EENG304L Lab 4 Report

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1 MOSFET Linear Amplifier Analysis

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1.1 Initial Parameters

Parameter	Purpose	Value
\overline{W}	Channel Width	$40~\mu\mathrm{m}$
$\mid L$	Channel Length	$1.6~\mu\mathrm{m}$
K'_n	Process Transconductance	$50 \ \mu \text{A/V}^2$
V_{to}	Threshold Voltage	0.5 V
C_{ox}	Gate Oxide Capacitance	2.3 mF/m^2
λ	Channel Length Modulation	0.0625 V^{-1}
$ \gamma $	Body Effect Parameter	$0.6 \text{ V}^{1/2}$
$ \phi $	Surface Potential	0.8 V

1.2 Circuit Conditions

Parameter	Purpose	Value
I_{BB}	DC Bias Current	$250~\mu\mathrm{A}$
$\mid V_{DD} \mid$	DC Supply Voltage	5 V
V_{BB}	DC Bias Voltage	2.5 V
R	Resistance	$10~\mathrm{k}\Omega$

Before executing any code, make sure to have all necesarry packages installed, This can be run from within using the "Run All" button.

Note: you may need to restart the kernel to use updated packages.

```
[1]: W = 40e-6

L = 1.6e-6

KN_PRIME = 50e-6

V_TO = 0.5

C_OX = 2.3e-3

I_BB = 250e-6

V_DD = 5
```

1.3 Equations

1.3.1 Channel Length Modulation Parameter

$$\lambda(L) = \frac{0.1 \mu m \cdot V^{-1}}{L}$$

1.3.2 MOSFET Saturation Region Current

$$I_{D} = \frac{1}{2} K_{n}^{\prime} \frac{W}{L} (V_{GS} - V_{to})^{2} (1 + \lambda V_{DS})$$

Where: - I_D is biased by I_{BB} at 250 A - We need to solve for V_{GS}

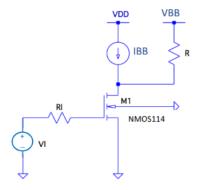


Figure 1.

IBB = 250 μA (DC bias current) VDD = 5V (DC supply voltage)

VBB = 2.5V (DC bias voltage)

 $R = 10 \text{ k}\Omega$

N - 10 K22

 $RI = 20 k\Omega$

 $W/L = 40 \mu m/1.6 \mu m$

1.4 Calculations

1.4.1 Solving for Channel Length Modulation

0.0625

1.4.2 Threshold Voltage (V_{TH})

1.4.3 Given Parameters

Parameter	Purpose	Value
V_{to}	Threshold Voltage	0.5 V
γ (Gamma)	Body Effect Parameter	$0.6 \text{ V}^{1/2}$
ϕ (phi)	Surface Potential	0.8 V
V_{SB}	Source-Bulk Voltage	0 V

1.4.4 Circuit Analysis

Since both the Source and Bulk are connected to ground: - Source voltage = 0V - Bulk voltage = 0V - Therefore, $V_{SB}=V_S-V_B=0$ V

Similarly, to solve the Drain and Bulk - Drain voltage = 2.5 V - Bulk voltage = 0V - Therefore, $V_{DB}=V_D-V_B=2.5~\rm V$

1.4.5 Threshold Voltage Equation

$$V_{TH} = V_{to} + \gamma(\sqrt{\phi + V_{SB}} - \sqrt{\phi})$$

```
[3]: import math

GAMMA = 0.6  # V^(1/2)

PHI = 0.8  # V

V_SB = 0  # V

V_DB = 2.5  # V

# Calculate Vth

Vth = V_TO + GAMMA * (math.sqrt(PHI + V_SB) - math.sqrt(PHI))

print(f"VTH = {Vth:.1f} V")
```

VTH = 0.5 V

Given that $\lambda = 0.0625 \text{ V}^{-1}$, and $V_{TH} = 0.5V$ we can solve for V_{GS} using the saturation region equation:

