

规格说明：输入两个 $\leq 80$ 的整数，求和，如果和 $\leq 100$ ，输出和；如果不满足上述条件，输出-1。

Z 表示：

Add
$a?, b? : Z$ $Sum! : Z$
$(0 \leq a? \leq 80 \wedge 0 \leq b? \leq 80 \wedge a? + b? \leq 100 \wedge sum! = a? + b?) \vee$ $(a? < 0 \vee a? > 80 \vee b? < 0 \vee b? > 80 \vee (0 \leq a? \leq 80 \wedge 0 \leq b? \leq 80 \wedge a? + b? > 100) \wedge sum! = -1)$

手工转换成析取范式：

$(0 \leq a? \leq 80 \wedge 0 \leq b? \leq 80 \wedge a? + b? \leq 100 \wedge sum! = a? + b?) \vee$   
 $(a? < 0 \wedge sum! = -1) \vee$   
 $(a? > 80 \wedge sum! = -1) \vee$   
 $(b? < 0 \wedge sum! = -1) \vee$   
 $(a? > 80 \wedge sum! = -1) \vee$   
 $(0 \leq a? \leq 80 \wedge 0 \leq b? \leq 80 \wedge a? + b? > 100 \wedge sum! = -1)$

将 Z 规格转换为 Z3:

```
(declare-const a Int)
(declare-const b Int)
(declare-const sum Int)

(assert (or (and (<= a 80) (<= 0 a) (<= b 80) (<= 0 b) (<= (+ a b) 100)
                (= (+ a b) sum))
            (and (or (< a 0) (> a 80) (< b 0) (> b 80) (and (<= a 80) (<= 0 a) (<= b 80)
                (<= 0 b) (> (+ a b) 100))) (= sum -1)))
))
```

Z3 生成 DNF:

```
-----DNF-----
(goals
(goal
  (<= a 80)
  (<= 0 a)
  (<= b 80)
  (<= 0 b)
  (<= (+ a b) 100)
  (= (+ a b) sum)
```

```

    :precision precise :depth 2)
(goal
  (not (<= 0 a))
  (= sum (- 1))
  :precision precise :depth 3)
(goal
  (not (<= a 80))
  (= sum (- 1))
  :precision precise :depth 3)
(goal
  (not (<= 0 b))
  (= sum (- 1))
  :precision precise :depth 3)
(goal
  (not (<= b 80))
  (= sum (- 1))
  :precision precise :depth 3)
(goal
  (<= a 80)
  (= sum (- 1))
  (<= 0 a)
  (<= b 80)
  (<= 0 b)
  (not (<= (+ a b) 100))
  :precision precise :depth 3)
)

```