

Puffin: Overview

July 16, 2016

The code Puffin[1] is an FEL simulation code - it is a so-called ‘unaveraged’ FEL code, which has an enhanced resolution over that of more conventional averaged codes. It can model fast changes in both the electron beam and radiation temporal structure, and can model any frequency (limited by the Niquist condition). The code has undergone many improvements and extended its functionality since the initial publication in [1]. It no longer uses an external linear solver package, and some of the scaling has changed - see below. Before, only the electron beam was distributed in memory across MPI nodes - now both the field and the beam are stored and solved in parallel, enabling the modelling of extremely large systems.

Puffin can now output data in hdf5 format, with VizSchema metadata added to allow visualization with *e.g.* Visit on a cluster. Some visualization examples are shown below in figures 1 and 2.

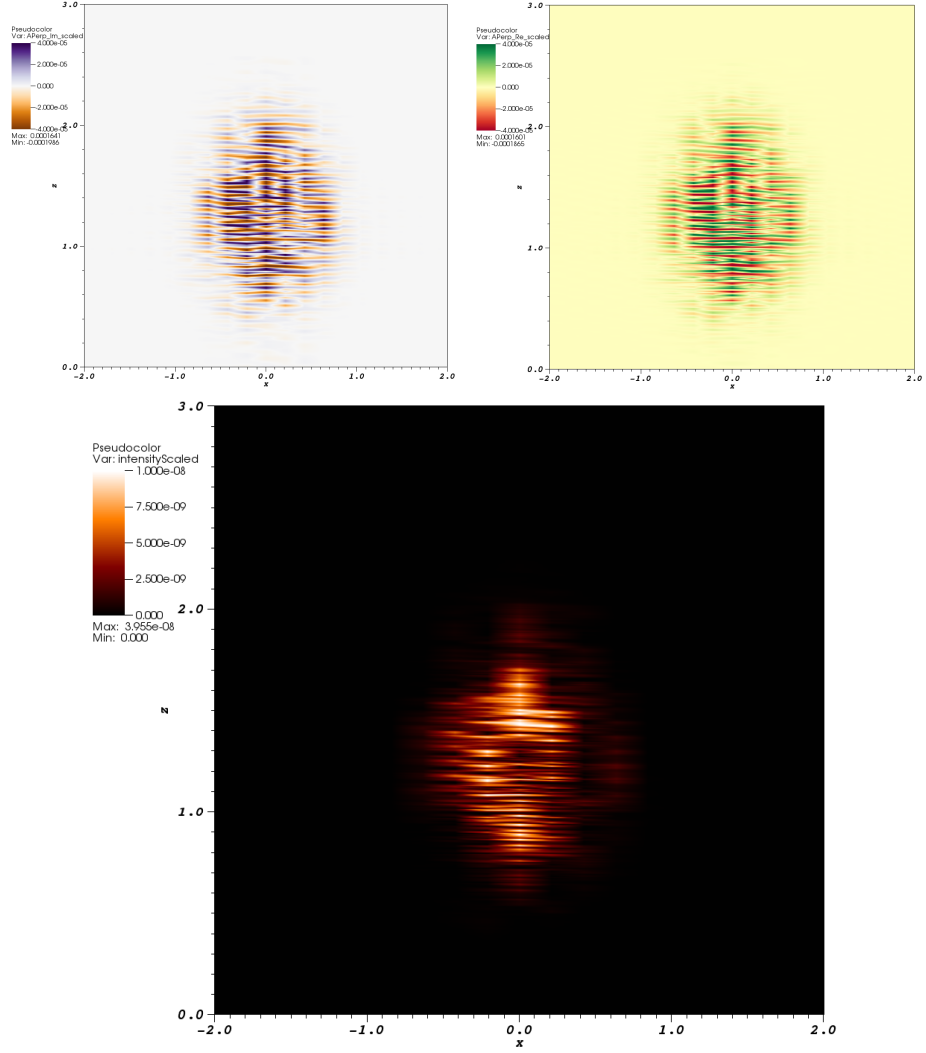


Figure 1: Radiated spontaneous field from Puffin in the first few undulator periods - x (top left) and y (top right) polarized fields, and instantaneous intensity (bottom), at $y = 0$. Radiation is propagating in the negative z direction (the vertical axis). One can see the noisy phase of the radiation in both transverse (x) and temporal (z) directions, which is due to the shot-noise of the electron beam.

