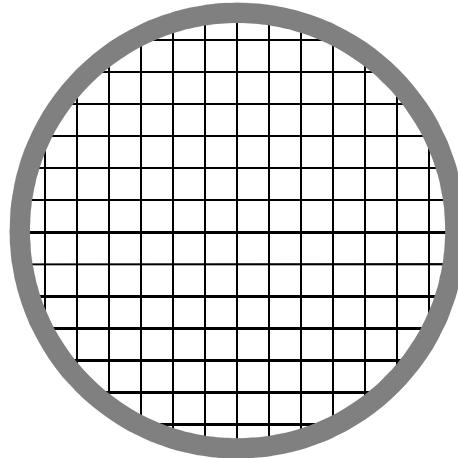
[1] vjtech (2013a) VJT0017 - Riffle Box (Slot Width 13 mm, 12 Slots) [Online], Available from: http://www.vjtech.co.uk/Products/SoilRock/ClassificationTesting/tabcid/205/ProdID/402/CatID/83/Riffle_Boxes.aspx [Accessed: 9th Aug 2013].

PSD - Coarse Fraction



[2]

Plan view



Aperture
Size

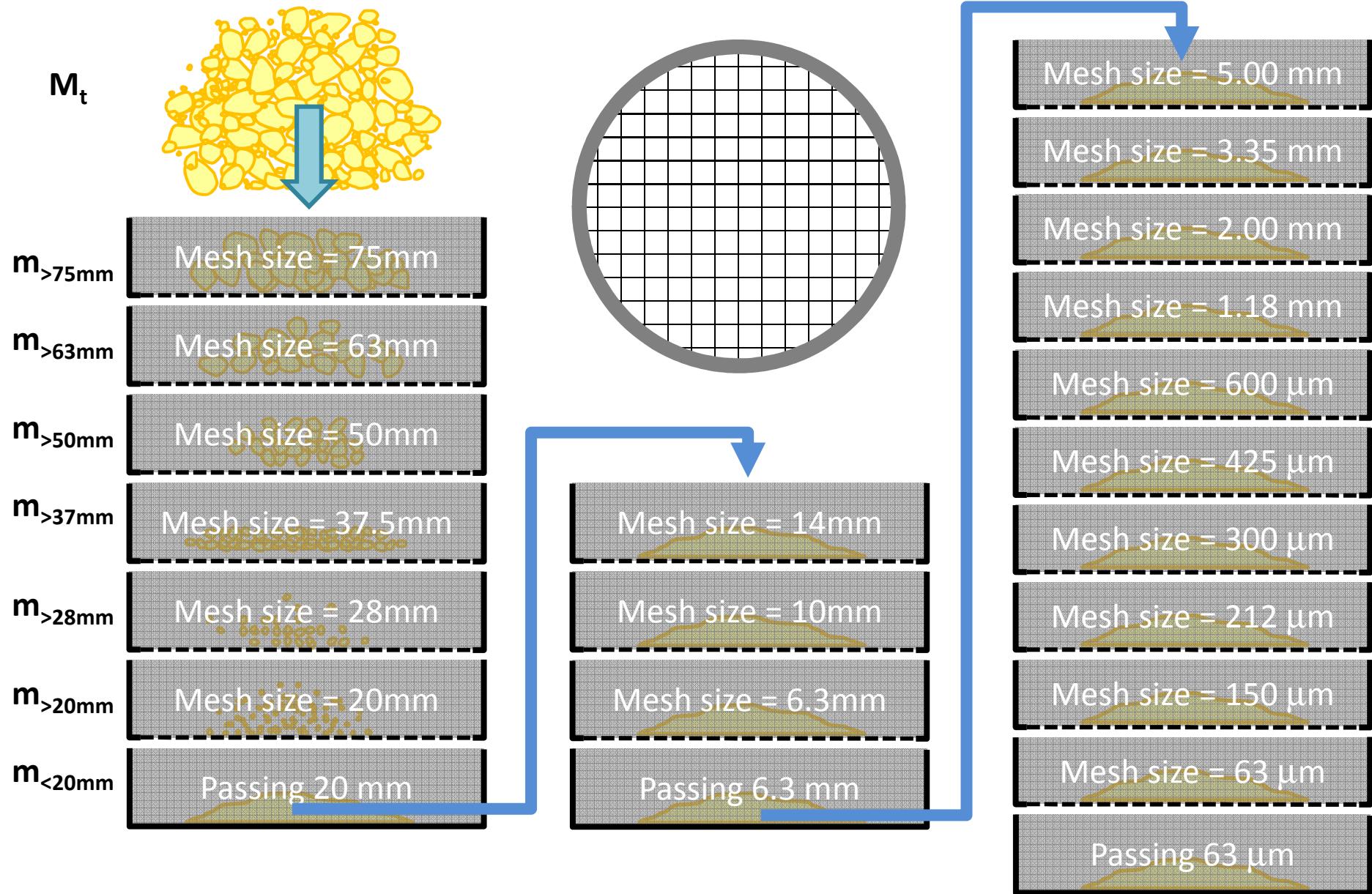
w = aperture size

d = wire diameter

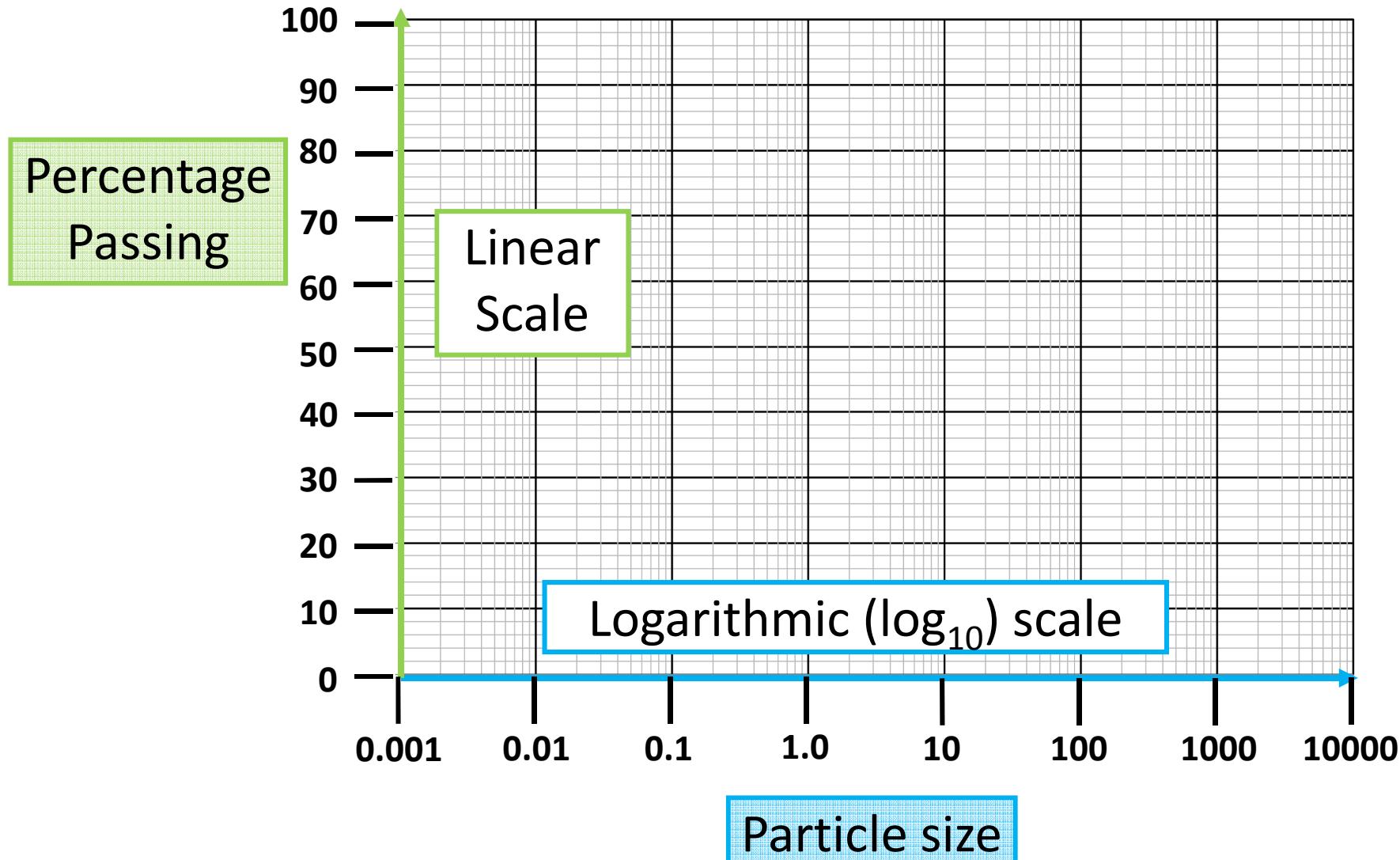
p = pitch ($w + d$)

[3]

