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LEC 32 Qu	iz 3 Review 217
6.1-2 N a	ndx $Ax=1x$
6.3 du/dt	=Au and eAt
6.4 A = A T	= Au and e At = 212T 11 6.5 positive definite
6.6. Similar	B=MTAM 6.7 B=USVI
	same eigenvalues SVD
$\frac{\int u}{dt} = Au = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$	10]
$U(t) = C_1 e^{\lambda_1 t}$	$x_1 + c_2 e^{n_2 t} x_2 + c_3 e^{n_3 t} x_3$
A is sign singu	lar, so 1, = 0
Γ-λ -1 0	
1 -1	$=-1/3^{3}-21/1=0$
	カ(カギン)=0
⇒ ∧,= <u>5</u> i,	12=151
$\Rightarrow u(t) = C_1 \times_1 +$	C2 e Fit X2 + C3 e -12it X3
	go around at unit circle
t=0 U(07 =	$GX_1 + G_2X_2 + G_3X_3$
what's the per	riod?
er (e	51 = 1 $51 = 27$
. (a	cast sho, il

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so the Periodic T=	17/2
orthogonal eigenvector	symmetric, antisymouth
back to e bt du	orthopnal veetors
e^{At} $u(t) = e^{A(t)}u(0)$	
$e^{At} (if A = SAS^{-1})$ $= se^{s}$	cigen veeters one independent ont and #= n
$ \begin{array}{ll} \lambda_{1} = 0, & \lambda_{2} = c, & \lambda_{3} = 2 \\ \lambda_{1} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, & \lambda_{2} = \begin{bmatrix} 1 \\ -1 \end{bmatrix} \\ \lambda_{3} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, & \lambda_{4} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, & \lambda_{5} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, & \lambda_{5$	
(b) symmetric? <u>all red</u> (c) positive definite?	2/c
semi 11	
(d) merkov motrix? (e) (A) projectkin matrix?	

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	AIA:	AT =AT	7: eigenveets	8
Why	$V_i^T f$	7 V2 = 12 V1	_	
symmetric		$1)^T V_2 = \lambda$		
=) oothogon		=> NIVITVI	$= \lambda_2 V_1^7 V_2$	
eigen vec			$^{7}V_{2}=0$	

ATA =
$$(V \Sigma^{T} U^{T}) (U \cdot \Sigma V^{T}) = U (\Sigma^{T} \Sigma) V^{T}$$

(Symmetric $u=v=s$ (SAS-1)

=) $v=es$ evector for ATA

= 6i = ricaTA)

$$XTATAX = (Ax)^{T} \cdot Ax = ||Ax||^{n^{2}} > 0$$

why pta alweads positive definite?

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they way to decitive	e decide sign of eigenvector
Instead Avi = 6; Wi	
[a, u][3][v, v2]	77
[30] > A.	s singular, rank=1
U Vz is	the basis of MA)
•	1/s real
Given A is symmetric	and orthogonal - IN =1
1) eigenvalues can be	1 and -1. $Qx = \lambda x$
To sychiation Con occupants Front S (A+I) is a project	ctbn mutrix 2.1/x1 = 1/1 1/x1)
$Prof$ $(P^2 = P and sy mme)$	tric)
\$ (A)+2AI+I') =	₹ (A+I)
what is A?? A?	$A^T = A^{-1}$ $AA^{-1} = I$
	(I+A)) = = ((A+I)

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The summar of		/ /	•
1 g orthogon	al matri,	X	
$Q \cdot Q^T = I \cdot c$	[x, x2 x 3 x 4	The second of th	cĪ
det/adf = so d		n .	
1. orthonormal: Q	$\cdot Q^T = I$, det (a) =	
$2, Q_1Q_2 = Q_3$	two o	orthogonal matrix o	ultply
$Q_3^7 \cdot Q_3 = Q_2^7$	Q,7. Q,.Q2	= I =) ort	hogona (
3, Qx = x			
4. 1/1 = 1,	leigenveets	rs are orthogonal	
5, SVD: A alu	rays = U or	· V]	
	•		
2 symmetric	mertarix		
1. A=AT			
h A are all rea			
3, leigenvectors	orthogonal	Au = 274.	
4, A=QAQT	<i>J</i>	AV2=12/12	
51 SUD 7) U=V	5=1	(AVI) () = (14)	1. V2
		A VI NE	

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	Hitte Mariety
- 37 - 37	Symmetric + 1>0
2 3 1000	1 >0 det >0
5 310 7	5=1
- segretal m	atol X
1 1 5 世	e diagnols
I STATE	(2) arithment built
- 500 = A	=5
キョルングレイ	U: Aum verter orthyses/
James 10015	of ON V: duns vector ordersonal
	= mass of CATI
Per MIN 30	ATA's eigen vectors
1/2 column 2	ATA'S eigenvectors
The set degen	d on the sort of shyulur values
S ANT	,
y symmetric	2 gure