# **R9 Graphs BFS**

#### 3.27 https://github.com/GUMI-21/MIT6.006\_note

A graph G = (V, E) is a mathematical object comprising a set of vertices V (also called nodes) and a set of edges E.

- directed (u,v)
- undirected {u,v}

The *in-degree* and *out-degree* of a vertex v denotes the number of incoming and outgoing edges connected to v respectively.

When talk about degree, generally mean out-degree.

path

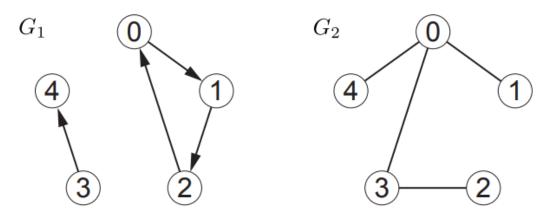
A path1 in a graph is a sequence of vertices (v0, ..., vk) such that for every ordered pair of vertices (vi, vi+1), there exists an outgoing edge in the graph from vi to vi+1.

The length of a path is the number of edges in the path

## **Graph Representations**

### adjacency list

The most common way is to store a Set data structure Adj mapping each vertex u to another data structure Adj(u) storing the adjacencies of v, the set of vertices that are accessible from v via a single outgoing edge.



example of *adjacency list* in python of G1 & G2. Using a direct access array for the top-level Set and an array for each adjacency list.

```
A1 = [[1],[2],[0],[4],[]]

A2 = [[1,3,4],[0],[3],[0,2],[0]]
```

example of hash table for outer Adj Set and inner adjacency lists Adj(u), using Python dictionaries

```
S1 = {0:{1},1:{2},2:{0},3:{4}},

S2 = {0:{1,3,4}, 1:{0}, 2:{3}, 3:{0,2}, 4:{0}}
```

### **Breadth-First Search**

A breadth-first search (BFS) from s discovers the level sets of s: level Li is the set of vertices reachable from s via a shortest path of length i (not reachable via a path of shorter length).

- level  $L_i$  is the set of vertices reachable from s via a shortest path of length i.
- $L_0 = \{s\}$
- So to compute level Li+1, include every vertex with an incoming edge from a vertex in Li, that has not already been assigned a level., means not repeated vertices.

runtime

```
so the runtime is O(|E| + |V|)
```