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## University of Brasilia

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```
set ts=4 sw=4 sta nu rnu sc stl+=%F cindent
imap {<CR> {<CR>}<Esc>0
nmap <F2> 0V$%d
nmap <C-down> :m+1<CR>
nmap <C-up> :m-2<CR>
vmap < C-c > "+y
nmap <C-a> ggVG
syntax on
alias cmp='g++ -Wall -Wformat=2 -Wshadow -Wconversion -
  fsanitize=address -fsanitize=undefined -fno-sanitize-
  recover -std=c++14'
```

#### **Data Structures**

#### **Merge Sort Tree**

```
struct MergeTree{
   int n:
   vector<vector<int>> st;
   void build(int p, int L, int R, const int v[]){
       if(L == R){
          st[p].push_back(v[L]);
          return:
       }
      int mid = (L+R)/2;
      build(2*p, L, mid, v);
      build(2*p+1, mid+1, R, v);
       st[p].resize(R-L+1);
      merge(st[2*p].begin(), st[2*p].end(),
              st[2*p+1].begin(), st[2*p+1].end(),
              st[p].begin());
   }
   int query(int p, int L, int R, int i, int j, int x)
     const{
       if(L > j || R < i) return 0;</pre>
       if(L >= i && R <= j){</pre>
          int id = lower_bound(st[p].begin(), st[p].end
             (), x) - st[p].begin();
          return int(st[p].size()) - id;
      }
       int mid = (L+R)/2;
      return query(2*p, L, mid, i, j, x) +
          query(2*p+1, mid+1, R, i, j, x);
   }
public:
   MergeTree(int sz, const int v[]): n(sz), st(4*sz){
      build(1, 1, n, v);
   //number of elements >= x on segment [i, j]
   int query(int i, int j, int x) const{
       if(i > j) swap(i, j);
       return query(1, 1, n, i, j, x);
   }
};
Wavelet Tree
template<typename T>
class wavelet{
   T L, R;
```

```
vector<int> 1;
vector<T> sum; // <<</pre>
wavelet *lef, *rig;
```

```
int r(int i) const{ return i - l[i]; }
public:
   template<typename ITER>
   wavelet(ITER bg, ITER en){
       lef = rig = nullptr;
       L = *bg, R = *bg;
       for(auto it = bg; it != en; it++)
          L = min(L, *it), R = max(R, *it);
       if(L == R) return;
       T mid = L + (R - L)/2;
       1.reserve(std::distance(bg, en) + 1);
       sum.reserve(std::distance(bg, en) + 1);
       1.push_back(0), sum.push_back(0);
       for(auto it = bg; it != en; it++)
          l.push_back(l.back() + (*it <= mid)),</pre>
          sum.push_back(sum.back() + *it);
       auto tmp = stable_partition(bg, en, [mid](T x){
          return x <= mid;</pre>
       });
       if(bg != tmp) lef = new wavelet(bg, tmp);
       if(tmp != en) rig = new wavelet(tmp, en);
   }
    ~wavelet(){
       delete lef;
       delete rig;
   // 1 index, first is 1st
   T kth(int i, int j, int k) const{
       if(L >= R) return L;
       int c = l[j] - l[i-1];
       if(c >= k) return lef->kth(l[i-1]+1, l[j], k);
       else return rig->kth(r(i-1)+1, r(j), k - c);
   // # elements > x on [i, j]
   int cnt(int i, int j, T x) const{
       if(L > x) return j - i + 1;
       if(R <= x || L == R) return 0;
       int ans = 0;
       if(lef) ans += lef->cnt(l[i-1]+1, l[j], x);
       if(rig) ans += rig->cnt(r(i-1)+1, r(j), x);
       return ans;
   }
   // sum of elements <= k on [i, j]</pre>
   T sumk(int i, int j, T k){
       if(L == R) return R <= k ? L * (j - i + 1) : 0;
       if(R <= k) return sum[j] - sum[i-1];</pre>
       int ans = 0;
       if(lef) ans += lef->sumk(l[i-1]+1, l[j], k);
      if(rig) ans += rig->sumk(r(i-1)+1, r(j), k);
      return ans;
   // swap (i, i+1) just need to update "array" l[i]
};
Order Set
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
```

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```
next(v)):
#include <ext/pb_ds/detail/standard_policies.hpp>
                                                                  while(y != begin() && bad(prev(y))) erase(prev(y)
                                                                     );
using namespace __gnu_pbds; // or pb_ds;
                                                               ll eval(ll x){
                                                                   auto 1 = *lower_bound((Line) { x, is_query });
template<typename T, typename B = null_type>
using oset = tree<T, B, less<T>, rb_tree_tag,
                                                                  return 1.m * x + 1.b;
  tree_order_statistics_node_update>;
                                                               }
// find_by_order / order_of_key
                                                           };
Hash table
                                                           Min queue
                                                           template<typename T>
#include <ext/pb_ds/assoc_container.hpp>
                                                           class minQ{
using namespace __gnu_pbds;
                                                               deque<tuple<T, int, int> > p;
                                                               T delta;
struct custom_hash {
                                                               int sz;
   static uint64_t splitmix64(uint64_t x) {
                                                           public:
       // http://xorshift.di.unimi.it/splitmix64.c
                                                               minQ() : delta(0), sz(0) {}
      x += 0x9e3779b97f4a7c15;
                                                               inline int size() const{ return sz; }
      x = (x \hat{ } (x >> 30)) * 0xbf58476d1ce4e5b9;
                                                               inline void add(T x){ delta += x; }
      x = (x ^(x >> 27)) * 0x94d049bb133111eb;
                                                               inline void push(T x, int id){
      return x \hat{ } (x >> 31);
                                                                  x -= delta, sz++;
   }
                                                                  int t = 1;
                                                                   while(p.size() > 0 && get<0>(p.back()) >= x)
   size_t operator()(uint64_t x) const {
                                                                      t += get<1>(p.back()), p.pop_back();
       static const uint64_t FIXED_RANDOM = chrono::
                                                                  p.emplace_back(x, t, id);
         steady_clock::now().time_since_epoch().count();
                                                               }
       return splitmix64(x + FIXED_RANDOM);
                                                               inline void pop(){
   }
                                                                  get<1>(p.front())--, sz--;
};
                                                                   if(!get<1>(p.front())) p.pop_front();
gp_hash_table<long long, int, custom_hash> table;
unordered_map<long long, int, custom_hash> uhash;
                                                               T getmin() const{ return get<0>(p.front())+delta; }
                                                               int getid() const{ return get<2>(p.front()); }
uhash.reserve(1 << 15);</pre>
                                                           };
uhash.max_load_factor(0.25);
                                                           Sparse Table
Convex Hull Trick
                                                           const int N = 100005;
const ll is_query = -(1LL<<62);</pre>
struct Line{
                                                           int v[N], n;
   11 m, b;
                                                           int dn[N][20];
   mutable function<const Line*()> succ;
                                                           int fn(int i, int j){
   bool operator<(const Line& rhs) const{</pre>
                                                               if(j == 0) return v[i];
       if(rhs.b != is_query) return m < rhs.m;</pre>
                                                               if(~dn[i][j]) return dn[i][j];
       const Line* s = succ();
                                                               return dn[i][j] = min(fn(i, j-1), fn(i + (1 << (j-1)))
       if(!s) return 0;
                                                                 ), j-1));
       11 x = rhs.m;
                                                           }
       return b - s->b < (s->m - m) * x;
                                                           int lg(int x){ return 31 - __builtin_clz(x); }
};
struct Cht : public multiset<Line>{ // maintain max
                                                           int getmn(int 1, int r) { // [1, r]
   bool bad(iterator y){
                                                               int lz = lg(r - 1 + 1);
       auto z = next(y);
                                                               return min(fn(1, lz), fn(r - (1 << lz) + 1, lz));
       if(y == begin()){
                                                           }
          if(z == end()) return 0;
                                                           Treap
          return y->m == z->m \&\& y->b <= z->b;
                                                           // source: https://github.com/victorsenam/caderno/blob/
       auto x = prev(y);
       if(z == end()) return y->m == x->m && y->b <= x->
                                                             master/code/treap.cpp
                                                           //const int N = ; typedef int num;
       return (x->b - y->b)*(z->m - y->m) >= (y->b - z->
                                                           num X[N]; int en = 1, Y[N], sz[N], L[N], R[N];
         b)*(y->m - x->m);
                                                           void calc (int u) { // update node given children info
                                                               sz[u] = sz[L[u]] + 1 + sz[R[u]];
   void insert_line(ll m, ll b){
                                                               // code here, no recursion
      auto y = insert({ m, b });
                                                           }
      y->succ = [=]{ return next(y) == end() ? 0 : &*
                                                           void unlaze (int u) {
         next(y); };
                                                               if(!u) return;
       if(bad(y)){ erase(y); return; }
                                                               // code here, no recursion
       while(next(y) != end() && bad(next(y))) erase(
```

