Contents

1. Basic	2
1.1. pbds.h	
2. Ds	
2.1. bst.h	3
2.2. dsu.h	5
2.3. segTree_add.h	
2.4. segTree_add_setto.h	
2.5. segTree MX MI.h	
2.6. ST.h	
2.7. twoDimPrfxSum.h	15
3. Geo	17
3.1. Rotating_Calipers.h	17
4. Graph	
4.1. Flow	19
4.1.1. max_Flow_print.h	19
4.1.2. min_Cost.h	21
4.2. Tree	24
4.2.1. hld.h	24
4.2.2. lca.h	25
5. Матн	27
5.1. Number_theory	27
5.1.1. basic.h	27
5.1.2. Comb.h	28
5.1.3. CRT.h	29
5.1.4. Eular_phi.h	30
5.1.5. Eular_sieve.h	31
5.1.6. factor_pr.h	32
5.2. Other	36
5.2.1. Frac.h	36
6. String	38
6.1. AC_automaton.h	38
6.2. compress_print.h	40
6.3. get_occr.h	41
6.4. hash_print.h	42
6.5. KMP.h	44
6.6. trie Tree.h	45

1. Basic

1.1. pbds.h

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
using namespace std;
using ord_set = tree<int, null_type, less<int>, rb_tree_tag,
tree_order_statistics_node_update>;
using ord_mset = tree<int, null_type, less_equal<int>, rb_tree_tag,
tree_order_statistics_node_update>;
//find_by_order
//order_of_key
```

2. Ds

2.1. bst.h

```
const int N=1e5+100;
2
   struct node{
3
      int s[2];
4
      int v,p,cnt,sz;
5
      void init(int p1,int v1){
6
        p=p1;v=v1;
7
        cnt=sz=1;
8
      }
    }tr[N];
9
10
    int root=0,idx=0;
    void pushup(int x){
11
12
      tr[x].sz=tr[x].cnt+tr[tr[x].s[1]].sz+tr[tr[x].s[0]].sz;
13
    }
14
    void rotate(int x){
15
      int y=tr[x].p;
16
      int z=tr[y].p;
17
      int k=tr[y].s[1]==x;
18
      tr[y].s[k]=tr[x].s[k^1];
      tr[tr[x].s[k^1]].p=y;
19
      tr[z].s[tr[z].s[1]==y]=x;
20
21
      tr[x].p=z;
      tr[y].p=x;
23
      tr[x].s[k^1]=y;
      pushup(y);pushup(x);
24
    }
25
26
    void splay(int x,int k){s
27
      while(tr[x].p!=k){
28
        int y=tr[x].p;
29
        int z=tr[y].p;
        if(z!=k) (tr[y].s[0]==x)^(tr[z].s[0]==y) ? rotate(x) : rotate(y);
30
31
        rotate(x);
32
33
      if(k==0) root=x;
34
   }
35
    void find(int v){
36
      int x=root;
      while(tr[x].v!=v && tr[x].s[v>tr[x].v] ) x=tr[x].s[v>tr[x].v];
37
38
      splay(x,0);
39
    }
40
    int get_pre(int v){
41
      find(v);
42
      int x=root;
      if(tr[x].v<v) return x;</pre>
43
44
      x=tr[x].s[0];
45
      while(tr[x].s[1]) x=tr[x].s[1];
46
      splay(x,0);
47
      return x;
   }
48
49
    int get_suc(int v){
50
      find(v);
51
      int x=root;
52
      if(tr[x].v>v) return x;
53
      x=tr[x].s[1];
```

```
54
       while(tr[x].s[0]) x=tr[x].s[0];
55
       splay(x, 0);
56
      return x;
57
    }
58
    void del(int v){
59
       int pre=get_pre(v);
       int suc=get_suc(v);
60
61
       splay(pre,0);splay(suc,pre);
       int d=tr[suc].s[0];
62
       if(tr[d].cnt>1){
63
64
         tr[d].cnt--;splay(d,0);
65
66
       else{
67
         tr[suc].s[0]=0;splay(suc,0);
68
       }
69
    }
70
    void insert(int v){
71
       int x=root;
72
       int p=0;
       while(x && tr[x].v!=v){
73
74
         p=x;x=tr[x].s[v>tr[x].v];
75
76
       if(x) tr[x].cnt++;
77
       else{
78
         x=++idx;
79
         tr[p].s[v>tr[p].v]=x;
80
         tr[x].init(p,v);
81
82
       splay(x,0);
83
    }
84
    int get_rank(int v){
85
      insert(v);
       int res=tr[tr[root].s[0]].sz;
86
87
       del(v);
88
       return res;
89
    }
90
    int get val(int k){
91
       int x=root;
92
      while(1){
93
         int y=tr[x].s[0];
94
         if(tr[x].cnt+tr[y].sz<k){</pre>
95
           k-=tr[y].sz+tr[x].cnt;
96
           x=tr[x].s[1];
97
         }
         else{
98
99
           if(tr[y].sz>=k) x=tr[x].s[0];
100
           else break;
101
         }
102
103
       splay(x,0);
104
       return tr[x].v;
105
    }
```

2.2. dsu.h

```
class DSU {
2
        std::vector<int> f, siz;
3
   public:
        DSU() {}
4
5
        DSU(int n) {
6
            init(n);
7
8
        void init(int n) {
9
10
            f.resize(n);
11
            for(int i = 0;i < n;i ++) f[i] = i;</pre>
12
            siz.assign(n, 1);
13
        }
14
        int find(int x) {
15
16
            while (x != f[x]) {
17
                 x = f[x] = f[f[x]];
18
19
            return x;
20
        }
21
        bool same(int x, int y) {
22
23
            return find(x) == find(y);
24
25
26
        bool merge(int x, int y) {
27
            x = find(x);
28
            y = find(y);
29
            if (x == y) {
30
                 return false;
31
            siz[x] += siz[y];
32
33
            f[y] = x;
34
            return true;
35
        }
36
37
        int size(int x) {
            return siz[find(x)];
38
39
        }
40
    };
```

2.3. segTree_add.h

```
1 // AC 带懒惰标记线段树
template <class TYPE NAME>
   class lazyTree
4
   {
5
6
          TYPE_NAME 需要支持: + += != 和自定义的合并运算符
7
          实现了懒惰标记, 仅支持区间批量增加
        * 区间批量减需要 TYPE_NAME 支持-, 且有-a = 0 - a
8
9
        * 额外处理了一个单点修改为对应值的函数, 非原生实现, 其复杂度为 4logn
10
        * 不提供在线
11
        * 不提供持久化
        */
12
13
   private:
14
       vector<TYPE_NAME> d;
15
       vector<TYPE_NAME> a;
16
       vector<TYPE_NAME> b;
17
       const TYPE NAME INI = 0; // 不会影响合并运算的初始值,如 max 取 INF, min 取 0,
18
   mti 取 1
19
20
       void subbuild(int s, int t, int p)
21
       {
22
           if (s == t)
23
           {
24
              d[p] = a[s];
25
              return;
26
27
           int m = s + ((t - s) >> 1); // (s+t)/2
           subbuild(s, m, p * 2);
28
           subbuild(m + 1, t, p * 2 + 1);
29
           d[p] = d[p * 2] + d[p * 2 + 1];
30
31
               合并运算符 ↑
32
       }
33
       TYPE_NAME subGetSum(int 1, int r, int s, int t, int p)
34
35
36
           if (1 <= s && t <= r)
37
              return d[p];
           int m = s + ((t - s) >> 1);
38
           if (b[p] != 0)
39
40
              d[p * 2] += b[p] * (m - s + 1); // 合并运算符的高阶运算 此处运算为应
   用懒惰标记
              d[p * 2 + 1] += b[p] * (t - m); // 合并运算符的高阶运算 此处运算为应
42
   用懒惰标记
43
                                           // 下传标记, 无需修改
              b[p * 2] += b[p];
44
                                           // 下传标记, 无需修改
              b[p * 2 + 1] += b[p];
45
              b[p] = 0;
46
47
           TYPE NAME ansl = INI;
           TYPE NAME ansr = INI;
48
           if (1 <= m)
49
              ansl = subGetSum(1, r, s, m, p * 2);
50
           if (r > m)
51
52
              ansr = subGetSum(1, r, m + 1, t, p * 2 + 1);
```

