$$A = \frac{1}{2} r \cdot d\varphi \cdot r = \frac{1}{2} r^2 \cdot d\varphi$$