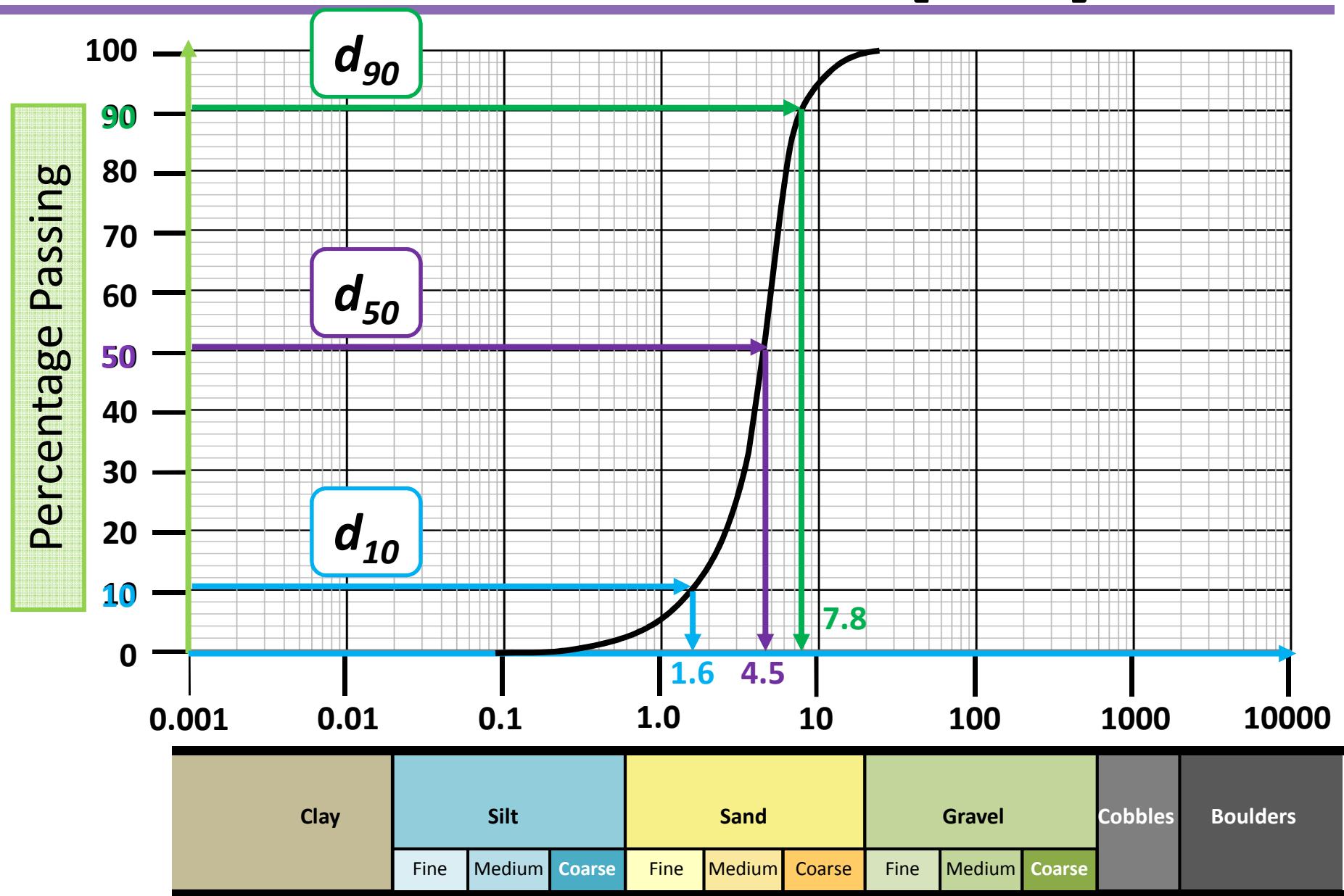
Particle Size Distribution [PSD]



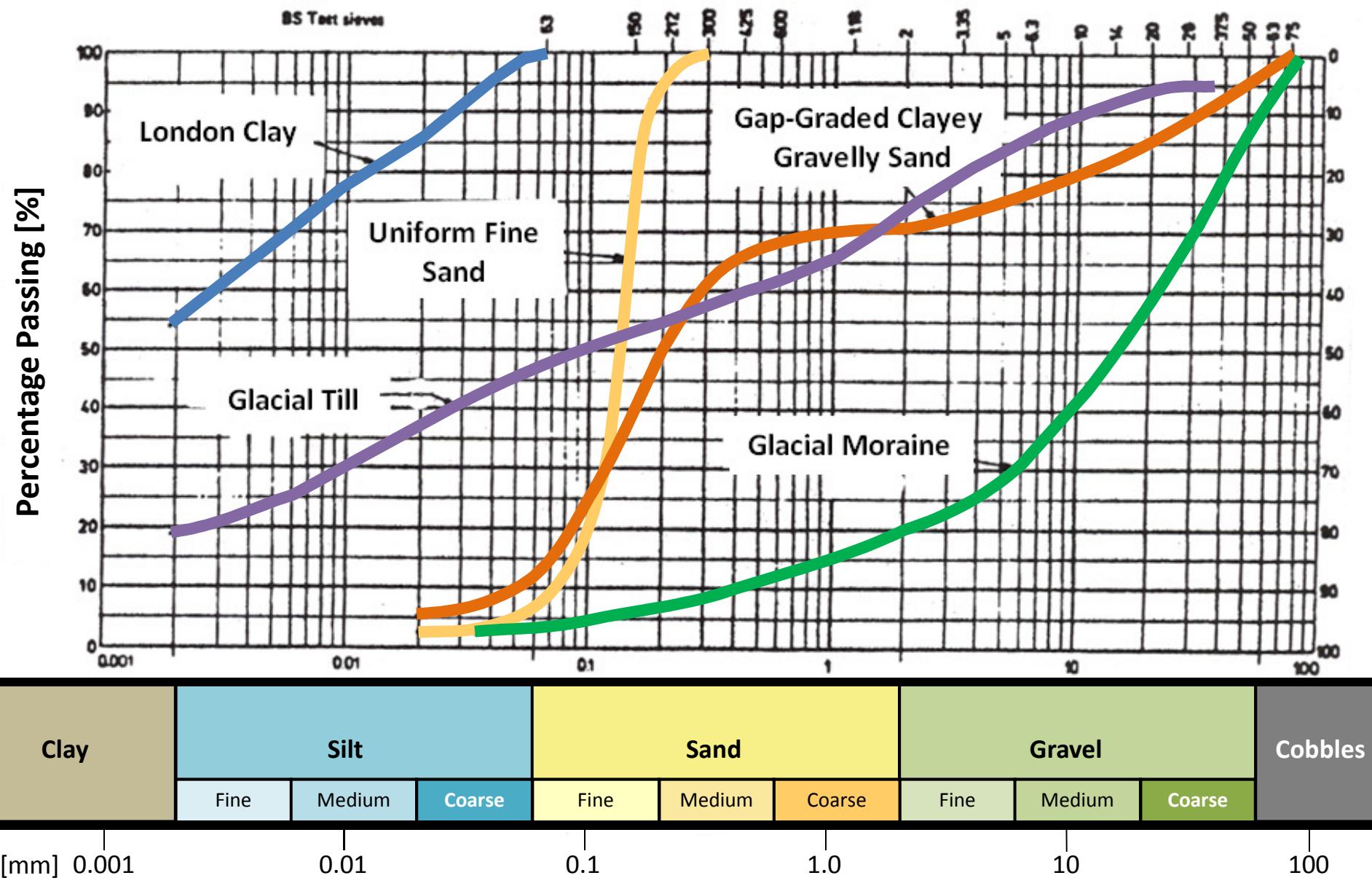
Particle Size Distribution [PSD]