```
53
            return ansl + ansr;
            // 合并运算符↑
54
55
        }
56
57
        void subUpdate(int 1, int r, TYPE_NAME c, int s, int t, int p)
58
            if (1 <= s && t <= r)
59
60
            {
               d[p] += (t - s + 1) * c; // 合并运算符的高阶运算 此处运算为修改整匹配
61
    区间值
                                      // 记录懒惰标记, 无需修改
62
               b[p] += c;
               return;
63
64
            }
65
            int m = s + ((t - s) >> 1);
            if (b[p] != 0 && s != t)
66
67
            {
               d[p * 2] += b[p] * (m - s + 1); // 合并运算符的高阶运算 此处运算为应
68
    用懒惰标记
               d[p * 2 + 1] += b[p] * (t - m); // 合并运算符的高阶运算 此处运算为应
69
    用懒惰标记
                                              // 下传标记, 无需修改
70
               b[p * 2] += b[p];
71
               b[p * 2 + 1] += b[p];
                                         // 下传标记, 无需修改
72
               b[p] = 0;
73
            }
           if (1 <= m)
74
75
                subUpdate(1, r, c, s, m, p * 2);
            if(r > m)
76
               subUpdate(1, r, c, m + 1, t, p * 2 + 1);
78
           d[p] = d[p * 2] + d[p * 2 + 1];
79
                合并运算符 ↑
80
        }
81
82
    public:
83
        lazyTree(TYPE_NAME _n)
84
        {
85
            n = _n;
            d.resize(4 * n + 5);
86
            a.resize(4 * n + 5);
87
            b.resize(4 * n + 5);
88
89
        }
90
91
        void build(vector<TYPE_NAME> _a)
92
        {
93
            a = _a;
94
            subbuild(1, n, 1);
95
        }
96
97
        TYPE NAME getsum(int 1, int r)
98
99
            return subGetSum(l, r, 1, n, 1);
100
        }
101
102
        void update(int 1, int r, TYPE_NAME c) // 修改区间
103
        {
104
            subUpdate(1, r, c, 1, n, 1);
105
        }
106
```

```
void update(int idx, TYPE_NAME tar)
{    // 修改单点, 未测试

    TYPE_NAME tmp = getsum(idx, idx);
    tar -= tmp;
    subUpdate(idx, idx, tar, 1, n, 1);
}

113 };
```

2.4. segTree add setto.h

```
template <typename T>
   class SegTreeLazyRangeSet {
3
      vector<T> tree, lazy;
4
      vector<T> *arr;
5
      vector<bool> ifLazy;
6
      int n, root, n4, end;
7
      void maintain(int cl, int cr, int p) {
8
        int cm = cl + (cr - cl) / 2;
9
        if (cl != cr && ifLazy[p]) {
10
11
          lazy[p * 2] = lazy[p], ifLazy[p*2] = 1;
          lazy[p * 2 + 1] = lazy[p], ifLazy[p*2+1] = 1;
13
          tree[p * 2] = lazy[p] * (cm - cl + 1);
14
          tree[p * 2 + 1] = lazy[p] * (cr - cm);
15
          lazy[p] = 0;
16
          ifLazy[p] = 0;
        }
17
      }
18
19
      T range_sum(int 1, int r, int cl, int cr, int p) {
20
        if (1 <= cl && cr <= r) return tree[p];</pre>
        int m = cl + (cr - cl) / 2;
        T sum = 0;
23
24
        maintain(cl, cr, p);
25
        if (1 <= m) sum += range_sum(1, r, c1, m, p * 2);</pre>
26
        if (r > m) sum += range_sum(1, r, m + 1, cr, p * 2 + 1);
27
        return sum;
28
      }
29
      void range_set(int l, int r, T val, int cl, int cr, int p) {
30
31
        if (1 <= c1 && cr <= r) {
32
          lazy[p] = val;
33
          ifLazy[p] = 1;
          tree[p] = (cr - cl + 1) * val;
34
35
          return;
36
37
        int m = cl + (cr - cl) / 2;
38
        maintain(cl, cr, p);
39
        if (1 <= m) range_set(1, r, val, cl, m, p * 2);</pre>
40
        if (r > m) range_set(l, r, val, m + 1, cr, p * 2 + 1);
41
        tree[p] = tree[p * 2] + tree[p * 2 + 1];
42
      }
43
      void build(int s, int t, int p) {
44
45
        if (s == t) {
46
          tree[p] = (*arr)[s];
47
          return;
48
49
        int m = s + (t - s) / 2;
50
        build(s, m, p * 2);
51
        build(m + 1, t, p * 2 + 1);
        tree[p] = tree[p * 2] + tree[p * 2 + 1];
52
      }
53
54
     public:
      explicit SegTreeLazyRangeSet<T>(vector<T> v) {
56
57
        n = v.size();
```

```
58
        n4 = n * 4;
59
        tree = vector<T>(n4, 0);
        lazy = vector<T>(n4, 0);
60
61
        ifLazy = vector<bool>(n4,0);
62
        arr = \&v;
        end = n - 1;
63
64
        root = 1;
        build(0, end, 1);
65
        arr = nullptr;
66
67
      }
68
      void show(int p, int depth = 0) {
69
        if (p > n4 || tree[p] == 0) return;
70
        show(p * 2, depth + 1);
71
        for (int i = 0; i < depth; ++i) putchar('\t');</pre>
72
73
        printf("%d:%d\n", tree[p], lazy[p]);
74
        show(p * 2 + 1, depth + 1);
      }
75
76
77
      T range_sum(int 1, int r) { return range_sum(1, r, 0, end, root); }
      void range_set(int 1, int r, T val) { range_set(1, r, val, 0, end, root); }
79
80
    };
```

2.5. segTree MX MI.h

```
//AC MJ 的 MIN/MAX 树
   template<class Info>
3
   struct SegmentTree {
4
        int n;
5
        std::vector<Info> info;
6
        SegmentTree() : n(0) {}
7
        SegmentTree(int n_, Info v_ = Info()) {
            init(n_, v_);
8
9
        }
10
        template<class T>
11
        SegmentTree(std::vector<T> init_) {
12
            init(init_);
13
14
        void init(int n_, Info v_ = Info()) {
15
            init(std::vector(n_, v_));
16
17
        template<class T>
18
        void init(std::vector<T> init_) {
19
            n = init_.size();
            info.assign(4 << std::__lg(n), Info());</pre>
20
            std::function<void(int, int, int)> build = [&](int p, int l, int r) {
21
22
                if (r - 1 == 1) {
23
                     info[p] = init_[1];
24
                     return;
                }
25
26
                int m = (1 + r) / 2;
27
                build(2 * p, 1, m);
                build(2 * p + 1, m, r);
28
29
                pull(p);
30
            };
31
            build(1, 0, n);
32
        void pull(int p) {
            info[p] = info[2 * p] + info[2 * p + 1];
34
35
36
        void modify(int p, int l, int r, int x, const Info &v) {
37
            if (r - 1 == 1) {
38
                info[p] = v;
39
                return;
40
41
            int m = (1 + r) / 2;
42
            if (x < m) {
43
                modify(2 * p, 1, m, x, v);
44
            } else {
45
                modify(2 * p + 1, m, r, x, v);
46
            }
47
            pull(p);
48
        void modify(int p, const Info &v) {
49
50
            modify(1, 0, n, p, v);
51
        Info rangeQuery(int p, int l, int r, int x, int y) {
52
            if (1 >= y || r <= x) {
53
54
                return Info();
55
56
            if (1 >= x \&\& r <= y) {
```