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```
void split_val(int u, num x, int &l, int &r) { // l gets
                                                                  it = ranges.lower_bound(r);
   <= x, r gets > x
                                                                   if(it != ranges.begin()) {
   unlaze(u); if(!u) return (void) (l = r = 0);
                                                                      it--;
   if(X[u] <= x) { split_val(R[u], x, 1, r); R[u] = 1;</pre>
                                                                      if(it->r > r) {
                                                                          auto cur = *it;
     1 = u; }
   else { split_val(L[u], x, 1, r); L[u] = r; r = u; }
                                                                          ranges.erase(it);
   calc(u);
                                                                          ranges.insert(Range(cur.1, r, cur.v));
                                                                          ranges.insert(Range(r, cur.r, cur.v));
void split_sz(int u, int s, int &l, int &r) { // l gets
                                                                      }
  first s, r gets remaining
   unlaze(u); if(!u) return (void) (l = r = 0);
                                                                   for(it = ranges.lower_bound(1); it != ranges.end
   if(sz[L[u]] < s)  { split_sz(R[u], s - sz[L[u]] - 1,
                                                                     () && it->l < r; it++) {
     1, r); R[u] = 1; 1 = u; }
                                                                      ans.push_back(*it);
   else { split_sz(L[u], s, l, r); L[u] = r; r = u; }
                                                                  ranges.erase(ranges.lower_bound(1), ranges.
   calc(u);
                                                                     lower_bound(r));
int merge(int 1, int r) { // els on l <= els on r</pre>
                                                                   ranges.insert(Range(1, r, v));
   unlaze(1); unlaze(r); if(!1 || !r) return 1 + r; int
                                                                   return ans;
                                                               }
   if(Y[1] > Y[r]) { R[1] = merge(R[1], r); u = 1; }
                                                           private:
   else { L[r] = merge(l, L[r]); u = r; }
                                                               std::set<Range> ranges;
   calc(u); return u;
                                                           };
                                                            Heavy Light Decomposition
void init(int n=N-1) { // XXX call before using other
                                                            void dfs_sz(int u){
   for(int i = en = 1; i \le n; i++) { Y[i] = i; sz[i] =
                                                               sz[u] = 1;
      1; L[i] = R[i] = 0; }
   random_shuffle(Y + 1, Y + n + 1);
                                                               for(auto &v : g[u]) if(v == p[u]){
                                                                   swap(v, g[u].back());
                                                                   g[u].pop_back();
ColorUpdate
                                                                  break;
                                                               }
// source: https://github.com/tfg50/Competitive-
  Programming/tree/master/Biblioteca/Data%20Structures
                                                               for(auto &v : g[u]){
                                                                  p[v] = u;
#include <set>
                                                                  dfs_sz(v);
#include <vector>
                                                                   sz[u] += sz[v];
                                                                   if(sz[v] > sz[g[u][0]])
template <class Info = int>
                                                                      swap(v, g[u][0]);
class ColorUpdate {
                                                               }
public:
                                                           }
   struct Range {
       Range(int l = 0) { this->l = 1; }
                                                            // nxt[u] = start of path with u
       Range(int 1, int r, Info v) {
                                                            // set nxt[root] beforehand
          this \rightarrow 1 = 1;
                                                            void dfs_hld(int u){
          this->r = r;
                                                               in[u] = t++;
          this->v = v;
                                                               rin[in[u]] = u;
                                                               for(auto v : g[u]){
       int 1, r;
                                                                  nxt[v] = (v == g[u][0] ? nxt[u] : v);
      Info v:
                                                                   dfs_hld(v);
                                                               }
      bool operator < (const Range &b) const { return 1</pre>
                                                               out[u] = t;
          < b.1: }
   }:
                                                            // subtree of u => [ in[u], out[u] )
   std::vector<Range> upd(int 1, int r, Info v) {
                                                            // path from nxt[u] to u => [ in[ nxt[u] ], in[u] ]
       std::vector<Range> ans;
       if(1 >= r) return ans;
                                                           Iterative Segtree
       auto it = ranges.lower_bound(1);
       if(it != ranges.begin()) {
                                                           T query(int 1, int r, int &pos){ // [1, r]
          it--;
                                                               T rl, rr;
          if(it->r>1) {
                                                               for(1 += n, r += n+1; 1 < r; 1 >>= 1, r >>= 1){
                                                                   if(1 & 1) rl = merge(rl, st[1++]);
              auto cur = *it;
              ranges.erase(it);
                                                                  if(r & 1) rr = merge(st[--r], rr);
              ranges.insert(Range(cur.1, 1, cur.v));
                                                               }
              ranges.insert(Range(1, cur.r, cur.v));
                                                               return merge(rl, rr);
                                                           }
          }
       }
```

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```
// initially save v[i] in st[n+i] for all i
                                                               if(!to[last][c])
void build(){
   for(int p = n-1; p > 0; p--)
                                                                   len[sz] = len[last] + 2;
       st[p] = merge(st[2*p], st[2*p+1]);
                                                                   link[sz] = to[get_link(link[last])][c];
                                                                   diff[sz] = len[sz] - len[link[sz]];
                                                                   if(diff[sz] == diff[link[sz]])
void update(int p, T val){
                                                                      slink[sz] = slink[link[sz]];
   st[p += n] = val;
   while(p >>= 1) st[p] = merge(st[2*p], st[2*p+1]);
                                                                      slink[sz] = link[sz];
                                                                   to[last][c] = sz++;
LiChao's Segtree
                                                               last = to[last][c];
                                                           }
void add_line(line nw, int v = 1, int l = 0, int r =
 maxn) \{ // [1, r) \}
                                                           int main()
   int m = (1 + r) / 2;
                                                            {
   bool lef = nw.eval(1) < st[v].eval(1);</pre>
                                                               ios::sync_with_stdio(0);
   bool mid = nw.eval(m) < st[v].eval(m);</pre>
                                                               cin.tie(0);
   if(mid) swap(st[v], nw);
                                                               init();
   if(r - 1 == 1) {
                                                               string s;
      return;
                                                               cin >> s;
   } else if(lef != mid) {
                                                               int n = s.size();
       add_line(nw, 2 * v, 1, m);
                                                               int ans[n + 1];
   } else {
                                                               memset(ans, 63, sizeof(ans));
       add_line(nw, 2 * v + 1, m, r);
                                                               ans[0] = 0;
   }
                                                               for(int i = 1; i <= n; i++)</pre>
}
                                                                   add_letter(s[i - 1]);
int get(int x, int v = 1, int l = 0, int r = maxn) {
                                                                   for(int v = last; len[v] > 0; v = slink[v])
   int m = (1 + r) / 2;
   if(r - 1 == 1) {
                                                                      series_ans[v] = ans[i - (len[slink[v]] + diff
       return st[v].eval(x);
                                                                        [v])]:
   else if(x < m) {
                                                                      if(diff[v] == diff[link[v]])
       return min(st[v].eval(x), get(x, 2*v, 1, m));
                                                                          series_ans[v] = min(series_ans[v],
                                                                            series_ans[link[v]]);
      return min(st[v].eval(x), get(x, 2*v+1, m, r));
                                                                      ans[i] = min(ans[i], series_ans[v] + 1);
                                                                   }
                                                                   cout << ans[i] << "\n";
Palindromic tree
                                                               }
                                                               return 0;
#include <bits/stdc++.h>
                                                            Math
using namespace std;
                                                            Euclides Extendido
const int maxn = 3e5 + 1, sigma = 26;
int len[maxn], link[maxn], to[maxn][sigma];
int slink[maxn], diff[maxn], series_ans[maxn];
                                                            // a*x + b*y = gcd(a, b), < gcd, x, y>
int sz, last, n;
                                                            tuple<int, int, int> euclidesExt(int a, int b) {
char s[maxn];
                                                               if(b == 0) return make_tuple(a, 1, 0);
                                                               int q, w, e;
void init()
                                                               tie(q, w, e) = euclidesExt(b, a % b);
                                                               return make_tuple(q, e, w - e * (a / b));
   s[n++] = -1;
   link[0] = 1;
                                                            Preffix inverse
   len[1] = -1;
   sz = 2;
                                                           inv[1] = 1;
                                                            for(int i = 2; i < p; i++)</pre>
                                                               inv[i] = (p - (p/i) * inv[p%i] % p) % p;
int get_link(int v)
                                                            Pollard Rho
   while(s[n - len[v] - 2] != s[n - 1]) v = link[v];
                                                           ll rho(ll n){
   return v;
}
                                                               if(n % 2 == 0) return 2;
                                                               11 d, c, x, y;
void add_letter(char c)
                                                               do{
   s[n++] = c -= 'a';
                                                                   c = 11rand() % n, x = 11rand() % n, y = x;
   last = get_link(last);
```

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```
x = add(mul(x, x, n), c, n);
                                                                        while(n % i == 0) n /= i;
                                                                    }
          y = add(mul(y, y, n), c, n);
          y = add(mul(y, y, n), c, n);
                                                                }
          d = \_gcd(abs(x - y), n);
       }while(d == 1);
                                                                if(n > 1) ans = ans / n * (n - 1);
   }while(d == n);
                                                                return ans;
   return d;
                                                             Mobius Function
ll pollard_rho(ll n){
                                                             memset(mu, 0, sizeof mu);
   11 x, c, y, d, k;
                                                             mu[1] = 1;
   int i;
                                                             for(int i = 1; i < N; i++)</pre>
   do{
                                                                 for(int j = i + i; j < N; j += i)
       i = 1;
                                                                    mu[j] -= mu[i];
       x = 11rand() % n, c = 11rand() % n;
                                                             // g(n) = sum{f(d)} => f(n) = sum{mu(d)*g(n/d)}
       y = x, k = 4;
                                                             Mulmod TOP
       do{
          if(++i == k) y = x, k *= 2;
                                                             constexpr uint64_t mod = (1ull<<61) - 1;</pre>
          x = add(mul(x, x, n), c, n);
                                                             uint64_t modmul(uint64_t a, uint64_t b){
           d = \_gcd(abs(x - y), n);
                                                                uint64_t 11 = (uint32_t)a, h1 = a>>32, 12 = (
       }while(d == 1);
                                                                   uint32_t)b, h2 = b>>32;
   }while(d == n);
                                                                uint64_t 1 = 11*12, m = 11*h2 + 12*h1, h = h1*h2;
   return d;
                                                                uint64_t ret = (1&mod) + (1>>61) + (h << 3) + (m >>
}
                                                                   29) + (m \ll 35 \gg 3) + 1;
                                                                ret = (ret & mod) + (ret>>61);
void factorize(ll val, map<ll, int> &fac){
                                                                ret = (ret & mod) + (ret>>61);
   if(rabin(val)) fac[ val ]++;
                                                                return ret-1;
   else{
       11 d = pollard_rho(val);
                                                             Determinant
       factorize(d, fac);
       factorize(val / d, fac);
                                                             const double EPS = 1E-9;
   }
                                                             int n:
}
                                                             vector < vector<double> > a (n, vector<double> (n));
map<ll, int> factor(ll val){
                                                             double det = 1;
   map<ll, int> fac;
                                                             for (int i=0; i<n; ++i) {</pre>
   if(val > 1) factorize(val, fac);
                                                                 int k = i;
   return fac;
                                                                 for (int j=i+1; j<n; ++j)</pre>
                                                                    if (abs (a[j][i]) > abs (a[k][i]))
Miller Rabin
                                                                       k = j;
                                                                if (abs (a[k][i]) < EPS) {</pre>
bool rabin(ll n){
                                                                    det = 0;
   if(n <= 1) return 0;</pre>
                                                                    break;
   if(n <= 3) return 1;
   11 s = 0, d = n - 1;
                                                                swap (a[i], a[k]);
   while(d % 2 == 0) d /= 2, s++;
                                                                if (i != k)
   for(int k = 0; k < 64; k++){
                                                                    det = -det;
       11 a = (11rand() \% (n - 3)) + 2;
                                                                 det *= a[i][i];
       11 x = fexp(a, d, n);
                                                                 for (int j=i+1; j<n; ++j)</pre>
       if(x != 1 \&\& x != n-1){
                                                                    a[i][j] /= a[i][i];
           for(int r = 1; r < s; r++){
                                                                 for (int j=0; j<n; ++j)</pre>
              x = mul(x, x, n);
                                                                    if (j != i && abs (a[j][i]) > EPS)
              if(x == 1) return 0;
                                                                        for (int k=i+1; k<n; ++k)</pre>
              if(x == n-1) break;
                                                                           a[j][k] -= a[i][k] * a[j][i];
          }
                                                             }
          if(x != n-1) return 0;
       }
                                                             cout << det;</pre>
   }
                                                             FFT
   return 1;
                                                             struct base{
Totiente
                                                                double r, i;
                                                                base(double _r = 0, double _i = 0) : r(_r), i(_i) {}
ll totiente(ll n){
                                                                base operator*(base &o) const{
   11 \text{ ans} = n;
                                                                    return {r*o.r - i*o.i, r*o.i + o.r*i};
   for(ll i = 2; i*i <= n; i++){</pre>
       if(n \% i == 0){
                                                                 double real() const{ return r; }
           ans = ans / i * (i - 1);
                                                                void operator*=(const base &o){
```

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```
(*this) = \{r*o.r-i*o.i, r*o.i+o.r*i\};
   }
   void operator+=(const base &o){r += o.r, i += o.i; }
   void operator/=(const double &o){ r /= o, i /= o; }
   void operator==(const base &o){r == o.r, i == o.i; }
   base operator+(const base &o){return {r+o.r,i+o.i};}
   base operator-(const base &o){return {r-o.r,i-o.i};}
};
double PI = acos(-1);
void fft(vector<base> &a, bool inv){
   int n = (int)a.size();
   for(int i = 1, j = 0; i < n; i++){
       int bit = n \gg 1;
       for(; j >= bit; bit >>= 1) j -= bit;
       j += bit;
       if(i < j) swap(a[i], a[j]);</pre>
   for(int sz = 2; sz <= n; sz <<= 1) {</pre>
       double ang = 2*PI/sz * (inv ? -1 : 1);
       base wlen(cos(ang), sin(ang));
       for(int i = 0; i < n; i += sz){
          base w(1);
          for(int j = 0; j < sz/2; j++){
              base u = a[i+j], v = a[i+j+sz/2] * w;
              a[i+j] = u + v;
              a[i+j+sz/2] = u - v;
              w *= wlen;
          }
       }
   if(inv) for(int i = 0; i < n; i++) a[i] /= 1.0 * n;
void multiply(const vector<int> &a, const vector<int> &b
  , vector<int> &res){
   vector<base> fa(a.begin(), a.end());
   vector<base> fb(b.begin(), b.end());
   size_t n = 1;
   while(n < a.size()) n <<= 1;</pre>
   while(n < b.size()) n <<= 1;</pre>
   n <<= 1:
   fa.resize(n), fb.resize(n);
   fft(fa, false), fft(fb, false);
   for(size_t i = 0; i < n; i++)</pre>
       fa[i] *= fb[i];
   fft(fa, true);
   res.resize (n);
   for(size_t i = 0; i < n; ++i)</pre>
       res[i] = int(fa[i].real() + 0.5);
NTT
const int mod = 7340033;
const int root = 5;
const int root_1 = 4404020;
const int root_pw = 1<<20;</pre>
void fft (vector<int> & a, bool invert) {
   int n = (int) a.size();
   for (int i=1, j=0; i<n; ++i) {
```

```
int bit = n \gg 1;
       for (; j>=bit; bit>>=1)
          j -= bit;
       j += bit;
       if (i < j)
           swap (a[i], a[j]);
   }
   for (int len=2; len<=n; len<<=1) {</pre>
       int wlen = invert ? root_1 : root;
       for (int i=len; i<root_pw; i<<=1)</pre>
           wlen = int (wlen * 111 * wlen % mod);
       for (int i=0; i<n; i+=len) {</pre>
           int w = 1;
           for (int j=0; j<len/2; ++j) {</pre>
              int u = a[i+j], v = int (a[i+j+len/2] * 1
                11 * w % mod);
              a[i+j] = u+v < mod ? u+v : u+v-mod;
              a[i+j+len/2] = u-v >= 0 ? u-v : u-v+mod;
              w = int (w * 111 * wlen % mod);
          }
       }
   }
   if (invert) {
       int nrev = reverse (n, mod);
       for (int i=0; i<n; ++i)</pre>
           a[i] = int (a[i] * 111 * nrev % mod);
   }
}
Graphs
Dinic
const int N = 100005;
const int E = 2000006;
vector<int> g[N];
int ne;
struct Edge{
   int from, to;
   ll flow, cap;
} edge[E];
int lvl[N], vis[N], pass, start = N-2, target = N-1;
int qu[N], qt, px[N];
11 run(int s, int sink, ll minE){
   if(s == sink) return minE;
   11 ans = 0;
   for(; px[s] < (int)g[s].size(); px[s]++){</pre>
       int e = g[s][ px[s] ];
       auto &v = edge[e], &rev = edge[e^1];
       if(lvl[v.to] != lvl[s]+1 || v.flow >= v.cap)
         continue:
```