Particle Size Distribution [PSD]



Particle Size Distribution [PSD]



PSD – grading descriptions

Well Graded

Silty Clayey SAND

Poorly
Graded

Uniformly
Graded

Glacial
Till

Gap-Graded

Clay

PSD – parameters

d_{50}

- The diameter at which 50% of grains are smaller than

Coefficient of Uniformity, C_u

$$C_u = \frac{d_{60}}{d_{10}}$$

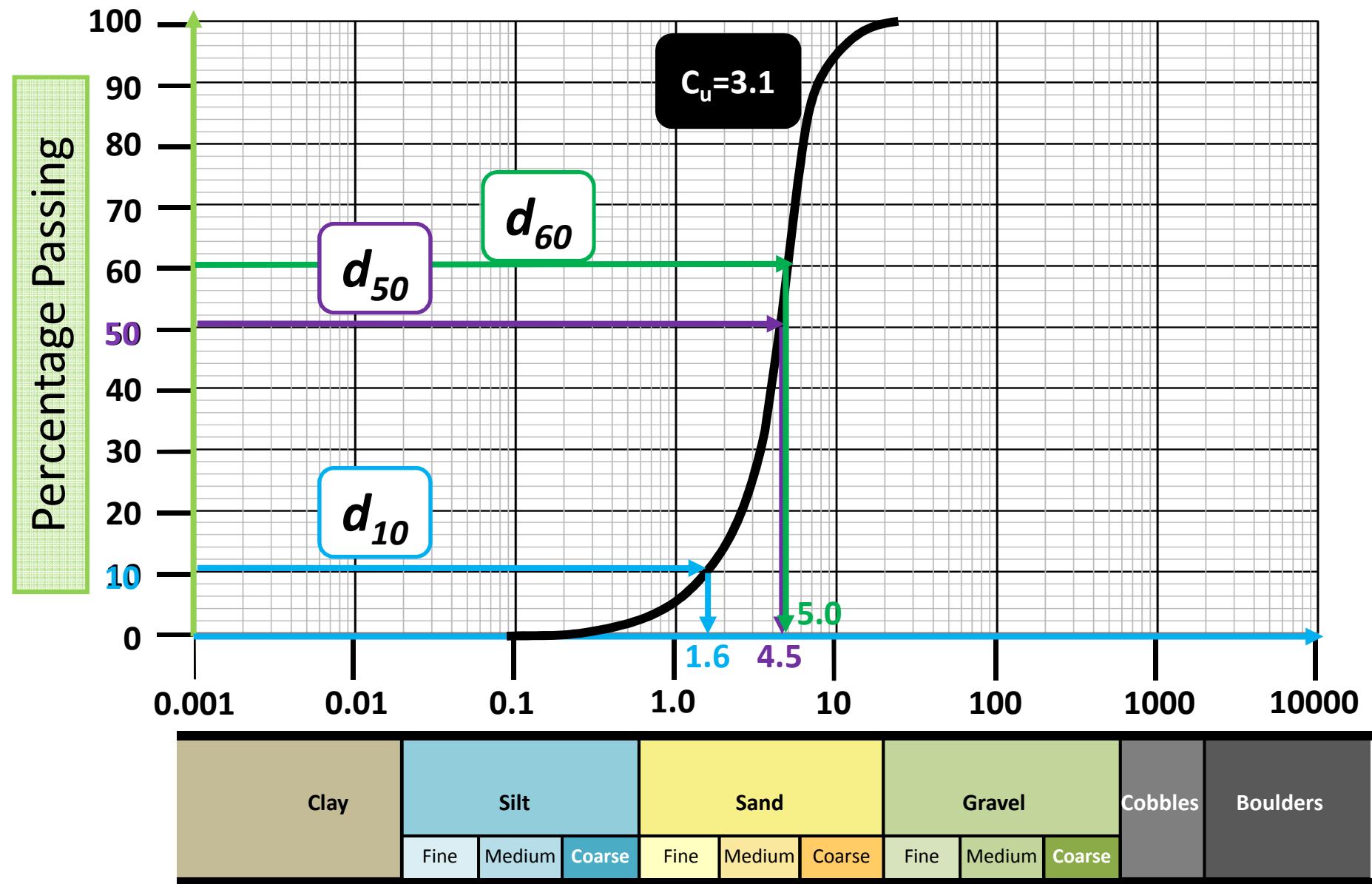
- d_{60} , The diameter at which 60% of grains are smaller than
- d_{10} , The diameter at which 10% of grains are smaller than