```
57
                 return info[p];
58
             }
             int m = (1 + r) / 2;
59
             return rangeQuery(2 * p, 1, m, x, y) + rangeQuery(2 * p + 1, m, r, x,
60
    y);
61
         Info rangeQuery(int 1, int r) {
62
63
            return rangeQuery(1, 0, n, 1, r);
64
65
        template<class F>
66
         int findFirst(int p, int l, int r, int x, int y, F &&pred) {
67
             if (1 >= y || r <= x) {
68
                 return -1;
69
70
             if (1 >= x \&\& r <= y \&\& !pred(info[p])) {
71
                 return -1;
72
             }
73
             if (r - 1 == 1) {
74
                 return 1;
75
             }
76
             int m = (1 + r) / 2;
77
             int res = findFirst(2 * p, 1, m, x, y, pred);
78
             if (res == -1) {
79
                 res = findFirst(2 * p + 1, m, r, x, y, pred);
80
81
             return res;
82
         }
83
        template<class F>
84
         int findFirst(int 1, int r, F &&pred) {
85
             return findFirst(1, 0, n, l, r, pred);
86
         }
87
         template<class F>
88
         int findLast(int p, int l, int r, int x, int y, F &&pred) {
89
             if (1 >= y || r <= x) {
90
                 return -1;
91
92
             if (1 >= x && r <= y && !pred(info[p])) {
93
                 return -1;
94
             if (r - 1 == 1) {
95
96
                 return 1;
97
             }
98
             int m = (1 + r) / 2;
99
             int res = findLast(2 * p + 1, m, r, x, y, pred);
100
             if (res == -1) {
101
                 res = findLast(2 * p, 1, m, x, y, pred);
102
103
             return res;
104
         }
         template<class F>
106
         int findLast(int 1, int r, F &&pred) {
             return findLast(1, 0, n, l, r, pred);
107
108
109
    };
    const int inf = 1E9;
110
    struct Info
112
    {
```

```
113
        int mn {inf}, mnId, mx {-inf}, mxId;
114
    };
    Info operator+(Info a, Info b)
115
116
        if (a.mn > b.mn)
117
118
            a.mn = b.mn, a.mnId = b.mnId;
        if (a.mx < b.mx)</pre>
119
120
            a.mx = b.mx, a.mxId = b.mxId;
121
        return a;
122
```

2.6. ST.h

```
class SparseTable
2
    {
        using func_type = function<int(const int &, const int &)>;
3
4
5
        vector<vector<int>> ST;
6
        int len;
7
        vector<int> preLog;
8
        func_type op;
        static int default_func(const int &t1, const int &t2) { return max(t1,
9
    t2); }
10
   public:
11
        void build(const vector<int> &v, func_type _func = default_func)
13
14
            op = _func;
            len = v.size();
15
16
            int l1 = ceil(log2(len)) + 1;
17
            ST.assign(len, vector<int>(l1, 0));
            for (int i = 0; i < len; ++i)</pre>
18
19
            {
20
                ST[i][0] = v[i];
            }
            for (int j = 1; j < l1; ++j)
23
24
                 int pj = (1 << (j - 1));
25
                 for (int i = 0; i + pj < len; ++i)</pre>
26
                 {
                     ST[i][j] = op(ST[i][j-1], ST[i+(1 << (j-1))][j-1]);
                 }
28
29
            }
            preLog.resize(len + 1);
30
31
            lop(i, 1, len + 1) preLog[i] = floor(log2(i));
32
        }
33
        int getsum(int 1, int r)
34
35
            if (r < 1)
36
37
                 return 0;
38
            1 = \max(0, 1), r = \min(len - 1, r);
39
            if (r == 0)
                 return 0;
40
            int lt = r - l + 1;
41
            int q = preLog[lt];
42
43
            return op(ST[1][q], ST[r - (1 << q) + 1][q]);</pre>
44
        }
45
    };
```

2.7. twoDimPrfxSum.h

```
1
    class prfx 2{
2
    public:
3
        vector<vector<int>> mtx;
4
        int n,m;
5
        public:
6
        prfx_2(vector<vector<int>> _mtx){init(_mtx);};
7
        prfx_2() { };
        void init(vector<vector<int>> _mtx)
8
9
10
            n = _mtx.size();
11
            m = _mtx[0].size();
12
            mtx.resize(n+1);
13
            for(auto &x:mtx) x.resize(m+1);
14
            lop(i,1,n+1)
15
                lop(j,1,m+1)
                    mtx[i][j] = mtx[i-1][j] + mtx[i][j-1] - mtx[i-1][j-1] +
16
    _mtx[i-1][j-1];
17
18
19
        int getsum(int x1,int y1,int x2,int y2)
20
            x1 ++,x2 ++,y1 ++,y2 ++;
            return mtx[x2][y2] - mtx[x1-1][y2] - mtx[x2][y1-1] + mtx[x1-1][y1-1];
23
24
        int getsum(pii d1,pii d2)
26
27
            auto [x1,y1] = d1;
28
            auto [x2,y2] = d2;
29
            x1 ++,x2 ++,y1 ++,y2 ++;
            return mtx[x2][y2] - mtx[x1-1][y2] - mtx[x2][y1-1] + mtx[x1-1][y1-1];
30
31
        }
        vector<int> & operator[](std::size t i)
34
35
            return mtx[i];
36
        }
37
38
    };
39
40
    class conj diff 2{
41
        vector<vector<int>> mtx;
42
        vector<vector<int>> prf;
43
        int n,m;
44
        public:
45
        conj_diff_2(int _n,int _m)
46
47
48
            n = n+1, m = m+1;
49
            vector<vector<int>> initmp(n, vector<int> (m,0));
50
            init(initmp);
51
        }
52
53
        conj_diff_2(vector<vector<int>> _mtx)
54
55
            this->init(_mtx);
        }
56
```

```
57
58
        conj_diff_2(){ }
59
        void init(vector<vector<int>> _mtx)
60
61
62
             n = mtx.size();
            m = mtx[0].size();
63
            mtx.resize(n+2);
64
65
            for(auto &x:mtx) x.resize(m+2);
             prf.resize(n+2);
66
67
             for(auto &x:prf) x.resize(m+2);
68
            lop(i,1,n+1)
69
                 lop(j,1,m+1)
70
                     prf[i][j] = _mtx[i-1][j-1];
71
        }
72
        void modify(int x1,int y1,int x2,int y2,int k)
73
74
75
             x1 ++,x2 ++,y1 ++,y2 ++;
76
            mtx[x1][y1] += k;
            mtx[x2+1][y1] -= k, mtx[x1][y2+1] -= k;
77
            mtx[x2+1][y2+1] += k;
78
79
        }
80
        void modify(pii d1,pii d2,int k)
81
82
83
             this->modify(d1.fi,d1.se,d2.fi,d2.se,k);
84
        }
85
86
        vector<vector<int>> cacu()
87
88
             auto res = prfx_2(mtx);
             vector<vector<int>> rst(n,vector<int>(m));
89
90
             lop(i,1,n+1)
91
                 lop(j,1,m+1)
                     rst[i-1][j-1] = prf[i][j] + res[i+1][j+1];
92
93
             return rst;
94
        }
95
        vector<int> & operator[](std::size t i)
96
97
        {
98
             return mtx[i];
99
         }
100
    };
```

3. Geo

3.1. Rotating_Calipers.h