1.4.6 Solving for V_{GS} using the saturation region equation

```
[4]: # Calculate beta term
beta = KN_PRIME * (W/L)
Id = I_BB

# Solve for Vgs using saturation equation
# ID = (1/2) * beta * (Vgs - Vto)^2 * (1 + lambda * Vds)
term1 = 2 * Id / (beta * (1 + lambda_val * V_DS))
Vgs = math.sqrt(term1) + Vth
```

```
print(f"VGS = {Vgs:.3f} V")
```

VGS = 1.088 V

1.4.7 Small Signal Parameters Calculation

Given Values:

Parameter	Purpose	Value
V_{GS}	Gate-Source Voltage	1.088 V
V_{TH}	Threshold Voltage	$0.5~\mathrm{V}$

Small Signal Equations Transconductance:

$$g_m = \frac{2I_D}{V_{GS} - V_{TH}}$$

Output Conductance:

$$g_{ds} = \lambda \cdot I_D$$

Gate-to-Source Capacitance:

$$C_{gs} = \frac{2}{3} \cdot C_{ox} \cdot W \cdot L$$

```
[5]: # Calculate gm
gm = (2 * Id) / (Vgs - Vth)

# Calculate gds
gds = lambda_val * Id

# Calculate Cgs
Cgs = (2/3) * C_OX * W * L

print(f"gm = {gm*1e3:.3f} mS")
print(f"gds = {gds*1e6:.3f} µS")
print(f"Cgs = {Cgs*1e15:.3f} fF")
```

```
gm = 0.850 mS
gds = 15.625 \muS
Cgs = 98.133 fF
```

As expected, the the analysis of the MOSFET parameters yielded the following results:

Parameter	Purpose	Value
g_m	Transconductance	$850~\mu\mathrm{S}$
g_{ds}	Output Conductance	$15.625~\mu\mathrm{S}$
C_{gs}	Gate-Source Capacitance	98.133 fF

1.5 Capacitance Analysis

1.5.1 Device Parameters

The following parameters are required for extrinsic capacitance calculations:

Parameter	Purpose	Value
CGDO, CGSO	Gate-Drain/Source Overlap Capacitance	$0.5~\mathrm{fF}/\mu\mathrm{m}$
CJ	Zero-Bias Area Capacitance	$0.1 \text{ fF}/\mu\text{m}^2$
CJSW	Zero-Bias Sidewall Capacitance	$0.5~\mathrm{fF}/\mu\mathrm{m}$
PB	Junction Potential	0.95 V
PBSW	Junction Potential Sidewall	0.95 V
MJ	Area Junction Grading Coefficient	0.5
MJSW	Sidewall Junction Grading Coefficient	0.33
HDIF	Half Length of S/D Diffusion	$1.5~\mu\mathrm{m}$

The following equations are used to determine the intermediate values:

- 1. Diffusion Length:
 - $L_{DIF} = 2 \times HDIF = 2 \times 1.5 \ \mu \text{m} = 3 \ \mu \text{m}$
- 2. Source/Drain Areas:
- 3. Source/Drain Perimeters:
 - $P_d = P_s = 2 \times L_{DIF} + W = 2 \times 3 \ \mu\text{m} + 40 \ \mu\text{m} = 46 \ \mu\text{m}$

```
[6]: HDIF = 1.5e-6  # m
    CGDO = CGSO = 2e-14  # F/m
    CJ = 0.1e-15 * 1e12  # F/m²
    CJSW = 0.5e-15 * 1e6  # F/m
    PB = PBSW = 0.95  # V
    MJ = 0.5
    MJSW = 0.33

# Calculate intermediate values
LDIF = 2 * HDIF  # meters
Ad = As = 2 * HDIF * W  # Area of drain/source in m²
Pd = Ps = 2 * LDIF + W  # Perimeter of drain/source in m

print(f"LDIF = {LDIF*1e6:.1f} m")
    print(f"Ad = As = {Ad*1e12:.1f} m²")
    print(f"Pd = Ps = {Pd*1e6:.1f} m")
```

```
LDIF = 3.0 m
Ad = As = 120.0 m<sup>2</sup>
Pd = Ps = 46.0 m
```

