

GZHU I_WANT_TO_EAT_MCDONALD'S

Snippet

C++

```
#define pb push_back
#define sz(s) ((int)s.size())
#define all(vec) vec.begin(), vec.end()

typedef long long ll;
typedef vector<ll> VL;
typedef vector<int> VI;
typedef pair<int, int> pii;

#ifdef local
#define debug(x...) do { cout << "[ "#x" ] -> "; err(x); } while (0)
template <class T>
inline void _E(T x) { cout << x; }
template <class L, class R>
inline void _E(pair<L, R> arg) {
    cout << "("; _E(arg.first), _E(','), _E(' '), _E(arg.second); cout << ")";
}
template <template <class...> class T, class t>
inline void _E(T<t> arr) {
    cout << "[";
    for (auto it = begin(arr), en = end(arr); it != en; it++) {
        if (it != begin(arr)) cout << ", "; _E(*it);
    }
    cout << "]";
}
inline void _E(string s) { cout << "\"" + s + "\""; }

inline void err() { cout << std::endl; }
template <class T, class... U>
inline void err(T arg, U... args) {
    _E(arg); if (sizeof...(args)) cout << ", "; err(args...);
}
#else
#define debug(...) do {} while (0)
#endif
```

Java

```

import java.io.*;
import java.util.*;
import java.math.BigInteger;

public class Main {
    public static void main(String[] args) {
        InputReader in = new InputReader(System.in);
        PrintWriter out = new PrintWriter(System.out);
        Task solver = new Task();
        int taskNum = 1;
        // int taskNum = in.nextInt();
        solver.solve(taskNum, in, out);
        out.close();
    }

    public static class Task {
        void solve(int t, InputReader in, PrintWriter out) {

        }
    }

    static class InputReader {
        public BufferedReader reader;
        public StringTokenizer tokenizer;

        public InputReader(InputStream stream) {
            reader = new BufferedReader(new InputStreamReader(stream), 32768);
            tokenizer = null;
        }

        public String next() {
            while (tokenizer == null || !tokenizer.hasMoreTokens()) {
                try {
                    tokenizer = new StringTokenizer(reader.readLine());
                } catch (IOException e) {
                    throw new RuntimeException(e);
                }
            }
            return tokenizer.nextToken();
        }

        public int nextInt() {
            return Integer.parseInt(next());
        }

        public BigInteger nextBigInteger() {
            return new BigInteger(next());
        }
    }
}

```

unordered_map

```

struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }

    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM = chrono::steady_clock::now().\
            time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};

unordered_map<long long, int, custom_hash> safe_map;

```

io buffer

```

namespace io {
    const int SZ = (1 << 22) + 1;
    char buf[SZ], *ptr = NULL, *bnd = NULL;
    #define GC() ((ptr == bnd) ? (ptr = buf, bnd = buf + fread(buf, 1, SZ, stdin),\
(ptr == bnd) ? EOF : (*(ptr++))) : (*(ptr++)))
    #define STATE(c) { if (c == '-') sgn = -1; else if (c == EOF) return false; }
    inline bool skip(const char& c) { return c < '0' || c > '9'; }
    template <class V>
    inline bool Read(V &v) {
        register char c, sgn = 1;
        while (skip(c = GC())) STATE(c);
        for (v = c - '0'; !skip(c = GC()); v = v * 10 + c - '0');
        return (v *= sgn), true;
    }

    char oBuf[SZ], *oCur = oBuf, *oBnd = oBuf + SZ, oStk[21], top = 0;
    inline void flush() { if (oCur - oBuf) fwrite(oBuf, 1, oCur - oBuf, stdout),\
oCur = oBuf; }
    inline void pc(char c) { *(oCur++) = c; if (oCur == oBnd) flush(); }
    template <class V>
    inline void Print(V v) {
        if (!v) return pc('0');
        if (v < 0) v = -v, pc('-');
        while (v) oStk[top++] = v % 10, v /= 10;
        while (top) pc(oStk[--top] + '0');
    }
    template <class V>
    inline void Println(const V& v) { Print(v), pc('\n'); }
    struct flusher { ~flusher() { flush(); } } __flusher__;
}

using io::Read;
using io::Println;

```

DataStructure

区间增减树状数组

```
struct Interval {
    int N, base[2][maxn];
    void setN(int n) { N = n; }
    void init() { memset(base, 0, sizeof base); }
    void add(int at, int v) {
        if (!at) return;
        for (int i = at; i <= N; i += i & -i) {
            base[0][i] += v, base[1][i] -= v * at;
        }
    }
    void add(int l, int r, int v) {
        add(l, v), add(r + 1, -v);
    }
    int getSum(int at) {
        int sum = 0, mul = at + 1;
        for (int i = at; i; i -= i & -i) {
            sum += mul * base[0][i] + base[1][i];
        }
        return sum;
    }
    int query(int l, int r) {
        return getSum(r) - getSum(l - 1);
    }
};
```

无旋Treap

```
struct Treap {
#define ls(x) T[x].son[0]
#define rs(x) T[x].son[1]

    struct Node {
        int son[2], size, v, key, rev;
    } T[maxn];
    int tot, root;

    Treap() { tot = root = 0; }

    inline void init() { tot = root = 0; }

    inline void pushup(int i) {
        T[i].size = T[ls(i)].size + T[rs(i)].size + 1;
    }
    inline void pushdown(int i) {
```

```

    if (T[i].rev) {
        swap(ls(i), rs(i));
        T[ls(i)].rev ^= 1, T[rs(i)].rev ^= 1;
        T[i].rev = 0;
    }
}

void split(int rt, int &x, int &y, int v) {
    if (!rt) return (x = y = 0);
    pushdown(rt);
    if (T[rt].v <= v) {
        x = rt, split(rs(rt), rs(x), y, v);
    } else {
        y = rt, split(ls(rt), x, ls(y), v);
    }
    pushup(rt);
}

void merge(int &rt, int x, int y) {
    if (!x || !y) {
        rt = x + y;
        return;
    }
    if (T[x].key < T[y].key) {
        pushdown(x), rt = x, merge(rs(rt), rs(x), y);
    } else {
        pushdown(y), rt = y, merge(ls(rt), x, ls(y));
    }
    pushup(rt);
}

inline void insert(int &rt, int v) {
    int x = 0, y = 0, z = ++tot;
    T[z].v = v, T[z].key = rand(), T[z].size = 1, T[z].rev = 0;
    split(rt, x, y, v), merge(x, x, z), merge(rt, x, y);
}

inline void erase(int &rt, int v) {
    int x = 0, y = 0, z = 0;
    split(rt, x, y, v), split(x, x, z, v - 1);
    merge(z, ls(z), rs(z)), merge(x, x, z), merge(rt, x, y);
}

inline int findkth(int rt, int k) {
    if (k == 0) return -inf;
    pushdown(rt);
    while (T[ls(rt)].size + 1 != k) {
        if (T[ls(rt)].size >= k) rt = ls(rt);
        else k -= (T[ls(rt)].size + 1), rt = rs(rt);
    }
    pushdown(rt);
    return T[rt].v;
}

inline int getrank(int &rt, int v) {
    int x = 0, y = 0, res;
    split(rt, x, y, v - 1), res = T[x].size + 1;
}

```

```

    return merge(rt, x, y), res;
}
inline int getpre(int &rt, int v) {
    int x = 0, y = 0, res;
    split(rt, x, y, v - 1), res = findkth(x, T[x].size);
    return merge(rt, x, y), res;
}
inline int getsuf(int &rt, int v) {
    int x = 0, y = 0, res;
    split(rt, x, y, v), res = findkth(y, 1);
    return merge(rt, x, y), res;
}

inline void insert(int v) { insert(root, v); }
inline void erase(int v) { erase(root, v); }
inline int findkth(int k) { return findkth(root, k); }
inline int getrank(int v) { return getrank(root, v); }
inline int getpre(int v) { return getpre(root, v); }
inline int getsuf(int v) { return getsuf(root, v); }
} treap;

```

ST表

```

struct ST {
    vector<vector<int>> table;
    ST(vector<int> a = {}) {
        int n = a.size();
        table.resize(n, vector<int>(32 - __builtin_clz(n)));
        for (int i = 0; i < n; i++) {
            table[i][0] = a[i];
        }
        for (int j = 1; (1 << j) - 1 < n; j++) {
            for (int i = 0; i + (1 << j) - 1 < n; i++) {
                int x = table[i][j - 1], y = table[i + (1 << (j - 1))][j - 1];
                table[i][j] = min(x, y);
            }
        }
    }
    inline int getMin(int l, int r) {
        int k = 31 - __builtin_clz(r - l + 1);
        return min(table[l][k], table[r - (1 << k) + 1][k]);
    }
};

