## Algorithm for the skip gram word2vec model

### let $\mathbf{U} \in \mathbb{R}^{K imes N}$ be our center word embeddings corresponding to $\mathbf{x}_{\scriptscriptstyle w}$

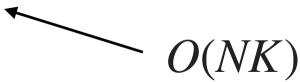
 $\forall (\mathbf{x}_w, \mathbf{x}_c) \in D \text{ do:}$ 

 $\mathbf{U}_{w} \leftarrow \mathbf{U}_{w} - \eta \nabla_{\mathbf{U}_{w}} NLL$ 

set  $\mathbf{u}_{\scriptscriptstyle W} = \mathbf{U}_{\scriptscriptstyle W}$  via the non-zero indice of our one-hot center word  $\mathbf{x}_{\scriptscriptstyle W}$ 

cross entropy loss:  $\mathbf{L}(U, V | \mathbf{x}_w, \mathbf{x}_c) = -\mathbf{x}_c \cdot \log p(\mathbf{x}_c | \mathbf{x}_w; \mathbf{U}, \mathbf{V})$ 

#### gradient descent:



### let $\mathbf{V} \in \mathbb{R}^{K imes N}$ be our center word embeddings corresponding to $\mathbf{x}_c$

compute inner product between  $\mathbf{u}_w$  and all context vectors  $\mathbf{V}:\mathbf{u}_w\cdot\mathbf{V}\in\mathbb{R}^N$ 

 $\exp(\mathbf{u}_{w}\cdot\mathbf{V})$ 

 $\sum_{i=1}^{N} \exp(\mathbf{u}_{w} \cdot \mathbf{V})_{j}$ 

compute probability over all context words given center word:  $\frac{chp(\mathbf{u}_w - \mathbf{v})}{dt}$ 

gradients:  $\nabla_{U_w} NLL = \mathbf{V} \cdot (P_{\mathbf{x}_c | \mathbf{x}_w} - \mathbf{x}_c)^T \in \mathbb{R}^K$ 

$$\nabla_{V} NLL = \mathbf{u}_{w} \cdot \left( P_{\mathbf{x}_{c} | \mathbf{x}_{w}} - \mathbf{x}_{c} \right) \in \mathbb{R}^{K \times N}$$

$$\mathbf{V} \leftarrow \mathbf{V} - \eta \, \nabla_{\mathbf{V}} NLL$$

encodes distributional hypothesis

#### only $w^{th}$ row of ${f U}$ gets updated

#### entire V gets updated

## Algorithm for the skip gram word2vec model

let  $\mathbf{U} \in \mathbb{R}^{K \times N}$  be our center word embeddings corresponding to  $\mathbf{x}_w$ 

let  $\mathbf{V} \in \mathbb{R}^{K \times N}$  be our center word embeddings corresponding to  $\mathbf{x}_c$ 

$$\forall (\mathbf{x}_w, \mathbf{x}_c) \in D \text{ do:}$$

set  $\mathbf{u}_{w} = \mathbf{U}_{w}$  via the non-zero indice of our one-hot center word  $\mathbf{x}_{w}$ 

compute inner product between  $\mathbf{u}_w$  and all context vectors  $\mathbf{V}:\mathbf{u}_w\cdot\mathbf{V}\in\mathbb{R}^N$ 

compute probability over all context words given center word :  $\frac{\exp(\mathbf{u}_w \cdot \mathbf{V})}{\sum_{j=1}^N \exp(\mathbf{u}_w \cdot \mathbf{V})_j}$ 

cross entropy loss:  $\mathbf{L}(U, V | \mathbf{x}_w, \mathbf{x}_c) = -\mathbf{x}_c \cdot \log p(\mathbf{x}_c | \mathbf{x}_w; \mathbf{U}, \mathbf{V})$ 

gradients:  $\nabla_{U_w} NLL = \mathbf{V} \cdot (P_{\mathbf{x}_c | \mathbf{x}_w} - \mathbf{x}_c)^T \in \mathbb{R}^K$ 

 $\nabla_{V} NLL = \mathbf{u}_{w} \cdot \left( P_{\mathbf{x}_{c} | \mathbf{x}_{w}} - \mathbf{x}_{c} \right) \in \mathbb{R}^{K \times N}$ 

gradient descent:  $\mathbf{U}_w \leftarrow \mathbf{U}_w - \eta \nabla_{\mathbf{U}_w} NLL$  only  $w^{th}$  row of  $\mathbf{U}$  gets updated

 $\mathbf{V} \leftarrow \mathbf{V} - \eta \nabla_{\mathbf{V}} NLL$  entire  $\mathbf{V}$  gets updated

encodes

distributional

hypothesis

# For large N, we need to avoid the partition function

- The approach on the previous slide is the preferred method when N is a manageable size, say  $N < 10^5$ .
- When  $N>10^6$ , the partition function (denominator of the softmax function) becomes prohibitively expensive to compute due the  ${\rm O}(NK)$  scaling.
- There are several approaches to get around having to compute the (full) partition function:
  - Hierarchical softmax
  - Importance sampling (IS)
  - Adaptive IS
  - Target sampling
  - Noise contrastive estimation (NCE)
  - Negative sampling

 $\sim 10 - 100x$  speedup