Now knowing that the drain and source areas (A_d, A_s) are both 120 m² and their perimeters (P_d, P_s) are both 46 m, we can solve for the drain-bulk (C_{db}) and source-bulk (C_{sb})

1.5.2 Junction Equations

The drain-bulk and source-bulk junction capacitances are given by:

1. Drain-Bulk Capacitance:

$$C_{db} = \frac{A_D \cdot CJ}{(1 + \frac{V_{DB}}{PB})^{MJ}} + \frac{P_D \cdot CJSW}{(1 + \frac{V_{DB}}{PBSW})^{MJSW}}$$

2. Source-Bulk Capacitance:

$$C_{sb} = \frac{A_S \cdot CJ}{(1 + \frac{V_{SB}}{PB})^{MJ}} + \frac{P_S \cdot CJSW}{(1 + \frac{V_{SB}}{PBSW})^{MJSW}}$$

1.5.3 Known Values

Parameter	Purpose	Value
A_D, A_S	Drain/Source Area	$120 \; \mu {\rm m}^2$
P_D, P_S	Drain/Source Perimeter	$46~\mu\mathrm{m}$
V_{DB}	Drain-Bulk Voltage	2.5V
V_{SB}	Source-Bulk Voltage	0 V

Junction Capacitance Results:

Csb = 35.000 fFCdb = 21.325 fF

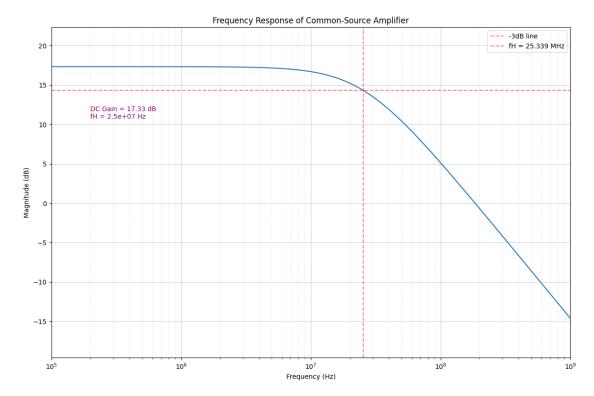
1.6 Amplifier DC Gain and Bandwidth Analysis

After calculating the small-signal parameters and extrinsic capacitances, we can now determine the amplifier's DC gain and bandwidth.