11 tmp = run(v.to, sink,min(minE, v.cap-v.flow));

v.flow += tmp, rev.flow -= tmp;

ans += tmp, minE -= tmp;

if(minE == 0) break;

bool bfs(int source, int sink){

qu[qt++] = source;

}

}

return ans;

qt = 0;

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```
lvl[source] = 1;
                                                            int dijkstra(){
   vis[source] = ++pass;
                                                                forn(i, N) d[i] = oo;
   for(int i = 0; i < qt; i++){
       int u = qu[i];
                                                               priority_queue<pair<ll, int> > q;
       px[u] = 0;
       if(u == sink) return true;
                                                                d[source] = 0;
       for(int e : g[u]){
                                                                q.emplace(0, source);
          auto v = edge[e];
          if(v.flow >= v.cap || vis[v.to] == pass)
                                                                while(!q.empty()){
            continue;
                                                                   11 dis = -q.top().ff;
          vis[v.to] = pass;
                                                                   int u = q.top().ss; q.pop();
          lvl[v.to] = lvl[u]+1;
                                                                   if(dis > d[u]) continue;
          qu[qt++] = v.to;
       }
   }
                                                                   for(int e : g[u]){
                                                                       auto v = edge[e];
   return false;
}
                                                                       if(v.cap <= 0) continue;</pre>
                                                                       if(d[u] + v.cost < d[v.to]){
11 flow(int source = start, int sink = target){
                                                                          d[v.to] = d[u] + v.cost;
   11 \text{ ans} = 0;
                                                                          p[v.to] = e;
   while(bfs(source, sink))
                                                                          q.emplace(-d[v.to], v.to);
       ans += run(source, sink, oo);
                                                                       }
                                                                   }
   return ans;
}
                                                               }
                                                               return d[target] != oo;
void addEdge(int u, int v, ll c = 1, ll rc = 0){
                                                            }
   edge[ne] = \{u, v, 0, c\};
   g[u].push_back(ne++);
                                                            pair<11, 11> mincost(){
   edge[ne] = {v, u, 0, rc};
                                                                ll ans = 0, mf = 0;
   g[v].push_back(ne++);
                                                                while(dijkstra()){
                                                                   11 f = back(target, oo);
                                                                   mf += f;
                                                                   ans += f * d[target];
void reset_flow(){
   for(int i = 0; i < ne; i++)</pre>
                                                               }
       edge[i].flow = 0;
                                                               return {mf, ans};
                                                            }
Min Cost Max Flow
                                                            void addEdge(int u, int v, ll c, ll cost){
                                                                edge[ne] = \{u, v, c, cost\};
const 11 oo = 1e18;
                                                                g[u].pb(ne++);
const int N = 505:
const int E = 30006;
                                                            Small to Large
vector<int> g[N];
                                                            void cnt_sz(int u, int p = -1){
int ne;
                                                                sz[u] = 1;
struct Edge{
                                                                for(int v : g[u]) if(v != p)
   int from, to;
                                                                   cnt_sz(v, u), sz[u] += sz[v];
   11 cap, cost;
                                                            }
} edge[E];
                                                            void add(int u, int p, int big = -1){
                                                                // Update info about this vx in global answer
int lvl[N], vis[N], pass, source, target, p[N], px[N];
11 d[N];
                                                                for(int v : g[u]) if(v != p && v != big)
                                                                   add(v, u);
11 back(int s, ll minE){
                                                            }
   if(s == source) return minE;
                                                            void dfs(int u, int p, int keep){
   int e = p[s];
                                                                int big = -1, mmx = -1;
   11 f = back(edge[e].from, min(minE, edge[e].cap));
   edge[e].cap -= f;
                                                                for(int v : g[u]) if(v != p \&\& sz[v] > mmx)
   edge[e^1].cap += f;
                                                                   mmx = sz[v], big = v;
   return f;
                                                                for(int v : g[u]) if(v != p && v != big)
}
```

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```
dfs(v, u, 0);
if(big != -1) dfs(big, u, 1);
add(u, p, big);
for(auto x : q[u]){
   // answer all queries for this vx
if(!keep){
   // Remove data from this subtree
```

#### Junior e Falta de Ideias

```
#include <bits/stdc++.h>
#define ff first
#define ss second
#define mp make_pair
using namespace std;
typedef long long 11;
vector<pair<int,int>> G[500005];
int subtree[500005], treesize, k;
bool vis[500005];
ll dist[500005], ans;
int dfs(int v, int p){
   subtree[v] = 1;
   for(pair<int,int> x : G[v])
       if(x.ff != p && !vis[x.ff]) subtree[v] += dfs(x.
         ff,v);
   return subtree[v];
}
int centroid(int v, int p){
   for(pair<int,int> x : G[v]){
       if(x.ff == p || vis[x.ff]) continue;
       if(subtree[x.ff]*2 > treesize) return centroid(x.
         ff,v);
   return v;
void procurar_ans(int v, int p, int d_atual, ll custo){
   ans = min(ans, dist[k-d_atual] + custo);
   if(d_atual == k) return;
   for(pair<int,int> x : G[v]){
       if(!vis[x.ff] && x.ff != p)
          procurar_ans(x.ff,v,d_atual+1,custo+x.ss);
}
void atualiza_distancia(int v, int p, int d_atual, 11
   dist[d_atual] = min(dist[d_atual], custo);
   if(d_atual == k) return;
   for(pair<int,int> x : G[v]){
       if(!vis[x.ff] && x.ff != p)
          atualiza_distancia(x.ff,v,d_atual+1,custo+x.
   }
}
```

```
void decomp(int v, int p){
   treesize = dfs(v,v);
    // if(treesize < k) return;</pre>
    int cent = centroid(v,v);
   vis[cent] = 1;
    for(int i = 1; i <= treesize; i++)</pre>
       dist[i] = 1e18;
    for(pair<int,int> x : G[cent]){
       if(!vis[x.ff]){
           procurar_ans(x.ff,cent,1,x.ss);
           atualiza_distancia(x.ff,cent,1,x.ss);
   }
    for(pair<int,int> x : G[cent]){
       if(!vis[x.ff])
           decomp(x.ff, cent);
}
int main(){
   int n,i,a,b;
    scanf("%d%d", &n,&k);
    for(i = 2; i <= n; i++){</pre>
       scanf("%d%d", &a,&b);
       G[i].push_back(mp(a,b));
       G[a].push_back(mp(i,b));
    }
    ans = 1e18;
   decomp(1,-1);
   printf("%1ld\n", ans == 1e18 ? -1 : ans);
   return 0;
}
Kosaraju
vector<int> g[N], gt[N], S;
int vis[N], cor[N], tempo = 1;
void dfs(int u){
   vis[u] = 1;
    for(int v : g[u]) if(!vis[v]) dfs(v);
   S.push_back(u);
}
int e;
void dfst(int u){
    cor[u] = e;
    for(int v : gt[u]) if(!cor[v]) dfst(v);
}
int main(){
   for(int i = 1; i <= n; i++) if(!vis[i]) dfs(i);</pre>
   e = 0:
   reverse(S.begin(), S.end());
   for(int u : S) if(!cor[u])
       e++, dfst(u);
   return 0;
}
```