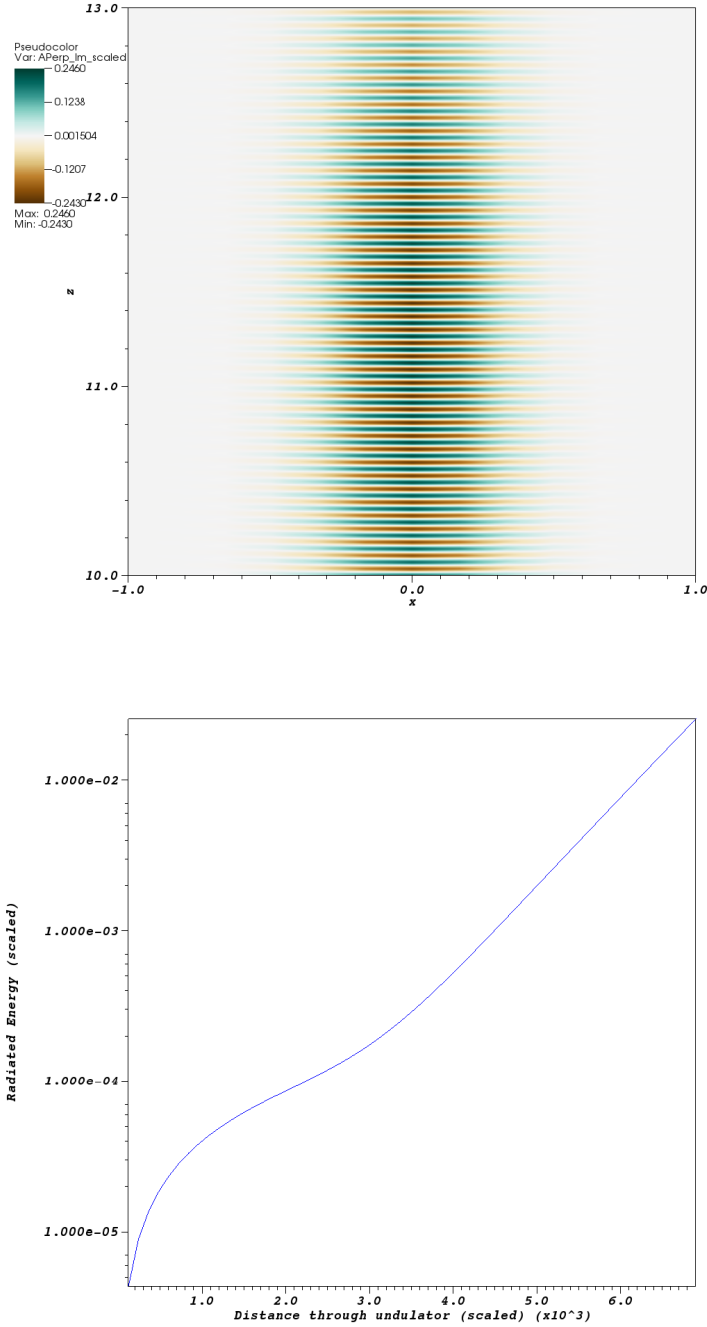


Figure 2: Radiated field from Puffin after amplification in the undulator - x polarized field (top). Radiated energy vs scaled distance through the undulator is on the bottom. Observe the noise from the previous figure has disappeared; the amplification process cause the electrons to align and radiate in phase.

1 Overview

The system of equations solved by Puffin have been altered from those described in [1]. They are now:

$$\left[\frac{1}{2} \left(\frac{\partial^2}{\partial \bar{x}^2} + \frac{\partial^2}{\partial \bar{y}^2} \right) - \frac{\partial^2}{\partial \bar{z} \partial \bar{z}_2} \right] A_\perp = -\frac{1}{\bar{n}_p} \frac{\partial}{\partial \bar{z}_2} \sum_{j=1}^N \frac{\bar{p}_{\perp j}}{\Gamma_j} (1 + \eta p_{2j}) \delta^3(\bar{x}_j, \bar{y}_j, \bar{z}_{2j}) \quad (1)$$

$$\frac{d\bar{p}_{\perp j}}{d\bar{z}} = \frac{1}{2\rho} \left[i\alpha b_\perp - \frac{\eta p_{2j}}{\kappa^2} A_\perp \right] - i\kappa \frac{\bar{p}_{\perp j}}{\Gamma_j} (1 + \eta p_{2j}) \alpha b_z \quad (2)$$

$$\frac{d\Gamma_j}{d\bar{z}} = -\rho \frac{(1 + \eta p_{2j})}{\Gamma_j} (\bar{p}_{\perp j} A_{\perp j}^* + c.c.) \quad (3)$$

$$\frac{d\bar{z}_{2j}}{d\bar{z}} = p_{2j} \quad (4)$$

$$\frac{d\bar{x}_j}{d\bar{z}} = \frac{2\rho\kappa}{\sqrt{\eta}\Gamma_j} (1 + \eta p_{2j}) \Re(\bar{p}_{\perp j}) \quad (5)$$

$$\frac{d\bar{y}_j}{d\bar{z}} = -\frac{2\rho\kappa}{\sqrt{\eta}\Gamma_j} (1 + \eta p_{2j}) \Im(\bar{p}_{\perp j}). \quad (6)$$