```
1 //Rotating_Calipers
template<typename VALUE_TYPE>
class Rotating_Calipers
4 {
5 public:
        using pv = pair<VALUE TYPE, VALUE TYPE>;
6
7
        using vec_pv = vector<pair<VALUE_TYPE, VALUE_TYPE>>;
8
        vec_pv p;
9
10
        static VALUE TYPE cross(pv p1, pv p2, pv p0)
11
            pv t1 = {p1.fi - p0.fi, p1.se - p0.se},
               t2 = {p2.fi - p0.fi, p2.se - p0.se};
13
14
            return t1.fi * t2.se - t1.se * t2.fi;
15
        }
16
        static VALUE_TYPE dis(const pv &p1,const pv &p2){
17
            return (p1.fi - p2.fi) * (p1.fi - p2.fi) + (p1.se - p2.se) * (p1.se -
18
    p2.se);
19
        };
20
21
    public:
22
23
        Rotating Calipers() {}
24
25
        Rotating_Calipers(vec_pv _A) {
26
            build( A);
27
28
29
        void build(const vec_pv & _A) {
30
            p = ConvexHull( A);
31
        }
32
        static vec_pv ConvexHull(vec_pv A, VALUE_TYPE flag = 1)
33
34
35
            int n = A.size();
36
            if (n <= 2) return A;</pre>
            vec_pv ans(n * 2);
37
            sort(A.begin(), A.end(),
38
39
            [](pv a,pv b) -> bool {
40
                if(fabs(a.fi - b.fi) < 1e-10)</pre>
41
                     return a.se < b.se;</pre>
42
                else return a.fi < b.fi;}</pre>
43
            int now = -1;
44
            for (int i = 0; i < n; i++)
45
            { // 维护下凸包
                while (now > 0 && cross(A[i], ans[now], ans[now - 1]) < flag)</pre>
46
    now--;
47
                ans[++now] = A[i];
48
            }
49
            int pre = now;
50
            for (int i = n - 2; i >= 0; i--)
            { // 维护上凸包
51
```

```
while (now > pre && cross(A[i], ans[now], ans[now - 1]) < flag)</pre>
52
    now--;
53
                 ans[++now] = A[i];
54
             }
55
             ans.resize(now);
56
             return ans;
57
58
        VALUE_TYPE getDiameter() {
59
60
             int j = 1;
             VALUE_TYPE ans = 0;
61
             int m = p.size();
62
63
             p.push_back(p[0]);
64
             for(int i = 0;i < m;i ++)</pre>
65
                 while (cross(p[i+1],p[j],p[i]) > cross(p[i+1],p[j+1],p[i])) j =
66
    (j+1)%m;
                 ans = \max(ans, \max(dis(p[i],p[j]), dis(p[i+1],p[j])));
67
68
             }
69
             p.pop_back();
70
             return ans;
71
        }
72
73
        VALUE_TYPE getPerimeter() {
74
             VALUE_TYPE sum = 0;
75
             p.pb(p[0]);
76
             for(int i = 0;i < (int)p.size() - 1;i ++)</pre>
77
             {
78
                 sum += sqrtl(dis(p[i],p[i+1]));
79
             p.pop_back();
80
81
             return sum;
82
        }
83
84
    };
```

4. GRAPH

4.1. FLOW

4.1.1. max_Flow_print.h

```
class maxFlow//AC
2
   {
3
   private:
4
        class edge
5
        {
        public:
6
7
            11 int nxt, cap, flow;
8
            pair<int, int> revNodeIdx;
9
        public:
10
            edge(int nxt, int cap)
11
            {
12
                nxt = _nxt,cap = _cap,flow = 0;
13
14
            void setRevIdx(int _i, int _j) { revNodeIdx = {_i,_j}; }
15
        };
16
        vector<vector<edge>> edgeList;
17
        vector<int> dep,fir;
18
        11 int maxFlowAns;
19
        int T, S;
20
    public:
21
        maxFlow(int _n)
22
23
            maxFlowAns = 0;
24
            S = 1;
            T = n;
            edgeList.resize(_n + 1);
26
27
            dep.resize(_n + 1);
            fir.resize(_n+1);
28
29
        void resetTS(int _T, int _S) { T = _T,S = _S; }
30
        void addedge(int _u, int _v, int _w)
32
33
34
            edgeList[_u].push_back(edge(_v, _w));
35
            edgeList[_v].push_back(edge(_u, 0));
            edgeList[_u][edgeList[_u].size() - 1].setRevIdx(_v,
36
    edgeList[_v].size() - 1);
            edgeList[_v][edgeList[_v].size() - 1].setRevIdx(_u,
37
    edgeList[_u].size() - 1);
38
        }
39
40
        bool bfs()
41
        {
42
            queue<int> que;
43
            for (auto x = dep.begin(); x != dep.end(); x++) (*x) = 0;
44
            dep[S] = 1;
45
            que.push(S);
46
            while (que.size())
47
                 11 int at = que.front();
48
49
                que.pop();
```

```
50
                for (int i = 0; i < edgeList[at].size(); i++)</pre>
51
                {
                    auto tar = edgeList[at][i];
53
                    if ((!dep[tar.nxt]) && (tar.flow < tar.cap))</pre>
54
55
                        dep[tar.nxt] = dep[at] + 1;
                        que.push(tar.nxt);
56
57
                    }
                }
58
59
60
            return dep[T];
61
        }
62
        11 int dfs(int at, 11 int flow)
63
64
        {
65
            if ((at == T) || (!flow))
                return flow; // 到了或者没了
66
            ll int ret = 0; // 本节点最大流
67
            for (int &i = fir[at]; i < edgeList[at].size(); i++)</pre>
68
69
70
                auto tar = edgeList[at][i];
                                              // 目前遍历的边
71
                int tlFlow = 0; // 目前边的最大流
72
                if (dep[at] == dep[tar.nxt] - 1) // 遍历到的边为合法边
73
                    tlFlow = dfs(tar.nxt, min((ll)tar.cap - tar.flow, flow -
74
    ret));
                    if (!tlFlow)
75
                                    // 若最大流为 0, 什么都不做
76
                        continue;
                                   // 本节点最大流累加
77
                    ret += tlFlow;
78
                    edgeList[at][i].flow += tlFlow; // 本节点实时流量
                    edgeList[tar.revNodeIdx.first][tar.revNodeIdx.second].flow -=
79
    tlFlow; // 反向边流量
80
                    if (ret == flow)
81
                        return ret; // 充满了就不继续扫了
82
                }
83
84
            return ret;
85
        }
86
        11 int dinic()
87
88
89
            if (maxFlowAns)
90
                return maxFlowAns;
91
            while (bfs())
92
            {
93
                for(auto x = fir.begin(); x != fir.end(); x ++) (*x) = 0;
94
                maxFlowAns += dfs(S, INT_MAX);
95
96
            return maxFlowAns;
97
        }
98
    };
```

4.1.2. min_Cost.h

