

Digital Design

Chapter 3: Sequential Logic Design -- Controllers

Slides to accompany the textbook *Digital Design*, First Edition,
by Frank Vahid, John Wiley and Sons Publishers, 2007.
<http://www.dvvhid.com>

Copyright © 2007 Frank Vahid

Instructors of courses adopting Vahid's Digital Design textbook published by John Wiley and Sons have permission to modify and use these slides for customary course-related activities, subject to keeping this copyright notice in place and unmodified. These slides may be posted as pdf versions on publicly-accessible course websites. PowerPrint source (or pdf with annotations) may also be posted to publicly-accessible websites, but may be posted for students on internal protected sites or distributed directly to students by other electronic means. Instructors may make portions of the slides available to students for a reasonable photocopying charge, without incurring royalties. Any other use requires explicit permission. Instructors may obtain PowerPrint source or obtain special use permissions from Wiley -- see <http://www.wiley.com/go/permissions> for information.

EEL7020 – Sistemas Digitais

Aula 8: Circuitos sequenciais – Máquinas de Estado

Prof. Djones Vinicius Lettnin
lettnin@eel.ufsc.br
<http://dlettnin.paginas.ufsc.br/>

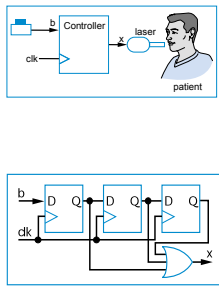
Disclaimer: slides adapted for EEL7020 by D. Lettnin from the original
slides made available by the author F. Vahid.

Digital Design
Copyright © 2006
Frank Vahid

Finite-State Machines (FSMs) and Controllers

3.3

- Want sequential circuit with particular behavior over time
- Example: Laser timer
 - Push button: $x=1$ for 3 clock cycles
 - How? Let's try three flip-flops
 - $b=1$ gets stored in first D flip-flop
 - Then 2nd flip-flop on next cycle, then 3rd flip-flop on next
 - OR the three flip-flop outputs, so x should be 1 for three cycles



Digital Design
Copyright © 2006
Frank Vahid

3

Need a Better Way to Design Sequential Circuits

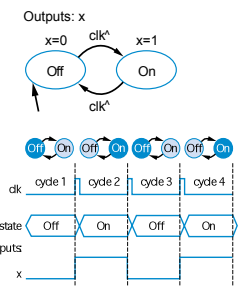
- Trial and error is not a good design method
 - Will we be able to "guess" a circuit that works for other desired behavior?
 - How about counting up from 1 to 9? Pulsing an output for 1 cycle every 10 cycles? Detecting the sequence 1 3 5 in binary on a 3-bit input?
 - And, a circuit built by guessing may have undesired behavior
 - Laser timer: What if press button again while $x=1$? x then stays one another 3 cycles. Is that what we want?
- Combinational circuit design process had two important things
 - A formal way to describe desired circuit behavior
 - Boolean equation, or truth table
 - A well-defined process to convert that behavior to a circuit
- We need those things for sequence circuit design

Digital Design
Copyright © 2006
Frank Vahid

4

Describing Behavior of Sequential Circuit: FSM

- Finite-State Machine (FSM)
 - A way to describe desired behavior of sequential circuit
 - Akin to Boolean equations for combinational behavior
 - List states, and transitions among states
 - Example: Make x change toggle (0 to 1, or 1 to 0) every clock cycle
 - Two states: "Off" ($x=0$), and "On" ($x=1$)
 - Transition from Off to On, or On to Off, on rising clock edge
 - Arrow with no starting state points to initial state (when circuit first starts)

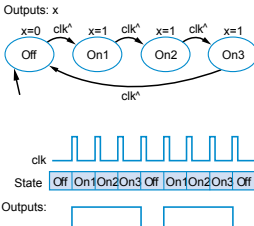


Digital Design
Copyright © 2006
Frank Vahid

5

FSM Example: 0, 1, 1, repeat

- Want 0, 1, 1, 0, 1, 1, 1, ...
 - Each value for one clock cycle
- Can describe as FSM
 - Four states
 - Transition on rising clock edge to next state

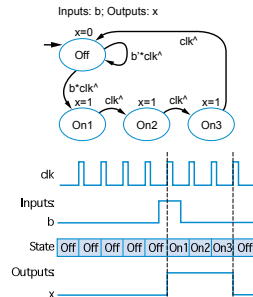


Digital Design
Copyright © 2006
Frank Vahid

6

Extend FSM to Three-Cycles High Laser Timer

- Four states
- Wait in "Off" state while b is 0 (b')
- When b is 1 (and rising clock edge), transition to On1
 - Sets $x=1$
 - On next two clock edges, transition to On2, then On3, which also set $x=1$
- So $x=1$ for three cycles after button pressed