Scaled parameters are:-

$$\begin{aligned} \bar{z}_{2j} &= \frac{ct_j - z}{l_c}, & \bar{z} &= \frac{z}{l_g}, \\ \bar{p}_\perp &= \frac{p_\perp}{mca_u}, & A_\perp &= \frac{e\kappa l_g}{\gamma_0 m c^2} E_\perp, \\ (\bar{x}, \bar{y}) &= \frac{(x, y)}{\sqrt{l_g l_c}}, & l_g &= \frac{\lambda_w}{4\pi\rho}, \\ l_c &= \frac{\lambda_r}{4\pi\rho}, & \Gamma_j &= \frac{\gamma_j}{\gamma_0}, \\ \rho &= \frac{1}{\gamma_0} \left(\frac{a_u \omega_p}{4ck_u} \right)^{2/3}, & a_u &= \frac{eB_0}{mck_u}, \\ \kappa &= \frac{a_u}{2\rho\gamma_0}, & b_\perp &= b_x - ib_y, \end{aligned}$$

B_0 is the peak magnetic field in the wiggler. $\omega_p = \sqrt{e^2 n_p / \epsilon_0 m}$ is the (non-relativistic) plasma frequency, and n_p is the peak spatial number density of the electron beam ($N_e / \delta_x \delta_y \delta_z$). $E_\perp = E_x - iE_y$ are the x and y radiation electric field vectors. γ_0 is the reference energy (Lorentz factor), which is usually taken as the mean beam energy.

The scaled reference velocity,

$$\eta = \frac{1 - \beta_{zr}}{\beta_{zr}} = \frac{\lambda_r}{\lambda_u} = \frac{l_c}{l_g}, \quad (7)$$

where β_{zr} is some reference velocity scaled to c , which is sensible (but not, strictly speaking, necessary) to take as the mean longitudinal electron velocity in the wiggler, so that

$$\beta_{zr} = \sqrt{1 - \frac{1}{\gamma_0^2} (1 + \bar{a}_u^2)}, \quad (8)$$

where \bar{a}_u is the *rms* undulator parameter. This defines the velocity at which the electrons travel in the scaled \bar{z}_2 frame. More generally, η describes an *ideal* resonance condition - electrons resonant with wavelength λ_r will travel with velocity $p_2 = 1$ through the \bar{z}_2 frame.

p_{2j} may be worked out analytically from

$$p_{2j} = \frac{1}{\eta} \left[\left(1 - \frac{(1 + a_u^2 |\bar{p}_{\perp j}|^2)}{\gamma_r^2 \Gamma_j^2} \right)^{-1/2} - 1 \right] \quad (9)$$

at each step. It is NOT output from Puffin.

Outputs from Puffin are the scaled radiation field A_\perp , electron phase space coords $\bar{x}, \bar{y}, \bar{z}_2, \bar{p}_\perp, \Gamma$, and scaled distance through the undulator \bar{z} . The normalized electron weights are in the file NormChiDataFile.dat (normalised to the peak *spatial* (3D) density).

Compared to the original Puffin paper [1], now the peak magnetic fields are used to scale the system of eqns (as opposed to the *rms* values used previously). Previously (e.g. as described in [1]), the energy exchange was

modelled through the scaled longitudinal velocity p_2 . This was problematic in multiple ways from a computational point of view, since p_2 is a function of the energy, p_x and p_y , so that the same quantity was essentially being calculated twice, leading to large errors in some cases. The energy exchange is instead now modelled directly through the scaled variable $\Gamma_j = \gamma_j/\gamma_r$, meaning smaller numerical errors and enabling a significantly larger step size.

The formalism for including a variation in the magnetic undulator field, so that $B_0(\bar{z})$ now varies, was included in [2], and is varied using the parameter $\alpha(\bar{z}) = \frac{B_0(\bar{z})}{B_0(\bar{z}=0)}$.

In the most basic form, the input requires 3 files - a ‘main’ input file for parameters, numerical integration, and description of the field mesh, a ‘beam’ input file describing the electron beam, and a ‘seed’ input file describing the radiation seed. Optionally, a lattice file can be used to setup an undulator-chicane lattice.

1.1 Parameters

Description of parameters:-

sRho

ρ , the FEL parameter. This specifies the scaling of the system. It does **not** have to be strictly correct - it only describes the scaling. The simulation can be performed, and the system may be scaled back to SI units using the supplied scripts (NOT SUPPLIED YET!!). If it is correct, however (meaning, it has been calculated from the beam and undulator parameters input), then the scaled notation becomes physically relevant. For an ideal, 1D system, the system should saturate at intensity $|A|^2 \approx 1$, and the system should be firmly in the high or exponential gain regime at $\bar{z} \approx 2 - 3$. This allows one to see how efficiently the system is lasing w.r.t its ideal case.

saw

a_u , the undulator parameter defined with the peak on-axis magnetic field.

sgamma_r

γ_0 , the reference (usually the mean) beam energy.

lambda_w

λ_u , the undulator, or wiggler, period.

zundType

Allows one to select from a choice of undulators. Choices are ‘curved’, ‘planepole’, and ‘helical’, described analytically below. If neither of these are chosen, then the default elliptical undulator is chosen, with polarization specified by u_x and u_y .

sux, suy

u_x and u_y - the relative peak magnetic field of the undulator in each transverse polarization. Usually, at least one should be = 1, and the other between 0 (planar) and 1 (helical). If they are not defined, the default is helical, $u_x = u_y = 1$.