```

并查集(带权)

```

template <int NV> class Dsu {
    int anc[NV], weight[NV];
    void init(int n = NV) {

```

```

    iota(anc.begin(), next(anc.begin(), n), 0);
    fill(anc.begin(), next(anc.begin(), n), 0);
}
int find(int x) {
    if (x == anc[x]) return x;
    int fa = anc[x];
    anc[x] = find(anc[x]);
    weight[x] += weight[fa];
    return anc[x];
}
bool unite(int u, int v, int w = 0) {
    int a = find(u), b = find(v);
    if (a == b) return false;
    anc[b] = a;
    weight[b] = weight[u] + w - weight[v];
    return true;
}
};

```

String

kmp

```

template <template<class...> class T, class t>
VI getfail(const T<t>& s) {
    int n = sz(s);
    VI fail(n + 1);
    for (int i = 0, j = fail[0] = -1; i < n; i++, j++) {
        while (~j && s[j] != s[i]) j = fail[j];
        fail[i + 1] = j + 1;
    }
    return fail;
}

// candidate
VI getfail(const string& s) {
    int n = sz(s);
    VI fail(n + 1);
    for (int i = 0, j = fail[0] = -1; i < n; i++, j++) {
        while (~j && s[i] != s[j]) j = fail[j];
        fail[i + 1] = (s[i + 1] == s[j + 1]) ? fail[j + 1] : (j + 1);
    }
    return fail;
}

template <template<class...> class T, class t>
int match(const T<t> &s, const T<t> &par, const VI &fail) {
    int n = sz(s), m = sz(par);
    for (int i = 0, j = 0; i < n; ) {

```

```

        while (~j && par[j] != s[i]) j = fail[j];
        ++i, ++j;
        if (j >= m) return i - m + 1;
    }
    return -1;
}

```

Z-function

```

VI Zfunc(string s) {
    int n = sz(s);
    VI z(n);
    for (int i = 1, l = 0, r = 0; i < n; i++) {
        if (i <= r) z[i] = min(r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]]) ++z[i];
        if (i + z[i] - 1 > r) l = i, r = i + z[i] - 1;
    }
    return z;
}

```

Suffix Array

```

template <typename T>
VI build_sa(int n, const T &s, int charset) {
    VI a(n);
    if (n == 0) {
        return a;
    }
    if (charset != -1) {
        VI aux(charset, 0);
        for (int i = 0; i < n; i++) {
            aux[ s[i] ]++;
        }
        int sum = 0;
        for (int i = 0; i < charset; i++) {
            int add = aux[i];
            aux[i] = sum;
            sum += add;
        }
        for (int i = 0; i < n; i++) {
            a[ aux[ s[i] ]++ ] = i;
        }
    } else {
        iota(a.begin(), a.end(), 0);
        sort(a.begin(), a.end(), [&s](int i, int j) { return s[i] < s[j];
    });
    }
    VI sorted_by_second(n), ptr_group(n);
    VI new_group(n), group(n);
}

```



```

group[ a[0] ] = 0;
for (int i = 1; i < n; i++) {
    group[ a[i] ] = group[ a[i - 1] ] + ( !(s[ a[i] ] == s[ a[i - 1] ])
);
}
int cnt = group[a[n - 1]] + 1;
int step = 1;
while (cnt < n) {
    int at = 0;
    for (int i = n - step; i < n; i++) {
        sorted_by_second[at++] = i;
    }
    for (int i = 0; i < n; i++) {
        if (a[i] - step >= 0) {
            sorted_by_second[at++] = a[i] - step;
        }
    }
    for (int i = n - 1; i >= 0; i--) {
        ptr_group[ group[ a[i] ] ] = i;
    }
    for (int i = 0; i < n; i++) {
        int x = sorted_by_second[i];
        a[ ptr_group[ group[x] ]++ ] = x;
    }
    new_group[a[0]] = 0;
    for (int i = 1; i < n; i++) {
        if (group[ a[i] ] != group[ a[i - 1] ]) {
            new_group[ a[i] ] = new_group[ a[i - 1] ] + 1;
        } else {
            int pre = ( (a[i - 1] + step >= n) ? -1 : group[ a[i - 1] +
step ] );
            int cur = ( (a[i] + step >= n) ? -1 : group[ a[i] + step ] );
            new_group[ a[i] ] = new_group[ a[i - 1] ] + (pre != cur);
        }
    }
    swap(group, new_group);
    cnt = group[ a[n - 1] ] + 1;
    step <= 1;
}
return a;
}

```

one more

```

namespace SuffixArray {
    const int maxn = "edit";

    int wa[maxn], wb[maxn], c[maxn], d[maxn];

    inline bool cmp(int *r, int a, int b, int k) {

```

```

    return (r[a] == r[b]) && (r[a + k] == r[b + k]);
}

void da(int *r, int *sa, int n, int m) {
    int i, j, p, *x = wa, *y = wb, *t;

    for (i = 0; i < m; i++) d[i] = 0;
    for (i = 0; i < n; i++) d[x[i] = r[i]]++;

    for (i = 1; i < m; i++) d[i] += d[i - 1];
    for (i = n - 1; i >= 0; i--) sa[--d[x[i]]] = i;

    for (j = 1, p = 1; j <= n; j <= 1, m = p) {
        for (p = 0, i = n - j; i < n; i++) y[p++] = i;
        for (i = 0; i < n; i++) if (sa[i] >= j) y[p++] = sa[i] - j;

        for (i = 0; i < n; i++) c[i] = x[y[i]];
        for (i = 0; i < m; i++) d[i] = 0;

        for (i = 0; i < n; i++) d[c[i]]++;
        for (i = 1; i < m; i++) d[i] += d[i - 1];

        for (i = n - 1; i >= 0; i--) sa[--d[c[i]]] = y[i];
        for (t = x, x = y, y = t, p = 1, x[sa[0]] = 0, i = 1; i < n; i++)
        {
            x[sa[i]] = cmp(y, sa[i - 1], sa[i], j) ? (p - 1) : (p++);
        }
    }
}

int rank[maxn], height[maxn];
void calheight(int *r, int *sa, int n) {
    int i, j, k = 0;
    for (i = 1; i <= n; i++) rank[sa[i]] = i;
    for (i = 0; i < n; i++) {
        if (k) --k;
        for (j = sa[rank[i] - 1]; r[i + k] == r[j + k]; k++);
        // blank
        height[rank[i]] = k;
    }
}
}

```

Suffix Automa

```

struct SAM {
    int last, tot, sz[maxn << 1], len[maxn << 1], fa[maxn << 1];
    int ch[maxn << 1][30];

    SAM() {
        tot = 0, last = newNode(0), len[0] = -1;
    }
}

```

```

    memset(sz, 0, sizeof sz);
}
inline int newNode(int v) {
    len[++tot] = v, fa[tot] = 0;
    memset(ch[tot], 0, sizeof ch[tot]);
    return tot;
}
void append(int c) {
    int p = last, u = newNode(len[last] + 1);
    for (; p && !ch[p][c]; p = fa[p]) {
        ch[p][c] = u;
    }
    if (p == 0) {
        fa[u] = 1;
    } else {
        int q = ch[p][c];
        if (len[q] == len[p] + 1) {
            fa[u] = q;
        } else {
            int nq = newNode(len[p] + 1);
            memcpy(ch[nq], ch[q], sizeof ch[q]);
            fa[nq] = fa[q], fa[u] = fa[q] = nq;
            for (; p && (ch[p][c] == q); p = fa[p]) {
                ch[p][c] = nq;
            }
        }
    }
    last = u;
}
void match(char *s) {
    int pos = 1, length = 0;
    for (int i = 0, n = strlen(s); i < n; i++) {
        while (pos && !ch[pos][s[i] - 'a']) {
            pos = fa[pos], length = len[pos];
        }
        if (pos) {
            ++length, pos = ch[pos][s[i] - 'a'];
            // update ans
        } else {
            pos = 1, length = 0;
        }
    }
}
} sam;

```

最小表示法

对于一个字符串S，求S的循环的同构字符串S'中字典序最小的一个。

字符串"abcd"的循环同构字符串有：["abcd", "bcda", "cdab", "dabc"]。

```

int minPresentation(string &s) {
    int n = s.length();
    int i = 0, j = 1, k = 0;
    while (k < n && i < n && j < n) {
        if (s[(i + k) % n] == s[(j + k) % n]) {
            ++k;
        } else {
            s[(i + k) % n] > s[(j + k) % n] ? (i += k + 1) : (j += k + 1);
            i += (i == j);
            k = 0;
        }
    }
    return min(i, j);
}

