

Base R 1: Vectors

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February 04, 2018

1. Create the vectors:

(a) (1, 2, 3, . . . , 19, 20)

```
1:20
```

```
## [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
```

(b) (20, 19, . . . , 2, 1)

```
20:1
```

```
## [1] 20 19 18 17 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1
```

(c) (1, 2, 3, . . . , 19, 20, 19, 18, . . . , 2, 1)

```
c(1:20, 19:1)
```

```
## [1] 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 19 18 17
## [24] 16 15 14 13 12 11 10 9 8 7 6 5 4 3 2 1
```

(d) assign vector `c(4, 6, 3)` variable name `tmp`

Use `tmp` for parts (e), (f) and (g)

```
tmp <- c(4, 6, 3)
```

(e) (4, 6, 3, 4, 6, 3, . . . , 4, 6, 3) where there are 10 occurrences of 4.

```
rep(tmp, times=10)
```

```
## [1] 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3
```

(f) (4, 6, 3, 4, 6, 3, . . . , 4, 6, 3, 4) where there are 11 occurrences of 4, 10 occurrences of 6 and 10 occurrences of 3.

```
c(rep(tmp, times=10), 4)
```

```
## [1] 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4 6 3 4
```

(g) (4, 4, . . . , 4, 6, 6, . . . , 6, 3, 3, . . . , 3) where there are 10 occurrences of 4, 20 occurrences of 6 and 30 occurrences of 3.

```
rep(tmp, times=c(10,20,30))
```

```
## [1] 4 4 4 4 4 4 4 4 4 4 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 3 3 3 3 3
## [36] 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3
```

2. Create a vector of the values of

$e^x \cos(x)$ at $x = 3, 3.1, 3.2, \dots, 6$.

```
# I elected to use a new variable instead of reusing "tmp"
x <- seq(from = 3, to = 6, by = 0.1)
exp(x)*cos(x)
```

```
## [1] -19.884531 -22.178753 -24.490697 -26.773182 -28.969238 -31.011186
## [7] -32.819775 -34.303360 -35.357194 -35.862834 -35.687732 -34.685042
## [13] -32.693695 -29.538816 -25.032529 -18.975233 -11.157417 -1.362099
## [19] 10.632038 25.046705 42.099201 61.996630 84.929067 111.061586
## [25] 140.525075 173.405776 209.733494 249.468441 292.486707 338.564378
## [31] 387.360340
```

```
head(x, n = 30)
```

```
## [1] 3.0 3.1 3.2 3.3 3.4 3.5 3.6 3.7 3.8 3.9 4.0 4.1 4.2 4.3 4.4 4.5 4.6
## [18] 4.7 4.8 4.9 5.0 5.1 5.2 5.3 5.4 5.5 5.6 5.7 5.8 5.9
```

```
# To keep the listing shorter
```

3. Create the following vectors:

(a) $(0.1^3 0.2^1, 0.1^6 0.2^4, \dots, 0.1^{36} 0.2^{34})$

```
i = c(0.1, 0.2)
j = c(3, 1)
k = rep(c(0:33), rep(2, 34))
i^(j+k)
```

```
## [1] 1.000000e-03 2.000000e-01 1.000000e-04 4.000000e-02 1.000000e-05
## [6] 8.000000e-03 1.000000e-06 1.600000e-03 1.000000e-07 3.200000e-04
## [11] 1.000000e-08 6.400000e-05 1.000000e-09 1.280000e-05 1.000000e-10
## [16] 2.560000e-06 1.000000e-11 5.120000e-07 1.000000e-12 1.024000e-07
## [21] 1.000000e-13 2.048000e-08 1.000000e-14 4.096000e-09 1.000000e-15
## [26] 8.192000e-10 1.000000e-16 1.638400e-10 1.000000e-17 3.276800e-11
```

```
## [31] 1.000000e-18 6.553600e-12 1.000000e-19 1.310720e-12 1.000000e-20
## [36] 2.621440e-13 1.000000e-21 5.242880e-14 1.000000e-22 1.048576e-14
## [41] 1.000000e-23 2.097152e-15 1.000000e-24 4.194304e-16 1.000000e-25
## [46] 8.388608e-17 1.000000e-26 1.677722e-17 1.000000e-27 3.355443e-18
## [51] 1.000000e-28 6.710886e-19 1.000000e-29 1.342177e-19 1.000000e-30
## [56] 2.684355e-20 1.000000e-31 5.368709e-21 1.000000e-32 1.073742e-21
## [61] 1.000000e-33 2.147484e-22 1.000000e-34 4.294967e-23 1.000000e-35
## [66] 8.589935e-24 1.000000e-36 1.717987e-24
```