qOneD

Logical. If **.true.**, Puffin will be run in 1D mode. Default is **.true.**, since this is the least computationally expensive option.

qFieldEvolve

Logical. If = **.false.**, then the radiation field evolution will be switched off. This is obviously artificial and very rarely used, but can be useful for debugging in some instances. Default is = **.true.**

qElectronsEvolve

Logical. If = **.false.**, then the electron equations are not solved in the integration steps. Like when qFieldEvolve= **.false.**, this is obviously artificial and very rarely used, but can be useful for debugging in some instances. Default is = **.true.**

qElectronFieldCoupling

Logical. If = **.false.**, then the radiation field feedback onto the electrons is switched off by setting the field terms in the electron evolution equations = 0, and so switches off the amplification of the radiation from the electrons. This is unphysical, but is used more often than when qFieldEvolve and qElectronsEvolve = **.false.** . It can often be used to check for gain in the FEL in low gain situations, or to check whether amplification has occurred rather than coherent emission (CSE) effects due to *e.g.* fine structure in the beam. When = **.false.**, this will give the purely spontaneous emission (coherent or incoherent) from the electrons in the wiggler. If there is no appreciable difference between the qElectronFieldCoupling=true and false cases, then there has been negligible FEL amplification.

qFocussing

Allows one to switch the strong focussing channel on or off. If =bf **.true.**, the strong focusing is switched on with values specified by sKBetaXSF and sKBetaYSF. If qFocussing=**.true.**, yet no focussing strength is specified (sKBetaXSF or sKBetaYSF), then strong focusing is effectively switched off in that dimension. Default = **.false.**.

qDiffraction

Switches modelling of diffraction of the radiation field on or off. If =**.true.**, field diffraction is modelled. This can be useful to switch off only really for debugging purposes. Default = **.true.**.

1.2 3D Magnetic Fields

The undulator is modelled analytically, and the model must include the fast wiggle motion. Puffin may be modified in the future to allow a map of the undulator field to be input. For now, there are a few generic undulator model employed. The magnetic fields for use in Puffin are the helical, plane-pole, and canted-pole undulator fields discussed in [3], which in the scaled notation

here are:-

helical

$$b_x = \cos(\bar{z}/2\rho) \quad (10)$$

$$b_y = \sin(\bar{z}/2\rho) \quad (11)$$

$$b_z = \frac{\sqrt{\eta}}{2\rho}(-\bar{x} \sin(\bar{z}/(2\rho)) + \bar{y} \cos(\bar{z}/(2\rho))) \quad (12)$$

plane-pole

$$b_x = 0 \quad (13)$$

$$b_y = \cosh((\sqrt{\eta}/2\rho)\bar{y}) \sin(\bar{z}/2\rho) \quad (14)$$

$$b_z = \sinh((\sqrt{\eta}/2\rho)\bar{y}) \cos(\bar{z}/(2\rho)) \quad (15)$$

canted-pole

$$b_x = \frac{\bar{k}_{\beta x}}{\bar{k}_{\beta y}} \sinh(\bar{k}_{\beta x}\bar{x}) \sinh(\bar{k}_{\beta y}\bar{y}) \sin(\bar{z}/2\rho) \quad (16)$$

$$b_y = \cosh(\bar{k}_{\beta x}\bar{x}) \cosh(\bar{k}_{\beta y}\bar{y}) \sin(\bar{z}/2\rho) \quad (17)$$

$$b_z = \frac{\sqrt{\eta}}{2\rho\bar{k}_{\beta x}} \cosh(\bar{k}_{\beta x}\bar{x}) \sinh(\bar{k}_{\beta y}\bar{y}) \cos(\bar{z}/2\rho) \quad (18)$$

variably polarized elliptical

$$b_x = u_x \cos(\bar{z}/2\rho) \quad (19)$$

$$b_y = u_y \sin(\bar{z}/2\rho) \quad (20)$$

$$b_z = \frac{\sqrt{\eta}}{2\rho}(u_x\bar{x} \sin(\bar{z}/(2\rho)) + u_y\bar{y} \cos(\bar{z}/(2\rho))) \quad (21)$$

In the 1D approximation, $b_z = 0$.

All of the above have an associated ‘natural’ focusing channel, which arises from the off-axis variation in the magnetic fields. This motion arises naturally when numerically solving the equations, and is not superimposed upon the electron motion.

1.3 Undulator Ends

The undulators also include entry and exit tapers, and they may be switched on or off in the input file with the flag **qUndEnds**. Setting this to true will model a smooth taper up and down of the undulator magnetic fields in the first and last 2 periods of the undulator, taking the form of a \cos^2 . If they are switched off, the beam is artificially initialized with an ‘expected’ initial condition in the transverse coordinates for that undulator. Including these ends will model a more realistic and natural entry and exit from the undulator, and will reduce CSE effects from the shape of the wiggler.

The precise description of the undulator ends are as follows. Note the presence of corrective terms in addition to the main \cos^2 term, which ensure the beam oscillates close to the axis. (Note also the very small non-zero initial z -magnetic field in each case, which we find has no noticeable deleterious effects in practice.)