```
1
   const int INF = 0x3f3f3f3f
2
3
   class PD//AC
4 {
5
   public:
6
        class edge
7
        {
8
        public:
9
            int v, f, c, next;
10
            edge(int _v,int _f,int _c,int _next)
11
                v = _v,f = _f,c = _c,next = _next;
12
13
            }
14
            edge() { }
15
        };
16
        void vecset(int value, vector<int> &arr)
17
18
            for(int i = 0;i < arr.size();i ++) arr[i] = value;</pre>
19
20
21
        }
22
        class node
23
24
        {
25
        public:
26
           int v, e;
27
28
29
        class mypair
30
31
        public:
            int dis, id;
32
33
34
            bool operator<(const mypair &a) const { return dis > a.dis; }
35
36
            mypair(int d, int x)
37
38
                dis = d;
39
                id = x;
            }
40
41
        };
42
        vector<int> head,dis,vis,h;
43
44
        vector<edge> e;
45
        vector<node> p;
46
        int n, m, s, t, cnt = 1, maxf, minc;
47
        PD(int _n,int _m,int _s,int _t)
48
49
50
            n = _n, m = _m, s = _s, t = _t;
51
            maxf = 0, minc = 0;
            head.resize(n+2), dis.resize(n+2), vis.resize(n+2);
52
53
            e.resize(2);
54
            h.resize(n+2), p.resize(m+2);
55
        }
56
57
        void addedge(int u, int v, int f, int c)
58
        {
```

```
59
             e.push_back(edge(v,f,c,head[u]));
60
             head[u] = e.size()-1;
             e.push_back(edge(u,0,-c,head[v]));
61
62
             head[v] = e.size()-1;
63
         }
64
         bool dijkstra()
65
66
67
             priority_queue<mypair> q;
68
             vecset(INF,dis);
             vecset(0,vis);
69
70
             dis[s] = 0;
71
             q.push(mypair(0, s));
72
             while (!q.empty())
73
74
                 int u = q.top().id;
75
                 q.pop();
76
                  if (vis[u])
77
                      continue;
78
                 vis[u] = 1;
79
                 for (int i = head[u]; i; i = e[i].next)
80
                      int v = e[i].v, nc = e[i].c + h[u] - h[v];
81
82
                      if (e[i].f && dis[v] > dis[u] + nc)
83
                      {
84
                          dis[v] = dis[u] + nc;
85
                          p[v].v = u;
86
                          p[v].e = i;
87
                          if (!vis[v])
88
                              q.push(mypair(dis[v], v));
89
                      }
90
                 }
91
92
             return dis[t] != INF;
93
         }
94
95
         void spfa()
96
97
             queue<int> q;
98
             vecset(63,h);
99
             h[s] = 0, vis[s] = 1;
100
             q.push(s);
             while (!q.empty())
101
102
                 int u = q.front();
103
104
                 q.pop();
105
                 vis[u] = 0;
106
                 for (int i = head[u]; i; i = e[i].next)
107
108
                      int v = e[i].v;
109
                      if (e[i].f && h[v] > h[u] + e[i].c)
110
                          h[v] = h[u] + e[i].c;
111
                          if (!vis[v])
                          {
114
                              vis[v] = 1;
                              q.push(v);
                          }
```

```
117
                        }
                   }
118
119
              }
120
          }
          int pd()
124
              spfa();
125
              while (dijkstra())
126
127
                   int minf = INF;
                   for (int i = 1; i <= n; i++)
128
129
                        h[i] += dis[i];
                   for (int i = t; i != s; i = p[i].v)
    minf = min(minf, e[p[i].e].f);
130
131
132
                   for (int i = t; i != s; i = p[i].v)
133
                        e[p[i].e].f -= minf;
134
                        e[p[i].e ^ 1].f += minf;
135
136
                   }
                   maxf += minf;
137
                   minc += minf * h[t];
138
139
140
              return 0;
141
          }
142
143
          pair<int,int> get()
144
145
              return {maxf,minc};
146
          }
147
     };
```

4.2. TREE

4.2.1. hld.h

```
void dfs1(int o) {
      son[o] = -1;
      siz[o] = 1;
3
4
      for (int j = h[o]; j; j = nxt[j])
        if (!dep[p[j]]) {
5
6
          dep[p[j]] = dep[o] + 1;
7
          fa[p[j]] = o;
8
          dfs1(p[j]);
9
          siz[o] += siz[p[j]];
10
          if (son[o] == -1 \mid | siz[p[j]] > siz[son[o]]) son[o] = p[j];
11
        }
12
   }
13
   void dfs2(int o, int t) {
14
      top[o] = t;
16
      cnt++;
17
      dfn[o] = cnt;
18
      rnk[cnt] = o;
      if (son[o] == -1) return;
19
      dfs2(son[o], t); // 优先对重儿子进行 DFS, 可以保证同一条重链上的点 DFS 序连续
20
      for (int j = h[o]; j; j = nxt[j])
22
        if (p[j] != son[o] && p[j] != fa[o]) dfs2(p[j], p[j]);
23
   }
24
   int lca(int u, int v) {
26
      while (top[u] != top[v]) {
27
        if (dep[top[u]] > dep[top[v]])
28
          u = fa[top[u]];
29
        else
          v = fa[top[v]];
30
31
32
      return dep[u] > dep[v] ? v : u;
33
    }
34
    // st 是线段树结构体
35
36
    int querymax(int x, int y) {
37
      int ret = -inf, fx = top[x], fy = top[y];
38
      while (fx != fy) {
39
        if (dep[fx] >= dep[fy])
40
          ret = max(ret, st.query1(1, 1, n, dfn[fx], dfn[x])), x = fa[fx];
41
        else
          ret = max(ret, st.query1(1, 1, n, dfn[fy], dfn[y])), y = fa[fy];
42
43
        fx = top[x];
44
        fy = top[y];
45
      if (dfn[x] < dfn[y])</pre>
46
47
        ret = max(ret, st.query1(1, 1, n, dfn[x], dfn[y]));
48
49
        ret = max(ret, st.query1(1, 1, n, dfn[y], dfn[x]));
50
      return ret;
51
    }
```

4.2.2. lca.h

```
1
    class LCA{
2
    public:
3
        vector<vector<pii>>> cnj;
4
        vector<int> lg,dep;
5
        vector<array<int,32>> fa,wei;
6
        int n;
7
8
         LCA(int n) {
9
             n = _n;
10
             cnj.resize(n+1);
             lg.resize(n+1), fa.resize(n+1), dep.resize(n+1), wei.resize(n+1);
             for(int i = 1; i <= n; i ++)
13
                 lg[i] = lg[i-1] + (1 \leftrightarrow lg[i-1] == i);
14
         }
16
        void addEdge(int u,int v,int w) {
17
             cnj[u].push_back({v,w});
18
             cnj[v].push_back({u,w});
19
         }
20
        void build(int rt = 1) {
21
22
             using itf = function<void(int,int)>;
23
             itf dfs = [\&](int p, int f) \rightarrow void {
24
                 fa[p][0] = f, dep[p] = dep[f] + 1;
25
                 // wei[p][0] = 0;
                 for(int i = 1;i <= lg[dep[p]];i ++) fa[p][i] = fa[fa[p][i-1]]</pre>
26
    [i-1];
                 for(int i = 1; i \leftarrow lg[dep[p]]; i \leftrightarrow ledow in [p][i] = max(wei[p]]
27
    [i-1],wei[fa[p][i-1]][i-1]);
28
                 for(auto [x,w]:cnj[p]) if(x == f) continue;
29
                 else wei[x][0] = w, dfs(x,p);
30
             dfs(rt,0);
31
32
         int get(int x,int y) {
34
             if(dep[x] < dep[y]) swap(x,y);</pre>
35
36
             while(dep[x] > dep[y]) x = fa[x][lg[dep[x] - dep[y]] - 1];
37
             if(x == y) return x;
             for(int k = lg[dep[x]]-1;k \ge 0;k --) if(fa[x][k] != fa[y][k]) x =
38
    fa[x][k],y = fa[y][k];
39
             return fa[x][0];
40
41
         int getmaxw(int x,int y) {
42
43
             int curmx = 0;
             if(dep[x] < dep[y]) swap(x,y);</pre>
44
             while(dep[x] > dep[y]) curmx = max(curmx,wei[x][lg[dep[x] - dep[y]] -
45
    1]), x = fa[x][lg[dep[x] - dep[y]] - 1];
46
             if(x == y) return curmx;
             for(int k = \lg[dep[x]]-1;k >= 0;k --)
47
                 if(fa[x][k] != fa[y][k])
48
49
                     curmx = max(curmx, wei[x][k]), x = fa[x][k],
50
                      curmx = max(curmx,wei[y][k]),y = fa[y][k];
51
             return max({curmx,wei[x][0],wei[y][0]});
52
         }
```

53 };

5. MATH

5.1. Number_theory

5.1.1. basic.h