(b) $(2, \frac{2^2}{2}, \frac{2^3}{3}, \dots, \frac{2^{25}}{25})$

```
i <- c(2)
j <- c(1:25)
i^j/j
```

```
## [1] 2.000000e+00 2.000000e+00 2.666667e+00 4.000000e+00 6.400000e+00
## [6] 1.066667e+01 1.828571e+01 3.200000e+01 5.688889e+01 1.024000e+02
## [11] 1.861818e+02 3.413333e+02 6.301538e+02 1.170286e+03 2.184533e+03
## [16] 4.096000e+03 7.710118e+03 1.456356e+04 2.759411e+04 5.242880e+04
## [21] 9.986438e+04 1.906502e+05 3.647221e+05 6.990507e+05 1.342177e+06
```

4. Calculate the following:

(a) $\sum_{i=10}^{100} (i^3 + 4i^2)$

```
i <- c(10:100)
sum(i^3 + 4*i^2)
```

```
## [1] 26852735
```

(b) $\sum_{i=1}^{25} (\frac{2^i}{i} + \frac{3^i}{i^2})$

```
i <- c(1:25)
sum(2^i/i + 3^i/i^2)
```

```
## [1] 2129170437
```

5. Use the function paste() to create the following character vectors of length 30:

- (a) ("label 1", "label 2", ..., "label 30"). Note that there is a single space between label and the number following.

```
paste(c("label"), c(1:30), sep=" ")
```

```
## [1] "label 1" "label 2" "label 3" "label 4" "label 5" "label 6"
## [7] "label 7" "label 8" "label 9" "label 10" "label 11" "label 12"
## [13] "label 13" "label 14" "label 15" "label 16" "label 17" "label 18"
## [19] "label 19" "label 20" "label 21" "label 22" "label 23" "label 24"
## [25] "label 25" "label 26" "label 27" "label 28" "label 29" "label 30"
```

(b) ("fn1", "fn2", ..., "fn30").

In this case, there is no space between fn and the number following. *****

```
paste(c("fn"), c(1:30), sep="")
```

```
## [1] "fn1" "fn2" "fn3" "fn4" "fn5" "fn6" "fn7" "fn8" "fn9" "fn10"
## [11] "fn11" "fn12" "fn13" "fn14" "fn15" "fn16" "fn17" "fn18" "fn19" "fn20"
## [21] "fn21" "fn22" "fn23" "fn24" "fn25" "fn26" "fn27" "fn28" "fn29" "fn30"
```

6. Execute the following lines which create two vectors of random integers which are chosen with replacement from the integers 0, 1, . . . , 999. Both vectors have length 250.

```
set.seed(50)
xVec <- sample(0:999, 250, replace=T)
yVec <- sample(0:999, 250, replace=T)
```

Suppose $x = (x_1, x_2, \dots, x_n)$ denotes the vector xVec and $y = (y_1, y_2, \dots, y_n)$ denotes the vector yVec.