```

Manacher

```

int p[maxn << 1];
char str[maxn << 1];

int manacher(char *s, int n) {
    str[0] = '$'; str[1] = '#';

    for (int i = 0; i < n; i++) {
        str[(i << 1) + 2] = s[i];
        str[(i << 1) + 3] = '#';
    }
    n = (n + 1) << 1;
    str[n] = 0;

    int ret = 0, mx = 0, pos;
    for (int i = 1; i < n; i++) {
        p[i] = mx > i ? min(p[(pos << 1) - i], mx - i) : 1;

        while (str[i - p[i]] == str[i + p[i]]) p[i]++;

        if (p[i] + i > mx) mx = p[i] + i, pos = i;

        ret = max(ret, p[i]);
    }
    return ret - 1;
}

```

AC Automa

```

namespace acam {
    struct Node {
        int son[26], fail;
        void init() {

```

```

        fail = 0;
        memset(son, 0, sizeof son);
    }
} T[N];
int tot;

#define Son(i, x) T[i].son[x]
#define trans(c) (c - 'A')

void init() {
    tot = 0, T[0].init();
}

void insert(char *s, int index) {
    int cur = 0;
    for (int i = 0; s[i]; i++) {
        int c = trans(s[i]);
        if (!Son(cur, c)) {
            Son(cur, c) = ++tot;
            T[tot].init();
        }
        cur = Son(cur, c);
    }
}

void build() {
    queue<int> Q;
    for (int i = 0; i < 26; i++) {
        if (Son(0, i)) Q.push(Son(0, i));
    }
    while (!Q.empty()) {
        int u = Q.front(); Q.pop();
        for (int i = 0; i < 26; i++) {
            if (Son(u, i)) {
                T[Son(u, i)].fail = T[T[u].fail].son[i];
                Q.push(Son(u, i));
            } else {
                T[u].son[i] = T[T[u].fail].son[i];
            }
        }
    }
}

int query(char *t) {
    int ans = 0, cur = 0;
    for (int i = 0; t[i]; i++) {
        int c = trans(t[i]);
        cur = Son(cur, c);
        for (int j = cur; j; j = T[j].fail) {
            // upd ans;
        }
    }
    return ans;
}

```

```

    }
}

```

PAM

```

struct PAM {
    struct Node {
        int son[27], fail, len, dep;
        void init(int l, int f, int d = 0) {
            fail = f, len = l, dep = d;
            memset(son, 0, sizeof son);
        }
    } T[N + 5];
    int tot, prefix, suffix, l, r;
    int s[N * 2 + 5];

    void init() {
        ans = 0;
        tot = 1, l = N + 1, r = N, prefix = suffix = 0;
        T[0].init(0, 1), T[1].init(-1, 0);
        memset(s, 0, sizeof s);
    }

    void encode(int &c) {
        // keep c > 0
        c = c - 'a' + 1;
    }

    int pre_fail(int cur) {
        while (s[l + T[cur].len + 1] != s[l]) {
            cur = T[cur].fail;
        }
        return cur;
    }

    int suf_fail(int cur) {
        while (s[r - T[cur].len - 1] != s[r]) {
            cur = T[cur].fail;
        }
        return cur;
    }

    void push_front(int c) {
        encode(c), s[--l] = c;
        prefix = pre_fail(prefix);
        if (!T[prefix].son[c]) {
            int f = pre_fail(T[prefix].fail);
            T[++tot].init(T[prefix].len + 2, T[f].son[c], T[T[f].son[c]].dep
+ 1);
            T[prefix].son[c] = tot;
        }
        prefix = T[prefix].son[c];
        if (T[prefix].len == r - l + 1) {
            suffix = prefix;

```

```

    }
}
void push_back(int c) {
    encode(c), s[++r] = c;
    suffix = suf_fail(suffix);
    if (!T[suffix].son[c]) {
        int f = suf_fail(T[suffix].fail);
        T[++tot].init(T[suffix].len + 2, T[f].son[c], T[T[f].son[c]].dep
+ 1);
        T[suffix].son[c] = tot;
    }
    suffix = T[suffix].son[c];
    if (T[suffix].len == r - 1 + 1) {
        prefix = suffix;
    }
}
}
} pam;

```

Graph

2-sat

```

struct twoSat {
    struct edge {
        int v, next;
        edge(int a = 0, int b = 0) : v(a), next(b) {}
    }G[maxm];
    int tot, head[maxn], mark[maxn], sz, stk[maxn];
    void init() {
        tot = 0;
        memset(mark, 0, sizeof mark);
        memset(head, -1, sizeof head);
    }
    // for every case u, (status[u] xor status[u ^ 1]) == true.
    //
    // addcase: if status[u] == true then status[v] == true,
    // but if status[u] == false then status[v] can be true or false.
    //
    void addcase(int u, int v) {
        G[tot] = edge(v, head[u]); head[u] = tot++;
    }
    int dfs(int u) {
        if (mark[u ^ 1]) return 0;
        if (mark[u]) return 1;
        stk[sz++] = u, mark[u] = 1;
        for (int i = head[u]; ~i; i = G[i].next) {
            if (!dfs(G[i].v)) return 0;
        }
        return 1;
    }
};

```

```

    }
    int solve(int n) {
        for (int i = 0; i < n; i += 2) {
            if (!mark[i] && !mark[i ^ 1]) {
                sz = 0;
                if (!dfs(i)) {
                    while (sz > 0) mark[stk[--sz]] = 0;
                    if (!dfs(i ^ 1)) return 0;
                }
            }
        }
        return 1;
    }
}
}sat;

```

强连通

Tarjan

```

struct Scc {
    vector<int> G[maxn];
    int N, tag, tot, dfn[maxn], low[maxn], sccno[maxn];
    stack<int> S;

    void init(int n) {
        N = n, tag = tot = 0;
        for (int i = 1; i <= n; i++) {
            dfn[i] = low[i] = sccno[i] = 0;
            G[i].clear();
        }
    }

    void addedge(int u, int v) {
        G[u].push_back(v);
    }

    void dfs(int u) {
        dfn[u] = low[u] = ++tag;
        S.push(u);
        for (auto& v : G[u]) {
            if (!dfn[v]) {
                dfs(v);
                low[u] = min(low[u], low[v]);
            } else if (!sccno[v]) {
                low[u] = min(low[u], dfn[v]);
            }
        }
        if (low[u] == dfn[u]) {
            ++tot;
            while (true) {
                int x = S.top(); S.pop();
                sccno[x] = tot;
            }
        }
    }
}

```



```

        if (x == u) break;
    }
}
}
void solve() {
    for (int i = 1; i <= N; i++) {
        if (!dfn[i]) dfs(i);
    }
}
} scc;

```

kosaraju

```

struct kosaraju {
    int N, tot, scc[maxn], vis[maxn];
    vector<int> G[maxn], R[maxn], acc;
    void init(int n) {
        N = n;
        tot = 0, acc.clear();
        for (int i = 1; i <= N; i++) {
            G[i].clear(), R[i].clear();
            vis[i] = 0, scc[i] = 0;
        }
    }
    void DFS1(int u) {
        vis[u] = 1;
        for (auto& v : G[u]) {
            if (!vis[v]) DFS1(v);
        }
        acc.push_back(u);
    }
    void DFS2(int u, int p) {
        scc[u] = p;
        for (auto& v : R[u]) {
            if (!scc[v]) DFS2(v, p);
        }
    }
    void solve() {
        for (int i = 1; i <= N; i++) {
            if (!vis[i]) DFS1(i);
        }
        reverse(acc.begin(), acc.end());
        for (auto& u : acc) {
            if (!scc[u]) DFS2(u, ++tot);
        }
    }
};

```

双连通

点双

```
struct bcc {
    struct edge { int u, v; };
    vector<int> G[N], cont[N];
    int Nx, tag, tot, dfn[N], bccno[N];
    bool iscut[N];
    stack<edge> S;

    void init(int n) {
        Nx = n, tag = tot = 0;
        for (int i = 1; i <= Nx; i++) {
            G[i].clear();
            dfn[i] = bccno[i] = 0;
            iscut[i] = false;
        }
        while (!S.empty()) S.pop();
    }
    void addedge(int u, int v) {
        G[u].push_back(v), G[v].push_back(u);
    }
    int dfs(int u, int f) {
        int lowu = dfn[u] = ++tag;
        int child = 0;
        for (auto& v : G[u]) {
            if (!dfn[v]) {
                ++child, S.push({ u, v });
                int lowv = dfs(v, u);
                lowu = min(lowu, lowv);
                if (lowv >= dfn[u]) {
                    iscut[u] = true;
                    cont[++tot].clear();
                    while (true) {
                        edge e = S.top(); S.pop();
                        if (bccno[e.u] != tot) {
                            cont[tot].push_back(e.u);
                            bccno[e.u] = tot;
                        }
                        if (bccno[e.v] != tot) {
                            cont[tot].push_back(e.v);
                            bccno[e.v] = tot;
                        }
                    }
                    if (e.u == u && e.v == v) {
                        break;
                    }
                }
            }
            else if (dfn[v] < dfn[u] && v != f) {
                S.push({ u, v });
                lowu = min(lowu, dfn[v]);
            }
        }
    }
};
```

```

    }
}
if (f < 0 && child == 1) {
    iscut[u] = false;
}
return lowu;
}
void solve() {
    for (int i = 1; i <= Nx; i++) {
        if (!dfn[i]) dfs(i, -1);
    }
}
} gao;