Helical Front

$$b_x = \frac{1}{4} \sin(\bar{z}/16\rho) \cos(\bar{z}/16\rho) \sin(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \quad (22)$$

$$b_y = -\frac{1}{4} \sin(\bar{z}/16\rho) \cos(\bar{z}/16\rho) \cos(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \quad (23)$$

$$\begin{aligned} b_z = \frac{\sqrt{\eta}}{2\rho} \Big[& \bar{x} \left(\frac{1}{32} \cos(\bar{z}/8\rho) \sin(\bar{z}/2\rho) + \frac{1}{4} \sin(\bar{z}/8\rho) \cos(\bar{z}/2\rho) \right. \\ & \left. - \sin^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right) \\ & \bar{y} \left(-\frac{1}{32} \cos(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \frac{1}{4} \sin(\bar{z}/8\rho) \sin(\bar{z}/2\rho) \right. \\ & \left. + \sin^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \right) \Big] \quad (24) \end{aligned}$$

Helical Back

$$b_x = -\frac{1}{4} \cos(\bar{z}/16\rho) \sin(\bar{z}/16\rho) \sin(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \quad (25)$$

$$b_y = \frac{1}{4} \cos(\bar{z}/16\rho) \sin(\bar{z}/16\rho) \cos(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \quad (26)$$

$$b_z = \frac{\sqrt{\eta}}{2\rho} \left[\bar{x} \left(-\frac{1}{32} \cos(\bar{z}/8\rho) \sin(\bar{z}/2\rho) - \frac{1}{4} \sin(\bar{z}/8\rho) \cos(\bar{z}/2\rho) \right. \right. \\ \left. \left. - \cos^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right) \right. \\ \left. \bar{y} \left(\frac{1}{32} \cos(\bar{z}/8\rho) \cos(\bar{z}/2\rho) - \frac{1}{4} \sin(\bar{z}/8\rho) \sin(\bar{z}/2\rho) \right. \right. \\ \left. \left. + \cos^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \right) \right] \quad (27)$$

Plane-Pole Front

$$b_x = 0, \quad (28)$$

$$b_y = \cosh(\sqrt{\eta}\bar{y}/2\rho) \left[-\frac{1}{4} \sin(\bar{z}/16\rho) \cos(\bar{z}/16\rho) \cos(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right], \quad (29)$$

$$b_z = \sinh(\sqrt{\eta}\bar{y}/2\rho) \left[-\frac{1}{32} \cos(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \right. \\ \left. \frac{1}{4} \sin(\bar{z}/8\rho) \sin(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \right], \quad (30)$$

Plane-Pole Back

$$b_x = 0, \quad (31)$$

$$b_y = \cosh(\sqrt{\eta}\bar{y}/2\rho) \left[\frac{1}{4} \sin(\bar{z}/16\rho) \cos(\bar{z}/16\rho) \cos(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right], \quad (32)$$

$$b_z = \sinh(\sqrt{\eta}\bar{y}/2\rho) \left[\frac{1}{32} \cos(\bar{z}/8\rho) \cos(\bar{z}/2\rho) - \right. \\ \left. \frac{1}{4} \sin(\bar{z}/8\rho) \sin(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \right]. \quad (33)$$

Curved-Pole Front

$$b_x = \frac{\bar{k}_{\beta x}}{\bar{k}_{\beta y}} \sinh(\bar{k}_{\beta x} \bar{x}) \sinh(\bar{k}_{\beta y} \bar{y}) \left[-\frac{1}{8} \sin(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right], \quad (34)$$

$$b_y = \cosh(\bar{k}_{\beta x} \bar{x}) \cosh(\bar{k}_{\beta y} \bar{y}) \left[-\frac{1}{8} \sin(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right], \quad (35)$$

$$b_z = \frac{\sqrt{\eta}}{2\rho \bar{k}_{\beta y}} \cosh(\bar{k}_{\beta x} \bar{x}) \sinh(\bar{k}_{\beta y} \bar{y}) \left[-\frac{1}{32} \cos(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \frac{1}{4} \sin(\bar{z}/8\rho) \sin(\bar{z}/2\rho) + \sin^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \right]. \quad (36)$$

Curved-Pole Back

$$b_x = \frac{\bar{k}_{\beta x}}{\bar{k}_{\beta y}} \sinh(\bar{k}_{\beta x} \bar{x}) \sinh(\bar{k}_{\beta y} \bar{y}) \left[\frac{1}{8} \sin(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right], \quad (37)$$

$$b_y = \cosh(\bar{k}_{\beta x} \bar{x}) \cosh(\bar{k}_{\beta y} \bar{y}) \left[\frac{1}{8} \sin(\bar{z}/8\rho) \cos(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \sin(\bar{z}/2\rho) \right], \quad (38)$$

$$b_z = \frac{\sqrt{\eta}}{2\rho \bar{k}_{\beta y}} \cosh(\bar{k}_{\beta x} \bar{x}) \sinh(\bar{k}_{\beta y} \bar{y}) \left[\frac{1}{32} \cos(\bar{z}/8\rho) \cos(\bar{z}/2\rho) - \frac{1}{4} \sin(\bar{z}/8\rho) \sin(\bar{z}/2\rho) + \cos^2(\bar{z}/16\rho) \cos(\bar{z}/2\rho) \right]. \quad (39)$$