(a) Create the vector $(y_2 - x_1, \dots, y_n - x_{n-1})$.

```
yVec[-1] - xVec[-length(xVec)]
```

```
## [1] 163 -122 317 -146 417 393 249 -489 741 771 81 402 -549 338
## [15] 583 -403 -67 217 307 -121 -269 36 -706 -563 102 48 397 297
## [29] -45 -152 497 405 339 -400 499 -89 211 -670 87 74 554 149
## [43] -183 612 193 -453 -70 -141 127 -709 -708 -722 -64 388 -184 -212
## [57] 242 430 275 672 -150 275 -96 -255 512 577 264 439 149 -916
## [71] 374 -889 -332 324 -553 394 -87 -75 345 -735 -55 100 -40 15
## [85] 279 409 790 -547 -487 -399 -619 -168 -185 19 645 551 227 -366
## [99] 242 147 247 -499 -614 758 63 -227 247 379 -472 566 -762 152
## [113] 493 360 69 190 544 -176 216 -676 -205 782 -109 189 -233 505
## [127] -219 288 -57 487 256 300 -192 -263 704 674 217 280 17 -68
## [141] 259 612 -127 1 545 -231 -191 -338 333 495 -21 -4 294 -668
## [155] -814 420 793 631 -67 655 143 611 -220 -518 -285 327 523 -13
## [169] -679 -241 39 193 342 588 469 68 895 -658 232 -331 27 441
## [183] -733 -182 -399 79 -469 371 475 265 -407 211 59 -974 -90 218
## [197] 396 -486 -963 -327 425 220 128 235 294 -107 -365 146 -588 449
## [211] -434 221 846 386 -910 161 206 109 712 -334 -434 7 640 -350
## [225] 923 353 -579 225 327 410 568 -195 -83 154 -486 -195 667 -144
## [239] 272 410 546 380 -559 414 674 193 222 -92 553
```