```

割顶/桥

```

struct edge {
    int v, next;
} G[M];
int tot, h[N], ord, dfn[N], low[N];
bool iscut[N], isbridge[M];

void init() {
    tot = ord = 0;
    memset(h, -1, sizeof h);
    memset(dfn, 0, sizeof dfn);
    memset(low, 0, sizeof low);
    memset(iscut, false, sizeof iscut);
    memset(isbridge, false, sizeof isbridge);
}

void addedge(int u, int v) {
    G[tot] = { v, h[u] }, h[u] = tot++;
    G[tot] = { u, h[v] }, h[v] = tot++;
}

void dfs(int u, int f) {
    low[u] = dfn[u] = ++ord;
    int child = 0;
    for (int i = h[u]; ~i; i = G[i].next) {
        edge &e = G[i];
        if (!dfn[e.v]) {
            ++child, dfs(e.v, u);
            low[u] = min(low[u], low[e.v]);
            if (low[e.v] >= dfn[u]) {
                iscut[u] = true;
            }
            if (low[e.v] > dfn[u]) {
                isbridge[i] = isbridge[i ^ 1] = true;
            }
        }
    }
}

```

```

        } else if (dfn[e.v] < dfn[u] && e.v != f) {
            low[u] = min(low[u], dfn[e.v]);
        }
    }
    if (f == -1 && child == 1) {
        iscut[u] = false;
    }
}

void solve(int n) {
    for (int i = 1; i <= n; i++) {
        if (!dfn[i]) dfs(i, -1);
    }
}

```

边双(kuangbin)

```

struct edge {
    int v, next;
    bool cut;
} G[M];
int tot, h[N];
int ord, top, bcc_cnt, bridge, dfn[N], low[N], in[N], stk[N];
bool instk[N];

void init() {
    tot = 0;
    memset(h, -1, sizeof h);
}

void addedge(int u, int v) {
    G[tot] = { v, h[u], false }, h[u] = tot++;
    G[tot] = { u, h[v], false }, h[v] = tot++;
}

void dfs(int u, int f) {
    low[u] = dfn[u] = ++ord;
    stk[top++] = u, instk[u] = true;
    int f_cnt = 0;
    for (int i = h[u]; ~i; i = G[i].next) {
        int v = G[i].v;
        if (v == f && f_cnt == 0) { ++f_cnt; continue; }
        if (!dfn[v]) {
            dfs(v, u);
            if (low[u] > low[v]) low[u] = low[v];
            if (low[v] > dfn[u]) {
                ++bridge;
                G[i].cut = G[i ^ 1].cut = true;
            }
        }
        else if (instk[v] && low[u] > dfn[v]) {

```

```

        low[u] = dfn[v];
    }
}
if (low[u] == dfn[u]) {
    int v;
    ++bcc_cnt;
    do {
        v = stk[--top];
        instk[v] = false;
        in[v] = bcc_cnt;
    } while (v != u);
}
}

void solve(int n) {
    for (int i = 1; i <= n; i++) {
        if (!dfn[i]) dfs(i, -1);
    }
}

```

欧拉路

无向

```

// undirected, 0-base
template <int NV> class Hierholzer {
public:
    vector<int> path;
    multiset<int> G[NV];

    void addedge(int u, int v) {
        G[u].insert(v), G[v].insert(u);
    }

    void dfs(int cur) {
        while (!G[cur].empty()) {
            int tar = *G[cur].begin();
            G[cur].erase(G[cur].begin());
            G[tar].erase(G[tar].find(cur));
            dfs(tar);
        }
        path.push_back(cur);
    }

    bool get() {
        int src = -1, odd = 0, tot = 0;
        for (int i = 0; i < NV; i++) {
            tot += G[i].size();
            if (G[i].size() % 2 == 1) {
                odd++, src = (~src) ? src : i;
            }
        }
        if (odd > 1) return false;
        if (src == -1) src = 0;
        dfs(src);
        return true;
    }
};

```

```

    }
}
if (odd != 0 && odd != 2) return false;
dfs(odd ? src : 0);
reverse(path.begin(), path.end());
return (int)path.size() == tot / 2 + 1;
}

vector<int> get(int src) {
    dfs(src);
    reverse(path.begin(), path.end());
    return path;
}
};

```

有向

```

// directed, 0-base.
template <int NV> class Hierholzer {
public:
    int deg[NV];
    vector<int> path;
    multiset<int> G[NV];

    void addedge(int u, int v) {
        G[u].insert(v), deg[u]++, deg[v]--;
    }

    void dfs(int cur) {
        while (!G[cur].empty()) {
            int tar = *G[cur].begin();
            G[cur].erase(G[cur].begin());
            dfs(tar);
        }
        path.push_back(cur);
    }

    bool get() {
        int src = -1, tot = 0, U = 0, D = 0, UZ = 0;
        for (int i = 0; i < NV; i++) {
            tot += G[i].size();
            if (deg[i] != 0) {
                U += (deg[i] == 1), D += (deg[i] == -1), UZ++;
                src = (~src) ? src : i;
            }
        }
        if (UZ != 0 && (UZ != 2 || U != 1 || D != 1)) return false;
        dfs(UZ ? src : 0);
        reverse(path.begin(), path.end());
        return (int)path.size() == tot + 1;
    }
};

```

```

    }

    vector<int> get(int src) {
        dfs(src);
        reverse(path.begin(), path.end());
        return path;
    }
};

```

费用流

```

struct edge {
    int v, cost, flow, cap, next;
    edge() {}
    edge(int V, int Cost, int Flow, int Cap, int nxt) : \
        v(V), cost(Cost), flow(Flow), cap(Cap), next(nxt) {}
} G[maxm << 1];
int tot, head[maxn], cost[maxn], inq[maxn], pre[maxn];

void init() {
    tot = 0;
    memset(head, -1, sizeof head);
}

void addedge(int u, int v, int cap, int cost) {
    G[tot] = edge(v, cost, 0, cap, head[u]); head[u] = tot++;
    G[tot] = edge(u, -cost, cap, cap, head[v]); head[v] = tot++;
}

bool spfa(int src, int dst) {
    memset(inq, 0, sizeof inq);
    memset(pre, -1, sizeof pre);
    memset(cost, 0x3f, sizeof cost);
    queue<int> Q; Q.push(src), cost[src] = 0;
    while (!Q.empty()) {
        int u = Q.front(); Q.pop(), inq[u] = 0;
        for (int i = head[u]; ~i; i = G[i].next) {
            edge &e = G[i];
            if (e.flow < e.cap && chkmin(cost[e.v], cost[u] + e.cost)) {
                pre[e.v] = i;
                if (!inq[e.v]) Q.push(e.v), inq[e.v] = 1;
            }
        }
    }
    return cost[dst] < 0x3f3f3f3f;
}

pair<int, int> mcmf(int src, int dst) {
    int totCost = 0, totFlow = 0;
    while (spfa(src, dst)) {

```

```

int maxFlow = 0x3f3f3f3f;
for (int u = dst; u != src; u = G[pre[u] ^ 1].v) {
    edge &e = G[pre[u]]; // , &r = G[pre[u] ^ 1];
    maxFlow = min(maxFlow, e.cap - e.flow);
}
totCost += maxFlow * cost[dst], totFlow += maxFlow;
for (int u = dst; u != src; u = G[pre[u] ^ 1].v) {
    edge &e = G[pre[u]], &r = G[pre[u] ^ 1];
    e.flow += maxFlow, r.flow -= maxFlow;
}
}
return { totFlow, totCost };
}

```

二分图匹配

```

struct maxMatch {
    int link[maxn], vis[maxn];
    bool find(int u) {
        for (int i = head[u]; i != -1; i = G[i].next) {
            int v = G[i].v;
            if (!vis[v]) {
                vis[v] = 1;
                if (link[v] == -1 || find(link[v])) {
                    link[v] = u;
                    // link[u] = v;
                    return true;
                }
            }
        }
        return false;
    }
    int getans(int n) {
        int ans = 0;
        memset(link, -1, sizeof link);
        for (int i = 1; i <= n; i++) {
            if (link[i] == -1) {
                memset(vis, 0, sizeof vis);
                if (find(i)) ++ans;
            }
        }
        return ans;
    }
};