1.4 Natural Undulator Focusing

Each undulator type has an associated natural focusing wavenumber. In the helical case, the natural betatron wavenumber is

$$\bar{k}_{\beta nx} = \bar{k}_{\beta ny} = \frac{a_w}{2\sqrt{2}\rho\gamma_0}, \quad (40)$$

with γ_0 being the average beam energy (and not necessarily $= \gamma_r$)

In the planar case,

$$\bar{k}_{\beta ny} = \frac{a_w}{2\sqrt{2}\rho\gamma_0}. \quad (41)$$

In the canted pole case,

$$\bar{k}_{\beta nx,y} = \frac{a_w \bar{k}_{x,y}}{\sqrt{2}\eta\gamma_0}, \quad (42)$$

where $\bar{k}_{x,y}$ describe the hyperbolic variation in the transverse directions (see eqns (16 - 18)), and must obey

$$\bar{k}_x^2 + \bar{k}_y^2 = \frac{\eta}{4\rho^2} \quad (43)$$

to be physically valid. They determine the focusing strength in the \bar{x} and \bar{y} dimensions. For the case of equal focusing, then,

$$\bar{k}_{\beta nx} = \bar{k}_{\beta ny} = \frac{a_w}{4\rho\gamma_0}. \quad (44)$$

1.5 Strong Beam Focusing

In addition to the natural focusing channel, a constant, ‘strong’ focussing channel may be utilized, to focus the beam to a smaller transverse area. This is a magnetic field super-imposed upon the wiggler. It may be switched on or off with the flag **qFocussing** in the main input file, and is specified through the use of the variables **sKBetaXSF** and **sKBetaYSF**. It is probably highly artificial - it may be thought of as physically similar to an ion channel. Nevertheless it allows one to obtain strong focusing without using a lattice. It is defined very simply as

$$b_x = \sqrt{\eta} \frac{\bar{k}_{\beta y}^2}{\kappa} \bar{y}_j, \quad (45)$$

$$b_y = -\sqrt{\eta} \frac{\bar{k}_{\beta x}^2}{\kappa} \bar{x}_j \quad (46)$$

If either **sKBetaXSF** or **sKBetaYSF** are not specified, then no focusing channel will be added for that dimension, even if the **qFocussing** flag is true.

Magnetic quads will be added soon.

1.6 Auto beam-matching

The beam, when specified by the ‘simple’ method (see below) may be matched to the focusing channel automatically with the flag **qMatched_A** in the beam file - the option can be set for each beam. In the scaled notation,

$$\bar{\sigma}_{x,y} = \sqrt{\frac{\rho \bar{\epsilon}_{x,y}}{\bar{k}_{\beta x,y}}} \quad (47)$$

where $\bar{\epsilon}_{x,y} = \epsilon_{x,y}/(\lambda_r/4\pi)$ are the transverse emittances scaled to the so-called Kim criterion.

The spread in the transverse momentum directions is then given by

$$\bar{\sigma}_{px,py} = \frac{\sqrt{\eta}}{2\kappa} \left\langle \frac{\Gamma}{1 + \eta p_2} \right\rangle \frac{\bar{\epsilon}_{x,y}}{\bar{\sigma}_{x,y}}. \quad (48)$$

where angular brackets indicate the ensemble average of the beam.

If **qFocussing** is true and the strong betatron wavenumber is given, then the strong betatron wavenumber is used to match the beam. Otherwise the beam is auto-matched to the natural focusing channel of the undulator.

1.7 To scale or not to scale?

The main algorithm in Puffin utilizes scaled variables to make the numbers ‘nicer’ to work with. The system saturates with scaled intensity ~ 1 , the scaled perpendicular momentum of the beam in the wiggler oscillates between -1 and 1 , and so forth. The distance through the wiggler is given in units of a (1D) gain length, and the beam coordinate in the radiation frame is in units of the cooperation length, so that an electron slips $1l_c$ through the

Table 1: Input Dimensions and Units for Beam and Radiation Field

Unscaled	units	unscaled equivalent
x	metres (m)	\bar{x}
y	metres (m)	\bar{y}
dx/dz	dimensionless	\bar{p}_x
dy/dz	dimensionless	\bar{p}_y
t	seconds (s)	\bar{z}_2

radiation field in 1 gain length. The scaling defines a frame of reference which normalises the quantities not only to numerically more manageable numbers, but to *characteristic* variables.

The two dominant variables for the scaling are ρ and η . η is a function of the wiggler parameters a_u and λ_u , and reference beam energy γ_r , and is calculated in Puffin from these variables. The ρ parameter is a quite complicated variable, and is dependent on the peak electron beam number density, amongst other things.