Coefficient of Curvature, C_z

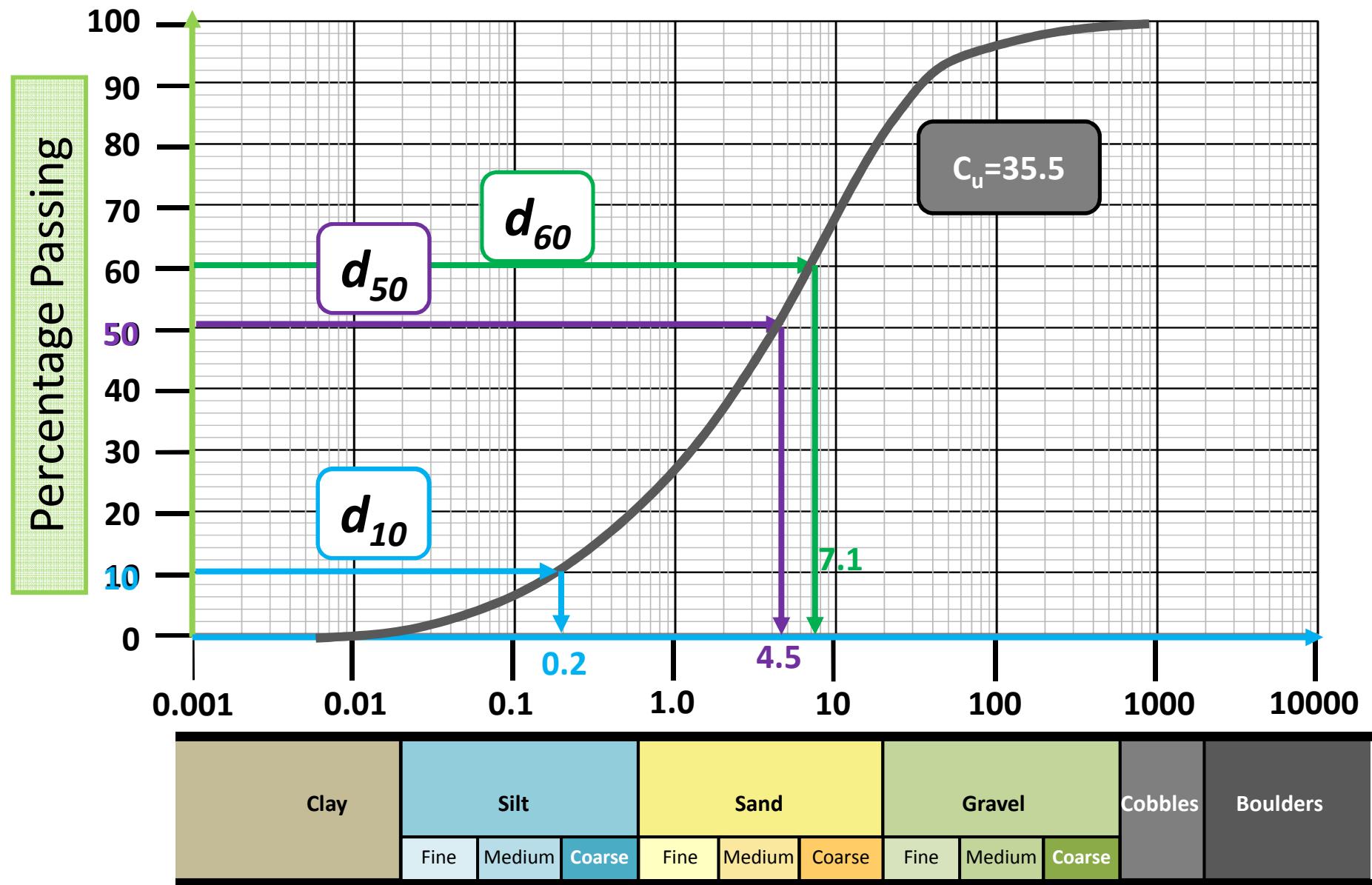
$$C_z = \frac{(d_{30})^2}{d_{60} \cdot d_{10}}$$