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```
Tarjan
int cnt = 0, root;
void dfs(int u, int p = -1){
   low[u] = num[u] = ++t;
   for(int v : g[u]){
       if(!num[v]){
          dfs(v, u);
          if(v == root) cnt++;
          if(low[v] >= num[u]) u PONTO DE ARTICULAÇÃO;
          if(low[v] > num[u]) ARESTA u->v PONTE;
          low[u] = min(low[u], low[v]);
      else if(v != p) low[u] = min(low[u], num[v]);
}
root PONTO DE ARTICULAÇÃO <=> cnt > 1
void tarjanSCC(int u){
   low[u] = num[u] = cnt++;
   vis[u] = 1;
   S.push_back(u);
   for(int v : g[u]){
       if(!num[v]) tarjanSCC(v);
       if(vis[v]) low[u] = min(low[u], low[v]);
   if(low[u] == num[u]){
       ssc[u] = ++ssc\_cnt; int v;
          v = S.back(); S.pop_back(); vis[v] = 0;
          ssc[v] = ssc_cnt;
      }while(u != v);
   }
}
Max Clique
long long adj[N], dp[N];
for(int i = 0; i < n; i++){
   for(int j = 0; j < n; j++){
       int x;
       scanf("%d",&x);
       if(x \mid | i == j)
          adj[i] |= 1LL << j;
   }
}
int resto = n - n/2;
int C = n/2;
for(int i = 1; i < (1 << resto); i++){</pre>
   int x = i;
   for(int j = 0; j < resto; j++)
       if(i & (1 << j))</pre>
          x \&= adj[j + C] >> C;
   if(x == i){
      dp[i] = __builtin_popcount(i);
   }
}
for(int i = 1; i < (1 << resto); i++)</pre>
   for(int j = 0; j < resto; j++)
      if(i & (1 << j))
          dp[i] = max(dp[i], dp[i ^ (1 << j)]);
int maxCliq = 0;
for(int i = 0; i < (1 << C); i++){
```

```
int x = i, y = (1 << resto) - 1;
   for(int j = 0; j < C; j++)
       if(i & (1 << j))
          x \&= adj[j] \& ((1 << C) - 1), y \&= adj[j] >>
            С;
   if(x != i) continue;
   maxCliq = max(maxCliq, __builtin_popcount(i) + dp[y
     ]);
Dominator Tree
vector<int> g[N], gt[N], T[N];
vector<int> S;
int dsu[N], label[N];
int sdom[N], idom[N], dfs_time, id[N];
vector<int> bucket[N];
vector<int> down[N];
void prep(int u){
   S.push_back(u);
   id[u] = ++dfs_time;
   label[u] = sdom[u] = dsu[u] = u;
   for(int v : g[u]){
       if(!id[v])
          prep(v), down[u].push_back(v);
       gt[v].push_back(u);
   }
}
int fnd(int u, int flag = 0){
   if(u == dsu[u]) return u;
   int v = fnd(dsu[u], 1), b = label[ dsu[u] ];
   if(id[ sdom[b] ] < id[ sdom[ label[u] ] ])</pre>
       label[u] = b;
   dsu[u] = v;
   return flag ? v : label[u];
void build_dominator_tree(int root, int sz){
   // memset(id, 0, sizeof(int) * (sz + 1));
   // for(int i = 0; i <= sz; i++) T[i].clear();
   prep(root);
   reverse(S.begin(), S.end());
   int w;
   for(int u : S){
       for(int v : gt[u]){
          w = fnd(v);
          if(id[ sdom[w] ] < id[ sdom[u] ])</pre>
              sdom[u] = sdom[w];
       gt[u].clear();
       if(u != root) bucket[ sdom[u] ].push_back(u);
       for(int v : bucket[u]){
          w = fnd(v);
          if(sdom[w] == sdom[v]) idom[v] = sdom[v];
          else idom[v] = w;
       bucket[u].clear();
       for(int v : down[u]) dsu[v] = u;
```

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```
down[u].clear();
   }
                                                               for(int i = 0; str[i]; i++){
                                                                   if(!to[p][ str[i] ]) to[p][ str[i] ] = ne++;
   reverse(S.begin(), S.end());
                                                                  p = to[p][ str[i] ];
                                                               }
   for(int u : S) if(u != root){
                                                               term[p] = 1;
       if(idom[u] != sdom[u]) idom[u] = idom[ idom[u] ];
       T[ idom[u] ].push_back(u);
                                                            int go(int s, char c){
                                                               while(s && !to[s].count(c)) s = fail[s];
   S.clear();
                                                               if(to[s].count(c)) return to[s][c];
                                                               return s;
                                                            }
Min Cost Matching
                                                            void init(){
// Min cost matching
// O(n^2 * m)
                                                               queue<int> q;
// n == nro de linhas
                                                               q.push(0);
// m == nro de colunas
// n <= m | flow == n
                                                               int u, v; char c;
// a[i][j] = custo pra conectar i a j
                                                               while(!q.empty()){
vector < int > u(n + 1), v(m + 1), p(m + 1), way(m + 1);
                                                                  u = q.front(); q.pop();
for(int i = 1; i <= n; ++i){</pre>
   p[0] = i;
                                                                   for(auto w : to[u]){
   int j0 = 0;
                                                                      tie(c, v) = w;
   vector<int> minv(m + 1 , oo);
                                                                      q.push(v);
   vector<char> used(m + 1 , false);
                                                                      if(u){
                                                                          fail[v] = go(fail[u], c);
      used[j0] = true;
                                                                          term[v] |= term[ fail[v] ];
       int i0 = p[j0] , delta = oo, j1;
                                                                      }
       for(int j = 1; j <= m; ++j)
                                                                   }
          if(! used[j]){
                                                               }
              int cur = a[i0][j] - u[i0] - v[j];
              if(cur < minv[j])</pre>
                 minv[j] = cur, way[j] = j0;
                                                            Suffix Array
              if(minv[j] < delta)</pre>
                 delta = minv[j] , j1 = j;
          }
                                                            char s[N];
       for(int j = 0; j <= m; ++j)
                                                            int n, sa[N], tsa[N], lcp[N], r[N], nr[N], c[N];
          if(used[i])
             u[p[j]] += delta, v[j] -= delta;
                                                            void sort(int k, int mx){
          else
                                                               mx += 2:
             minv[j] -= delta;
                                                               memset(c, 0, sizeof(int) * mx);
       j0 = j1;
                                                               for(int i = 0; i < n; i++) c[i + k < n ? r[i+k]+2 :
   }while(p[j0] != 0);
                                                                 1]++;
                                                               partial_sum(c, c+mx, c);
   do{
                                                               int t;
       int j1 = way[j0];
                                                               for(int i = 0; i < n; i++)
      p[j0] = p[j1];
                                                                   t = sa[i]+k < n ? r[ sa[i]+k ]+1 : 0,
       j0 = j1;
                                                                   tsa[c[t]++] = sa[i];
   }while(j0);
                                                               memcpy(sa, tsa, sizeof(int) * n);
}
// match[i] = coluna escolhida para linha i
                                                            void build_sa(){
vector<int> match(n + 1);
for(int j = 1; j \le m; ++j)
                                                               for(int i = 0; i < n; i++) sa[i] = i, r[i] = s[i];</pre>
   match[p[j]] = j;
                                                               int t = 300, a, b;
int cost = -v[0];
                                                               for(int sz = 1; sz < n; sz *= 2){
Strings
                                                                   sort(sz, t), sort(0, t);
                                                                   t = nr[ sa[0] ] = 0;
Aho Corasick
                                                                   for(int i = 1; i < n; i++){
                                                                      a = sa[i]+sz < n ? r[ sa[i]+sz ] : -1;
map<char, int> to[N];
                                                                      b = sa[i-1]+sz < n ? r[ sa[i-1]+sz ] : -1;
int ne = 1, term[N], fail[N];
                                                                      nr[ sa[i] ] = r[ sa[i] ] == r[ sa[i-1] ] && a
                                                                         == b ? t : ++t;
void add_string(char *str){
   int p = 0;
                                                                   if(t == n-1) break;
```