```
__builtin_ffsll(x)
   // 返回 x 的二进制末尾最后一个 1 的位置
    builtin clzll(x)
4
  // 返回 x 的二进制的前导 0 的个数。
5
    builtin_ctzll(x)
7
  // 返回 x 的二进制末尾连续 0 的个数。
8
9
    builtin clrsbll(x)
// 当 x 的符号位为 Ø 时返回 x 的二进制的前导 Ø 的个数减一, 否则返回 x 的二进制的前导
   1 的个数减一。
12
    __builtin_popcountll(x)
13
14 // 返回 x 的二进制中 1 的个数。
15
__builtin_parity(x)
  // 判断 x 的二进制中 1 的个数的奇偶性。
17
18
  int binpow(int x, int y)
19
20
21
       int res = 1;
       while (y > 0)
23
          if (y & 1)
24
             res = res * x \% mod;
25
26
          x = x * x % mod;
27
          y >>= 1;
28
29
       return res;
   }
30
31
   void exgcd(int a, int b, int& x, int& y) {
32
     if (b == 0) {
33
34
       x = 1, y = 0;
35
       return;
36
37
     exgcd(b, a % b, y, x);
38
     y -= a / b * x;
39
40
binpow(x, mod-2)
```

5.1.2. Comb.h

```
const int N = 1e6;
const int mod = 1e9+7;
3
int binpow(int x, int y)
5 {
        int ans = 1;
6
7
        while (y)
8
9
            if (y & 1) ans = ans * x % mod;
            x = x * x % mod;
10
11
            y >>= 1;
12
        return ans;
13
14
    }
15
   vector<int> fac(N), inv(N);
16
17
   void init()
18
19
    {
        fac[0] = inv[0] = 1;
20
        for (int i = 1; i < N; i++) fac[i] = fac[i - 1] * i % mod;</pre>
21
22
        inv[N-1] = binpow(fac[N-1], mod-2);
23
        for (int i = N - 2; i >= 1; i--)
24
        {
25
            inv[i] = inv[i + 1] * (i + 1) % mod;
26
27
    }
28
29
   auto C = [\&](int x, int y) \rightarrow int
30
31
        return (fac[x] * inv[y] % mod) * inv[x - y] % mod;
32
    };
```

5.1.3. CRT.h

```
int CRT(vector<int> &r, vector<int> &a)
   { // % r === a
        int n = a.size();
3
4
         int128 k = 1, ans = 0;
5
        for (int i = 0; i < n; i++) k *= r[i];
6
        for (int i = 0; i < n; i++)
7
              _int128 m = k / r[i];
8
            int b, y;
9
10
            exgcd(m, r[i], b, y); // b * m mod r[i] = 1
            ans = (ans + a[i] * m * b % k) % k;
11
12
        }
13
        return (ans % k + k) % k;
14
    }
15
    int mul(int a, int b, int m) {
18
19
        return (__int128)a * b % m;
20
    }
21
    int exgcd (int a,int b,int &x,int &y) {
        if (b == 0) \{ x = 1, y = 0; return a; \}
23
24
        int g = exgcd(b, a \% b, x, y), tp = x;
25
        x = y, y = tp - a / b * y;
26
        return g;
27
    };
28
    int EXCRT(vector<int> &a, vector<int> &r) { // % r == a
29
30
        int x, y, k;
31
        int n = r.size();
32
        int M = a[0], ans = r[0];
33
        for (int i = 1; i < n; ++ i) {
            int ca = M, cb = a[i], cc = (r[i] - ans \% cb + cb) \% cb;
34
            int gcd = exgcd(ca, cb, x, y), bg = cb / gcd;
35
            if (cc % gcd != 0) return -1;
36
37
            x = mul(x, cc / gcd, bg);
38
            ans += x * M;
39
            M *= bg;
40
            ans = (ans \% M + M) \% M;
41
42
        return (ans % M + M) % M;
43
```

5.1.4. Eular_phi.h

```
int euler_phi(int n) {
  int ans = n;
  for (int i = 2; i * i <= n; i++)
    if (n % i == 0) {
      ans = ans / i * (i - 1);
      while (n % i == 0) n /= i;
    }
  if (n > 1) ans = ans / n * (n - 1);
  return ans;
}
```

5.1.5. Eular_sieve.h

```
vector<int> init(int n)
2 {
3
        vector<int> pri;
4
        vector<bool> vis(n, 0);
5
        for (int i = 2; i <= n; i++)
6
7
            if (!vis[i])
                pri.push_back(i);
8
9
            for (int j = 0; j < pri.size(); j++)</pre>
10
                if (i * pri[j] > n)
11
12
                    break;
13
                vis[pri[j] * i] = 1;
                if (i % pri[j] == 0)
14
15
                    break;
            }
16
17
18
        return pri;
19 }
```

5.1.6. factor_pr.h

```
#define int long long
#define pii pair<int, int>
const int INF = 1145141919810LL;
using namespace std;
6 class Pollard_Rho
7 {
8
   private:
9
        vector<int> B;
10
11
        int mul(int a, int b, int m)
12
13
            int r = a * b - m * (int)(1.L / m * a * b);
14
            return r - m * (r >= m) + m * (r < 0);
15
16
        }
17
        int mypow(int a, int b, int m)
18
19
20
            int res = 1 % m;
21
            for (; b; b >>= 1, a = mul(a, a, m))
22
23
                if (b & 1)
24
                {
25
                    res = mul(res, a, m);
26
                }
27
            }
28
            return res;
29
        }
30
        bool MR(int n)
31
32
33
            if (n \leftarrow 1)
34
                return 0;
35
            for (int p : B)
36
37
                if (n == p)
38
                    return 1;
39
                if (n \% p == 0)
40
                    return 0;
            }
41
42
            int m = (n - 1) >> __builtin_ctz(n - 1);
            for (int p : B)
43
44
45
                int t = m, a = mypow(p, m, n);
                while (t != n - 1 && a != 1 && a != n - 1)
46
47
                {
48
                    a = mul(a, a, n);
49
                    t *= 2;
50
51
                if (a != n - 1 && t % 2 == 0)
52
                    return 0;
53
54
            return 1;
55
        }
56
57
        inline const int getfecsum(int _n)
```