- d_{30} , The diameter at which 30% of grains are smaller than

Particle Size Distribution [PSD]



Particle Size Distribution [PSD]



PSD – parameters

Coefficient of Uniformity, C_u

$$\uparrow C_u$$

$$\uparrow \text{range of sizes}$$

$$C_u = \frac{d_{60}}{d_{10}}$$

Coefficient of Curvature, C_z

$$1 < C_z < 3$$

Well graded
Poorly sorted

$$C_z = \frac{(d_{30})^2}{d_{60} \cdot d_{10}}$$

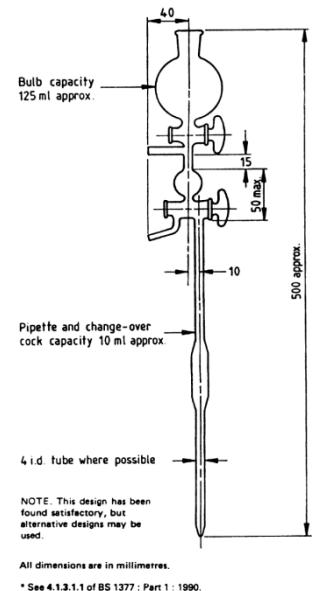
Fine fraction

Classification of particle size

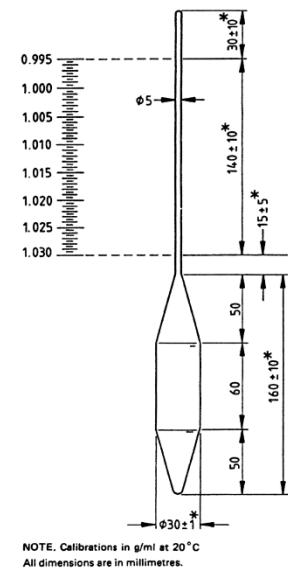
Sedimentation

Methods to determine the particle size distribution of fine particles (< 425 microns) involve sedimentation analysis

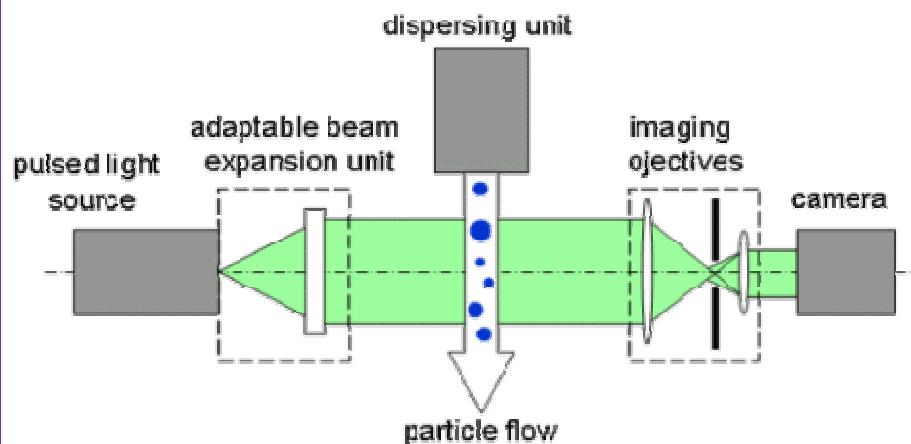
Pippette



Hydrometer



Laser diffraction



(Above) Sympatec (2013) *Sympatec's Image Analysis Overview and Concept*. [Online]

Settling Velocity:

The speed with which particles of a certain diameter settle out from a fluid

Dispersing Agent:

Added to soil/water solution to prevent particles from sticking together

Hydrometer

A device to measure the density of a fluid.

