## Zipf's Law and informativeness

- Remember Zipf's Law? It describes the distribution of word frequencies found in natural text.
- A key feature that we wish to endow IR systems with is the ability to focus on informative words that carry meaning, and ignore ones that don't. Empirically we know that high frequency words carry far less meaning that those words on the long-tail of the word frequency distribution.
- Given this, a reasonable goal is to build IR systems that are sensitive to low frequency words, and insensitive to high frequency ones.

English		German		Spanish		Italian		Dutch	
1 the	61,847	1 der	7,377,879	1 que	32,894	1 non	25,757	1 <b>de</b>	4,770
2 <b>of</b>	29,391	2 die	7,036,092	2 <b>de</b>	32,116	2 <b>di</b>	22,868	2 <b>en</b>	2,709
3 and	26,817	3 und	4,813,169	3 <b>no</b>	29,897	3 <b>che</b>	22,738	3 het/'t	2,469
4 <b>a</b>	21,626	4 <b>in</b>	3,768,565	4 <b>a</b>	22,313	4 è	18,624	4 van	2,259
5 in	18,214	5 den	2,717,150	5 <b>la</b>	21,127	5 <b>e</b>	17,600	5 ik	1,999
6 <b>to</b>	16,284	6 von	2,250,642	6 <b>el</b>	18,112	6 <b>la</b>	16,404	6 te	1,935
7 <b>it</b>	10,875	7 <b>zu</b>	1,992,268	7 <b>es</b>	16,620	7 <b>i</b> l	14,765	7 dat	1,875
8 <b>is</b>	9,982	8 das	1,983,589	8 <b>y</b>	15,743	8 <b>un</b>	14,460	8 die	1,807
9 <b>to</b>	9,343	9 mit	1,878,243	9 en	15,303	9 a	13,915	9 in	1,639
10 was	9.236	10 sich	1.680.106	10 <b>lo</b>	14.010	10 per	10.501	10 een	1.637

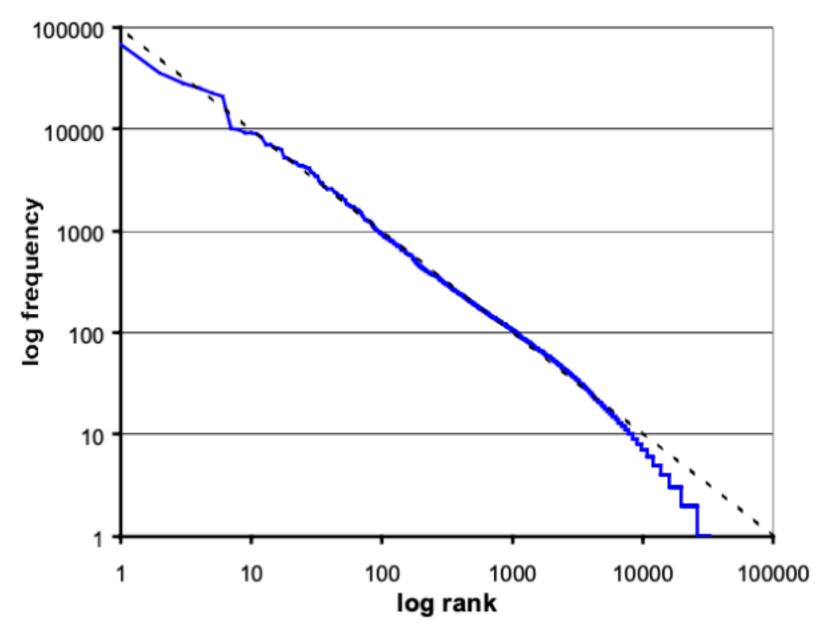


Figure 2 Zipf curve for the unigrams extracted from the 1 million words of the Brown corpus

## TF-IDF weighting

- TF stands for term frequency
- IDF stands for inverse document frequency
- Given a collection of documents, D, a word, w, and a document from the collection,  $d \in D$ , the relevance score,  $W_{d,w}$ , assigned to that word-document pair is shown below:

$$W_{d,w} = (1 + \log f_{D,w}) \cdot \log \frac{|D|}{f_{d,w}}$$

where  $f_{d,w}$  = number of documents containing term w  $f_{D,w}$  = frequency of term w in corpus D

- There are several variants of this weighting scheme, the above is most popular.
- TF-IDF score for a query (q) document (d) pair:  $score_{q,d} = \sum_{w \in q \cap d} W_{d,w}$