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```
memcpy(r, nr, sizeof(int) * n);
                                                           int min_rotation(int *s, int N) {
   }
                                                             REP(i, N) s[N+i] = s[i];
}
                                                             int a = 0;
void build_lcp(){ // lcp[i] = lcp(s[:i], s[:i+1])
                                                             REP(b, N) REP(i, N) {
   int k = 0;
                                                               if (a+i == b \mid \mid s[a+i] < s[b+i]) { b += max(0, i-1);}
   for(int i = 0; i < n; i++) r[ sa[i] ] = i;
                                                                  break; }
                                                               if (s[a+i] > s[b+i]) \{ a = b; break; \}
   for(int i = 0; i < n; i++){
       if(r[i] == n-1) k = 0;
                                                             return a;
       else{
          int j = sa[r[i]+1];
                                                            All palindrome
          while(i+k < n \&\& j+k < n \&\& s[i+k] == s[j+k])
                                                            void manacher(char *s, int N, int *rad) {
                                                             static char t[2*MAX];
       lcp[r[i]] = k;
                                                             int m = 2*N - 1;
       if(k) k--;
   }
                                                             REP(i, m) t[i] = -1;
}
                                                             REP(i, N) t[2*i] = s[i];
int comp_lcp(int i, int j){
                                                             int x = 0;
   if(i == j) return n - i;
                                                             FOR(i, 1, m) {
   if(r[i] > r[j]) swap(i, j);
                                                               int &r = rad[i] = 0;
   return min(lcp[k] for k in [r[i], r[j]-1]);
                                                               if (i <= x+rad[x]) r = min(rad[x+x-i], x+rad[x]-i);</pre>
                                                               while (i-r-1 >= 0 \& i+r+1 < m \& t[i-r-1] == t[i+r]
Z Algorithm
                                                                 +1]) ++r;
                                                               if (i+r >= x+rad[x]) x = i;
vector<int> z_algo(const string &s) {
   int n = s.size(), L = 0, R = 0;
   vector<int> z(n, 0);
                                                             REP(i, m) if (i-rad[i] == 0 || i+rad[i] == m-1) ++rad[
   for(int i = 1; i < n; i++){</pre>
       if(i \le R) z[i] = min(z[i-L], R - i + 1);
                                                             REP(i, m) rad[i] /= 2;
       while(z[i]+i < n \& s[z[i]+i] == s[z[i]])
          z[i]++;
                                                            Palindromic Tree
       if(i+z[i]-1 > R) L = i, R = i + z[i] - 1;
   }
                                                            const int MAXN = 105000;
   return z;
}
                                                            struct node {
Prefix function/KMP
                                                               int next[26];
                                                               int len;
vector<int> preffix_function(const string &s){
                                                               int sufflink;
   int n = s.size();
                                                               int num:
   vector<int> b(n+1);
                                                           }:
   b[0] = -1;
   int i = 0, j = -1;
                                                            int len;
   while(i < n){
                                                            char s[MAXN];
       while(j >= 0 && s[i] != s[j]) j = b[j];
                                                           node tree[MAXN]:
       b[++i] = ++j;
                                                           int num; // node 1 - root with len -1, node 2 - root
   }
                                                             with len 0
   return b;
                                                           int suff; // max suffix palindrome
}
                                                           long long ans;
void kmp(const string &t, const string &p){
                                                           bool addLetter(int pos) {
   vector<int> b = preffix_function(p);
                                                               int cur = suff, curlen = 0;
   int n = t.size(), m = p.size();
                                                               int let = s[pos] - 'a';
   int j = 0;
   for(int i = 0; i < n; i++){
                                                               while(true){
       while(j >= 0 && t[i] != p[j]) j = b[j];
                                                                   curlen = tree[cur].len;
       i++:
                                                                   if (pos-1 - curlen) = 0 && s[pos-1 - curlen] == s
       if(j == m){
                                                                     [pos])
          //patern of p found on t
                                                                      break:
          j = b[j];
                                                                  cur = tree[cur].sufflink;
       }
   }
                                                               if (tree[cur].next[let]) {
}
                                                                   suff = tree[cur].next[let];
Min rotation
                                                                   return false;
```

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```
}
   num++;
   suff = num:
                                                            Suffix Tree
   tree[num].len = tree[cur].len + 2;
   tree[cur].next[let] = num;
                                                            namespace sf {
   if (tree[num].len == 1){
       tree[num].sufflink = 2;
       tree[num].num = 1;
       return true;
                                                            struct node {
   while (true){
                                                               map<char, int> adj;
      cur = tree[cur].sufflink;
       curlen = tree[cur].len;
       if(pos-1 - curlen) == 0 \&\& s[pos-1 - curlen] == s[
          tree[num].sufflink = tree[cur].next[let];
          break;
                                                                 }
       }
                                                            } t[N]:
   tree[num].num = 1 + tree[tree[num].sufflink].num;
   return true:
}
                                                                 ; cn = cd = 0;
void initTree() {
   num = 2; suff = 2;
   tree[1].len = -1; tree[1].sufflink = 1;
   tree[2].len = 0; tree[2].sufflink = 1;
                                                                          cd++:
int main() {
                                                                          else {
   initTree();
   for (int i = 0; i < len; i++) {</pre>
      addLetter(i);
   return 0;
}
Suffix Automaton
                                                                       } else {
map<char, int> to[2*N];
int link[2*N], len[2*N], last = 0, sz = 1;
void add_letter(char c){
   int p = last;
   last = sz++;
   len[last] = len[p] + 1;
   for(; !to[p][c]; p = link[p]) to[p][c] = last;
   if(to[p][c] == last){
      link[last] = 0;
      return;
                                                                            p;
   int u = to[p][c];
   if(len[u] == len[p]+1){
      link[last] = u;
      return:
   }
   int c1 = sz++;
   to[c1] = to[u];
   link[c1] = link[u];
   len[c1] = len[p]+1;
                                                                       }
   link[last] = link[u] = c1;
```

```
for(; to[p][c] == u; p = link[p]) to[p][c] = c1;
// const int NS = ; const int N = * 2;
int cn, cd, ns, en = 1, lst;
string S[NS]; int si = -1;
vector<int> sufn[N]; // sufn[si][i] no do sufixo S[si][i
   int 1, r, si, p, suf;
   node() : 1(0), r(-1), suf(0), p(0) {}
   node(int L, int R, int S, int P) : 1(L), r(R), si(S)
   inline int len() { return r - l + 1; }
   inline int operator[](int i) { return S[si][l + i];
   inline int& operator()(char c) { return adj[c]; }
inline int new_node(int L, int R, int S, int P) { t[en]
  = node(L, R, S, P); return en++; }
void add_string(string s) {
   s += '; S[++si] = s; sufn[si].resize(s.size() + 1)
   int i = 0; const int n = s.size();
   for(int j = 0; j < n; j++)
       for(; i <= j; i++) {</pre>
          if(cd == t[cn].len() \&\& t[cn](s[j])) { cn = t}
             [cn](s[j]); cd = 0; }
          if(cd < t[cn].len() \& t[cn][cd] == s[j]) {
              if(j < s.size() - 1) break;</pre>
                 if(i) t[lst].suf = cn;
                  for(; i <= j; i++) { sufn[si][i] = cn;</pre>
                    cn = t[cn].suf; }
          } else if(cd == t[cn].len()) {
              sufn[si][i] = en;
              if(i) t[lst].suf = en; lst = en;
              t[cn](s[j]) = new_node(j, n - 1, si, cn);
              cn = t[cn].suf; cd = t[cn].len();
              int mid = new_node(t[cn].1, t[cn].1 + cd -
                 1, t[cn].si, t[cn].p);
              t[t[cn].p](t[cn][0]) = mid;
              if(ns) t[ns].suf = mid;
              if(i) t[lst].suf = en; lst = en;
              sufn[si][i] = en;
              t[mid](s[j]) = new_node(j, n - 1, si, mid)
              t[mid](t[cn][cd]) = cn;
              t[cn].p = mid; t[cn].l += cd; cn = t[mid].
              int g = cn? j - cd : i + 1; cn = t[cn].suf
              while (g < j \&\& g + t[t[cn](S[si][g])].len
                () <= j) {
                 cn = t[cn](S[si][g]); g += t[cn].len();
              if(g == j) \{ ns = 0; t[mid].suf = cn; cd = 0 \}
                 t[cn].len(); }
              else { ns = mid; cn = t[cn](S[si][g]); cd
                = j - g;  }
```

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```
}
};
```

### Geometry

#### 2D basics

```
typedef double cod;
double eps = 1e-7;
bool eq(cod a, cod b){ return abs(a - b) <= eps; }</pre>
struct vec{
   cod x, y; int id;
   vec(cod a = 0, cod b = 0) : x(a), y(b) {}
   vec operator+(const vec &o) const{
       return \{x + o.x, y + o.y\};
   vec operator-(const vec &o) const{
       return {x - o.x, y - o.y};
   }
   vec operator*(cod t) const{
       return {x * t, y * t};
   }
   vec operator/(cod t) const{
       return {x / t, y / t};
   cod operator*(const vec &o) const{ // cos
       return x * o.x + y * o.y;
   }
   cod operator^(const vec &o) const{ // sin
       return x * o.y - y * o.x;
   }
   bool operator==(const vec &o) const{
       return eq(x, o.x) && eq(y, o.y);
   bool operator<(const vec &o) const{</pre>
       if(!eq(x, o.x)) return x < o.x;
       return y < o.y;</pre>
   }
   cod cross(const vec &a, const vec &b) const{
       return (a-(*this)) ^ (b-(*this));
   }
   int ccw(const vec &a, const vec &b) const{
       cod tmp = cross(a, b);
       return (tmp > eps) - (tmp < -eps);</pre>
   cod dot(const vec &a, const vec &b) const{
       return (a-(*this)) * (b-(*this));
   }
   cod len() const{
       return sqrt(x * x + y * y); // <</pre>
   double angle(const vec &a, const vec &b) const{
       return atan2(cross(a, b), dot(a, b));
   double tan(const vec &a, const vec &b) const{
       return cross(a, b) / dot(a, b);
   }
   vec unit() const{
       return operator/(len());
   }
   int quad() const{
       if(x > 0 \& y >=0) return 0;
       if(x <= 0 \&\& y > 0) return 1;
       if(x < 0 \&\& y <=0) return 2;
       return 3;
   }
```

```
bool comp(const vec &a, const vec &b) const{
       return (a - *this).comp(b - *this);
   bool comp(vec b){
       if(quad() != b.quad()) return quad() < b.quad();</pre>
       if(!eq(operator^(b), 0)) return operator^(b) > 0;
       return (*this) * (*this) < b * b;</pre>
   template<class T>
   void sort_by_angle(T first, T last) const{
       std::sort(first, last, [=](const vec &a, const
         vec &b){
          return comp(a, b);
       });
   3
   vec rot90() const{ return {-y, x}; }
   vec rot(double a) const{
       return {cos(a)*x -sin(a)*y, sin(a)*x +cos(a)*y};
};
struct line{
   cod a, b, c; vec n;
   line(vec q, vec w){ // q.cross(w, (x, y)) = 0
      a = -(w.y-q.y);
      b = w.x-q.x;
      c = -(a * q.x + b * q.y);
      n = \{a, b\};
   cod dist(const vec &o) const{
       return abs(eval(o)) / n.len();
   bool contains(const vec &o) const{
       return eq(a * o.x + b * o.y + c, \emptyset);
   }
   cod dist(const line &o) const{
       if(!parallel(o)) return 0;
       if(!eq(o.a * b, o.b * a)) return 0;
       if(!eq(a, 0))
          return abs(c - o.c * a / o.a) / n.len();
       if(!eq(b, 0))
          return abs(c - o.c * b / o.b) / n.len();
       return abs(c - o.c);
   bool parallel(const line &o) const{
       return eq(n ^ o.n, 0);
   bool operator==(const line &o) const{
       if(!eq(a*o.b, b*o.a)) return false;
       if(!eq(a*o.c, c*o.a)) return false;
       if(!eq(c*o.b, b*o.c)) return false;
       return true;
   bool intersect(const line &o) const{
       return !parallel(o) || *this == o;
   vec inter(const line &o) const{
       if(parallel(o)){
          if(*this == o){ }
          else{ /* dont intersect */ }
       }
       auto tmp = n ^ o.n;
       return {(o.c*b -c*o.b)/tmp, (o.a*c -a*o.c)/tmp};
   }
   vec at_x(cod x) const{
       return \{x, (-c-a*x)/b\};
```

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```
vec at_y(cod y) const{
      return \{(-c-b*y)/a, y\};
   }
   cod eval(const vec &o) const{
      return a * o.x + b * o.y + c;
};
struct segment{
   vec p, q;
   segment(vec a = vec(), vec b = vec()): p(a), q(b) {}
   bool onstrip(const vec &o) const{ // onstrip strip
       return p.dot(o, q) >= -eps && q.dot(o, p) >= -eps
   }
   cod len() const{
      return (p-q).len();
   }
   cod dist(const vec &o) const{
       if(onstrip(o)) return line(p, q).dist(o);
       return min((o-q).len(), (o-p).len());
   bool contains(const vec &o) const{
      return eq(p.cross(q, o), 0) && onstrip(o);
   }
   bool intersect(const segment &o) const{
       if(contains(o.p)) return true;
       if(contains(o.q)) return true;
       if(o.contains(q)) return true;
       if(o.contains(p)) return true;
       return p.ccw(q, o.p) * p.ccw(q, o.q) == -1
       && o.p.ccw(o.q, q) * o.p.ccw(o.q, p) == -1;
   bool intersect(const line &o) const{
      return o.eval(p) * o.eval(q) <= 0;</pre>
   }
   cod dist(const segment &o) const{
       if(line(p, q).parallel(line(o.p, o.q))){
          if(onstrip(o.p) || onstrip(o.q)
          || o.onstrip(p) || o.onstrip(q))
             return line(p, q).dist(line(o.p, o.q));
       else if(intersect(o)) return 0;
       return min(min(dist(o.p), dist(o.q)),
                min(o.dist(p), o.dist(q)));
   }
   cod dist(const line &o) const{
      if(line(p, q).parallel(o))
          return line(p, q).dist(o);
       else if(intersect(o)) return 0;
       return min(o.dist(p), o.dist(q));
};
struct hray{
   vec p, q;
   hray(vec a = vec(), vec b = vec()): p(a), q(b){}
   bool onstrip(const vec &o) const{ // onstrip strip
      return p.dot(q, o) >= -eps;
   }
   cod dist(const vec &o) const{
       if(onstrip(o)) return line(p, q).dist(o);
       return (o-p).len();
   bool intersect(const segment &o) const{
       if(!o.intersect(line(p,q))) return false;
```

```
if(line(o.p, o.q).parallel(line(p,q)))
          return contains(o.p) || contains(o.q);
       return contains(line(p,q).inter(line(o.p,o.q)));
   bool contains(const vec &o) const{
      return eq(line(p, q).eval(o), 0) && onstrip(o);
   cod dist(const segment &o) const{
       if(line(p, q).parallel(line(o.p, o.q))){
          if(onstrip(o.p) || onstrip(o.q))
              return line(p, q).dist(line(o.p, o.q));
          return o.dist(p);
       else if(intersect(o)) return 0;
       return min(min(dist(o.p), dist(o.q)),
                o.dist(p));
   bool intersect(const hray &o) const{
       if(!line(p, q).parallel(line(o.p, o.q)))
          return false;
       auto pt = line(p, q).inter(line(o.p, o.q));
       return contains(pt) && o.contains(pt); // <<</pre>
   bool intersect(const line &o) const{
       if(line(p, q).parallel(o)) return line(p, q)== o;
       if(o.contains(p) || o.contains(q)) return true;
       return (o.eval(p) >= -eps)^(o.eval(p)<o.eval(q));</pre>
       return contains(o.inter(line(p, q)));
   cod dist(const line &o) const{
       if(line(p,q).parallel(o))
          return line(p,q).dist(o);
       else if(intersect(o)) return 0;
       return o.dist(p);
   cod dist(const hray &o) const{
       if(line(p, q).parallel(line(o.p, o.q))){
          if(onstrip(o.p) || o.onstrip(p))
              return line(p,q).dist(line(o.p, o.q));
          return (p-o.p).len();
       else if(intersect(o)) return 0;
       return min(dist(o.p), o.dist(p));
   }
};
double heron(cod a, cod b, cod c){
   cod s = (a + b + c) / 2;
   return sqrt(s * (s - a) * (s - b) * (s - c));
Nearest Points
struct pt {
   int x, y, id;
};
inline bool cmp_x (const pt & a, const pt & b) {
   return a.x < b.x | | a.x == b.x && a.y < b.y;
inline bool cmp_y (const pt & a, const pt & b) {
   return a.y < b.y;</pre>
}
pt a[MAXN];
double mindist;
```