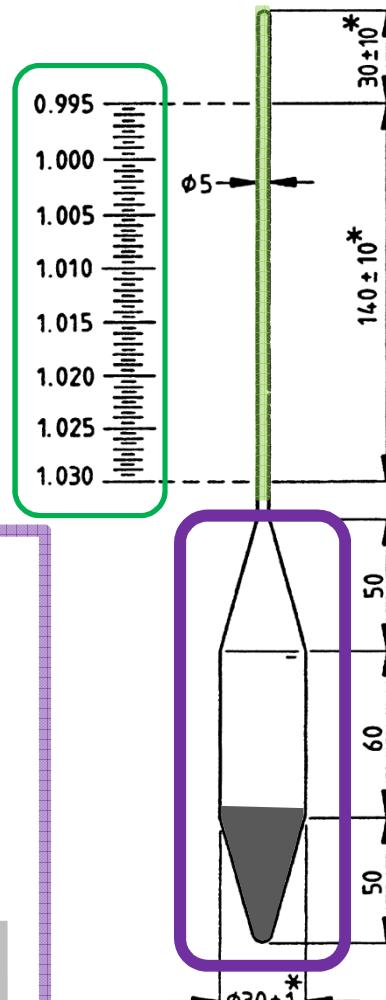
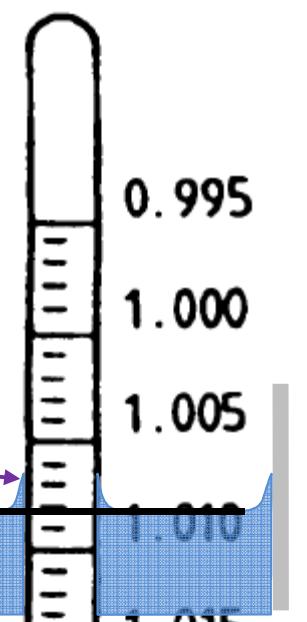
Consists of:

- graduated stem
- glass bulb

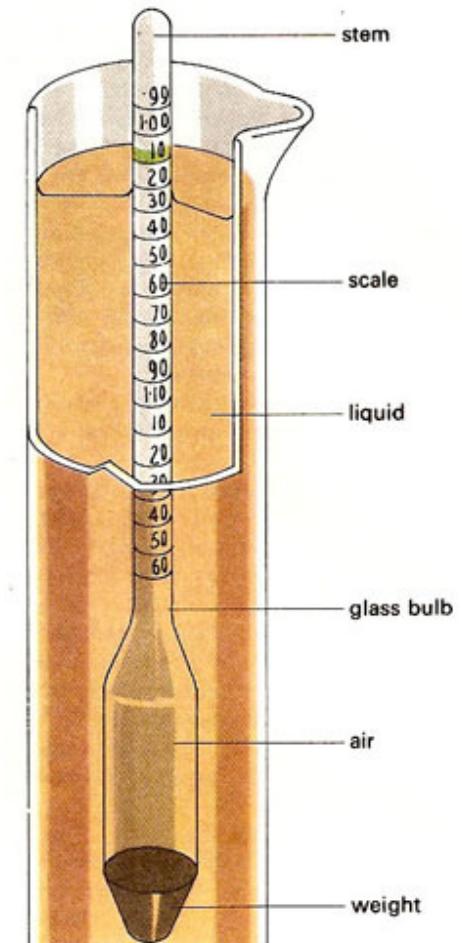
Place the hydrometer in the fluid which is to be measured and read the water level off the scale on the stem

Meniscus

1.008



NOTE. Calibrations in g/ml at 20 °C
All dimensions are in millimetres.
* See 4.1.3.1.1 of BS 1377 : Part 1 : 1990.



(above) daviddarling (2013)
Hydrometer. [Online]
(Left) BSI (1990) BS 1377-2

Hydrometer

Stokes Law:

- Smooth spherical particles
- Laminar flow
- Not applicable to particles <0.2 microns in diameter

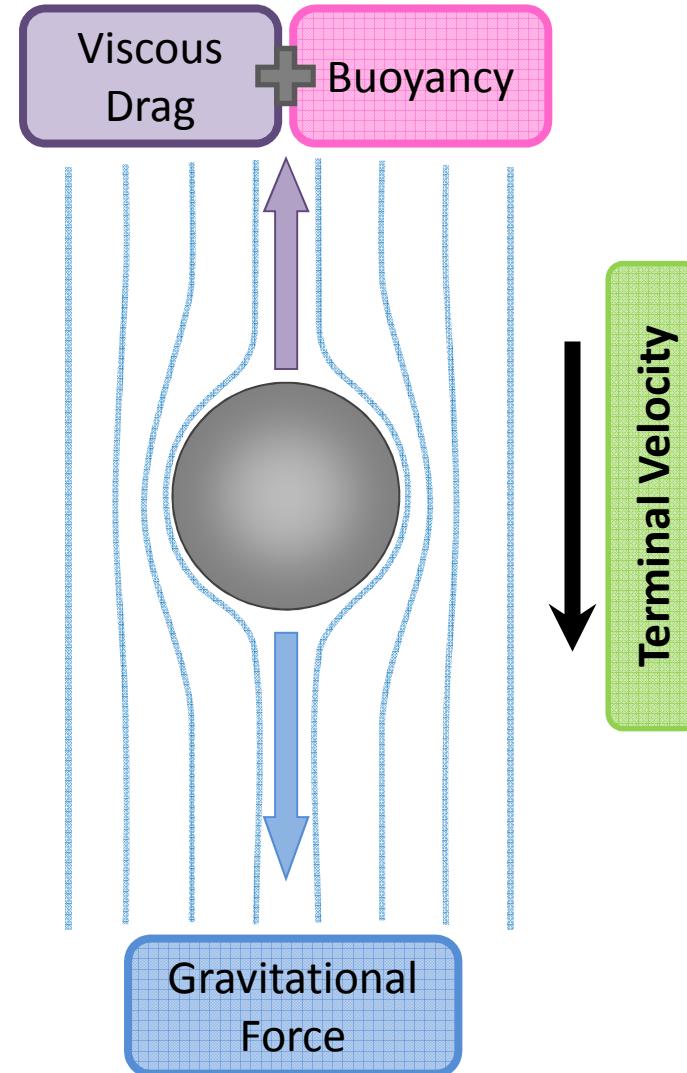
Brownian Motion

Real Soils:

- A range of particle roughness's
- Non-spherical particles!