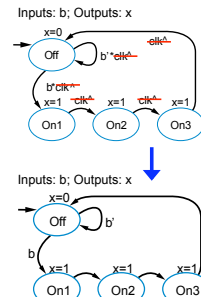


Digital Design
Copyright © 2006
Frank Vahid

7

FSM Simplification: Rising Clock Edges Implicit

- Showing rising clock on every transition: cluttered
 - Make implicit -- assume every edge has rising clock, even if not shown
 - What if we wanted a transition *without* a rising edge
 - We don't consider such asynchronous FSMs -- less common, and advanced topic
 - Only consider **synchronous** FSMs -- rising edge on *every* transition



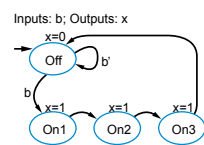
Note: Transition with no associated condition thus transitions to next state on next clock cycle

Digital Design
Copyright © 2006
Frank Vahid

8

FSM Definition

- FSM consists of
 - Set of states
 - Ex: {Off, On1, On2, On3}
 - Set of inputs, set of outputs
 - Ex: Inputs: {x}, Outputs: {b}
 - Initial state
 - Ex: "Off"
 - Set of transitions
 - Describes next states
 - Ex: Has 5 transitions
 - Set of actions
 - Sets outputs while in states
 - Ex: $x=0$, $x=1$, $x=1$, and $x=1$



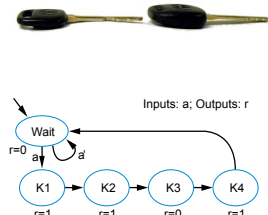
We often draw FSM graphically, known as **state diagram**
Can also use table (state table), or textual languages

Digital Design
Copyright © 2006
Frank Vahid

9

FSM Example: Secure Car Key

- Many new car keys include tiny computer chip
 - When car starts, car's computer (under engine hood) requests identifier from key
 - Key transmits identifier
 - If not, computer shuts off car
- FSM
 - Wait until computer requests ID ($a=1$)
 - Transmit ID (in this case, 1101)

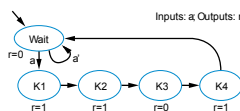


Digital Design
Copyright © 2006
Frank Vahid

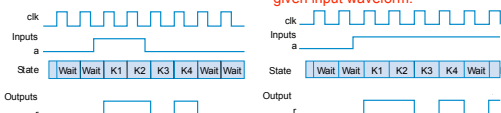
10

FSM Example: Secure Car Key (cont.)

- Nice feature of FSM
 - Can evaluate output behavior for different input sequence
 - Timing diagrams show states and output values for different input waveforms



Q: Determine states and r value for given input waveform:

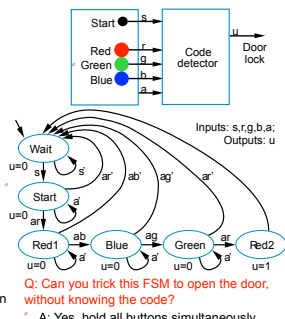


Digital Design
Copyright © 2006
Frank Vahid

11

FSM Example: Code Detector

- Unlock door ($u=1$) only when buttons pressed in sequence:
 - start, then red, blue, green, red
- Input from each button: s, r, g, b
 - Also, output a indicates that some colored button pressed
- FSM
 - Wait for start ($s=1$) in "Wait"
 - Once started ("Start")
 - If see red, go to "Red1"
 - Then, if see blue, go to "Blue"
 - Then, if see green, go to "Green"
 - Then, if see red, go to "Red2"
 - In that state, open the door ($u=1$)
 - Wrong button at any step, return to "Wait", without opening door



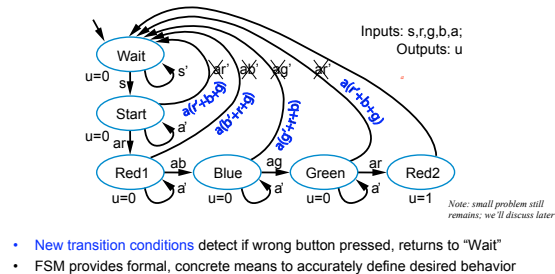
Q: Can you trick this FSM to open the door, without knowing the code?