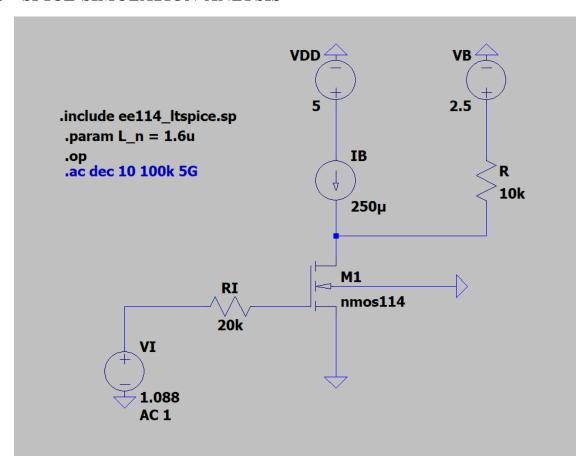
Key equations: - Output resistance:
$$r_o = \frac{1}{\lambda I_D}$$
 - DC Gain: $A_v = \frac{V_{out}}{V_{in}} = -g_m(r_o||R_L)$ - Unity gain frequency: $f_T = \frac{g_m}{2\pi C_{total}}$ - Bandwidth (Miller Approximation): $f_{-3dB} = \frac{1}{2\pi r_o(C_{gs} + C_{gd}(1 + gmr_o))}$ Where: - $C_{total} = C_{total} + C_{gd} + C_{gd} + C_{gd}$

```
[8]: import numpy as np
     import matplotlib.pyplot as plt
     # Calculate output resistance
     ro = 1 / (lambda_val * I_BB)
     # Calculate equivalent resistance
     R eq = (ro * R) / (ro + R)
     # Calculate DC gain
     gain_dc = -gm * R_eq
     gain_db = 20 * np.log10(abs(gain_dc))
     # Calculate capacitances
     Cgd_ov = CGDO * W # Gate-drain overlap capacitance
     Cgd = Cgd_ov # In saturation, intrinsic Cgd is negligible
     C_total = Cdb + Cgd + Cgs # Total capacitance affecting frequency response
     # Updated -3dB bandwidth formula
     fH_hand = 1 / (2 * np.pi * ro * (Cgs + Cgd*(1+abs(gain_dc)))) # Cutoff_{l}
      ⇔ frequency
     # Calculate unity gain frequency
     f_T = gm / (2 * np.pi * C_total)
     # Print results
     print(f"Output resistance (ro) = \{ro/1e3:.2f\} k\Omega")
     print(f"DC Gain = {gain_dc:.2f} V/V ({gain_db:.2f} dB)")
     print(f"Total output capacitance = {C_total*1e15:.2f} fF")
     print(f"-3dB Bandwidth = {fH hand/1e6:.3f} MHz")
     print(f"Unity gain frequency = {f_T/1e6:.2f} MHz")
     # Create frequency response plot
     f = np.logspace(5, 9, 1000) # 100kHz to 1GHz
     w = 2 * np.pi * f
     # Calculate frequency response using transfer function
     \# H(s) = Av / (1 + s/wp) \text{ where } wp = 2 * fH
     H = gain_dc / (1 + 1j * f/fH_hand)
     mag_db = 20 * np.log10(np.abs(H))
    plt.figure(figsize=(12, 8))
     plt.semilogx(f, mag_db)
     plt.grid(True, which='both')
     plt.xlabel('Frequency (Hz)')
```

Output resistance (ro) = $64.00~\rm k\Omega$ DC Gain = $-7.35~\rm V/V$ (17.33 dB) Total output capacitance = $119.46~\rm fF$ -3dB Bandwidth = $25.339~\rm MHz$ Unity gain frequency = $1132.58~\rm MHz$



