

CSEN911: Data Mining
Winter Term 2022

Problem Set 1 – Classification

Problem 1

Two document classification systems, X and Y, are being compared. Both are given the same query, applied to a collection of 1500 documents, and should return a set of documents that are relevant to the query. System X returns 400 documents, of which 40 are relevant to the query. System Y returns 30 documents, of which 15 are relevant to the query. Within the whole collection there are in fact 50 documents relevant to the query.

- a) What are the values of True Positives, False Positives, True Negatives, False Negatives for system X? *Hint*: The True Positives are the documents that are retrieved and relevant. The False Positives are the documents that are retrieved but are not relevant.
- b) Calculate the precision and recall for the 2 systems, showing the details of your calculations.

Problem 2

The following table shows the midterm and final exam grades obtained for students in a database course.

Student ID	x Quiz	y Midterm exam	z Final exam
1	8	14	84
2	7	10	63
3	6	14	78
4	9	19	90
5	6	17	75
6	9	16	79
7	5	6	52
8	9	18	74
9	5	13	77
10	8	16	90

Predict the final exam grade of a student who received a 9 on the quiz and a 17 on the midterm exam using the k -nearest neighbor algorithm with $k = 3$. **Hint:** Use the average of the final exam grades for the k -nearest neighbors for final prediction.

Problem 3

- a) We have a training set that includes three features, and we'd like to predict a binary output variable. Here is the whole training set.

x_1	x_2	x_3	y
A	X	P	True
A	X	Q	True
A	Y	P	False
A	Y	Q	False
B	X	P	True
B	X	Q	False
B	Y	P	False
B	Y	Q	False

- 1) If we train a decision tree classifier using this training set, which feature would be considered at the first “branch” of the decision tree (the top node)? Show your computations.
- 2) Compute the final tree that will be produced using the decision tree induction algorithm. Show your computation steps and provide a drawing of the final tree.

Problem Set 2 – Clustering and Outlier Analysis

Problem 4

The following table shows the midterm and final exam grades obtained for students in a database course.

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8	9	18	74
9	5	13	77
10	8	16	90

- a) If we want to group the students in the table into two clusters, and choose the initial cluster centroids to be the student with $ID = 2$ (for cluster C_1) and the student with $ID = 9$ (for cluster C_2). Which students will be clustered with student 2 in cluster C_1 and which students will be clustered with student 9 in cluster C_2 ? Use only the x and y attributes for clustering and ignore z . Show your solution steps.
- b) Comment on the choice of initial centroids. Did this choice result in a good cluster structure? Justify your answer.
- c) Assuming you will use the clusters computed in (a) to assign new students with either cluster. To which cluster will the student who received a 9 on the quiz and a 17 on the midterm exam be assigned?

Problem Set 3 – Association Rule Mining

Problem 5

Giving the following database with 5 transactions:

Transaction	List of Items
T1	A, B, C, D, E, F
T2	B, C, D, E, F, G
T3	A, D, E, H
T4	A, D, F, G, I, J
T5	B, D, E, K

Given **minimum support of 2/5** and **minimum confidence of 4/5**:

- Apply the Apriori algorithm to the dataset of transactions and identify all frequent k-itemsets. Show all of your work. You must show candidates but can cross them off to show the ones that pass the minimum support threshold. If a candidate itemset is pruned because it violates the Apriori property, you must indicate that it fails for this reason and not just because it does not achieve the necessary support count. So, explicitly tag the itemsets that are pruned due to violation of the Apriori property.
- Find all strong association rules that contain “A” in the left-hand part of the rule.

Problem Set 4 – Sentiment Analysis

Problem 6

- a) Assume the following likelihoods for each word being part of a positive or negative movie review, and equal prior probabilities for each class.

	positive	negative
I	0.09	0.16
always	0.07	0.06
like	0.29	0.06
foreign	0.04	0.15
films	0.08	0.11

What class will Naive Bayes assign to the sentence “*I always like foreign films.*”?

- b) Train two models, non-binarized multinomial naive Bayes and binarized naive Bayes, both with add-1 smoothing, on the following document **counts for key sentiment words**, with positive or negative class assigned as noted.

	“good”	“poor”	“great”	Class
Doc1	3	0	3	positive
Doc2	0	1	2	positive
Doc3	1	3	0	negative
Doc4	1	5	2	negative
Doc5	0	2	0	negative

Use binarized naive Bayes model to assign a class (positive or negative) to this sentence:

“*A good, good plot and great characters, but poor acting.*”

What is the final class for the sentence?

Formulas you may need:

Euclidean Distance:

$d(X, Y) = \sqrt{(x_1 - y_1)^2 + (x_2 - y_2)^2 + \dots + (x_p - y_p)^2}$, where X and Y are two data instances and p are attributes.

Manhattan Distance:

$d(X, Y) = |x_1 - y_1| + |x_2 - y_2| + \dots + |x_p - y_p|$, where X and Y are two data instances and p are attributes.

Decision Tree Classification:

$info(D) = entropy = - \sum_{x \in X} p(x) \log_2(p(x))$

$info_{Attribute}(D) = \sum_{j=1}^v \frac{|D_j|}{|D|} \times info(D_j)$, where $j = 1 \dots v$ are the attribute values

Association Rules Metrics:

$support(A \Rightarrow B) = P(A \cup B) = \frac{n(A \cup B)}{N}$

$confidence(A \Rightarrow B) = P(B|A) = \frac{n(A \cup B)}{n(A)}$

Bayes' Theorem:

$P(X) = \frac{P(Y)P(X|Y)}{P(Y)}$

$P(X|Y) = \prod_{k=1}^n P(x_k|Y) = P(x_1|Y) \times P(x_2|Y) \times \dots \times P(x_n|Y)$, where x_k is value of attribute k for object X

Naïve Bayes Rule for Sentiment Analysis:

$\hat{P}(w|c) = \frac{count(w,c)+1}{count(c)+|V|}$

where w is a word, c represents sentiment class, $|V|$ represents vocabulary size in training set