

R1 Intro about Algorithm

3.22 https://github.com/GUMI-21/MIT6.006_note

- A problem is a binary relation connecting problem inputs to correct outputs.
- A (deterministic) algorithm is a procedure that maps inputs to single outputs.
- An algorithm solves a problem if for every problem input it returns a correct output.

Correctness

often proof via induction.

Efficiency

storage space or running time.

use *asymptotic performance* and ignore constant factor differences in hardware performance.

Asymptotic Notation

upper bound

- O Notation: Non-negative function $g(n)$ is in $O(f(n))$ if and only if there exists a positive real number c and positive integer n_0 such that $g(n) \leq c \cdot f(n)$ for all $n \geq n_0$.

lower bounds

- Ω Notation: Non-negative function $g(n)$ is in $\Omega(f(n))$ if and only if there exists a positive real number c and positive integer n_0 such that $c \cdot f(n) \leq g(n)$ for all $n \geq n_0$.

tight bound

- Θ Notation: Non-negative $g(n)$ is in $\Theta(f(n))$ if and only if $g(n) \in O(f(n)) \cap \Omega(f(n))$.

Mod of Computation

we will use the *w-bit WordRAM* model of computation.

If a machine word contains only w bits, the processor will only be able to read and write from at most 2^w addresses in memory.

we will always assume our Word-RAM has a word size of at least $w > \log_2 n$ bits, or else the machine would not be able to access all of the input in memory. a Word-RAM model of a byte-addressable 64-bit machine allows inputs up to $\sim 10^{10}$ GB in size.

Data Structure

The set of operations supported by a data structure is called an *interface*

ex: static array

- `StaticArray(n)`: allocate a new static array of size n initialized to 0 in $\Theta(n)$ time
- `StaticArray.get at(i)`: return the word stored at array index i in $\Theta(1)$ time
- `StaticArray.set at(i, x)`: write the word x to array index i in $\Theta(1)$ time