Elongated

Platy



Nature and State

Sands

Nature;

The essential characteristics or basic qualities of the soil

Particle Size Distribution

Max Void Ratio
 e_{max}

Min Void Ratio
 e_{min}

Mineral Composition

State;

The physical condition in which the soil exists

In situ Void Ratio
 e_{insitu}

Natural Water Content, w

Relative Density D_r

Grain Structure

Learning Outcomes



Learning outcomes

1. Explain how particle size distributions (PSD) are measured for soils
2. Explain the terms:
 - a) Well graded,
 - b) Gap graded,
 - c) Poorly graded,

...and sketch their typical PSD's
3. Write down the definitions for:
 - a) Void Ratio, e ,
 - b) Specific Volume, v ,
 - c) Porosity, n ,
 - d) Water Content, w ,
 - e) Degree of Saturation, S_r
 - f) Coefficient of Uniformity, C_u

Learning outcomes

4. Sketch phase diagrams for:

- a) Dry,
- b) Fully Saturated,
- c) Partly Saturated soils

5. Working from the definitions of e , v and the phase relationships show:

$$a) v = e + 1$$

$$b) e = \frac{n}{1-n}$$

$$c) n = \frac{e}{1+e}$$

$$d) \rho = G_s \cdot \rho_w \cdot \left(\frac{1+w}{1+e} \right)$$

6. Plot and interpret a PSD, on semi-log graph paper, from sieve data

Learning outcomes

7. Read d_x (eg. d_{10} , d_{50} , d_{90}) data from PSD curves.
8. Calculate C_u and C_z values from PSD curves.
9. Understand and explain the difference between *nature* and *state*, giving examples of parameters which give an indication of each of the properties.

References

- Atkinson, J. H. (2007) *The Mechanics of Soils and Foundations*. 2nd Ed., London, Taylor & Francis. Section 5.1.
- Barnes, G.E. (2000) Soil Mechanics: Principles and Practice. 2nd Ed., Hounds mills, Palgrave.
- BSI (1990) BS 1377-2 *Methods of test for soils for civil engineering purposes – Part 2: Classification tests*. London, British Standards Institution.
- BSI (1999) BS 5930:1999 + A2:2010 *Code of practice for site investigations*. London, British Standards Institution.
- BSI (2000) BS 410-1:2000, ISO 3310:2000 *Test sieves. Technical requirements and testing. Test sieves of metal wire cloth*. London, British Standards Institution.
- Gasparre, A (2005) *Advanced laboratory characterisation of London Clay*. PhD thesis, Imperial College London.
- Knappett, J.A. & Craig, R.F. (2012) *Craig's Soil Mechanics*. 8th Ed, Abingdon, Spon Press.
- Schneider et al. (2011) Insights into pore-scale controls on mudstone permeability through resedimentation experiments. *Geology* 39 (11): 1011-1014.
- For interest:**
- Head, K.H. (1980). *Manual of Soil Laboratory Testing. Vol.1, Soil Classification and Compaction Tests*, Pentech Press, London.

Image references

daviddarling (2013) *Hydrometer*. [Online] Available from:

<http://www.daviddarling.info/encyclopedia/H/hydrometer.html> , [Accessed: 14/08/2013], [Modified: 18/06/2013]

Sympatec (2013) *Sympatec's Image Analysis Overview and Concept*. [Online] Available from:

<http://www.sympatec.com/EN/ImageAnalysis/ImageAnalysis.html> [Accessed: 14/08/2013], [Modified: 05/08/2013]

[1] vjtech (2013) VJT0017 - Riffle Box (Slot Width 13 mm, 12 Slots) [Online], Available from:

http://www.vjtech.co.uk/Products/SoilRock/ClassificationTesting/tabid/205/ProdID/402/CatID/83/Riffle_Boxes.aspx [Accessed: 9th Aug 2013].

[2] vjtech (2013b) VJT-200W-xx.xxMM - Stainless Steel Mesh Sieve (200 mm Diameter - selected mm apertures) [Online], Available from: http://www.vjtech.co.uk/Products/SoilRock/ClassificationTesting/tabid/205/ProdID/380/CatID/83/Stainless_Steel_Mesh_Sieve_200_mm_diameter_selected_mm_apertures.aspx [Accessed: 9th Aug 2013].