```
58
         {
59
             int sum = 0;
60
             while (_n)
61
             {
62
                 sum += _n % 10;
63
                 _n /= 10;
64
             }
65
             return sum;
66
         };
67
         int PR(int n)
68
69
70
             for (int p : B)
71
                 if (n % p == 0)
72
73
                     return p;
74
             auto f = [\&](int x) \rightarrow int
75
76
             {
77
                 x = mul(x, x, n) + 1;
78
                 return x >= n ? x - n : x;
79
             int x = 0, y = 0, tot = 0, p = 1, q, g;
80
             for (int i = 0; (i & 255) | (g = gcd(p, n)) == 1; i++, x = f(x), y =
81
    f(f(y))
82
             {
83
                 if(x == y)
84
85
                      x = tot++;
86
                      y = f(x);
87
88
                 q = mul(p, abs(x - y), n);
                 if (q)
89
90
                      p = q;
91
92
             return g;
93
         }
94
95
         vector<int> fac(int n)
96
97
             // if(n == 0)
             // #define pb emplace_back
98
             if (n \ll 1)
99
                 return {};
100
101
             if (MR(n))
                 return {n};
102
103
             int d = PR(n);
104
             auto v1 = fac(d), v2 = fac(n / d);
             auto i1 = v1.begin(), i2 = v2.begin();
105
106
             vector<int> ans;
             while (i1 != v1.end() || i2 != v2.end())
107
108
                 if (i1 == v1.end())
109
110
                      ans.pb(*i2++);
                 else if (i2 == v2.end())
113
114
```

```
115
                      ans.pb(*i1++);
                  }
                  else
118
                  {
                      if (*i1 < *i2)</pre>
119
120
                      {
121
                           ans.pb(*i1++);
                      }
                      else
124
                      {
                           ans.pb(*i2++);
126
                      }
                  }
128
             }
129
             return ans;
130
         }
131
     public:
134
         Pollard_Rho(){
             B = \{2, 3, 5, 7, 11, 13, 17, 19, 23\};
136
138
         vector<pii> fac_Comp(int n)
139
             auto srt = fac(n);
140
141
             map<int, int> cnt;
142
             for (auto x : srt)
143
                  cnt[x]++;
144
             vector<pii> rt;
             for (auto x : cnt)
145
146
                  rt.push_back(x);
147
             return rt;
148
         }
149
150
         vector<int> fac pri(int n)
         {
             return fac(n);
153
         }
154
155
         vector<int> fac_all(int n)
156
             vector<pii> rt = fac_Comp(n);
158
             vector<int> v;
159
             function<void(int, int)> dfs = [&](int id, int x)
160
                  if (id == rt.size())
                      v.push_back(x);
                      return;
                  for(int i = 0;i <= rt[id].se;i ++)</pre>
167
                      dfs(id + 1, x * (mypow(rt[id].fi, i, INF)));
168
169
170
             };
171
             dfs(0, 1);
172
             return v;
```

```
173 }
174 };
```

5.2. OTHER

5.2.1. Frac.h

```
template<class T>
   struct Frac {
        T num;
3
4
        T den;
5
        Frac(T num_, T den_) : num(num_), den(den_) {
6
            if (den < 0) {
7
                den = -den;
8
                num = -num;
9
            }
10
        Frac() : Frac(0, 1) {}
        Frac(T num_) : Frac(num_, 1) {}
13
        explicit operator double() const {
            return 1. * num / den;
14
15
        Frac &operator+=(const Frac &rhs) {
16
            num = num * rhs.den + rhs.num * den;
17
18
            den *= rhs.den;
19
            return *this;
20
        Frac &operator-=(const Frac &rhs) {
            num = num * rhs.den - rhs.num * den;
22
            den *= rhs.den;
23
24
            return *this;
        Frac &operator*=(const Frac &rhs) {
26
27
            num *= rhs.num;
28
            den *= rhs.den;
29
            return *this;
30
31
        Frac &operator/=(const Frac &rhs) {
            num *= rhs.den;
32
            den *= rhs.num;
33
34
            if (den < 0) {
35
                num = -num;
36
                den = -den;
            }
38
            return *this;
39
40
        friend Frac operator+(Frac lhs, const Frac &rhs) {
            return lhs += rhs;
41
42
43
        friend Frac operator-(Frac lhs, const Frac &rhs) {
44
            return lhs -= rhs;
45
46
        friend Frac operator*(Frac lhs, const Frac &rhs) {
            return lhs *= rhs;
47
48
49
        friend Frac operator/(Frac lhs, const Frac &rhs) {
50
            return lhs /= rhs;
51
52
        friend Frac operator-(const Frac &a) {
53
            return Frac(-a.num, a.den);
54
        }
```

```
55
        friend bool operator==(const Frac &lhs, const Frac &rhs) {
56
            return lhs.num * rhs.den == rhs.num * lhs.den;
        friend bool operator!=(const Frac &lhs, const Frac &rhs) {
58
59
            return lhs.num * rhs.den != rhs.num * lhs.den;
60
        friend bool operator<(const Frac &lhs, const Frac &rhs) {</pre>
61
            return lhs.num * rhs.den < rhs.num * lhs.den;</pre>
62
63
        friend bool operator>(const Frac &lhs, const Frac &rhs) {
64
65
            return lhs.num * rhs.den > rhs.num * lhs.den;
66
67
        friend bool operator<=(const Frac &lhs, const Frac &rhs) {</pre>
            return lhs.num * rhs.den <= rhs.num * lhs.den;</pre>
68
69
        friend bool operator>=(const Frac &lhs, const Frac &rhs) {
70
            return lhs.num * rhs.den >= rhs.num * lhs.den;
71
        friend std::ostream &operator<<(std::ostream &os, Frac x) {</pre>
73
            T g = std::gcd(x.num, x.den);
74
75
            if (x.den == g) {
76
                 return os << x.num / g;</pre>
77
            } else {
78
                 return os << x.num / g << "/" << x.den / g;</pre>
79
80
        }
81
    };
82
using F = Frac<int>;
```

6. STRING

6.1. AC automaton.h

```
struct ACAutomaton
2
    {
3
        static constexpr int N = 1e6 + 10;
4
        int ch[N][26], fail[N], cntNodes;
5
        int cnt[N];
6
        ACAutomaton()
7
8
            cntNodes = 1;
9
10
        void insert(string s)
11
        {
12
             int u = 1;
            for (auto c : s)
14
             {
15
                 int &v = ch[u][c - 'a'];
16
                 if (!v)
17
                     v = ++cntNodes;
18
                 u = v;
19
20
            cnt[u]++;
21
        void build()
23
24
             fill(ch[0], ch[0] + 26, 1);
            queue<int> q;
25
            q.push(1);
26
27
            while (!q.empty())
28
29
                 int u = q.front();
30
                 q.pop();
                 for (int i = 0; i < 26; i++)
31
32
                 {
33
                     int &v = ch[u][i];
34
                     if (!v)
35
                         v = ch[fail[u]][i];
36
                     else
37
                     {
38
                         fail[v] = ch[fail[u]][i];
39
                         q.push(v);
40
                     }
41
                 }
            }
42
43
44
        LL query(string t)
45
             LL ans = 0;
46
            int u = 1;
47
48
             for (auto c : t)
49
50
                 u = ch[u][c - 'a'];
                 for (int v = u; v && ~cnt[v]; v = fail[v])
51
52
                 {
53
                     ans += cnt[v];
```