(b) Create the vector $(\frac{\sin(y_1)}{\cos(x_2)}, \frac{\sin(y_2)}{x_3}, \dots, \frac{y_{n-1}}{\cos(x_n)})$.

```
sin(yVec[-length(yVec)]) / cos(xVec[-1])
```

```
## [1] 0.88603405 -1.44184825 0.82807258 -1.61591717 -0.86017343
## [6] 20.26356465 -0.79930406 1.72414444 -0.08094240 -0.74895634
## [11] -2.59866958 -0.37361045 31.11471579 0.12355916 -0.35925226
## [16] -0.90743608 0.34374436 5.78205917 -2.57418558 -0.78661325
## [21] -0.59855406 0.98936263 0.33042931 -1.75124647 -0.59435547
## [26] 1.05374692 0.65497397 -0.11596582 -0.97176537 0.57180267
## [31] 0.75799030 -0.49259143 -0.99433357 0.05377148 -3.77616264
## [36] 20.54902944 0.77784817 1.28146891 -0.51650728 6.66902699
## [41] -0.92970072 -10.93066299 -3.13102962 30.87943423 -1.14281543
## [46] 0.36757630 1.18479716 0.94594159 0.93339520 0.93632658
## [51] -11.05384468 2.76893270 0.97488334 -0.08932225 -1.33616578
## [56] -3.30065552 0.62663162 -1.96486337 0.08653876 0.56695489
## [61] 44.07630714 -1.11764853 0.11230330 -0.46073106 -0.13860882
## [66] 0.84026052 2.64708780 -1.63174570 -9.63022830 -2.15553419
## [71] -0.42770826 3.24955062 -4.23453154 0.93067452 -0.88388390
## [76] 0.69339350 1.72841015 -8.22082884 1.69276461 1.02074555
## [81] -3.21968328 -0.90739226 1.11331935 0.59579467 0.19571363
## [86] -0.17975474 4.38929818 0.64431266 -1.54509170 -0.26536991
## [91] -0.81679156 1.34164181 -1.03400420 -1.33639979 -0.44444499
## [96] 0.96777754 -0.09545121 -0.63686070 -2.30844090 -0.11384497
## [101] 1.08800453 1.06851885 -0.30428029 -1.77044888 -1.45269351
## [106] 0.97943716 -2.15021752 1.56128032 0.61018741 5.59692239
## [111] -1.03020002 -1.14632240 -0.81548097 0.95359082 74.12815803
## [116] -0.20329495 -0.08875385 -0.76023984 -0.42372635 -0.68385723
## [121] 1.28860542 0.94117702 1.89561343 0.69369539 4.15021756
## [126] -1.08026240 1.26615554 0.02147428 3.32694398 0.22930300
## [131] 1.14217476 0.73847767 8.72339712 -17.15727240 0.90435970
## [136] 1.07791792 0.75391899 -0.26297571 0.83894657 -1.22542984
## [141] -0.57277292 -1.22429033 2.10719833 -1.35745285 -0.84117115
## [146] -0.69663176 -0.99207337 -1.17363312 -5.50814669 -1.12309426
## [151] 0.60767585 0.32903697 -0.08845387 -4.42251048 -1.31360561
## [156] -1.05268827 -1.45007537 -1.03184453 0.38034305 2.06381128
## [161] -1.64568068 0.47938401 46.18666528 1.75988821 14.03349520
## [166] 1.99884446 -1.02170635 1.02445028 -0.15250370 -1.11793279
## [171] -4.12228606 1.02355677 0.89546497 0.74732250 -2.09533197
## [176] -2.40630344 -0.73530615 0.90759126 -0.87474163 -4.22536917
## [181] -2.04450866 -7.41320483 0.03607946 -0.85674969 -0.85648584
## [186] 2.58973778 8.68248704 -0.74202802 1.07347586 1.37638585
## [191] 1.73104746 -0.57596355 -0.49915725 0.11786229 -0.45584137
## [196] -0.97726281 -6.86428063 -0.60929448 -0.72132361 0.00000000
## [201] 1.00734878 4.20789995 -0.81616263 -1.72455176 10.00784534
## [206] 0.71310632 8.77005056 -0.64297796 0.24086573 -6.12424634
## [211] 0.94848253 9.22132979 -5.85933168 -0.77292827 -0.85749485
## [216] 0.80000340 -10.45187777 2.91489552 0.86914823 0.93956496
## [221] 1.15020196 -4.25009579 -0.97278301 1.05669698 23.96919924
## [226] -0.11659711 0.58615433 -1.23512544 1.08111948 3.37846777
## [231] 0.96204558 -1.18727215 0.77801767 2.39161655 1.01270315
## [236] 0.30508064 -1.13987140 1.35085069 2.13213714 0.95034702
## [241] 0.48941676 -1.03804260 1.11768517 -0.25446052 -15.07630921
```

```
## [246] 1.12429826 0.28067653 -0.75125301 -1.91160477
```

```
tmp1 <- sin(yVec[-length(yVec)]) / cos(xVec[-1])
```

```
head(tmp1, n = 30)
```

```
## [1] 0.8860340 -1.4418482 0.8280726 -1.6159172 -0.8601734 20.2635647
## [7] -0.7993041 1.7241444 -0.0809424 -0.7489563 -2.5986696 -0.3736105
## [13] 31.1147158 0.1235592 -0.3592523 -0.9074361 0.3437444 5.7820592
## [19] -2.5741856 -0.7866133 -0.5985541 0.9893626 0.3304293 -1.7512465
## [25] -0.5943555 1.0537469 0.6549740 -0.1159658 -0.9717654 0.5718027
```