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```
int ansa, ansb;
inline void upd_ans (const pt & a, const pt & b) {
   double dist = sqrt((a.x-b.x)*(a.x-b.x) + (a.y-b.y)
      *(a.y-b.y) + .0);
   if (dist < mindist)</pre>
       mindist = dist, ansa = a.id, ansb = b.id;
}
                                                             }
void rec (int 1, int r) {
   if (r - 1 <= 3) {
       for (int i=1; i<=r; ++i)</pre>
           for (int j=i+1; j<=r; ++j)</pre>
              upd_ans (a[i], a[j]);
       sort (a+1, a+r+1, &cmp_y);
       return:
                                                             }
   }
   int m = (1 + r) >> 1;
   int midx = a[m].x;
                                                               > &hi, vec p){
   rec (1, m), rec (m+1, r);
   static pt t[MAXN];
   merge (a+1, a+m+1, a+m+1, a+r+1, t, &cmp_y);
   copy (t, t+r-l+1, a+l);
                                                                   hull
   int tsz = 0;
   for (int i=1; i<=r; ++i)</pre>
                                                             // borders included
       if (abs (a[i].x - midx) < mindist) {</pre>
           for (int j=tsz-1; j>=0 && a[i].y - t[j].y <</pre>
             mindist; --j)
              upd_ans (a[i], t[j]);
           t[tsz++] = a[i];
       }
}
sort (a, a+n, &cmp_x);
mindist = 1E20;
rec (0, n-1);
                                                                 while(L <= R){</pre>
Convex Hull
                                                                      +1;
vector<vec> monotone_chain_ch(vector<vec> P){
                                                                    else R = mid-1;
   sort(P.begin(), P.end());
   vector<vec> L, U;
   for(auto p : P){
       while(L.size() >= 2 && L[L.size() - 2].cross(L.
                                                             Minkowski sum
         back(), p) < 0)
          L.pop_back();
                                                                 int i = 0, j = 0;
       L.push_back(p);
   }
                                                                    i = k:
   reverse(P.begin(), P.end());
   for(auto p : P){
                                                                    i = k:
       while(U.size() >= 2 && U[U.size() - 2].cross(U.
         back(), p) < 0)
                                                                 vector<vec> c;
          U.pop_back();
       U.push_back(p);
   }
   L.pop_back(), U.pop_back();
                                                                        c.pop_back();
                                                                    c.push_back(pt);
   L.reserve(L.size() + U.size());
   L.insert(L.end(), U.begin(), U.end());
   return L;
```

### Check point inside polygon

```
bool below(const vector<vec> &vet, vec p){
   auto it = lower_bound(vet.begin(), vet.end(), p);
   if(it == vet.end()) return false;
   if(it == vet.begin()) return *it == p;
   return prev(it)->cross(*it, p) <= 0;</pre>
bool above(const vector<vec> &vet, vec p){
   auto it = lower_bound(vet.begin(), vet.end(), p);
   if(it == vet.end()) return false;
   if(it == vet.begin()) return *it == p;
   return prev(it)->cross(*it, p) >= 0;
// lowerhull, upperhull and point, borders included
bool inside_poly(const vector<vec> &lo, const vector<vec</pre>
   return below(hi, p) && above(lo, p);
```

# Check point inside polygon without lower/upper

```
// must not have 3 colinear consecutive points
bool inside_poly(const vector<vec> &v, vec p){
   if(v[0].ccw(v[1], p) < 0) return false;
   if(v[0].ccw(v.back(), p) > 0) return 0;
   if(v[0].ccw(v.back(), p) == 0)
       return v[0].dot(p, v.back()) >= 0
          && v.back().dot(p, v[0]) >= 0;
   int L = 1, R = (int)v.size() - 1, ans = 1;
      int mid = (L+R)/2;
      if(v[0].ccw(v[mid], p) >= 0) ans = mid, L = mid
   return v[ans].ccw(v[(ans+1)%v.size()], p) >= 0;
```

```
vector<vec> mk(const vector<vec>&a,const vector<vec>&b){
   for(int k = 0; k < (int)a.size(); k++)if(a[k] < a[i])
   for(int k = 0; k < (int)b.size(); k++)if(b[k] < b[j])
   c.reserve(a.size() + b.size());
   for(int k = 0; k < int(a.size()+b.size()); k++){
       vec pt{a[i] + b[j]};
       if((int)c.size() >= 2
       && c[c.size()-2].ccw(c.back(), pt) == 0)
       int q = i+1, w = j+1;
       if(q == int(a.size())) q = 0;
       if(w == int(b.size())) w = 0;
       if(c.back().ccw(a[i]+b[w], a[q]+b[j]) < 0) i = q;
```

```
else j = w;
                                                                   fill(change.begin(), change.end(), 0);
   }
                                                                   bipartite = true;
                                                               }
   c.shrink_to_fit();
                                                               void rollback(){
   return c;
                                                                   int u = get<0>(modifications.back());
                                                                   tie(ignore, change[u], bipartite) = modifications
Miscellaneous
                                                                     .back();
                                                                   sz[p[u]] = sz[u];
LIS
                                                                  p[u] = u;
                                                                   modifications.pop_back();
multiset<int> S;
                                                               }
for(int i = 0; i < n; i++){
   auto it = S.upper_bound(a[i]); // low for inc
                                                               void reload(){
   if(it != S.end()) S.erase(it);
                                                                   while(modifications.size() > saves.back())
   S.insert(a[i]);
                                                                      rollback():
                                                                   saves.pop_back();
ans = S.size();
                                                               }
DSU rollback
                                                               void save(){
#include <bits/stdc++.h>
                                                                   saves.push_back(modifications.size());
using namespace std;
                                                            };
struct DSU{
                                                            const int N = 100005;
   vector<int> sz, p, change;
                                                            const int B = 318;
   vector<tuple<int, int, int>> modifications;
   vector<size_t> saves;
                                                            int n, m, q;
   bool bipartite;
                                                            int x[N], y[N], 1[N], r[N], ans[N];
   DSU(int n): sz(n+1, 1), p(n+1), change(n+1),
                                                            vector<int> qu[N];
     bipartite(true){
       iota(p.begin(), p.end(), 0);
                                                            int brute(int lef, int rig, DSU &s){
   }
                                                               s.save();
                                                               for(int i = lef; i <= rig; i++)</pre>
   void add_edge(int u, int v){
                                                                   s.add_edge(x[i], y[i]);
       if(!bipartite) return;
                                                               int ret = s.bipartite;
       int must_change = get_colour(u) == get_colour(v);
                                                               s.reload();
       int a = rep(u), b = rep(v);
                                                               return ret;
       if(sz[a] < sz[b]) swap(a, b);
                                                            }
       if(a != b){
          p[b] = a;
                                                            int main(){
          modifications.emplace_back(b, change[b],
            bipartite);
                                                               scanf("%d %d %d", &n, &m, &q);
          change[b] ^= must_change;
          sz[a] += sz[b];
                                                               for(int i = 1; i <= m; i++)</pre>
                                                                   scanf("%d %d", x+i, y+i);
       else if(must_change){
          modifications.emplace_back(0, change[0],
                                                               DSU s(n);
            bipartite);
                                                               for(int i = 0; i < q; i++){
          bipartite = false;
                                                                   scanf("%d %d", l+i, r+i);
      }
                                                                   if(r[i] - 1[i] \le B + 10)
   }
                                                                      ans[i] = brute(l[i], r[i], s);
                                                                   else qu[l[i] / B].push_back(i);
   int rep(int u){
                                                               }
      return p[u] == u ? u : rep(p[u]);
                                                               for(int i = 0; i <= m / B; i++){</pre>
                                                                   sort(qu[i].begin(), qu[i].end(),[](int a, int b){
   int get_colour(int u){
                                                                      return r[a] < r[b];</pre>
      if(p[u] == u) return change[u];
                                                                   }):
      return change[u] ^ get_colour(p[u]);
                                                                   s.reset():
   }
                                                                   int R = (i+1)*B-1;
   void reset(){
      modifications.clear();
                                                                   for(int id : qu[i]){
       saves.clear();
                                                                      while(R < r[id]) ++R, s.add_edge(x[R], y[R]);
       iota(p.begin(), p.end(), 0);
                                                                      s.save();
       fill(sz.begin(), sz.end(), 1);
```