The beam and radiation field parameters may be input in either SI units or the scaled units. Use the variable **qscaled** in the main input file to do this. If = **.true.**, then Puffin expects scaled variables are being used. If SI units are used, then the input parameters will be scaled according to the scaling values specified in the main input file. Note that they are only *scaling* parameters. The FEL parameter as input does not have to correspond the the beam being input for the results to be correct. The scaled parameters will behave ‘nicely’ if it does, but it is not necessary. When the result is unscaled, the resut will still be correct.

1.8 Beam Initialization

There are 3 different ways of defining and initializing the electron beam in Puffin:

1.8.1 Simple

The beam is described in terms of a homogeneous Gaussian function in every dimension. Some simple correlations in energy can be achieved by specifying an oscillation in the beam energy as a function of \bar{z}_2 , or as a simple linear energy chirp in \bar{z}_2 . The beam is generated in Puffin according to this description.

In general, the correct noise statistics are added to the beam with the method described in REF (see figure REF). This method, like other noise algorithms, requires a quiet beam to add the noise to. We include two methods of generating the beam - one with the correct noise in all dimensions, and one with the correct noise only in the temporal/ \bar{z}_2 dimension. In both methods, the beam is initially quiet in the temporal dimension before adding the noise, with an equispaced layout of the particles in this dimension. The beam MUST be created to appropriately sample the wavelength of emission/amplification - so at least 10 equispaced particles per resonant wavelength. The methods are:-

Equispaced Grid in Every Dimension

When using this option, the beam is initialized on an equispaced 6D grid. This requires very many particles to appropriately sample every dimension, and you may find it very easy to have more macroparticles than real electrons while loading the beam this way. However, we leave it up to the user to decide if this is appropriate - for some extreme dispersion situation with high charge it may be necessary to create the beam in this way. This can be activated by setting `qEquiXY = true` in the beam input. `qEquiXY` is actually an array of size `nbeams`, with a separate value for each beam if multiple beams are desired. `qEquiXY = false` by default.

Equispaced grid ONLY in \bar{z}_2

If `qEquiXY` is false, then the beam is initially generated as a 1D beam, with equispaced macroparticles. Each macroparticle is then split into many

particles in the other 5 dimensions, with coordinates generated by a quasi-random sequence in each dimension. The SAME SEQUENCE is used for each particle in z2 - the creates a series of beamlets in the \bar{z}_2 dimension, giving a quiet start in \bar{z}_2 . Because random sequences are used, the other 5-dimensions require orders of magnitude less particles to adequately fill the phase space than in the equispaced case. This is the default option, so if not specified, qEquiXY = false.

Both of the above methods may, of course, be replicated and modified by the user to suit a particular situation. The creation of the beam with the correct statistics, while still retaining the sampling necessary for the FEL interaction, is still an area of ongoing research, and is quite controversial. We ultimately leave it to the user to ensure the beam is appropriately initialized for their situation. The methods above can probably be replicated with just a few lines of *e.g.* Python. The generated beam can then be input into Puffin.

To use this, set the option dtype = ‘simple’ in the nblist namelist in the beam file. The parameters for the distribution are then set in the blist namelist in the same file.

1.8.2 Dist input

The input is composed of a description of temporal slices along the bunch, describing a Gaussian mean and standard deviation in every other dimension for each temporal slice. This information is used to generate the electron beam in Puffin.

1.8.3 Beam input

This method allows one to read in the 6D scaled particle coordinates from a text file. The beam is generated externally. (Arrangement?) The user is

then responsible for the noise in the pulse - it is not added by Puffin in this method.

1.9 Field Mesh

References

- [1] L.T. Campbell and B.W.J. McNeil, Physics of Plasmas **19**, 093119 (2012)
- [2] L T Campbell, B.W.J. McNeil and S. Reiche, New J. Phys. **16** (2014) 103019
- [3] E.T. Scharlemann, in High Gain, High Power FELs (edited by R. Bonifacio *et al*) (1989)