```

树剖(lca为例)

```

int SZ[N], fa[N], son[N], top[N], dep[N];
int dfn, in[N], out[N];

```



```

void getsz(int u, int d, int f) {
    SZ[u] = 1, dep[u] = d, fa[u] = f;
    son[u] = 0;
    for (auto& v : G[u]) {
        if (v != f) {
            getsz(v, d + 1, u);
            SZ[u] += SZ[v];
            if (SZ[son[u]] < SZ[v]) son[u] = v;
        }
    }
}

void dfs(int u, int t) {
    in[u] = ++dfn, top[u] = t;
    if (son[u]) dfs(son[u], t);
    for (auto& v : G[u]) {
        if (v != fa[u] && v != son[u]) {
            dfs(v, v);
        }
    }
    out[u] = dfn;
}

int getlca(int u, int v) {
    for (; top[u] != top[v]; u = fa[top[u]]) {
        if (dep[top[u]] < dep[top[v]]) swap(u, v);
    }
    return dep[u] < dep[v] ? u : v;
}

```

KM

```

const int N = 505;
const int maxn = 505;
const int INF = 0x3f3f3f3f;

int nx, ny; // point num
int G[maxn][maxn]; // graph
int link[maxn], lx[maxn], ly[maxn], slack[N];
bool visx[N], visy[N];

bool dfs(int x) {
    visx[x] = 1;
    for (int y = 0; y < ny; y++) {
        if (visy[y]) continue;
        int tmp = lx[x] + ly[y] - G[x][y];
        if (tmp == 0) {
            visy[y] = 1;
            if (link[y] == -1 || dfs(link[y])) {

```

```

        link[y] = x;
        return true;
    }
    } else if (slack[y] > tmp) {
        slack[y] = tmp;
    }
}
return false;
}

int KM() {
    memset(link, -1, sizeof link);
    memset(ly, 0, sizeof ly);
    for (int i = 0; i < nx; i++) {
        lx[i] = -INF;
        for (int j = 0; j < ny; j++) {
            if (G[i][j] > lx[i]) lx[i] = G[i][j];
        }
    }
    for (int x = 0; x < nx; x++) {
        memset(slack, 0x3f, sizeof slack);
        while (1) {
            memset(visx, 0, sizeof visx);
            memset(visy, 0, sizeof visy);
            if (dfs(x)) break;
            int d = INF;
            for (int i = 0; i < ny; i++) {
                if (!visy[i] && d > slack[i]) d = slack[i];
            }
            if (d == INF) return -1;
            for (int i = 0; i < nx; i++) {
                if (visx[i]) lx[i] -= d;
            }
            for (int i = 0; i < ny; i++) {
                if (visy[i]) ly[i] += d;
                else slack[i] -= d;
            }
        }
    }
    int res = 0;
    for (int i = 0; i < ny; i++) {
        if (~link[i]) res += G[link[i]][i];
    }
    return res;
}

```

isap

```

const int N = 1e2 + 5;
const int M = 2e4 + 5;

```

```

const int inf = 0x3f3f3f3f;

struct edge {
    int v, flow, cap, next;
} G[M];
int tot, n, src, dst, h[N], cur[N], gap[N], dep[N];

void init() {
    tot = 0;
    memset(h, -1, sizeof h);
}

void addedge(int u, int v, int w) {
    G[tot] = { v, 0, w, h[u] }, h[u] = tot++;
    G[tot] = { u, w, w, h[v] }, h[v] = tot++;
}

void bfs() {
    memset(gap, 0, sizeof gap);
    memset(dep, -1, sizeof dep);

    queue<int> Q; Q.push(dst);
    dep[dst] = 0, gap[0] = 1;
    while (!Q.empty()) {
        int u = Q.front(); Q.pop();
        for (int i = h[u]; ~i; i = G[i].next) {
            int v = G[i].v;
            if (~dep[v]) continue;
            Q.push(v), dep[v] = dep[u] + 1, gap[dep[v]]++;
        }
    }
}

int dfs(int u, int flow) {
    if (u == dst) return flow;
    int used = 0;
    for (int &i = cur[u]; ~i; i = G[i].next) {
        edge &e = G[i];
        if (e.flow < e.cap && dep[e.v] + 1 == dep[u]) {
            int tmp = dfs(e.v, min(e.cap - e.flow, flow - used));
            if (tmp == 0) continue;
            e.flow += tmp, G[i ^ 1].flow -= tmp, used += tmp;
            if (used == flow) return used;
        }
    }
    --gap[dep[u]];
    if (!gap[dep[u]]) dep[src] = n + 1;
    ++gap[++dep[u]];
    return used;
}

```

```

int isap() {
    bfs();
    int res = 0;
    while (dep[src] < n) {
        memcpy(cur, h, sizeof h);
        res += dfs(src, inf);
    }
    return res;
}

```

数学与数论

自适应Simpson积分

$$\int_a^b F(x)dx \Rightarrow \text{asr}(a, b, \text{eps}, \text{simpson}(a, b))$$

```

double simpson(const double& a, const double& b) {
    double c = (a + b) / 2;
    return (F(a) + 4 * F(c) + F(b)) * (b - a) / 6;
}
double asr(double a, double b, double eps, double A) {
    double c = (a + b) / 2;
    double L = simpson(a, c), R = simpson(c, b);
    if (fabs(L + R - A) <= 15 * eps)
        return L + R + (L + R - A) / 15.0;
    return asr(a, c, eps / 2, L) + asr(c, b, eps / 2, R);
}

```

BM推公式大法

```

struct BM {
    static const int MAXN = 10005;
    int n, pn, fail[MAXN];
    double delta[MAXN];
    vector<double> ps[MAXN];
    void Solve(double x[], const int &n) {
        pn = 0;
        memset(fail, 0, sizeof fail);
        memset(delta, 0, sizeof delta);
        ps[0].clear();
        for (int i = 1; i <= n; i++) {
            double dt = -x[i];
            for (int j = 0; j < ps[pn].size(); j++) {
                dt += x[i - j - 1] * ps[pn][j];
            }
            delta[i] = dt;
            if (fabs(dt) <= 1e-8) continue;
            fail[pn] = i;
        }
    }
}

```

```

        if (!pn) {
            ps[++pn].resize(1);
            continue;
        }
        vector<double> &ls = ps[pn - 1];
        double k = -dt / delta[fail[pn - 1]];
        vector<double> cur(i - fail[pn - 1] - 1);
        cur.push_back(-k);
        for (int j = 0; j < ls.size(); j++) {
            cur.push_back(ls[j] * k);
        }
        if (cur.size() < ps[pn].size()) {
            cur.resize(ps[pn].size());
        }
        for (int j = 0; j < ps[pn].size(); j++) {
            cur[j] += ps[pn][j];
        }
        ps[++pn] = cur;
    }
}

void print() {
    for (int i = 0; i < ps[pn].size(); i++) {
        printf("%lf%c", ps[pn][i], (i == ps[pn].size() - 1) ? '\n' : ' ');
    }
}

} B;
double x[BM::MAXN];
int main() {
    for (int n; ~scanf("%d", &n); ) {
        for (int i = 1; i <= n; i++) {
            scanf("%lf", &x[i]);
        }
        B.Solve(x, n), B.print();
    }
}

```

线性基

```

struct LinearBasis {
    const static int MAXL = 50;
    long long a[MAXL + 1];
    LinearBasis() {
        memset(a, 0, sizeof a);
    }
    void insert(long long t) {
        for (int j = MAXL; j >= 0; j--) {
            if (!(t & (1ll << j))) continue;
            if (a[j]) t ^= a[j];
            else {

```

```

        for (int k = 0; k < j; k++) if (t & (1ll << k)) t ^= a[k];
        for (int k = j + 1; k <= MAXL; k++) if (a[k] & (1ll << j)) a[k]
^= t;
        a[j] = t;
        return;
    }
}
};

```

扩展欧几里得

```

pll exgcd(const long long x, const long long y) {
    if (!y) return make_pair(1, 0);
    pll cur = exgcd(y, x % y);
    return make_pair(cur.second, cur.first - (x / y) * cur.second);
}

```

中国剩余定理

```

//v里每个pll中first为被模数, second为模数
pll crt(const vector<pll> & v) {
    ll a = 1, r = 0;
    const int len = v.size();
    for(int i = 0; i < len; i++) {
        pll cur = exgcd(a, v[i].first);
        ll gcd = a * cur.first + v[i].first * cur.second;
        if((v[i].second - r) % gcd != 0) {
            return make_pair(-1, -1);
        }
        const ll p = v[i].first / gcd;
        r += mod(cur.first * ((v[i].second - r) / gcd), p) * a;
        a *= p;
    }
    return make_pair(a, r);
}