(c) Create the vector $(x_1 + 2x_2 - x_3, x_2 + 2x_3 - x_4, \dots, x_{x-2} + 2x_{x-1} - x_n)$

```
xVec[c(1:(length(xVec) - 2))] + 2*xVec[c(2:(length(xVec) - 1))] - xVec[c(3:length(xVec))]
```

```
## [1] 1382 70 1221 1749 -98 796 1949 623 -134 618 288 1472 517 -45
## [15] 794 1982 1489 344 -206 1207 292 771 2085 810 1032 1547 767 537
## [29] 702 676 737 664 1451 435 1355 168 1150 989 926 348 1757 1299
## [43] 409 -497 501 2150 1157 1081 1323 2030 1887 1744 879 590 493 1330
## [57] 1254 1281 465 767 1691 464 1238 805 -519 1425 710 -611 1517 963
## [71] 1836 2243 -158 1860 606 506 1917 1304 2021 2025 238 226 733 1538
## [85] 581 -659 824 1109 1136 1339 1239 1584 2300 562 567 -375 1372 761
## [99] 1142 714 1801 2220 624 -806 1738 268 398 1941 668 2037 829 345
## [113] 337 -45 635 -285 1225 691 1792 2216 123 538 1130 1124 1172 944
## [127] 271 -62 229 785 -70 1346 1622 381 104 1036 1015 199 589 1399
## [141] 601 506 560 -145 171 1204 1427 1278 1128 615 269 37 1521 2172
## [155] 1602 464 74 1575 599 88 -267 1185 1655 1564 1420 880 229 1651
## [169] 959 1306 2008 1243 267 1110 556 -791 1300 844 1578 2427 708 1554
## [183] 1439 1150 1269 2274 1419 1067 187 2071 781 -148 1767 1851 1019 -196
## [197] 554 2223 1710 -90 788 1209 876 1322 275 1191 323 1570 1234 768
## [211] 1715 903 -768 1546 1452 -47 1125 -330 871 2463 894 133 975 201
## [225] -137 1553 299 865 746 184 267 839 -63 863 2411 133 1739 1145
## [239] 1015 47 209 1468 846 10 1146 31 1405 1058
```

(d) Calculate $\sum_{i=1}^{n-1} \frac{e^{-x_i+1}}{x_i+10}$

```
sum(exp(-xVec[c(2:length(xVec))])) / (xVec[c(1:(length(xVec) - 1))] + 10)
```

```
## [1] 0.01269872
```

7. This question uses the vectors `xVec` and `yVec` created in the previous question and the functions `sort`,

`order`, `mean`, `sqrt`, `sum`, and `abs`.

(a) Pick out the values in `yVec` which are > 600 .

```
yVec[yVec > 600]
```

```
## [1] 709 871 621 930 948 783 878 671 860 768 698 974 855 813 776 721 917
## [18] 985 705 884 840 687 957 955 786 938 930 641 615 988 881 881 997 823
## [35] 791 643 779 693 845 815 752 766 635 993 919 686 635 613 660 800 743
## [52] 965 743 615 615 803 948 760 604 800 772 863 902 689 881 941 924 693
## [69] 835 632 872 876 850 961 681 791 947 915 712 665 921 798 866 828 942
## [86] 841 645 681 827 884 890 970 632 717 846 952 609 824 695 675 777 813
## [103] 792 783 611 853 738 668 791
```

(b) What are the index positions in yVec of the values which are > 600?

```
hw19 = c(1:length(yVec))[yVec > 600]
hw19
```

```
## [1] 1 2 5 6 8 10 11 13 16 18 27 28 32 33 34 36 42
## [18] 43 45 48 50 55 58 59 60 61 63 66 67 68 72 79 80 86
## [35] 88 94 95 96 97 101 102 105 107 109 111 114 118 119 120 123 125
## [52] 127 131 132 134 136 137 138 139 142 143 150 151 154 157 158 159 161
## [69] 163 164 167 168 172 173 174 175 176 178 180 181 182 183 187 189 190
## [86] 203 204 205 206 211 213 214 219 220 224 226 227 230 232 237 238 239
## [103] 241 243 245 246 247 249 250
```

(c) What are the values in xVec which correspond to the values in yVec which are > 600? (By correspond, we mean at the same index positions.)

```
xVec[hw19]
```

```
## [1] 708 437 513 44 646 107 390 640 676 364 577 257 408 437 618 627 836
## [18] 278 55 458 803 358 525 511 266 578 197 38 724 61 995 652 956 19
## [35] 680 760 48 294 69 505 964 24 10 840 878 113 789 444 986 537 515
## [52] 263 359 189 457 274 543 324 176 160 260 407 216 977 148 293 660 137
## [69] 852 743 353 371 768 339 203 478 49 880 996 894 357 900 972 467 324
## [86] 517 446 533 190 501 124 14 5 863 399 256 678 188 258 110 957 285
## [103] 34 631 179 545 123 238 178
```