1.7 SPICE SIMULATION ANLYSIS



```
[9]: from PyLTSpice import RawRead

# Read the simulation data
LTR = RawRead("./EENG304L Lab 4.raw")

# Get frequency and voltage data
f = LTR.get_trace('frequency')
Vo = LTR.get_trace('V(n003)')
freq = f.get_wave(0)
Vout = np.array(Vo.get_wave(0), dtype=complex)

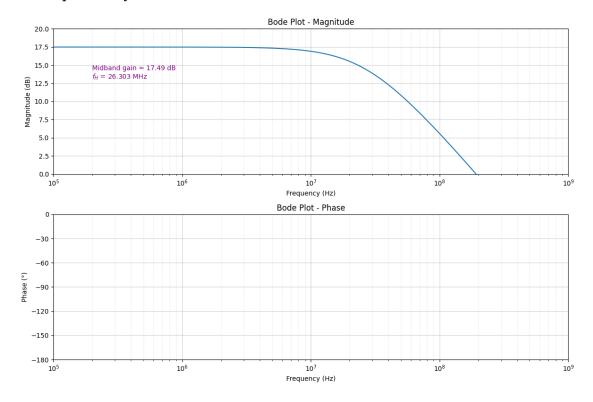
# Calculate magnitude in dB
mag = 20*np.log10(np.abs(Vout))
gain_db_spice = max(mag)

# Find -3dB frequency (cutoff)
cutoff_indices = np.where(mag <= gain_db_spice-3)
fH_spice = abs(freq[cutoff_indices[0][0]]) / 1e6 # Convert to MHz</pre>
```

```
# Print results
print(f"Midband gain: {gain_db_spice:.2f} dB")
print(f"High frequency cutoff: {fH_spice:.3f} MHz")
# Create Bode plot with adjusted figure size
fig, (ax1, ax2) = plt.subplots(2, 1, figsize=(12, 8))
# Magnitude plot with improved scaling
ax1.semilogx(freq, mag)
ax1.grid(True, which="both")
ax1.set_title("Bode Plot - Magnitude")
ax1.set_ylabel("Magnitude (dB)")
ax1.set_xlabel("Frequency (Hz)")
ax1.set_xlim(1e5, 1e9)
ax1.set_ylim(0, 20)
ax1.grid(True, which='minor', linestyle=':', alpha=0.4)
ax1.grid(True, which='major', linestyle='-', alpha=0.6)
# Add annotations in a better position
ax1.annotate(f'Midband gain = {gain_db_spice:.2f} dB\n$f_H$ = {fH_spice:.3f}_\_
 →MHz',
             xy=(2e5, 15), ha='left', va='top', color='purple')
# Phase plot with improved scaling
phase = np.angle(Vout, deg=True)
ax2.semilogx(freq, phase)
ax2.grid(True, which="both")
ax2.set_title("Bode Plot - Phase")
ax2.set_ylabel("Phase (°)")
ax2.set_xlabel("Frequency (Hz)")
ax2.set xlim(1e5, 1e9)
ax2.set_ylim(-180, 0)
ax2.set_yticks(np.arange(-180, 15, 30))
ax2.grid(True, which='minor', linestyle=':', alpha=0.4)
ax2.grid(True, which='major', linestyle='-', alpha=0.6)
plt.tight_layout()
plt.show()
Reading file with encoding utf_16_le
File contains 18 traces, reading 18
Binary RAW file with Normal access
Midband gain: 17.49 dB
High frequency cutoff: 26.303 MHz
/home/macbee280/anaconda3/envs/EENG304L/lib/python3.10/site-
```

packages/matplotlib/cbook.py:1709: ComplexWarning: Casting complex values to

real discards the imaginary part
 return math.isfinite(val)
/home/macbee280/anaconda3/envs/EENG304L/lib/python3.10/sitepackages/matplotlib/cbook.py:1345: ComplexWarning: Casting complex values to
real discards the imaginary part
 return np.asarray(x, float)



From our hand calculations we got a Cdb of 21.325fF which matches our SPICE analysis of Cbd

```
Name:
               m1
Model:
             nmos114
Id:
             2.50e-04
Vgs:
             1.09e+00
Vds:
             2.50e+00
Vbs:
             0.00e+00
Vth:
             5.00e-01
Vdsat:
             5.88e-01
Gm:
             8.50e-04
Gds:
             1.35e-05
Gmb:
             2.85e-04
Cbd:
             2.13e-14
Cbs:
             3.50e-14
             2.00e-14
Cgsov:
Cgdov:
             2.00e-14
Cqbov:
             0.00e+00
             9.82e-14
Cqs:
Cgd:
             0.00e+00
Cgb:
             0.00e+00
```

