OTE: Ohjelmointitekniikka Programming Techniques

course homepage: http://www.cs.uku.fi/~mnykanen/OTE/
Week 48/2008

Exercise 1.

- (a) What is the wp semantics of the *empty* if fi command which has no branches? Why?
- (b) What about the empty **do od** loop?

Exercise 2. The exponentiation algorithm in Figure 10 has an annoying design wrinkle: When p is odd, it subtracts 1 from p, making p even. Then it tests whether p is even or odd, even though this is already known.

- (a) Rewrite it to remove this wrinkle.
- (b) Prove that your algorithm in part (a) is also correct. What parts of the proof for the original algorithm can you recycle?

Exercise 3. Could the *bound* in Theorem 14 be real-valued instead? Why?

Exercise 4. Suppose that while verifying checkpoint 2 for a **do** \mathcal{B} **od** loop you managed to prove

$$invariant \land guard \Longrightarrow FALSE$$

for one of its branches. What does this mean?

Exercise 5.

- (a) How would you express in logic that u is the largest number found in the one-dimensional array a?
- (b) Write an algorithm in GCL to find this u from a.
- (c) Prove your algorithm correct.

Exercise 6. Consider the following code:

```
 \{ \text{ lower}(b) = \text{lower}(a) \land \text{ upper}(b) = \text{upper}(a) \} 
 s, i := 0, \text{ lower}(a); 
 do \ i \leq \text{upper}(a) \rightarrow 
 b[i] := s + a[i]; 
 s, i := b[i], i + 1; 
 od; 
 \{ \forall i \in \text{indices}(a).b[i] = \sum_{j=\text{lower}(a)}^{i} a[j] \}
```

(a) What do its pre- and postconditions claim that it computes?

- (b) The programmer (the lazy sod...) has omitted its loop invariant and bound. Add them.
- (c) If you think that this loop is correct, then prove it. If not, then give an input a which reveals a bug in it.