(d) Create the vector $(|x_1 - \bar{x}|^{1/2}, |x_2 - \bar{x}|^{1/2}, \dots, |x_n - \bar{x}|^{1/2})$

```
abs(xVec - mean(xVec))0.5
```

```
## [1] 16.0044994 3.8543482 15.8699716 17.7522956 7.8194629 20.1954450
## [7] 15.7208142 13.9335566 20.2449006 18.5702989 7.8648585 13.5224258
## [13] 13.7165593 19.3611983 13.2233127 14.9714395 19.5740645 9.3731532
## [19] 19.4385185 16.8480266 12.8118695 16.0890025 16.0668603 19.7520632
## [25] 11.9522383 14.0763632 11.1867779 13.9590831 11.3073427 9.1572922
## [31] 9.6879306 6.6223863 3.8543482 12.8896858 15.1610026 13.2341981
## [37] 18.1894475 15.7842960 8.8800901 2.4787093 9.4263461 19.5995918
## [43] 13.1854465 18.9434949 19.9212449 15.7525871 22.4085698 2.4787093
```

```
## [49] 16.1599505 18.7388367 23.3268943 17.6958752 13.6800585 12.3634947
## [55] 9.6879306 5.1822775 16.2217138 8.5524266 7.6905136 13.6329014
## [61] 11.2313846 14.2528594 15.9642100 11.5388041 17.9681941 20.3434510
## [67] 16.4967876 19.7700784 17.7723381 22.1843188 7.4259006 23.3054500
## [73] 14.4618118 19.4385185 22.6967839 17.4314658 14.3228489 22.4531512
## [79] 14.1472259 22.4531512 9.5469367 20.8532012 10.6233705 4.1405314
## [85] 9.5991666 20.8051917 21.2333700 15.1044364 9.2273506 13.8976257
## [91] 15.4642814 15.3669776 19.3944322 17.5540309 20.0961688 12.5640758
## [97] 19.5667064 18.8452647 11.8682770 14.7018366 7.2899931 22.6305988
## [103] 13.4217734 21.0678903 20.6846803 20.2520122 21.0203711 12.7335777
## [109] 19.7013705 9.9426355 20.6432556 19.4898948 16.0890025 18.4080417
## [115] 19.2316406 11.3954377 18.9962101 18.3614814 2.8028557 23.1115556
## [121] 13.1203658 20.8292103 9.2273506 10.1066315 7.9463199 2.8537694
## [127] 13.7424889 20.2449006 19.3870060 13.9948562 9.6361818 16.2128344
## [133] 18.8452647 2.2680388 18.7844617 13.3362663 9.5469367 11.3073427
## [139] 16.6089133 5.0143793 9.4416100 17.0837935 13.8512093 16.6690132
## [145] 20.0961688 6.0709143 15.9732276 13.1584194 8.8399095 6.6974622
## [151] 15.3576040 15.0948998 7.5402918 22.9160206 19.3944322 3.0239048
## [157] 17.4314658 12.6038089 14.4271965 20.3434510 17.7441821 15.0948998
## [163] 20.0035997 17.0629423 15.2034207 9.6511139 9.9426355 8.9919964
## [169] 20.3505282 0.3794733 18.9510950 17.7804387 10.6233705 15.7751704
## [175] 5.1131204 20.0712730 20.7811453 20.6916408 5.3050919 23.3268943
## [181] 21.0272205 9.7394045 21.1694119 12.2940636 14.6677878 18.3069386
## [187] 22.8066657 2.2680388 3.8915293 11.3073427 21.8207241 18.5163711
## [193] 9.3196566 23.1331796 10.9610219 13.1093860 18.4080417 15.8159413
## [199] 22.6084940 6.8451443 19.7194320 13.0055373 8.0711833 2.4199174
## [205] 9.0079964 16.1819653 13.6434600 13.2987217 20.3259440 4.1056059
## [211] 7.0102782 14.7358067 18.1067943 20.9250090 21.6366356 11.9939985
## [217] 19.1795725 8.4346903 21.1389688 20.2766861 20.2025741 18.2169152
## [223] 15.6797959 7.2702132 20.5634627 13.9948562 15.0380850 19.8205953
## [229] 6.7189285 16.2436449 18.0237621 13.9232180 8.7095350 16.7587589
## [235] 18.1423262 20.4485696 18.4893483 22.4754088 12.9172753 8.3579902
## [241] 20.4415264 6.9897067 13.3844686 15.9642100 16.5183534 9.6511139
## [247] 18.1343872 17.5540309 14.6238162 16.5485951
```