```

扩展卢卡斯

```

ll C(ll n, ll m, ll p) {
    if(m > n) return 0;
    ll ret = 1;
    for(ll i = 1; i <= m; i++) {
        ll a = (n + 1 - i) % p, b = mod(exgcd(i % p, p).first, p);
        ret = ret * a % p * b % p;
    }
    return ret;
}

```

```

ll lucas(ll n, ll m, ll p) {
    if(m == 0) {
        return 1;
    }
    return lucas(n / p, m / p, p) * C(n % p, m % p, p) % p;
}

ll cal(ll n, ll a, ll b, ll p) {
    if(!n) return 1;
    ll y = n / p, tmp = 1;
    for(ll i = 1; i <= p; i++) {
        if(i % a) {
            tmp = tmp * i % p;
        }
    }
    ll ans = fpow(tmp, y, p);
    for(ll i = y * p + 1; i <= n; i++) {
        if(i % a) {
            ans = ans * (i % p) % p;
        }
    }
    return ans * cal(n / a, a, b, p) % p;
}

ll multilucas(ll n, ll m, ll a, ll b, ll p) {
    ll s = 0;
    for(ll i = n; i; i /= a) s += i / a;
    for(ll i = m; i; i /= a) s -= i / a;
    for(ll i = n - m; i; i /= a) s -= i / a;
    ll tmp = fpow(a, s, p);
    ll t1 = cal(n, a, b, p), t2 = cal(m, a, b, p), t3 = cal(n - m, a, b,
p);
    return tmp * t1 % p * mod(exgcd(t2, p).first, p) % p * mod(exgcd(t3,
p).first, p) % p;
}

ll exlucas(ll n, ll m, ll p) {
    vector<ll>q, a;
    for(ll i = 2; i * i <= p; i++) {
        if(p % i == 0) {
            q.push_back(1);
            ll t = 0;
            while(p % i == 0) {
                p /= i;
                q.back() *= i;
                t++;
            }
            a.push_back(q.back() == i ? lucas(n, m, q.back()) : multilucas(n,
m, i, t, q.back()));
        }
    }
}

```

```

if(p > 1) {
    q.push_back(p);
    a.push_back(lucas(n, m, p));
}
const int e = q.size();
for(ll i = 1; i < e; i++) {
    pll d = exgcd(q[0], q[i]);
    ll c = a[i] - a[0], g = d.first * q[0] + d.second * q[i];
    if(c % g) exit(-1);
    a[0] = q[0] * mod(c / g * d.first, q[i] / g) + a[0];
    q[0] = q[0] * q[i] / g;
}
return a[0];
}

```

快速乘

```

// mod <= 1e12
inline ll mul(ll a, ll b, ll mod) {
    return (((a * (b >> 20) % mod) << 20) + (a * (b & ((1 << 20) - 1))))
    % mod;
}
// mod <= 1e18
inline ll mul(ll a, ll b, ll mod) {
    ll d = (ll)floor(a * (long double)b / mod + 0.5);
    ll ret = (a * b - d * mod) % mod;
    if (ret < 0) ret += mod;
    return ret;
}

```

exbsgs

```

ll bsgs(ll a, ll b, ll c, ll q = 1, ll d = 0) {
    unordered_map<ll, ll> x;
    ll m = sqrt(c) + 1;
    ll v = 1;
    if(d > 0) {
        for(int i = 1; i <= m; i++) {
            v = fmul(v, a, c);
            x[fmul(v, b, c)] = i;
        }
    } else {
        for(int i = 0; i < m; i++) {
            x[fmul(v, b, c)] = i;
            v = fmul(v, a, c);
        }
    }
    for(int i = 1; i <= m; i++) {
        q = fmul(q, v, c);
    }
}

```



```

        auto it = x.find(q);
        if(it != x.end()) {
            return i * m - it->second + d;
        }
    }
    return -1;
}
// 返回最小正整数n使得  $a^n \bmod m = b$ ;  $O(\sqrt{m})$ 
ll exbsgs(ll a, ll b, ll m) {
    a = mod(a, m), b = mod(b, m);
    if(a == 0) {
        return b > 1 ? -1 : b == 0 && m > 1;
    }
    if(b == 1 && gcd(a, m) != 1) { // b为1时随机应变吧。
        return -1;
    }
    ll g, c = 0, q = 1;
    while((g = gcd(a, m)) != 1) {
        if(b == 1) return c;
        if(b % g) return -1;
        c++;
        b /= g, m /= g;
        q = fmul(a / g, q, m);
    }
    return bsgs(a, b, m, q, c);
}

```

polysum

```

namespace polysum {
ll mod = 998244353LL;
#define rep(i,a,n) for (int i=a;i<n;i++)
#define per(i,a,n) for (int i=n-1;i>=a;i--)
const int D=200005;
ll a[D],f[D],g[D],p[D],p1[D],p2[D],b[D],h[D][2],C[D];
ll powmod(ll a,ll b) {
    ll res=1;
    a%=mod;
    assert(b>=0);
    for(; b; b>>=1) {
        if(b&1) res=res*a%mod;
        a=a*a%mod;
    }
    return res;
}
//函数用途: 给出数列的 (d+1) 项, 其中d为最高次方项
//求出数列的第n项, 数组下标从0开始
ll calcn(int d,ll *a,ll n) { // a[0].. a[d] a[n]
    if (n<=d) return a[n];
    p1[0]=p2[0]=1;

```

```

rep(i, 0, d+1) {
    ll t=(n-i+mod)%mod;
    p1[i+1]=p1[i]*t%mod;
}
rep(i, 0, d+1) {
    ll t=(n-d+i+mod)%mod;
    p2[i+1]=p2[i]*t%mod;
}
ll ans=0;
rep(i, 0, d+1) {
    ll t=g[i]*g[d-i]%mod*p1[i]%mod*p2[d-i]%mod*a[i]%mod;
    if ((d-i)&1) ans=(ans-t+mod)%mod;
    else ans=(ans+t)%mod;
}
return ans;
}

void init(int M) {
    f[0]=f[1]=g[0]=g[1]=1;
    rep(i, 2, M+5) f[i]=f[i-1]*i%mod;
    g[M+4]=powmod(f[M+4], mod-2);
    per(i, 1, M+4) g[i]=g[i+1]*(i+1)%mod;
}

//函数用途: 给出数列的 (m+1) 项, 其中m为最高次方
//求出数列的前 (n-1) 项的和
ll polysum(ll m, ll *a, ll n) { // a[0].. a[m] \sum_{i=0}^{n-1} a[i]
    ll b[D];
    for(int i=0; i<=m; i++) b[i]=a[i];
    b[m+1]=calcn(m, b, m+1);
    rep(i, 1, m+2) b[i]=(b[i-1]+b[i])%mod;
    return calcn(m+1, b, n-1);
}

ll qpolysum(ll R, ll n, ll *a, ll m) { // a[0].. a[m] \sum_{i=0}^{n-1} a[i]*R^i
    if (R==1) return polysum(n, a, m);
    a[m+1]=calcn(m, a, m+1);
    ll r=powmod(R, mod-2), p3=0, p4=0, c, ans;
    h[0][0]=0;
    h[0][1]=1;
    rep(i, 1, m+2) {
        h[i][0]=(h[i-1][0]+a[i-1])*r%mod;
        h[i][1]=h[i-1][1]*r%mod;
    }
    rep(i, 0, m+2) {
        ll t=g[i]*g[m+1-i]%mod;
        if (i&1) p3=((p3-h[i][0]*t)%mod+mod)%mod, p4=((p4-h[i][1]*t)%mod+mod)%mod;
        else p3=(p3+h[i][0]*t)%mod, p4=(p4+h[i][1]*t)%mod;
    }
    c=powmod(p4, mod-2)*(mod-p3)%mod;
    rep(i, 0, m+2) h[i][0]=(h[i][0]+h[i][1]*c)%mod;
    rep(i, 0, m+2) C[i]=h[i][0];
    ans=(calcn(m, C, n)*powmod(R, n)-c)%mod;
    if (ans<0) ans+=mod;
}

```

```

    return ans;
}
} // polysum::init();

```

线性筛

```

struct Seive {
    int maxn;
    vector<bool> isp;
    vector<int> p, phi, mu;
    Seive(int n = 0) : maxn(n), isp(n + 5, true), phi(n + 5, 0), mu(n + 5, 0) {
        solve();
    }
    void solve() {
        isp[0] = isp[1] = false;
        phi[1] = 1;
        mu[1] = 1;
        for (int i = 2; i <= maxn; i++) {
            if (isp[i]) {
                p.push_back(i);
                phi[i] = i - 1;
                mu[i] = -1;
            }
            for (int j = 0; j < (int)p.size() && i * p[j] <= maxn; j++) {
                const int cur = i * p[j];
                isp[cur] = false;
                if (i % p[j]) {
                    phi[cur] = phi[i] * (p[j] - 1);
                    mu[cur] = -mu[i];
                } else {
                    phi[cur] = phi[i] * p[j];
                    mu[cur] = 0;
                    break;
                }
            }
        }
    }
};