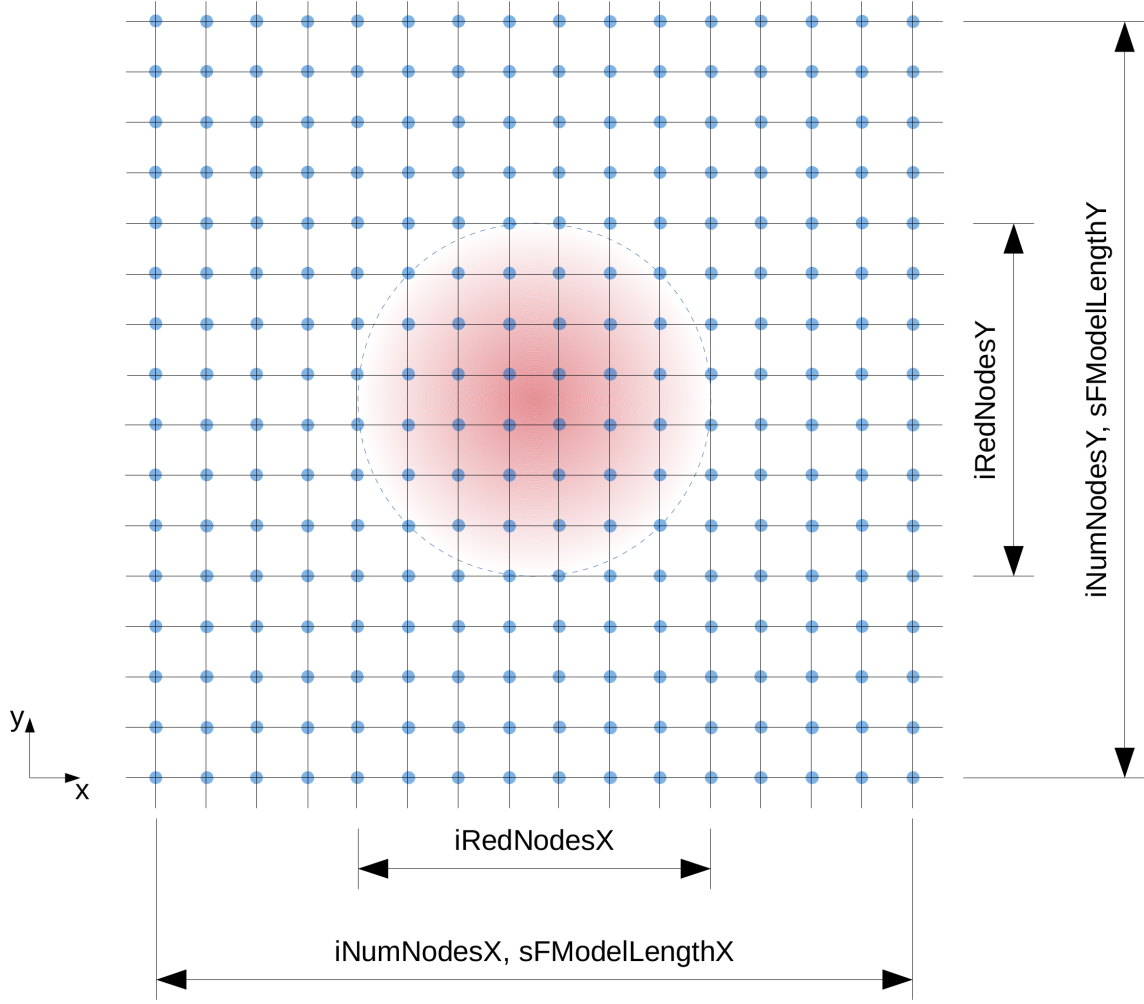


Figure 3: Transverse mesh to model the radiation field - the beam is indicated in red. The mesh may be ‘matched’ to the mesh initially by specifying the $iRedNodes$ parameters - these specify an inner set of nodes such that the mesh will be setup so that the beam is contained within this number of nodes. This is only an initial condition, but can aid in setting up the mesh.

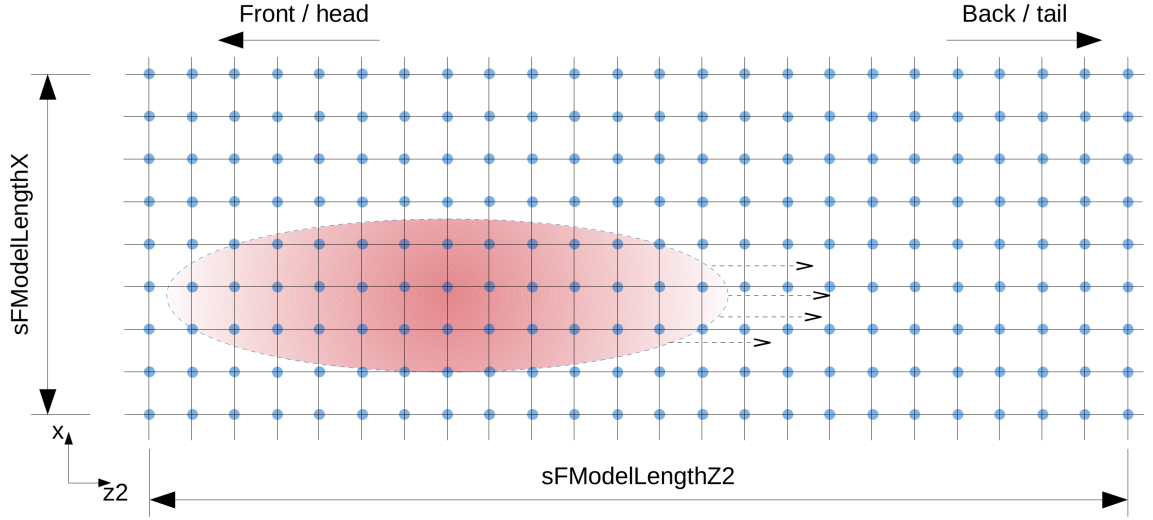


Figure 4: Showing the longitudinal setup of the radiation mesh. The beam is indicated in red. The scaled \bar{z}_2 coordinate is defined so that the front of the radiation and beam is to the left. This is the constant radiation frame, so the beam slips backwards through the field from left to right. In the lab frame, the beam and radiation propagates from right to left. The full length of the mesh must be large enough to contain the beam through propagation.