(e) How many values in yVec are within 200 of the maximum value of the terms in yVec?

```
length(yVec[yVec > max(yVec) - 200])
```

```
## [1] 57
```

(f) How many numbers in xVec are divisible by 2? (Note that the modulo operator is denoted %%.)

```
length(xVec[xVec %% 2 == 0])
```

```
## [1] 124
```

(g) Sort the numbers in the vector xVec in the order of increasing values in yVec.

```
xVec[order(yVec)]
```

```
## [1] 405 842 308 572 461 8 256 507 373 639 42 616 29 645 376 669 688
## [18] 197 63 638 862 77 996 93 59 585 661 72 339 20 206 537 174 322
## [35] 42 603 425 48 707 452 477 99 224 811 715 358 963 222 395 543 480
## [52] 193 683 710 691 954 700 614 787 835 275 435 309 368 224 460 497 944
## [69] 530 765 523 171 870 807 469 828 624 200 713 365 781 74 129 76 701
## [86] 760 193 866 353 168 967 545 920 541 650 148 277 18 667 865 987 120
## [103] 655 1 554 699 311 458 632 84 269 82 280 544 17 621 807 113 136
## [120] 457 702 91 625 767 828 109 860 363 121 657 668 324 382 956 299 403
## [137] 74 928 415 38 127 176 678 179 444 724 189 457 513 743 5 10 789
## [154] 38 760 446 986 894 238 640 110 203 533 113 358 977 294 137 258 577
## [171] 55 708 996 863 627 123 515 359 964 324 24 364 260 618 957 48 107
## [188] 631 266 680 478 178 34 900 537 160 274 437 285 505 19 188 190 467
## [205] 852 803 517 69 399 768 545 408 676 407 972 437 353 371 390 995 652
## [222] 148 458 501 124 216 880 836 878 357 660 44 197 578 293 324 49 646
## [239] 543 256 511 525 339 263 14 257 278 61 840 956
```

(h) Pick out the elements in `yVec` at index positions 1, 4, 7, 10, 13, . . .

```
yVec[c(1:83) * 3 - 2]
```

```
## [1] 709 517 437 783 671 860 581 347 279 974 216 776 538 460 985 248 317
## [18] 288 687 957 938 101 615 285 106 414 881 488 484 791 246 643 845 553
## [35] 465 87 993 116 473 635 310 428 965 19 489 803 604 800 175 516 902
## [52] 689 881 593 835 398 358 850 791 915 665 167 866 942 320 482 216 488
## [69] 681 273 884 970 469 717 127 952 284 695 325 777 792 72 738
```

8. By using the function `cumprod` or otherwise, calculate

$$1 + \frac{2}{3} + \left(\frac{2}{3}\frac{4}{5}\right) + \left(\frac{2}{3}\frac{4}{5}\frac{6}{7} + \dots + \left(\frac{2}{3}\frac{4}{5}\dots\frac{38}{39}\right)\right)$$

```
sum(
  cumprod(
    seq(from = 2, to = 38, by = 2) / seq(from = 3, to = 39, by = 2)
  )
) + 1
```

```
## [1] 6.976346
```
