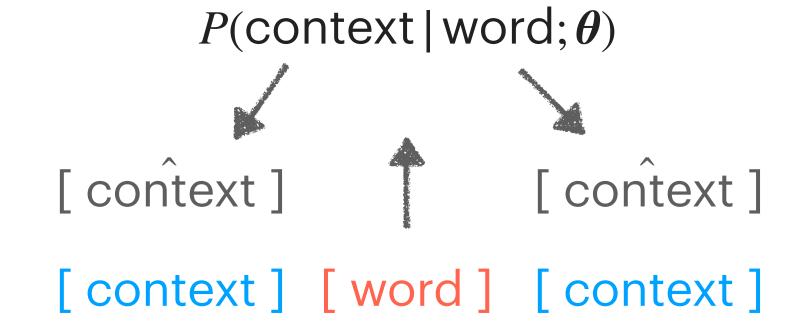
The skip gram model



Example: the quick brown fox jumped over the lazy dog
$$\mathbf{X}_{t-c}$$
 ... \mathbf{X}_{t} ... \mathbf{X}_{t+c}

Learning problem:
$$\hat{\boldsymbol{\theta}} = \arg\max_{\boldsymbol{\theta}} \prod_{t=1}^{T} \prod_{-c \leq j \leq c, j \neq 0} \mathbf{x}_{t+j} \cdot p(\mathbf{x}_{t+j} | \mathbf{x}_t; \boldsymbol{\theta})$$
$$= \arg\min_{\boldsymbol{\theta}} - \sum_{t=1}^{T} \sum_{-c \leq j \leq c, j \neq 0} \mathbf{x}_{t+j} \cdot \log p(\mathbf{x}_{t+j} | \mathbf{x}_t; \boldsymbol{\theta})$$

where
$$T = \text{corpus length}$$

$$c = \text{context window}$$

$$N = \text{vocabulary size}$$

$$\mathbf{x} \in \{0,1\}^N$$

$$\boldsymbol{\theta} = \text{parameterization}$$

Word2Vec: learn a feature representation that preserves semantic relationships between words based on distance