```
for(int k = 1[id]; k < (i+1)*B; k++)
              s.add_edge(x[k], y[k]);
          ans[id] = s.bipartite;
          s.reload();
       }
   }
   for(int i = 0; i < q; i++)
       printf("%s\n",ans[i] ? "Possible":"Impossible");
Buildings
// count the number of circular arrays
// of size m, with elements on range
// [1, c**(x*x)]
#include<bits/stdc++.h>
using namespace std;
#define debug(x) cerr << fixed << #x << " = " << x <<
  endl:
#define 11 long long
const int MOD = 1e9 + 7;
const int MAX = 1e5 + 5;
int dp[MAX];
inline int add(int a, int b) {
 a += b;
 if(a >= MOD) {
   a -= MOD;
 }
 return a;
inline int sub(int a, int b) {
 a -= b;
 if(0 > a) {
   a += MOD;
 return a:
}
inline int mult(int a, int b) {
 return (1LL * a * b) % MOD;
int f_exp(int x, int exp) {
 if(exp == 0) {
   return 1;
 else if(exp & 1) {
   return mult(x, f_exp(x, exp - 1));
 return f_exp(mult(x, x), exp / 2);
inline int inv(int x) {
 return f_exp(x, MOD - 2);
}
int main()
 ios::sync_with_stdio(false);
 cin.tie(NULL); cout.tie(NULL);
 int n, m, c;
```

```
cin >> n >> m >> c;
 int x = f_{exp}(c, n * n);
 int ans = f_{exp}(x, m);
 for(int i = 1; i <= m; i++) {</pre>
   if(m \% i == 0) {
     int y = f_exp(x, i);
     for(int j = 1; j < i; j++) {
       if(i % j == 0) {
        y = sub(y, mult(j, dp[j]));
     }
     dp[i] = mult(y, inv(i));
     ans = sub(ans, mult(i - 1, dp[i]));
 }
 cout << ans << '\n';</pre>
 return 0;
Rand
cout << RAND_MAX << endl;</pre>
mt19937 rng(chrono::steady_clock::now().time_since_epoch
  ().count());
vector<int> permutation(N);
iota(permutation.begin(), permutation.end(), 0);
shuffle(permutation.begin(), permutation.end(), rng);
iota(permutation.begin(), permutation.end(), 0);
for(int i = 1; i < N; i++){
   swap(permutation[i], permutation[
     uniform_int_distribution<int>(0, i)(rng)]);
Klondike
// minimum number of moves to make
// all elements equal
// move: change a segment of equal value
// elements to any value
int v[305];
int dp[305][305];
int rec[305][305];
int f(int 1, int r){
 if(r == 1) return 1;
 if(r < 1) return 0;</pre>
 if(dp[l][r] != -1) return dp[l][r];
 int ans = f(1+1, r) + 1;
 for(int i = l+1; i <= r; i++)</pre>
   if(v[i] == v[1])
     ans = min(ans, f(1, i - 1) + f(i+1, r));
 return dp[l][r] = ans;
}
int main() {
 int n. m:
 memset(dp, -1, sizeof dp);
 scanf("%d %d",&n , &m);
 for(int i = 0; i < n; i++){
```

```
scanf("%d",v+i);
   if(i \& v[i] == v[i-1]){
                                                           }
     i--;
                                                           Slope Trick
    n--:
   }
                                                           ///By woqja125, contest: Codeforces Round #371 (Div. 1),
 }
                                                              problem: (C) Sonya and Problem Wihtout a Legend,
 printf("%d\n",f(0, n-1) - 1);
                                                              Accepted, #
 // printf("%d\n",rec[0][n-1] );
 // printf("%d\n",rec[1][n-1] );
                                                           #include<stdio.h>
 // printf("%d\n",rec[2][n-3] );
                                                           #include<queue>
Hilbert Order
                                                           int main()
                                                           {
// maybe use B = n / sqrt(q)
                                                               int n, t;
inline int64_t hilbertOrder(int x, int y, int pow = 21,
                                                               long long ans = 0;
  int rotate = 0) {
                                                               std::priority_queue<int> Q;
   if(pow == 0) return 0;
                                                               scanf("%d%d", &n, &t);
   int hpow = 1 << (pow-1);</pre>
                                                               Q.push(t);
   int seg = (x < hpow) ? (
                                                               for(int i=1; i<n; i++)</pre>
       (y < hpow) ? 0 : 3
   ):(
                                                                  scanf("%d", &t); t-=i;
       (y < hpow) ? 1 : 2
                                                                  Q.push(t);
   );
                                                                  if(Q.top() > t)
   seg = (seg + rotate) & 3;
                                                                  {
   const int rotateDelta[4] = \{3, 0, 0, 1\};
                                                                      ans += Q.top() - t;
   int nx = x & (x \hat{p}), ny = y & (y \hat{p});
                                                                      Q.pop();
   int nrot = (rotate + rotateDelta[seg]) & 3;
                                                                      Q.push(t);
   int64_t subSquareSize = int64_t(1) << (2*pow - 2);</pre>
                                                                  }
   int64_t ans = seg * subSquareSize;
   int64_t add = hilbertOrder(nx, ny, pow-1, nrot);
                                                               printf("%11d", ans);
   ans += (seg == 1 || seg == 2) ? add : (subSquareSize
                                                               return 0;
      - add - 1);
   return ans;
                                                           Fast IO
Modular Factorial
                                                           #define pc(x) putchar_unlocked(x)
                                                           #define gc(x) getchar_unlocked(x)
// Compute (1*2*...*(p-1)*1*(p+1)*(p+2)*..*n) % p
// in O(p*lg(n))
                                                           inline void scan_int(int &x){
                                                               register int c = gc();
int factmod(int n, int p){
                                                               x = 0;
   int ans = 1;
                                                               int neg = 0;
   while(n > 1){
                                                               for(; ((c < '0' || c > '9') && c != '-'); c = gc());
       for(int i = 2; i <= n % p; i++)
                                                               if(c == '-'){
          ans = (ans * i) % p;
                                                                  neg = 1;
      n /= p;
                                                                  c = gc();
       if(n \% 2) ans = p - ans;
   }
                                                               for(; c >= '0' && c <= '9'; c = gc())
   return ans % p;
                                                                  x = (x << 1) + (x << 3) + c - '0';
}
                                                               if(neg) x = -x;
                                                           }
int fac_pow(int n, int p){
   int ans = 0;
                                                           inline void print_int(int n){
   while(n) n \neq p, ans += n;
                                                               int rev = 0, count = 0, neg;
   return ans;
                                                               if(n == 0){
                                                                  pc('0');
                                                                  return;
int C(int n, int k, int p){
   if(fac_pow(n, p) > fac_pow(n-k, p) + fac_pow(k, p))
                                                               if(n < 0) n = -n, neg = 1;
       return 0;
                                                               while(n % 10 == 0) count++, n /= 10;
   int tmp = factmod(k, p) * factmod(n-k, p);
                                                               for(rev = 0; n != 0; n /= 10)
   return (f_exp(tmp, p-2, p) * factmod(n, p)) % p;
                                                                  rev = (rev << 3) + (rev << 1) + n % 10;
                                                               if(neg) pc('-');
Enumarating all submasks of a bitmask
                                                               while(rev != 0) pc(rev % 10 + '0'), rev /= 10;
                                                               while(count--) pc('0');
// loop through all submask of a given bitmask
                                                               pc('\n');
// it does not include mask 0
                                                           }
for(int sub = mask; sub; sub = (sub-1)&mask){
```

```
inline void print_string(char *str){
   while(*str) pc(*str++);
   pc('\n');
}
Big int
 ########################### THE BIG INT
   ##############################
const int base = 1000000000;
const int base_digits = 9;
struct bigint {
   vector<int> a;
   int sign;
   /*<arpa>*/
   int size(){
      if(a.empty())return 0;
      int ans=(a.size()-1)*base_digits;
      int ca=a.back();
      while(ca)
          ans++, ca/=10;
      return ans;
   bigint operator ^(const bigint &v){
      bigint ans=1,a=*this,b=v;
      while(!b.isZero()){
          if(b%2)
             ans*=a;
          a*=a,b/=2;
      }
      return ans;
   }
   string to_string(){
      stringstream ss;
      ss << *this;
      string s;
      ss >> s;
      return s
   }
   int sumof(){
      string s = to_string();
      int ans = 0;
      for(auto c : s) ans += c - '0';
      return ans;
   /*</arpa>*/
   bigint():
      sign(1) {
   bigint(long long v) {
      *this = v;
   bigint(const string &s) {
      read(s);
   }
   void operator=(const bigint &v) {
      sign = v.sign;
      a = v.a;
   }
   void operator=(long long v) {
      sign = 1;
```

```
a.clear();
   if (v < 0)
       sign = -1, v = -v;
   for (; v > 0; v = v / base)
       a.push_back(v % base);
}
bigint operator+(const bigint &v) const {
   if (sign == v.sign) {
       bigint res = v;
       for (int i = 0, carry = 0; i < (int) \max(a.
         size(), v.a.size()) || carry; ++i) {
          if (i == (int) res.a.size())
              res.a.push_back(0);
          res.a[i] += carry + (i < (int) a.size() ?
             a[i] : 0);
          carry = res.a[i] >= base;
          if (carry)
              res.a[i] -= base;
       }
       return res;
   }
   return *this - (-v);
}
bigint operator-(const bigint &v) const {
   if (sign == v.sign) {
       if (abs() >= v.abs()) {
          bigint res = *this;
          for (int i = 0, carry = 0; i < (int) v.a.
             size() || carry; ++i) {
              res.a[i] -= carry + (i < (int) v.a.size
                () ? v.a[i] : 0);
              carry = res.a[i] < 0;
              if (carry)
                 res.a[i] += base;
          }
          res.trim():
          return res;
       }
       return -(v - *this);
   return *this + (-v);
}
void operator*=(int v) {
   if (v < 0)
       sign = -sign, v = -v;
   for (int i = 0, carry = 0; i < (int) a.size() ||</pre>
     carry; ++i) {
       if (i == (int) a.size())
          a.push_back(0);
       long long cur = a[i] * (long long) v + carry;
       carry = (int) (cur / base);
       a[i] = (int) (cur \% base);
       //asm("divl %%ecx" : "=a"(carry), "=d"(a[i])
         : "A"(cur), "c"(base));
   }
   trim();
}
bigint operator*(int v) const {
   bigint res = *this;
   res *= v;
   return res;
}
```

