



# NTK-DFL: Enhancing Decentralized Federated Learning in Heterogeneous Settings via Neural Tangent Kernel

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# Overview



**Introduction**

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**NTK-DFL Overview**

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**Results**

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**Takeaway + Future Directions**

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- **Federated Learning (FL)** jointly trains a machine learning model across multiple clients, without sharing training data
- **Decentralized Federated Learning (DFL)** does this without a central server

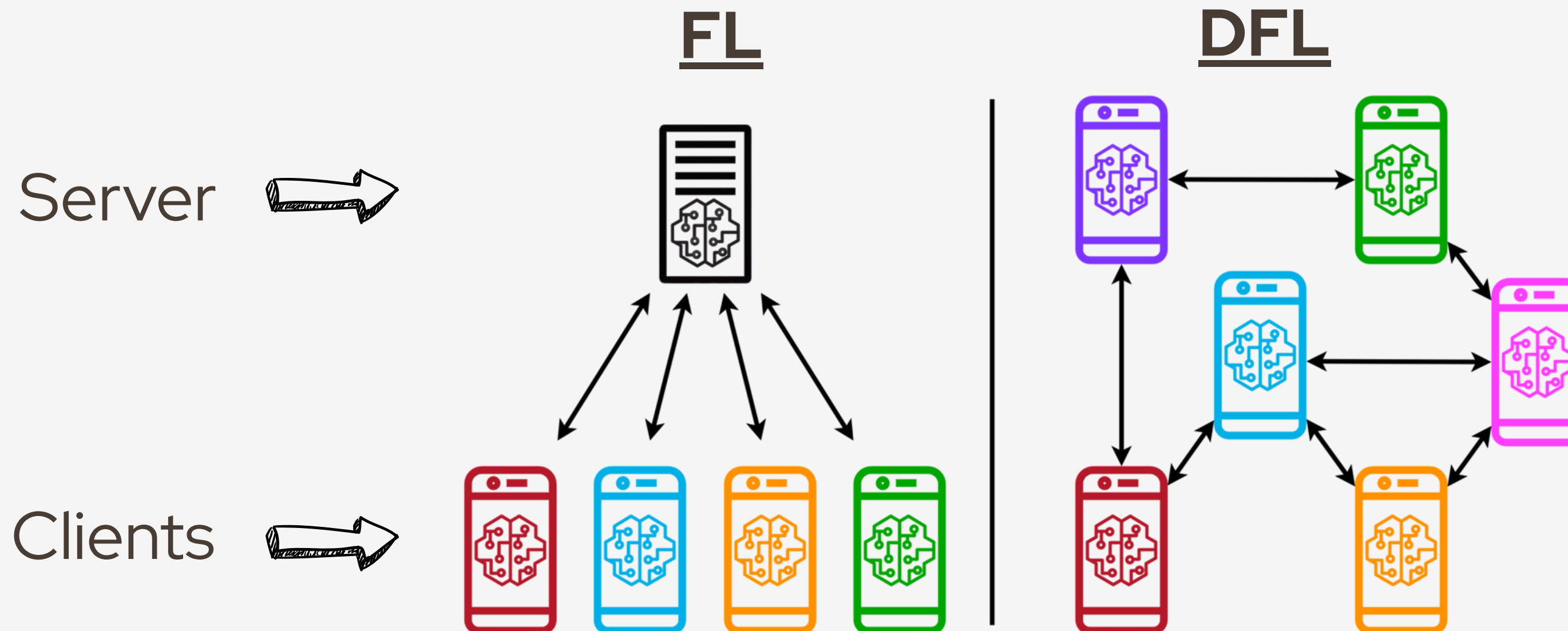


Image credit: <https://marc.damie.eu>

# Data Heterogeneity

- Clients possess various, non-IID data distributions
- This can disrupt training and hurt convergence