```

MillerRabin素性测试

```

const int psize = 1010000;
bool isp[psize];
int prime[psize], tot;
void prime_table() {
    register int i, j;
    for (i = 2, tot = 0; i < psize; i++) {
        if (!isp[i]) prime[tot++] = i;
        for (j = 0; j < tot && prime[j] * i < psize; j++) {
            isp[prime[j] * i] = true;
        }
    }
}

```

```

        if (i % prime[j] == 0) break;
    }
}
}
bool witness(ll a, ll n) {
    int t = 0;
    ll u = n - 1;
    for (; ~u & 1; u >>= 1) t++;
    ll x = qpow(a, u, n), _x = 0;
    while (t--) {
        _x = mul(x, x, n);
        if (_x == 1 && x != 1 && x != n - 1) return true;
        x = _x;
    }
    return _x != 1;
}
bool Miller(ll n) {
    if (n < 2) return false;
    if (n < psize) return !isp[n];
    if (~n & 1) return false;
    for (int j = 0; j <= 7; j++) {
        if (witness(rand() % (n - 1) + 1, n)) {
            return false;
        }
    }
    return true;
}
}

```

pollard_rho分解质因数

```

int tot;
long long factor[10000];
long long pollard_rho(long long x, long long c) {
    long long i = 1, k = 2;
    long long x0 = rand() % x, y = x0;
    while (true) {
        i++;
        x0 = (mul(x0, x0, x) + c) % x;
        long long d = __gcd(y - x0, x);
        if (d != 1 && d != x) return d;
        if (y == x0) return x;
        if (i == k) {
            y = x0, k <<= 1;
        }
    }
}
void findfac(long long n) {
    if (Miller(n)) {
        factor[tot++] = n;
        return;
    }
}

```

```

}
long long p = n;
while (p >= n) p = pollard_rho(p, rand() % (n - 1) + 1);
findfac(p), findfac(n / p);
}

```

fft

```

namespace fft {
    const double pi = acos(-1.0);
    struct Complex {
        double r, i;
        Complex(double x = 0, double y = 0) : r(x), i(y) {}
        Complex operator+ (const Complex& b) const {
            return Complex(r + b.r, i + b.i);
        }
        Complex operator- (const Complex& b) const {
            return Complex(r - b.r, i - b.i);
        }
        Complex operator* (const Complex& b) const {
            return Complex(r * b.r - i * b.i, r * b.i + i * b.r);
        }
    };
    Complex conj(Complex a) { return Complex(a.r, -a.i); }

    int base = 1;
    vector<int> rev = { 0, 1 };
    vector<Complex> roots = { { 0, 0 }, { 1, 0 } };

    void ensure_base(int nbase) {
        if (nbase <= base) return;
        rev.resize(1 << nbase);
        for (int i = 0; i < (1 << nbase); i++) {
            rev[i] = (rev[i >> 1] >> 1) + ((i & 1) << (nbase - 1));
        }
        roots.resize(1 << nbase);
        while (base < nbase) {
            double angle = 2 * pi / (1 << (base + 1));
            for (int i = 1 << (base - 1); i < (1 << base); i++) {
                roots[i << 1] = roots[i];
                double angle_i = angle * (2 * i + 1 - (1 << base));
                roots[(i << 1) + 1] = Complex(cos(angle_i), sin(angle_i));
            }
            base++;
        }
    }

    void fft(vector<Complex> &a, int n = -1) {
        if (n == -1) {
            n = a.size();
        }
    }
}

```

```

assert((n & (n - 1)) == 0);
int zeros = __builtin_ctz(n);
ensure_base(zeros);
int shift = base - zeros;
for (int i = 0; i < n; i++) {
    if (i < (rev[i] >> shift)) {
        swap(a[i], a[rev[i] >> shift]);
    }
}
for (int k = 1; k < n; k <= 1) {
    for (int i = 0; i < n; i += 2 * k) {
        for (int j = 0; j < k; j++) {
            Complex z = a[i + j + k] * roots[j + k];
            a[i + j + k] = a[i + j] - z;
            a[i + j] = a[i + j] + z;
        }
    }
}
}

vector<Complex> fa, fb;
vector<int> multiply(const vector<int> &a, const vector<int> &b) {
    int need = a.size() + b.size() - 1;
    int nbase = 32 - __builtin_clz(need) - (need - need & (-need) == 0);
    ensure_base(nbase);
    int sz = 1 << nbase;
    if (sz > (int) fa.size()) {
        fa.resize(sz);
    }
    for (int i = 0; i < sz; i++) {
        int x = (i < (int) a.size() ? a[i] : 0);
        int y = (i < (int) b.size() ? b[i] : 0);
        fa[i] = Complex(x, y);
    }
    fft(fa, sz);
    Complex r(0, -0.25 / sz);
    for (int i = 0; i <= (sz >> 1); i++) {
        int j = (sz - i) & (sz - 1);
        Complex z = (fa[j] * fa[j] - conj(fa[i] * fa[i])) * r;
        if (i != j) {
            fa[j] = (fa[i] * fa[i] - conj(fa[j] * fa[j])) * r;
        }
        fa[i] = z;
    }
    fft(fa, sz);
    vector<int> res(need);
    for (int i = 0; i < need; i++) {
        res[i] = fa[i].r + 0.5;
    }
    return res;
}

```

```

vector<int> multiply_mod(const vector<int> &a, const vector<int> &b, int m,
int eq = 0) {
    int need = a.size() + b.size() - 1;
    int nbase = 32 - __builtin_clz(need) - (need - need & (-need) == 0);
    ensure_base(nbase);
    int sz = 1 << nbase;
    if (sz > (int) fa.size()) {
        fa.resize(sz);
    }
    for (int i = 0; i < (int) a.size(); i++) {
        int x = (a[i] % m + m) % m;
        fa[i] = Complex(x & ((1 << 15) - 1), x >> 15);
    }
    fill(fa.begin() + a.size(), fa.begin() + sz, Complex {0, 0});
    fft(fa, sz);
    if (sz > (int) fb.size()) {
        fb.resize(sz);
    }
    if (eq) {
        copy(fa.begin(), fa.begin() + sz, fb.begin());
    } else {
        for (int i = 0; i < (int) b.size(); i++) {
            int x = (b[i] % m + m) % m;
            fb[i] = Complex(x & ((1 << 15) - 1), x >> 15);
        }
        fill(fb.begin() + b.size(), fb.begin() + sz, Complex {0, 0});
        fft(fb, sz);
    }
    double ratio = 0.25 / sz;
    Complex r2(0, -1), r3(ratio, 0), r4(0, -ratio), r5(0, 1);
    for (int i = 0; i <= (sz >> 1); i++) {
        int j = (sz - i) & (sz - 1);
        Complex a1 = (fa[i] + conj(fa[j]));
        Complex a2 = (fa[i] - conj(fa[j])) * r2;
        Complex b1 = (fb[i] + conj(fb[j])) * r3;
        Complex b2 = (fb[i] - conj(fb[j])) * r4;
        if (i != j) {
            Complex c1 = (fa[j] + conj(fa[i]));
            Complex c2 = (fa[j] - conj(fa[i])) * r2;
            Complex d1 = (fb[j] + conj(fb[i])) * r3;
            Complex d2 = (fb[j] - conj(fb[i])) * r4;
            fa[i] = c1 * d1 + c2 * d2 * r5;
            fb[i] = c1 * d2 + c2 * d1;
        }
        fa[j] = a1 * b1 + a2 * b2 * r5;
        fb[j] = a1 * b2 + a2 * b1;
    }
    fft(fa, sz);
    fft(fb, sz);
    vector<int> res(need);
    for (int i = 0; i < need; i++) {

```

```

        long long aa = fa[i].r + 0.5;
        long long bb = fb[i].r + 0.5;
        long long cc = fa[i].i + 0.5;
        res[i] = (aa + ((bb % m) << 15) + ((cc % m) << 30)) % m;
    }
    return res;
}

vector<int> square_mod(const vector<int> &a, int m) {
    return multiply_mod(a, a, m, 1);
}
}

