

INTEGRALI COMPOSTI

$$\int \underbrace{e^{x^2}}_{e^{f(x)}} \cdot \underbrace{2x}_{f'(x)} dx = e^{x^2} + C$$

$$\int e^{f(x)} \cdot f'(x) dx = e^{f(x)} + C$$

$$\int e^{x^2} \cdot x dx = \frac{1}{2} \int \underbrace{e^{x^2}}_{e^{f(x)}} \cdot \underbrace{2x}_{f'(x)} dx$$
$$= \frac{1}{2} e^{x^2} + C$$

$$y = e^x \rightarrow y' = e^x$$
$$y = e^{5x} \rightarrow y' = e^{5x} \cdot 5$$
$$y = e^{x^2} \rightarrow y' = e^{x^2} \cdot 2x$$
$$y = e^{f(x)} \rightarrow y' = e^{f(x)} \cdot f'(x)$$

$$\int e^{3x+1} dx = \frac{1}{3} \int 3 e^{3x+1} dx = \frac{1}{3} e^{3x+1} + c \quad \int e^{f(x)} \cdot f'(x) dx = e^{f(x)} + c$$

~~$$\int e^{x^3} dx$$~~

$$\int (e^x + 1) dx$$

$$\int e^{x^7} \cdot x^6 dx = \frac{1}{7} \int e^{x^7} \cdot 7x^6 dx = \frac{1}{7} e^{x^7} + c$$

$$\int e^{\sin x} \cdot \cos x dx = e^{\sin x} + c$$

$$\begin{aligned} & \int e^{-2\sin x} \cdot \cos x dx = \\ &= -\frac{1}{2} \int e^{-2\sin x} \cdot (-2\cos x) dx = \\ &= -\frac{1}{2} e^{-2\sin x} + c \end{aligned}$$

$$\begin{aligned}
 \int \underbrace{(2x^3 + x)}_{\substack{4x^3 + 2x}} e^{\underbrace{x^4 + x^2}} dx &= \frac{1}{2} \int 2(2x^3 + x) e^{x^4 + x^2} dx \\
 &= \frac{1}{2} e^{x^4 + x^2} + C
 \end{aligned}$$