# Cryptography Lecture 25

Arkady Yerukhimovich

December 2, 2024

### Outline

- Lecture 24 Review
- 2 Public-Key Crypto Protocol Review
- 3 Secure Multi-Party Computation (MPC)
- 4 A Simple MPC Protocol
- MPC Based on Secret Sharing
- 6 Defining MPC Security

### Lecture 24 Review

- Signatures from private-key primitives
- One-time signatures
- Going from one-time to standard signatures

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## Public-Key Protocols

## El Gamal Encryption: $\Pi = (Gen, Enc, Dec)$ with $\mathcal{M} = G$

- Gen(1<sup>n</sup>):  $(G, q, g) \leftarrow \text{Gen}(1^n)$ ,  $x \leftarrow \mathbb{Z}_q$ ,  $h = g^x$ , pk = (G, q, g, h) and sk = x
- $\operatorname{Enc}_{pk}(m)$ :  $y \leftarrow \mathbb{Z}_q$ , compute  $c = (g^y, h^y \cdot m)$
- Dec<sub>sk</sub>(c): Compute  $\hat{m} = c_2/c_1^x$

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### Plain RSA Encryption

- $Gen(1^n)$ :  $(N, e, d) \leftarrow GenRSA(1^n)$ , pk = (N, e), sk = (N, d)
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### Plain RSA Signature

- Gen:  $(N, e, d) \leftarrow \text{GenRSA}(1^n)$ , pk = N, e, sk = d
- Sign<sub>sk</sub> $(m \in \mathbb{Z}_N^*)$ :  $\sigma = [m^d \mod N]$
- Verify<sub>pk</sub> $(m \in \mathbb{Z}_N^*, \sigma \in \mathbb{Z}_N^*)$ : Output 1 if and only if  $m = [\sigma^e \mod N]$

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### The Need for Collaboration

#### Yao's Millionaire Problem





Who is the richest?

### The Need for Collaboration



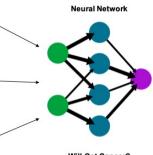




Name	Age	Smokes	Cancer
Jane Doe	25	Υ	Υ
John Doe	45	N	Υ

Name	Age	Smokes	Cancer
Jane Smith	35	Υ	N
John Smith	85	Υ	Υ

Name	Age	Smokes	Cancer
Joe Smith	50	N	N
Jim Doe	60	Υ	Υ



Will Get Cancer?

# The Security Challenge

#### Question

How do parties who *do not trust each other* work together to compute joint functions on their private data?

- Without revealing their data or intermediate results to each other
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Secure Multi-Party Computation (MPC or SMC) gives a solution:

- Originally developed in the 1980's
- Originally believed to be purely of theoretical interest
- But, since 2004 there have been many implementations showing real-world value
- Protocol and engineering improvements have yielded 6+ orders of magnitude speed up

### MPC in the Real World









**Gender Pay Equity** 



Cryptographic Key Control



**Federated Keyboard Prediction** 

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### Additive One-Time Pad

Given an Integer  $x \in \mathbb{Z}_N$ , consider the following scheme:

- Choose  $r \leftarrow \mathbb{Z}_N$  at random
- Compute  $y = x + r \mod N$
- Can recover x from y if know r

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### Hiding

Given y, the value of x is perfectly hidden:

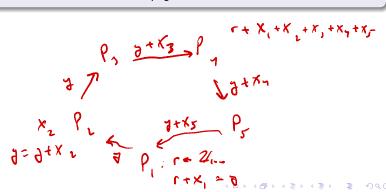
• Every value of  $x \in \mathbb{Z}_N$  is equally likely

### An MPC Protocol

#### Secure Summation

5 parties  $\{P_1,\ldots,P_5\}$  each with private input  $x_i\in\mathbb{Z}_{100}$  want to compute

$$y = \sum_{i=1}^{5} x_i$$



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We wish to distribute a secret value  $x \in \mathbb{Z}_N$  among n parties s.t.:

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- Any set of  $\leq n-1$  parties has no information about x

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• All parties send their shares to  $P_1$ , who computes  $x = \sum_{i=1}^n [x]_i$ 

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### Security

Easy to see that any set of n-1 parties has no info about x

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Suppose parties hold two secret shared values:

- $[x] = ([x]_1, [x]_2, \dots, [x]_n)$
- $[y] = ([y]_1, [y]_2, \dots, [y]_n)$
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- Problem: We need to compute the cross-terms (e.g.,  $[x]_1[y]_2$ )

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• Random values [a], [b], [c] such that  $c = a \cdot b$ 

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$$[x] \rightarrow [2x]$$

$$x_{i+}x_{i+}x_{j-} \times \lambda x_{i} + 2x_{i} + 2x_{i} + 2x_{i} + 2x_{i}$$

$$[x] \rightarrow [x + c] \quad \text{for patter} \quad C$$

$$[x]_{i} \rightarrow [x]_{i} = c$$

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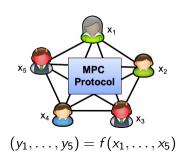
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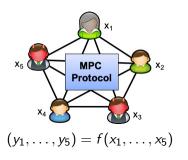
- Cost: 2 openings, and three local multiplications
- Security: Since a and b are random (x + a), (y + b) reveal nothing about x, y

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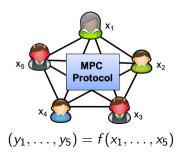
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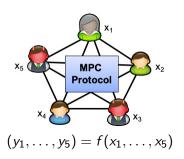




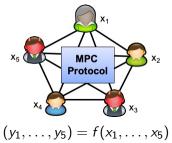
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$$(y_1,\ldots,y_5)=f(x_1,\ldots,x_5)$$

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- Adversary (A) controls some of the parties

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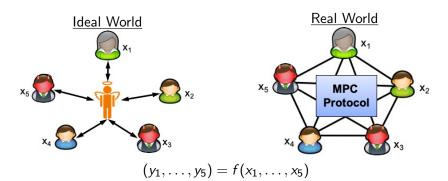
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#### **Defining Security**

We could give a security definition for each of these, but instead take a different approach.

# Real-Ideal Paradigm



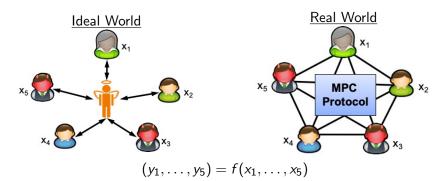
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MPC protocol emulates ideal-world execution

- Whatever security holds in ideal world holds in the real world
- ullet Formally: Can build an ideal-world adversary (Simulator) that produces same view as real-world adversary ( $\mathcal{A}$ )

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# Simulating the Sharing-based MPC protocol

ullet Assume that  ${\mathcal A}$  corrupts t < n parties

### Simulating the Sharing-based MPC protocol

- Assume that A corrupts t < n parties
- ullet Then, all  ${\cal A}$  even sees are random shares sent to parties he corrupts
- Since he never sees all *n*, these are completely random
- Simulator, can just send random values to  $\mathcal A$  to simulate his view (distributed the same as real protocol)

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#### Output may leak private information

- MPC guarantees that adversaries learn nothing more than the output
- But, MPC does not consider what the output reveals
- In particular, output may reveal parties' inputs: e.g. C(x,y) = x+y
- Deciding what functions are safe to compute is orthogonal to MPC this is studied by differential privacy

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- Deciding what functions are safe to compute is orthogonal to MPC this is studied by differential privacy

### Why does this not break security?

### Correctness of inputs

- MPC allows adversary to choose his own inputs
- No notion of "valid" input
- If you want to restrict inputs to have some properties need additional tools

#### Output may leak private information

- MPC guarantees that adversaries learn nothing more than the output
- But, MPC does not consider what the output reveals
- In particular, output may reveal parties' inputs: e.g. C(x,y) = x+y
- Deciding what functions are safe to compute is orthogonal to MPC this is studied by differential privacy

#### Why does this not break security?

Both of these limitations also happen in the ideal world

Arkady Yerukhimovich Cryptography December 2, 2024

# Adversary Types

#### Adversary type:

- Semi-honest (honest but curious) follows protocol, but tries to learn more
- Malicious may deviate from protocol arbitrarily
- Covert Malicious, but does not want to be caught

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#### Adversary threshold:

- t < n/2 honest majority
- t < n dishonest majority (particularly important for 2PC)
- t < n/3 allows highly optimized protocols