```

ntt

```

namespace ntt {
    int qpow(int a, int t, int mod) {
        ll b = 1;
        for (; t; t >>= 1, a = (ll)a * a % mod) {
            if (t & 1) b = b * a % mod;
        }
        return b;
    }
    int revv(int x, int bits) {
        int ret = 0;
        for (int i = 0; i < bits; i++) {
            ret <<= 1, ret |= x & 1, x >>= 1;
        }
        return ret;
    }
    void ntt(vector<int> &a, bool rev, int mod, int root) {
        int n = (int)a.size(), bits = 31 - __builtin_clz(n);
        for (int i = 0; i < n; i++) {
            int j = revv(i, bits);
            if (i < j) swap(a[i], a[j]);
        }
        for (int k = 1; k < n; k <= 1) {
            int e = qpow(root, (mod - 1) / 2 / k, mod);
            if (rev) e = qpow(e, mod - 2, mod); // exgcd is better
            for (int i = 0; i < n; i += 2 * k) {
                ll w = 1;
                for (int j = 0; j < k; j++, w = w * e % mod) {
                    int x = a[i + j], y = w * a[i + j + k] % mod;
                    a[i + j] = (x + y) % mod, a[i + j + k] = (x - y + mod) % mod;
                }
            }
        }
        if (rev) {
            int inv = qpow(n, mod - 2, mod); // exgcd is better
            for (int i = 0; i < n; i++) a[i] = 1ll * a[i] * inv % mod;
        }
    }
}

```



```

    }
    // mod = 998244353 = (119 << 23) + 1, root = 3, // = (119 << 23, 3)
    // For p < 2^30, (5 << 25, 3), (7 << 26, 3),
    // (479 << 21, 3) and (483 << 21, 5), last two are > 10^9
    vector<int> conv(const vector<int>& a, const vector<int>& b, const int mod =
(119 << 23) + 1, int root = 3) {
    int sz = (int)a.size() + (int)b.size() - 1;
    int L = sz > 1 ? (32 - __builtin_clz(sz - 1)) : 0, n = 1 << L;
    vector<int> av(n), bv(n);
    copy(a.begin(), a.end(), av.begin());
    copy(b.begin(), b.end(), bv.begin());
    ntt(av, false, mod, root), ntt(bv, false, mod, root);
    for (int i = 0; i < n; i++) {
        av[i] = 1ll * av[i] * bv[i] % mod;
    }
    ntt(av, true, mod, root);
    av.resize(sz);
    return av;
}
}

```

linear_seq

```

#define rep(i,a,n) for (int i=a;i<n;i++)
#define per(i,a,n) for (int i=n-1;i>=a;i--)
#define pb push_back
#define mp make_pair
#define all(x) (x).begin(), (x).end()
#define SZ(x) ((int)(x).size())
typedef vector<int> VI;
typedef pair<int, int> PII;
const ll mod = 1e9 + 7;
ll powmod(ll a, ll b) {
    ll res = 1; a %= mod;
    for (; b; b >>= 1, a = a * a % mod) {
        if (b & 1) res = res * a % mod;
    }
    return res;
}
namespace linear_seq {
    const int N = 10010;
    ll res[N], base[N], _c[N], _md[N];

    vector<int> Md;
    void mul(ll *a, ll *b, int k) {
        rep(i, 0, k + k) _c[i] = 0;
        rep(i, 0, k) if (a[i]) rep(j, 0, k) _c[i + j] = (_c[i + j] + a[i] * b[j]) %
mod;
        for (int i = k + k - 1; i >= k; i--) if (_c[i])

```

```

        rep(j, 0, SZ(Md)) _c[i - k + Md[j]] = (_c[i - k + Md[j]] - _c[i] *
_md[Md[j]]) % mod;
        rep(i, 0, k) a[i] = _c[i];
    }
int solve(ll n, VI a, VI b) {
    ll ans = 0, pnt = 0;
    int k = SZ(a);
    assert(SZ(a) == SZ(b));
    rep(i, 0, k) _md[k - 1 - i] = -a[i]; _md[k] = 1;
    Md.clear();
    rep(i, 0, k) if (_md[i] != 0) Md.push_back(i);
    rep(i, 0, k) res[i] = base[i] = 0;
    res[0] = 1;
    while ((1ll << pnt) <= n) pnt++;
    for (int p = pnt; p >= 0; p--) {
        mul(res, res, k);
        if ((n >> p) & 1) {
            for (int i = k - 1; i >= 0; i--) res[i + 1] = res[i]; res[0] = 0;
            rep(j, 0, SZ(Md)) res[Md[j]] = (res[Md[j]] - res[k] * _md[Md[j]]) % mod;
        }
    }
    rep(i, 0, k) ans = (ans + res[i] * b[i]) % mod;
    if (ans < 0) ans += mod;
    return ans;
}
VI BM(VI s) {
    VI C(1, 1), B(1, 1);
    int L = 0, m = 1, b = 1;
    rep(n, 0, SZ(s)) {
        ll d = 0;
        rep(i, 0, L + 1) d = (d + (1ll)C[i] * s[n - i]) % mod;
        if (d == 0) ++m;
        else if (2 * L <= n) {
            VI T = C;
            ll c = mod - d * powmod(b, mod - 2) % mod;
            while (SZ(C) < SZ(B) + m) C.pb(0);
            rep(i, 0, SZ(B)) C[i + m] = (C[i + m] + c * B[i]) % mod;
            L = n + 1 - L; B = T; b = d; m = 1;
        } else {
            ll c = mod - d * powmod(b, mod - 2) % mod;
            while (SZ(C) < SZ(B) + m) C.pb(0);
            rep(i, 0, SZ(B)) C[i + m] = (C[i + m] + c * B[i]) % mod;
            ++m;
        }
    }
    return C;
}
int gao(VI a, ll n) {
    VI c = BM(a);
    c.erase(c.begin());
    rep(i, 0, SZ(c)) c[i] = (mod - c[i]) % mod;

```

```

        return solve(n, c, VI(a.begin(), a.begin() + SZ(c)));
    }
};

```

MeisselLehmer

Count the number of primes in $[1, n]$.

```

namespace pcf {
const int N = 5e6 + 2;
bool np[N];
int prime[N], pi[N];
int getprime() {
    int cnt = 0;
    np[0] = np[1] = 1;
    pi[0] = pi[1] = 0;
    for (int i = 2; i < N; i++) {
        if (!np[i])
            prime[++cnt] = i;
        pi[i] = cnt;
        for (int j = 1; j <= cnt && i * prime[j] < N; ++j) {
            np[i * prime[j]] = 1;
            if (i % prime[j] == 0)
                break;
        }
    }
    return cnt;
}

const int M = 7;
const int PM = 2 * 3 * 5 * 7 * 11 * 13 * 17;
int phi[PM + 1][M + 1], sz[M + 1];
void init() {
    getprime();
    sz[0] = 1;
    for (int i = 0; i <= PM; i++)
        phi[i][0] = i;
    for (int i = 1; i <= M; i++) {
        sz[i] = prime[i] * sz[i - 1];
        for (int j = 1; j <= PM; j++)
            phi[j][i] = phi[j][i - 1] - phi[j / prime[i]][i - 1];
    }
}

int sqrt2(ll x) {
    ll r = ll(sqrt(x - 0.1));
    while (r * r <= x)
        ++r;
    return int(r - 1);
}

int sqrt3(ll x) {
    ll r = ll(cbrt(x - 0.1));

```

```

while (r * r * r <= x)
    ++r;
return int(r - 1);
}

ll getphi(ll x, int s) {
    if (s == 0)
        return x;
    if (s <= M)
        return phi[x % sz[s]][s] + (x / sz[s]) * phi[sz[s]][s];
    if (x <= prime[s] * prime[s])
        return pi[x] - s + 1;
    if (x <= prime[s] * prime[s] * prime[s] && x < N) {
        int s2x = pi[sqrt2(x)];
        ll ans = pi[x] - (s2x + s - 2) * (s2x - s + 1) / 2;
        for (int i = s + 1; i <= s2x; i++)
            ans += pi[x / prime[i]];
        return ans;
    }
    return getphi(x, s - 1) - getphi(x / prime[s], s - 1);
}

ll getpi(ll x) {
    if (x < N) return pi[x];
    ll ans = getphi(x, pi[sqrt3(x)]) + pi[sqrt3(x)] - 1;
    for (int i = pi[sqrt3(x)] + 1, ed = pi[sqrt2(x)]; i <= ed; ++i)
        ans -= getpi(x / prime[i]) - i + 1;
    return ans;
}

ll lehmer(ll x) {
    if (x < N) return pi[x];
    int a = int(lehmer(sqrt2(sqrt2(x))));
    int b = int(lehmer(sqrt2(x)));
    int c = int(lehmer(sqrt3(x)));
    ll sum = getphi(x, a) + ll(b + a - 2) * (b - a + 1) / 2;
    for (int i = a + 1; i <= b; i++) {
        ll w = x / prime[i];
        sum -= lehmer(w);
        if (i > c)
            continue;
        ll lim = lehmer(sqrt2(w));
        for (int j = i; j <= lim; j++)
            sum -= lehmer(w / prime[j]) - (j - 1);
    }
    return sum;
}
}

```