```
void operator*=(long long v) {
   if (v < 0)
       sign = -sign, v = -v;
   for (int i = 0, carry = 0; i < (int) a.size() ||</pre>
     carry; ++i) {
       if (i == (int) a.size())
          a.push_back(0);
       long long cur = a[i] * (long long) v + carry;
       carry = (int) (cur / base);
       a[i] = (int) (cur % base);
       //asm("divl %%ecx" : "=a"(carry), "=d"(a[i])
         : "A"(cur), "c"(base));
   trim();
}
bigint operator*(long long v) const {
   bigint res = *this;
   res *= v;
   return res;
}
friend pair<bigint, bigint> divmod(const bigint &a1,
   const bigint &b1) {
   int norm = base / (b1.a.back() + 1);
   bigint a = a1.abs() * norm;
   bigint b = b1.abs() * norm;
   bigint q, r;
   q.a.resize(a.a.size());
   for (int i = a.a.size() - 1; i >= 0; i--) {
      r *= base;
       r += a.a[i];
      int s1 = r.a.size() <= b.a.size() ? 0 : r.a[b</pre>
         .a.size()];
       int s2 = r.a.size() <= b.a.size() - 1 ? 0 : r</pre>
         .a[b.a.size() - 1];
       int d = ((long long) base * s1 + s2) / b.a.
        back();
       r -= b * d;
       while (r < 0)
          r += b, --d;
       q.a[i] = d;
   }
   q.sign = a1.sign * b1.sign;
   r.sign = a1.sign;
   q.trim();
   r.trim();
   return make_pair(q, r / norm);
bigint operator/(const bigint &v) const {
   return divmod(*this, v).first;
bigint operator%(const bigint &v) const {
   return divmod(*this, v).second;
void operator/=(int v) {
   if (v < 0)
       sign = -sign, v = -v;
   for (int i = (int) a.size() - 1, rem = 0; i >= 0;
       --i) {
       long long cur = a[i] + rem * (long long) base
```

```
a[i] = (int) (cur / v);
       rem = (int) (cur % v);
   }
   trim();
}
bigint operator/(int v) const {
   bigint res = *this;
   res /= v;
   return res;
int operator%(int v) const {
   if (v < 0)
       v = -v;
   int m = 0;
   for (int i = a.size() - 1; i >= 0; --i)
       m = (a[i] + m * (long long) base) % v;
   return m * sign;
void operator+=(const bigint &v) {
   *this = *this + v;
void operator-=(const bigint &v) {
   *this = *this - v;
void operator*=(const bigint &v) {
   *this = *this * v;
void operator/=(const bigint &v) {
   *this = *this / v;
bool operator<(const bigint &v) const {</pre>
   if (sign != v.sign)
       return sign < v.sign;</pre>
   if (a.size() != v.a.size())
       return a.size() * sign < v.a.size() * v.sign;</pre>
   for (int i = a.size() - 1; i >= 0; i--)
       if (a[i] != v.a[i])
           return a[i] * sign < v.a[i] * sign;</pre>
   return false;
}
bool operator>(const bigint &v) const {
   return v < *this;</pre>
bool operator<=(const bigint &v) const {</pre>
   return !(v < *this);</pre>
bool operator>=(const bigint &v) const {
   return !(*this < v);</pre>
bool operator==(const bigint &v) const {
   return !(*this < v) && !(v < *this);</pre>
bool operator!=(const bigint &v) const {
   return *this < v || v < *this;</pre>
}
void trim() {
   while (!a.empty() && !a.back())
       a.pop_back();
   if (a.empty())
       sign = 1;
```

```
}
bool isZero() const {
   return a.empty() || (a.size() == 1 && !a[0]);
bigint operator-() const {
   bigint res = *this;
   res.sign = -sign;
   return res;
bigint abs() const {
   bigint res = *this;
   res.sign *= res.sign;
   return res;
}
long longValue() const {
   long long res = 0;
   for (int i = a.size() - 1; i >= 0; i--)
      res = res * base + a[i];
   return res * sign;
}
friend bigint gcd(const bigint &a, const bigint &b)
   return b.isZero() ? a : gcd(b, a % b);
}
friend bigint lcm(const bigint &a, const bigint &b)
  {
   return a / gcd(a, b) * b;
void read(const string &s) {
   sign = 1;
   a.clear();
   int pos = 0;
   while (pos < (int) s.size() && (s[pos] == '-' ||</pre>
     s[pos] == '+')) {
       if (s[pos] == '-')
          sign = -sign;
       ++pos;
   for (int i = s.size() - 1; i >= pos; i -=
     base_digits) {
       int x = 0;
       for (int j = max(pos, i - base_digits + 1); j
          <= i; j++)
          x = x * 10 + s[j] - '0';
       a.push_back(x);
   trim();
friend istream& operator>>(istream &stream, bigint &
  v) {
   string s;
   stream >> s;
   v.read(s);
   return stream;
friend ostream& operator<<(ostream &stream, const</pre>
  bigint &v) {
   if (v.sign == -1)
       stream << '-';
```

```
stream << (v.a.empty() ? 0 : v.a.back());</pre>
   for (int i = (int) \ v.a.size() - 2; i >= 0; --i)
       stream << setw(base_digits) << setfill('0')</pre>
         << v.a[i]:
   return stream;
}
static vector<int> convert_base(const vector<int> &a
  , int old_digits, int new_digits) {
   vector<long long> p(max(old_digits, new_digits) +
       1);
   p[0] = 1;
   for (int i = 1; i < (int) p.size(); i++)</pre>
       p[i] = p[i - 1] * 10;
   vector<int> res;
   long long cur = 0;
   int cur_digits = 0;
   for (int i = 0; i < (int) a.size(); i++) {</pre>
       cur += a[i] * p[cur_digits];
       cur_digits += old_digits;
       while (cur_digits >= new_digits) {
           res.push_back(int(cur % p[new_digits]));
           cur /= p[new_digits];
           cur_digits -= new_digits;
       }
   }
   res.push_back((int) cur);
   while (!res.empty() && !res.back())
       res.pop_back();
   return res;
typedef vector<long long> vll;
static vll karatsubaMultiply(const vll &a, const vll
   &b) {
   int n = a.size();
   vll res(n + n);
   if (n <= 32) {
       for (int i = 0; i < n; i++)
           for (int j = 0; j < n; j++)
              res[i + j] += a[i] * b[j];
       return res;
   }
   int k = n \gg 1;
   vll a1(a.begin(), a.begin() + k);
   vll a2(a.begin() + k, a.end());
   vll b1(b.begin(), b.begin() + k);
   vll b2(b.begin() + k, b.end());
   vll a1b1 = karatsubaMultiply(a1, b1);
   vll a2b2 = karatsubaMultiply(a2, b2);
   for (int i = 0; i < k; i++)
       a2[i] += a1[i];
   for (int i = 0; i < k; i++)
       b2[i] += b1[i];
   vll r = karatsubaMultiply(a2, b2);
   for (int i = 0; i < (int) a1b1.size(); i++)</pre>
       r[i] -= a1b1[i];
    for (int i = 0; i < (int) a2b2.size(); i++)</pre>
       r[i] -= a2b2[i];
   for (int i = 0; i < (int) r.size(); i++)</pre>
       res[i + k] += r[i];
```

```
for (int i = 0; i < (int) a1b1.size(); i++)</pre>
         res[i] += a1b1[i];
      for (int i = 0; i < (int) a2b2.size(); i++)</pre>
         res[i + n] += a2b2[i];
      return res;
   }
   bigint operator*(const bigint &v) const {
      vector<int> a6 = convert_base(this->a,
        base_digits, 6);
      vector<int> b6 = convert_base(v.a, base_digits,
      vll a(a6.begin(), a6.end());
      vll b(b6.begin(), b6.end());
      while (a.size() < b.size())</pre>
         a.push_back(0);
      while (b.size() < a.size())</pre>
         b.push_back(0);
      while (a.size() & (a.size() - 1))
         a.push_back(0), b.push_back(0);
      vll c = karatsubaMultiply(a, b);
      bigint res;
      res.sign = sign * v.sign;
      for (int i = 0, carry = 0; i < (int) c.size(); i</pre>
         long long cur = c[i] + carry;
         res.a.push_back((int) (cur % 1000000));
         carry = (int) (cur / 1000000);
      res.a = convert_base(res.a, 6, base_digits);
      res.trim();
      return res;
   }
};
```

#### **Knapsack Bounded with Cost**

```
// menor custo para conseguir peso ate M usando N tipos
  diferentes de elementos, sendo que o i-esimo elemento
  pode ser usado b[i] vezes, tem peso w[i] e custo c[i]
// O(N * M)
int b[N], w[N], c[N];
MinQueue Q[M]
int d[M] //d[i] = custo minimo para conseguir peso i
for(int i = 0; i \le M; i++) d[i] = i? oo : 0;
for(int i = 0; i < N; i++){
   for(int j = 0; j < w[i]; j++)
       Q[j].clear();
   for(int j = 0; j <= M; j++){
      q = Q[j \% w[i]];
       if(q.size() >= q) q.pop();
      q.add(c[i]);
      q.push(d[j]);
      d[j] = q.getmin();
   }
```

#### Burnside's Lemma

Let  $(G, \oplus)$  be a finite group that acts on a set X. It should hold that  $e_g * x = x$  and  $g_1 * (g_2 * x) = (g_1 \oplus g_2) * x$ ,  $\forall x \in X, g_1, g_2 \in G$ . For each  $g \in G$  let  $X^g = \{x \in X \mid g * x = x\}$ . The number of

orbits its given by:  $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$ 

#### Wilson's Theorem

 $(n-1)! = -1 \mod n \iff n \text{ is prime}$ 

#### **Fibonacci**

- $F_{n-1}F_{n+1} F_n^2 = (-1)^n$
- $F_{n+k} = F_k F_{n+1} + F_{k-1} F_n$
- $GCD(F_n, F_m) = F_{GCD(n,m)}$
- $F_n = \frac{(\frac{1+\sqrt{5}}{2})^n (\frac{1-\sqrt{5}}{2})^n}{\sqrt{5}}$

#### Kirchhoff's Theorem

Laplacian matrix is L = D - A, where D is a diagonal matrix with vertex degrees on the diagonals and A is adjacency matrix.

The number of spanning trees is any cofactor of L. i-th cofactor is determinant of the matrix gotten by removing i-th row and column of L.

#### Multigraphs

In D[i][i] all loops are excluded. A[i][j] = number of edges from i to j.

#### Directed multigraphs

D[i][i] = indegree of i minus the number of loops at i. A[i][j] = number of edges from i to j.

The number of oriented spanning trees rooted at a vertex i is the determinant of the matrix gotten by removing the ith row and column of L.

#### **Edge coloring**

```
Data: A graph G

Result: A proper coloring c of the edges of G

Let U := E(G);

while U \neq \emptyset do

Let (u,v) be any edge in U;

Let F[1:k] be a maximal fan of u starting at F[1]=v;

Let c be a color that is free on u and d be a color that is free on F[k];

Invert the cd_u path;

Let w \in V(G) be such that w \in F, F' = [F[1]...w] is a fan and d is free on w;

Rotate F' and set C(u,w)=d;

U := U - (u,v);

end
```

#### Notes

When we repeat something and each time we have probability p to succeed then the expected number or tries is  $\frac{1}{p}$ , till we succeed.