1.8 Error

```
[]: import pandas as pd
     # Hand Calculations
     gain_db_hand = 20 * np.log10(abs(gain_dc))
     fH_hand = 1 / (2 * np.pi * ro * (Cgs + Cgd*(1+abs(gain_dc))))
     C_total_hand = Cdb + Cgd + Cgs
     C_{total\_spice} = (2.13e-14 + 0 + 9.82e-14)
     # SPICE Model Values
     comparison = pd.DataFrame({
         'Parameter': ['Midband Gain (dB)', 'Cutoff Frequency (MHz)', 'Total⊔

Gapacitance (fF)'],
         'Hand Calculation': [gain_db_hand, fH_hand/1e6, C_total_hand*1e15],
         'SPICE': [gain_db_spice, fH_spice/1e6, C_total_spice*1e15]
     })
     # Calculate errors
     comparison['Absolute Error'] = abs(comparison['Hand Calculation'] -
      ⇔comparison['SPICE'])
     comparison['Relative Error (%)'] = (comparison['Absolute Error'] / ___
      ⇔comparison['SPICE']) * 100
     # Format the numbers to be more readable
     pd.options.display.float_format = '{:.3f}'.format
     print("Comparison between Hand Calculations and SPICE Results:\n")
```

```
print(comparison.to_string(index=False))

print("\nCapacitance Breakdown:")
print(f"Hand Calculations:")
print(f" - Cdb = {Cdb*1e15:.2f} fF")
print(f" - Cgd = {Cgd*1e15:.2f} fF")
print(f" - Cgs = {Cgs*1e15:.2f} fF")
print(f" Total = {C_total_hand*1e15:.2f} fF")
print(f"\nSPICE:")
print(f" - Cbd = {2.13e-14*1e15:.2f} fF")
print(f" - Cgd = {0:.2f} fF")
print(f" - Cgs = {9.82e-14*1e15:.2f} fF")
print(f" Total = {C_total_spice*1e15:.2f} fF")
```

Comparison between Hand Calculations and SPICE Results:

```
Parameter Hand Calculation SPICE Absolute Error Relative Error (%)

Midband Gain (dB) 17.328 17.490 0.162
0.925
Cutoff Frequency (MHz) 25.339 26.303 0.964
3.664
Total Capacitance (fF) 119.459 119.500 0.041
0.034
```

Capacitance Breakdown:

Hand Calculations:

- Cdb = 21.32 fF
- Cgd = 0.00 fF
- Cgs = 98.13 fF

Total = 119.46 fF

SPICE:

- Cbd = 21.30 fF
- Cgd = 0.00 fF
- Cgs = 98.20 fF

Total = 119.50 fF

1.8.1 Comparison between Hand Calculations and SPICE Results

Parameter	Hand Calculation	SPICE	Absolute Error	Relative Error (%)
Midband Gain (dB)	17.328	17.490	0.162	0.925
Cutoff Frequency (MHz)	25.339	26.303	0.964	3.664
Total Capacitance (fF)	119.459	119.500	0.041	0.034

1.8.2 Capacitance Breakdown

Hand Calculations

- Cdb = 21.32 fF
- Cgd = 0.00 fF
- Cgs = 98.13 fF
- Total = 119.46 fF

SPICE

- Cbd = 21.30 fF
- Cgd = 0.00 fF
- Cgs = 98.20 fF
- Total = 119.50 fF

1.8.3 Explanation of Discrepancy

The largest discrepancy is in the cutoff frequency, where the hand calculation predicts **25.339** MHz, whereas SPICE simulation gives **26.303** MHz. The relative error is **3.664**%, which is significant. The difference is most likely the result of using the Miller Approximation over OCT.

1.8.4 Calculation of SPICE Capacitance

The total capacitance in SPICE was obtained by summing the individual capacitances:

where: * C_bd = 2.13 × 10^-14 F (21.30 fF) * C_gd = 0.00 F (0.00 fF) * C_gs = 9.82 × 10^-14 F (98.20 fF)

Thus,

C_total,SPICE =
$$2.13 \times 10^{-14} + 0 + 9.82 \times 10^{-14} = 1.195 \times 10^{-13} F$$
 (119.50 fF)

This closely matches the hand calculation, confirming that the capacitance assumptions were reasonable.