

Time complexity resume:

big O describes an upper bound on the time.

-common runtimes:

> $O(1)$, constant

> $O(\log n)$, expected cases

> $O(n)$, linear time , best case

> $O(n \log n)$

> $O(n^2)$, worst cases

> $O(2^n)$

> $O(n!)$

TIPS

*If your algorithm is in the form "do this, then, when you're all done, do that" then you add the runtimes.

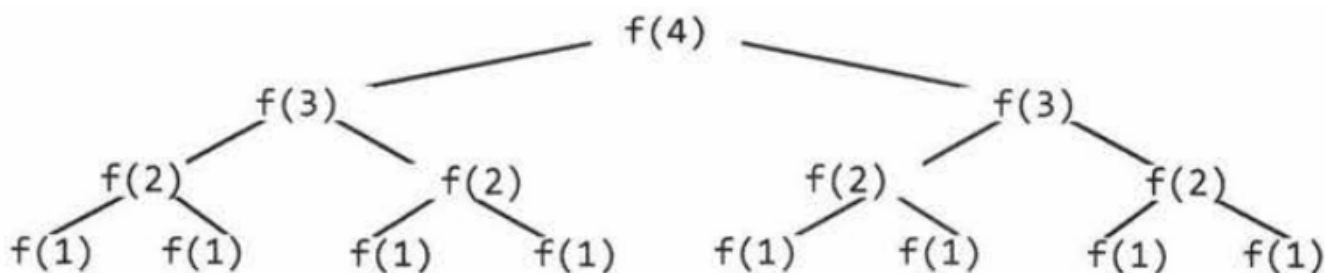
*If your algorithm is in the form "do this for each time you do that" then you multiply the runtimes.

* When you see a problem where the number of elements in the problem space gets halved each time, that will likely be a $O(\log \text{ base } 2 \text{ de } N)$ runtime. La base depende de por cuanto se divida.

$$2^4 = 16 \rightarrow \log_2 16 = 4$$

$$\log_2 N = k \rightarrow 2^k = N$$

* When you have a recursive function that makes multiple calls, the runtime will often (but not always) look like $O(\text{branches}^{\text{depth}})$, where branches is the number of times each recursive call branches. In this case, this gives us $O(2N)$.



Level	# Nodes	Also expressed as...	Or...
0	1		2^0
1	2	$2 * \text{previous level} = 2$	2^1
2	4	$2 * \text{previous level} = 2 * 2^1 = 2^2$	2^2
3	8	$2 * \text{previous level} = 2 * 2^2 = 2^3$	2^3
4	16	$2 * \text{previous level} = 2 * 2^3 = 2^4$	2^4

*Binary search is $O(\log n)$

We commonly see $O(\log N)$ in runtimes. Where does this come from? Let's look at binary search as an example. In binary search, we are looking for an example x in an N -element sorted array. We first compare x to the midpoint of the array. If $x == \text{middle}$, then we return. If $x < \text{middle}$, then we search on the left side of the array. If $x > \text{middle}$, then we search on the right side of the array.

search 9 within {1, 5, 8, 9, 11, 13, 15, 19, 21}
compare 9 to 11 -> smaller.
search 9 within {1, 5, 8, 9, 11}
compare 9 to 8 -> bigger
search 9 within {9, 11}
compare 9 to 9
return

*Suma de los primeros N numeros :

$$(N-1) + (N-2) + (N-3) + \dots + 2 + 1$$

$$= 1 + 2 + 3 + \dots + N-1$$

$$= \text{sum of 1 through N-1}$$

$$\text{The sum of 1 through N-1 is } \frac{N(N-1)}{2}$$

Que termina siendo $O(n^2)$

*Si recorremos dos arrays distintos en un for anidado, la complejidad del numero de operaciones es $O(ab)$ no $O(n^2)$, ya que no recorren el mismo array.