A: Yes, hold all buttons simultaneously

Digital Design
Copyright © 2006
Frank Vahid

12

Improve FSM for Code Detector



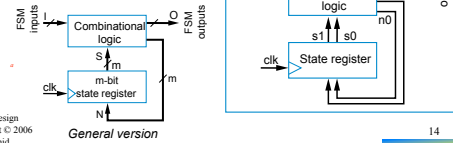
- New transition conditions detect if wrong button pressed, returns to "Wait"
- FSM provides formal, concrete means to accurately define desired behavior

Digital Design
Copyright © 2006
Frank Vahid

13

Standard Controller Architecture

- How implement FSM as sequential circuit?
 - Use standard architecture
 - State register -- to store the present state
 - Combinational logic -- to compute outputs, and next state
 - For laser timer FSM
 - 2-bit state register, can represent four states
 - Input b, output x
- Known as **controller**



Digital Design
Copyright © 2006
Frank Vahid

14

Controller Design

- Five step controller design process

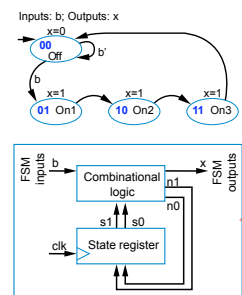
Step	Description
Step 1 <i>Capture the FSM</i>	Create an FSM that describes the desired behavior of the controller.
Step 2 <i>Create the architecture</i>	Create the standard architecture by using a state register of appropriate width, and combinational logic with inputs being the state register bits and the FSM inputs and outputs being the next state bits and the FSM outputs.
Step 3 <i>Encode the states</i>	Assign a unique binary number to each state. Each binary number representing a state is known as an <i>encoding</i> . Any encoding will do as long as each state has a unique encoding.
Step 4 <i>Create the state table</i>	Create a truth table for the combinational logic such that the logic will generate the correct FSM outputs and next state signals. Ordering the inputs with state bits first makes this truth table describe the state behavior, so the table is a state table.
Step 5 <i>Implement the combinational logic</i>	Implement the combinational logic using any method.

Digital Design
Copyright © 2006
Frank Vahid

15

Controller Design: Laser Timer Example

- Step 1: Capture the FSM**
 - Already done
- Step 2: Create architecture**
 - 2-bit state register (for 4 states)
 - Input b, output x
 - Next state signals n1, n0
- Step 3: Encode the states**
 - Any encoding with each state unique will work



Digital Design
Copyright © 2006
Frank Vahid

16

Controller Design: Laser Timer Example (cont)

- Step 4: Create state table

	Inputs			Outputs		
	s1	s0	b	x	n1	n0
Off	0	0	0	0	0	0
	0	0	1	0	0	1
On1	0	1	0	1	1	0
	0	1	1	1	1	0
On2	1	0	0	1	1	1
	1	0	1	1	1	1
On3	1	1	0	1	0	0
	1	1	1	1	0	0

Digital Design
Copyright © 2006
Frank Vahid

17

Controller Design: Laser Timer Example (cont)

- Step 5: Implement combinational logic

	Inputs			Outputs		
	s1	s0	b	x	n1	n0
Off	0	0	0	0	0	0
	0	0	1	0	0	1
On1	0	1	0	1	1	0
	0	1	1	1	1	0
On2	1	0	0	1	1	1
	1	0	1	1	1	1
On3	1	1	0	1	0	0
	1	1	1	1	0	0

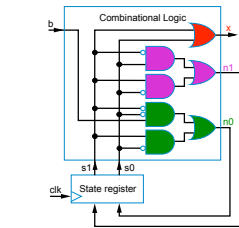
Digital Design
Copyright © 2006
Frank Vahid

18

Controller Design: Laser Timer Example (cont)

- Step 5: Implement combinational logic (cont)

Inputs		Outputs		
s1	s0	b	x	n1 n0
Off		0 0 0	0	0 0
On1		0 1 0	1	1 0
On2		1 0 0	1	1 1
On3		1 1 0	1	0 0



$$x = s1 + s0$$

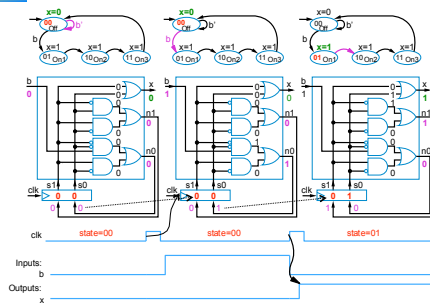
$$n1 = s1's0 + s1s0'$$

$$n0 = s1's0'b + s1s0'$$

Digital Design
Copyright © 2006
Frank Vahid

19

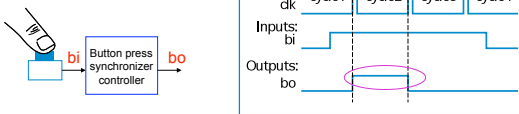
Understanding the Controller's Behavior



Digital Design
Copyright © 2006
Frank Vahid

20

Controller Example: Button Press Synchronizer

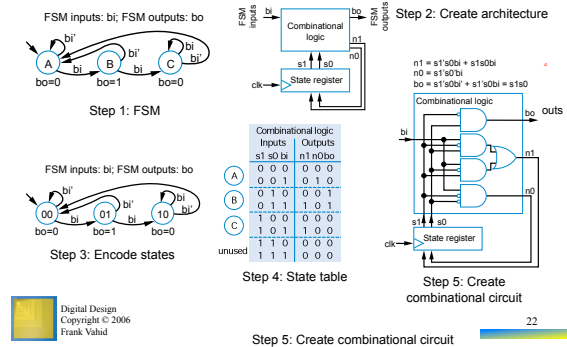


- Want simple sequential circuit that converts button press to single cycle duration, regardless of length of time that button actually pressed
 - We assumed such an ideal button press signal in earlier example, like the button in the laser timer controller