```
cnt[v] = -1;
```

6.2. compress_print.h

```
1 const int N = 1 \ll 21;
static const int mod1 = 1E9 + 7, base1 = 127;
static const int mod2 = 1E9 + 9, base2 = 131;
vector<int> val1;
   vector<int> val2;
   void init(int n = N)
7
    {
8
        val1.resize(n + 1), val2.resize(n + 2);
9
        val1[0] = 1, val2[0] = 1;
10
        for (int i = 1; i <= n; i++)
11
            val1[i] = val1[i - 1] * base1 % mod1;
            val2[i] = val2[i - 1] * base2 % mod2;
13
14
        }
15
    }
16
    string compress(vector<string> in)
17
    { // 前后缀压缩
18
19
        vector<int> h1{1};
20
        vector<int> h2{1};
        string ans = "#";
21
22
        for (auto s : in)
            s = "#" + s;
24
            int st = 0;
25
26
            int chk1 = 0;
27
            int chk2 = 0;
28
            for (int j = 1; j < s.size() && j < ans.size(); j++)</pre>
29
                chk1 = (chk1 * base1 % mod1 + s[j]) % mod1;
30
31
                chk2 = (chk2 * base2 % mod2 + s[j]) % mod2;
                if ((h1.back() == (h1[ans.size() - 1 - j] * val1[j] % mod1+ chk1)
32
    % mod1) &&
                    (h2.back() == (h2[ans.size() - 1 - j] * val2[j] % mod2+ chk2)
33
    % mod2)
               )
34
                    st = j;
35
36
            for (int j = st + 1; j < s.size(); j++)
37
                ans += s[j];
38
                h1.push_back((h1.back() * base1 % mod1 + s[j]) % mod1);
39
40
                h2.push_back((h2.back() * base2 % mod2 + s[j]) % mod2);
41
            }
42
        }
43
        return ans.substr(1);
44
    }
```

6.3. get occr.h

```
#include <template overAll.h>
2
3
    * 找到某一堆短字符串在长字符串中的出现位置
    * dira=1 为最早出现的后端点下标 dira=0 为最晚出现的前端点下标
    * 源字符串 s 长度为 | s |, 查找字符串列表中所有字符串长度和为 | s |
    * 则时间复杂度为 O(max(|_s|log(|_s|),|s|))
7
    */
   class get_occr
9
10
11
    private:
12
        string s;
13
    public:
14
        get_occr(string _s) { s = _s; }
15
        vector<int> locate(vector<string> _s,bool dira = 1)
16
17
            int n = _s.size();
            vector<int> occr(n,-1);
18
19
            map<char, vector<pair<int,int>>> gncing;
20
            if(dira == 1)
            {
                for(int i = 0;i < n;i++)</pre>
23
                    gncing[_s[i][0]].push_back({i,0});
24
                for(int i = 0;i < s.size();i ++)</pre>
25
                {
26
                    vector<pair<int,int>> gnctmp = gncing[s[i]];
                    gncing[s[i]].clear();
28
                    for(int j = 0;j < gnctmp.size();j ++)</pre>
29
                        if(gnctmp[j].se+1 < _s[gnctmp[j].fi].size())</pre>
30
                                gncing[_s[gnctmp[j].fi]
31
    [gnctmp[j].se+1]].push_back({gnctmp[j].fi,gnctmp[j].se+1});
32
                        else occr[gnctmp[j].fi] = i;
33
                    }
34
35
            } else {
                for(int i = 0;i < n;i++) gncing[_s[i]</pre>
36
    [_s[i].size()-1]].push_back({i,_s[i].size()-1});
37
                for(int i= s.size()-1;i >=0;i --)
38
                {
39
                    vector<pair<int,int>> gnctmp = gncing[s[i]];
40
                    gncing[s[i]].clear();
                    for(int j = 0;j < gnctmp.size();j ++)</pre>
41
42
                        if(gnctmp[j].se -1 >= 0)
43
                                gncing[_s[gnctmp[j].fi]
44
    [gnctmp[j].se-1]].push_back({gnctmp[j].fi,gnctmp[j].se-1});
45
                        else occr[gnctmp[j].fi] = i;
46
                    }
47
48
            }
49
            return occr;
50
        }
51
    };
```

6.4. hash_print.h

```
#define int long long
2 const int N = 1 \ll 21;
static const int mod1 = 1E9 + 7, base1 = 127;
4 static const int mod2 = 1E9 + 9, base2 = 131;
vector<int> val1;
vector<int> val2;
vsing puv = pair<int,int>;
   void init(int n = N)
9
10
       val1.resize(n + 1), val2.resize(n + 2);
       val1[0] = 1, val2[0] = 1;
11
        for (int i = 1; i <= n; i++)
13
            val1[i] = val1[i - 1] * base1 % mod1;
14
15
            val2[i] = val2[i - 1] * base2 % mod2;
16
17
   }
18
   class hstring
19
   {
   public:
20
21
       vector<int> h1;
       vector<int> h2;
23
        string s;
24
25
       hstring(string s_) : s(s_), h1{0}, h2{0}
26
27
            build();
28
        }
29
        void build()
30
31
        {
32
            for (auto it : s)
34
                h1.push_back((h1.back() * base1 % mod1 + it) % mod1);
                h2.push_back((h2.back() * base2 % mod2 + it) % mod2);
35
36
            }
37
        }
38
39
        puv get()
        { // 输出整串的哈希值
40
41
            return {h1.back(), h2.back()};
42
43
       puv substring(int 1, int r)
44
        { // 输出子串的哈希值
45
46
            if (1 > r) swap(1, r);
            int ans1 = (mod1 + h1[r + 1] - h1[l] * val1[r - l + 1] % mod1) % mod1;
47
48
            int ans2 = (mod2 + h2[r + 1] - h2[1] * val2[r - 1 + 1] % mod2) % mod2;
49
            return {ans1, ans2};
50
        }
51
       puv modify(int idx, char x)
        { //修改 idx 位为 x
53
54
            int n = s.size() - 1;
            int ans1 = (h1.back() + val1[n - idx] * (x - s[idx]) % mod1) % mod1;
55
            int ans2 = (h2.back() + val2[n - idx] * (x - s[idx]) % mod2) % mod2;
56
57
            return {ans1, ans2};
```

```
[58] };
[59] };
```

6.5. KMP.h

```
#include <template_overAll.h>
2
3 class KMP
4 {
5 private:
6
        string s;
        string inis;
7
8
    public:
        vector<int> pi;
9
10
        KMP(string _s)
11
        {
            s = _s;
13
            inis = s;
14
        }
15
        void prefix_function()
16
17
            pi.clear();
            int n = (int)s.length();
18
19
            pi.resize(n);
            for (int i = 1; i < n; i++)
20
22
                 int j = pi[i - 1];
                 while (j > 0 \&\& s[i] != s[j])
23
24
                     j = pi[j - 1];
                 if (s[i] == s[j])
25
26
                     j++;
27
                 pi[i] = j;
28
            }
29
            return;
30
        vector<int> find_occr(string p)
31
32
        {
33
            s = inis;
            s = p + "#" + s;
34
            prefix_function();
35
36
            vector<int> v;
            for (int i = p.size() + 1; i < s.size(); i++)</pre>
37
38
                 if (pi[i] == p.size())
                     v.push_back(i - 2 * p.size());
39
40
            return v;
41
        }
42
    };
```

6.6. trie_Tree.h

```
#include <template_overAll.h>
2
class Trie//AC
4 {
5
    public:
        vector<map<char, int>> t;
6
7
        int root = 0;
8
        Trie()
9
        {
10
            t.resize(1);
11
        void addedge(string _s)
13
        {
14
            int pvidx = root;
15
            _s.push_back('-');
            for (int i = 0; i < _s.size(); i++)</pre>
16
17
                 if (t[pvidx].find(_s[i]) != t[pvidx].end())
18
19
                 {
20
                     pvidx = t[pvidx][_s[i]];
                 }
                else
22
23
                 {
24
                     t[pvidx][_s[i]] = t.size();
                     t.push_back(map<char, int>());
25
26
                     pvidx = t[pvidx][_s[i]];
27
                 }
28
            }
29
30
        bool ifcmp(string &s)
31
32
            int pvidx = root;
33
            for(int i = 0;i < s.size();i ++)</pre>
34
            {
35
                 if(t[pvidx].find(s[i]) != t[pvidx].end()) pvidx = t[pvidx][s[i]];
36
                 else return 0;
37
38
            return t[pvidx].find('-') != t[pvidx].end();
39
        }
40
    };
```