

熱力学 4回目

[1] (i) 定容変化のとき, $dv = 0$ 熱力学第一法則より, $dq = du + pdv$

$$\rightarrow dq = du$$

$$C_v = \left(\frac{dq}{dT} \right)_v = \left(\frac{du}{dT} \right)_v \rightarrow \boxed{du = C_v dT}$$

・定圧変化のとき, $dp = 0$ 熱力学第一法則より, $dq = du + pdv$ エントルピーの関係式より, $h = u + pv \rightarrow dh = du + pdv + vdp$

$$\begin{cases} dq = du + pdv \\ dh = du + pdv + vdp \end{cases}$$

$$\rightarrow \begin{cases} dq = du + pdv - vdp \\ dq = dh - vdp \end{cases}$$

$$dq = dh - vdp \text{ より,}$$

$$dq = dh$$

$$C_p = \left(\frac{dq}{dT} \right)_p = \left(\frac{dh}{dT} \right)_p \rightarrow \boxed{dh = C_p dT}$$

(2) 理想気体の状態方程式より,

$$pv = RT$$

エントルピーの関係式より, $h = u + pv = u + RT$

$$\rightarrow dh = du + RdT$$

$$dh = C_p dT, \quad du = C_v dT \text{ より,}$$

$$C_p dT = C_v dT + R dT$$

$$C_p = C_v + R$$

$$\therefore C_p - C_v = \boxed{R}$$

(3) (i) 定容変化: $dv = 0$

$$dq = du + pdv \text{ より,}$$

$$dq = du$$

$$dq = T ds \text{ より,}$$

$$ds = \frac{dq}{T} = \frac{du}{T} = \frac{C_v dT}{T}$$

$$S = \boxed{C_v \ln T + S_1}$$

(ii) 定圧変化: $dp = 0$

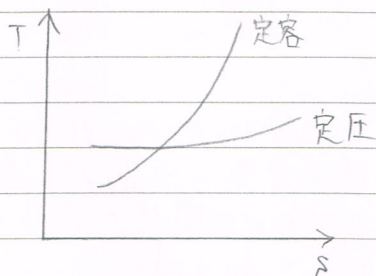
$$dq = dh - vdp \text{ より, } dq = dh$$

$$dq = T ds$$

$$ds = \frac{dq}{T} = \frac{C_p dT}{T} \rightarrow s = C_p \ln T + s_1$$

$$(4) \begin{cases} s = C_p \ln T + s_1 \rightarrow T = \frac{1}{C_p} \exp[s - s_1] \\ s = C_v \ln T + s_2 \rightarrow T = \frac{1}{C_v} \exp[s - s_2] \end{cases}$$

$$C_p > C_v \rightarrow \frac{1}{C_p} < \frac{1}{C_v} \text{ (f)},$$



$$(5) (i) ds = \frac{dq}{T} = \frac{C_p dT}{T} = \frac{(a + bT + cT^2)}{T} dT$$

$$\therefore s = a \ln T + bT + \frac{1}{2} cT^2 + s_1$$

$$(ii) ds = \frac{dq}{T} = \frac{C_p dT}{T} = \frac{(a + R + bT + cT^2)}{T} dT$$

$$\therefore s = (a + R) \ln T + bT + \frac{1}{2} cT^2 + s_2$$

[2] (1) 液体热: $Q_L = mc\Delta T = 1 \cdot 4.0 \cdot (450 - 300) = 600 \text{ (kJ/kg)}$

水: 1, 周围: 2

$$\Delta s_1 = -\int \frac{dq}{T}, \quad \Delta s_2 = \frac{Q_2}{T_2}$$

$$\Delta s = \Delta s_1 + \Delta s_2 = -\int \frac{dq}{T} + \frac{Q_2}{T_2} \geq 0 \rightarrow Q_2 \geq T_2 \int \frac{dq}{T}$$

$$\therefore Q'_0 = Q_{2min} = T_2 \int \frac{dq}{T} = 300 \cdot \int \frac{mcdT}{T} = 300 \cdot 1.4 \cdot \ln \frac{450}{300}$$

$$= 1200 \cdot 0.4 = 480 \text{ (kJ/kg)}$$

$$Q_a = Q_L - Q_a = 120 \text{ (kJ/kg)}$$

$$(2) \Delta s_1 = -\frac{Q}{T_1}, \quad \Delta s_2 = \frac{Q'_2}{T_2}$$

$$\Delta s = \Delta s_1 + \Delta s_2 = -\frac{Q}{T_1} + \frac{Q'_2}{T_2} \geq 0 \rightarrow Q'_2 \geq \frac{T_2}{T_1} Q$$

$$\therefore Q_0'' = Q_{2min} = \frac{T_2}{T_1} Q = \frac{300}{450} \cdot 1800 = 1200 \text{ (kJ/kg)}$$

$$Q_a'' = Q - Q_a' = 600 \text{ (kJ/kg)}$$

$$(3) Q_a = Q_a' + Q_a'' = 1720 \text{ (kJ/kg)}$$

$$Q_o = Q_o' + Q_o'' = 1680 \text{ (kJ/kg)}$$

$$[3] (1) h_2'' = 2600 \text{ (kJ/kg)}, h_2' = h_3 = 150 \text{ (kJ/kg)}$$

$$h_2 = h_2' + x(h_2'' - h_2') = 150 + 0.8(2600 - 150) = 2110 \text{ (kJ/kg)}$$

$$\therefore W_T = h_1 - h_2 = 3300 - 2110 = 1190 \text{ (kJ/kg)}$$

$$(2) q = h_1 - h_3 = 3300 - 150 = 3150 \text{ (kJ/kg)}$$

$$\therefore \eta_{th} = \frac{W_T}{q} = \frac{1190}{3150} \approx 0.38$$

(3) 蒸気の流動による損失 (摩擦・渦・絞り)

・ 周囲への熱損失

・ 蒸気の周囲への漏れ出し

・ 復水器などの周辺空気への漏れ込み

$$(4) W_T' = 0.8 \cdot W_T = 0.8 \cdot 1190 = 952 \text{ (kJ/kg)}$$

$$\eta_{th}' = \frac{W_T'}{q} = \frac{952}{3150} \approx 0.302$$