Digital Design
Copyright © 2006
Frank Vahid

21

Controller Example: Button Press Synchronizer (cont)

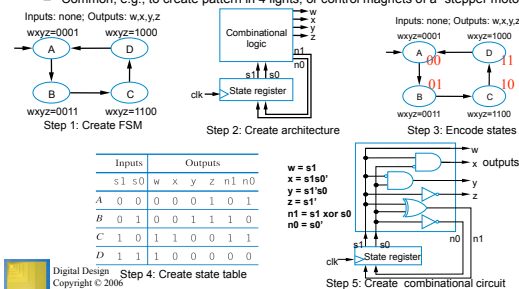


Digital Design
Copyright © 2006
Frank Vahid

22

Controller Example: Sequence Generator

- Want generate sequence 0001, 0011, 1100, 1000, (repeat)
 - Each value for one clock cycle
 - Common, e.g., to create pattern in 4 lights, or control magnets of a "stepper motor"

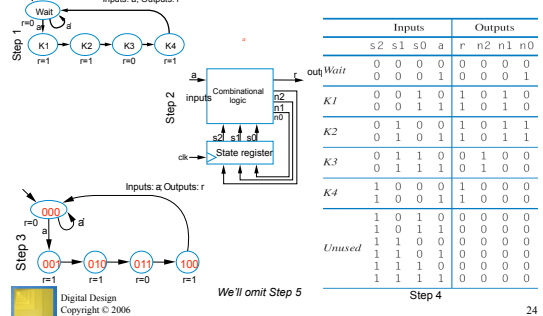


Digital Design
Copyright © 2006
Frank Vahid

23

Controller Example: Secure Car Key

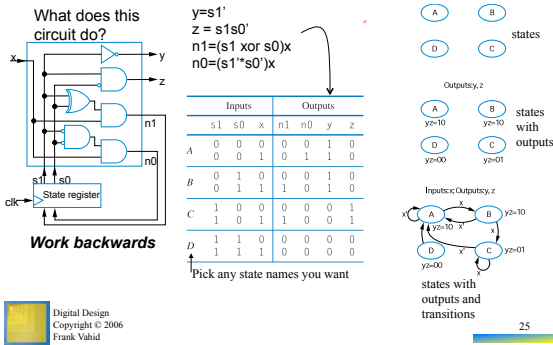
- (from earlier example)



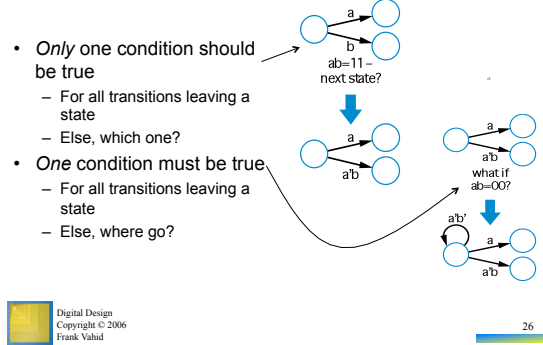
Digital Design
Copyright © 2006
Frank Vahid

24

Example: Seq. Circuit to FSM (Reverse Engineering)

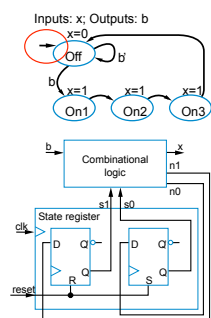


Common Pitfalls Regarding Transition Properties



Initial State of a Controller

- All our FSMs had initial state
 - But our sequential circuit designs did not
 - Can accomplish using flip-flops with reset/set inputs
 - Shown circuit initializes flip-flops to 01
 - Designer must ensure reset input is 1 during power up of circuit
 - By electronic circuit design



Chapter Summary

- Sequential circuits
 - Have state
- Created robust bit-storage device: D flip-flop
 - Put several together to build register, which we used to hold state
- Defined FSM formal model to describe sequential behavior
 - Using solid mathematical models -- Boolean equations for combinational circuit, and FSMs for sequential circuits -- is very important.
- Defined 5-step process to convert FSM to sequential circuit
 - Controller
- So now we know how to build the class of sequential circuits known as controllers