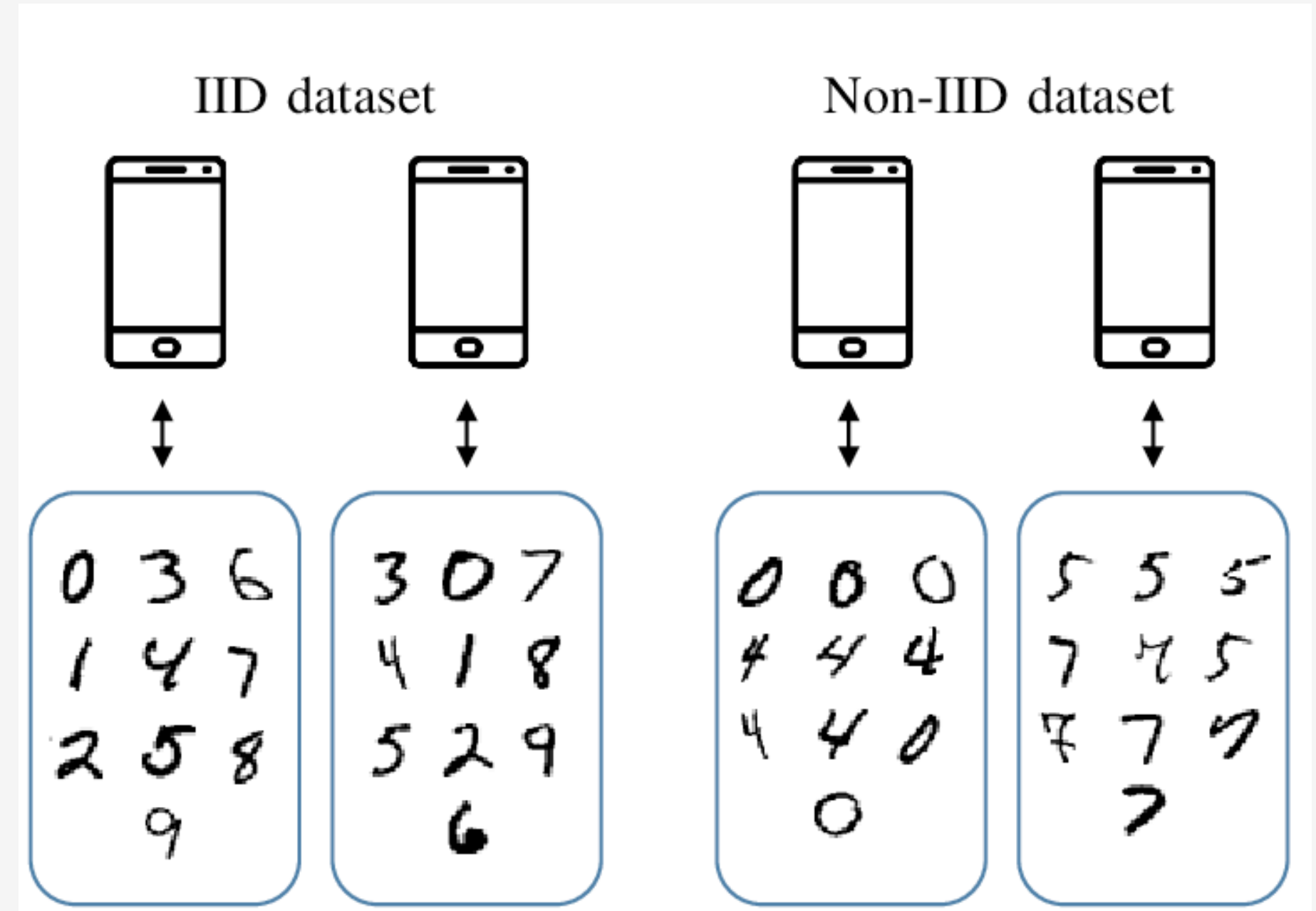
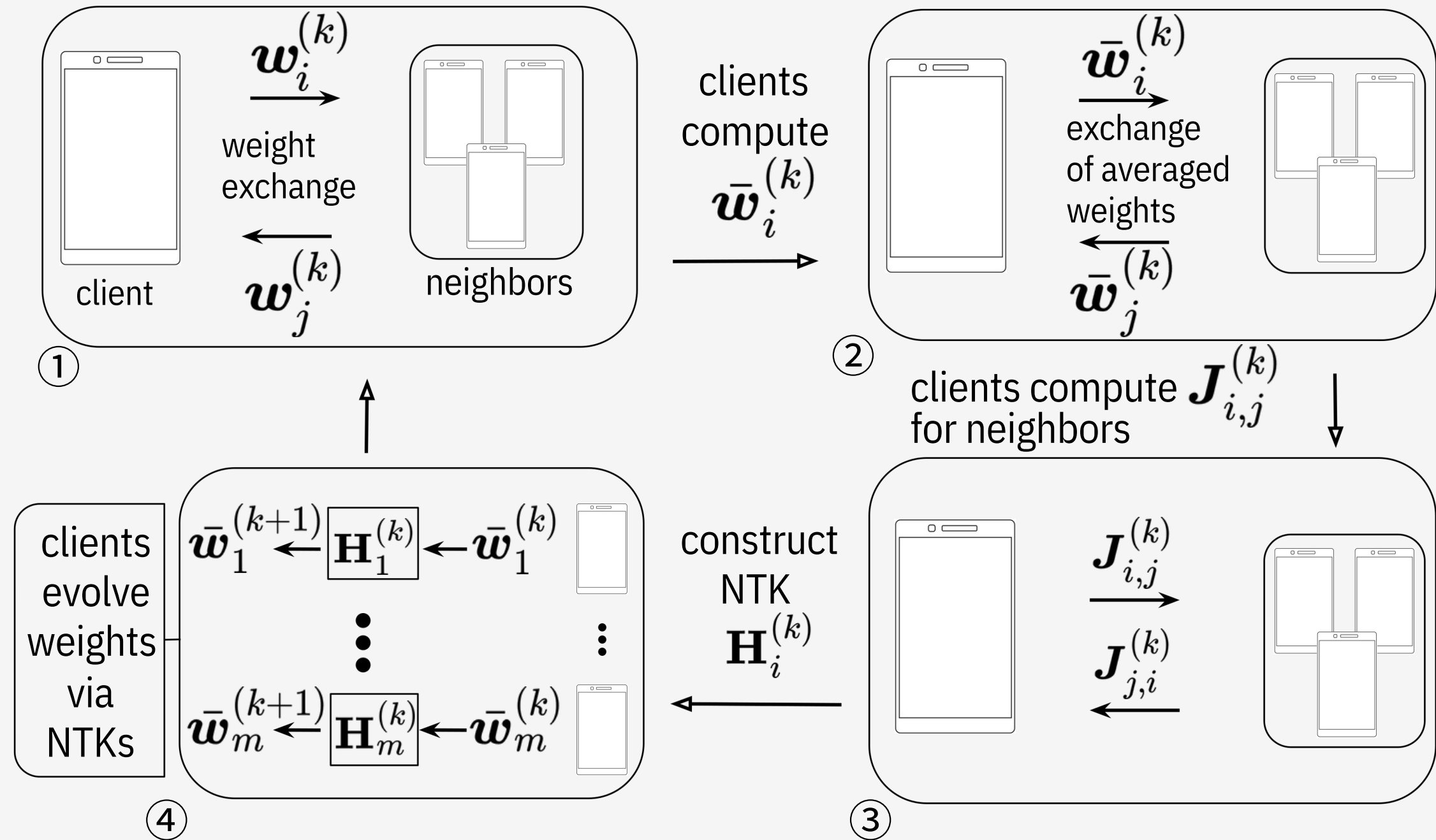


Image credit: Hellström, Henrik & Barros da Silva Júnior, José Mairton & Fodor, Viktoria & Fischione, Carlo. (2020). Wireless for Machine Learning.

- Yue et al. (2022) showed success of **neural tangent kernel** methods in centralized federated learning
- We replace gradient-based optimization from Sun et al. (2021) with neural tangent kernel optimization



- Yue et al. Neural tangent kernel empowered federated learning. 39th International Conference on Machine Learning, Jul 2022.
- Sun, T., Li, D., and Wang, B. Decentralized federated averaging. IEEE Transactions on Pattern Analysis and Machine Intelligence, 2021

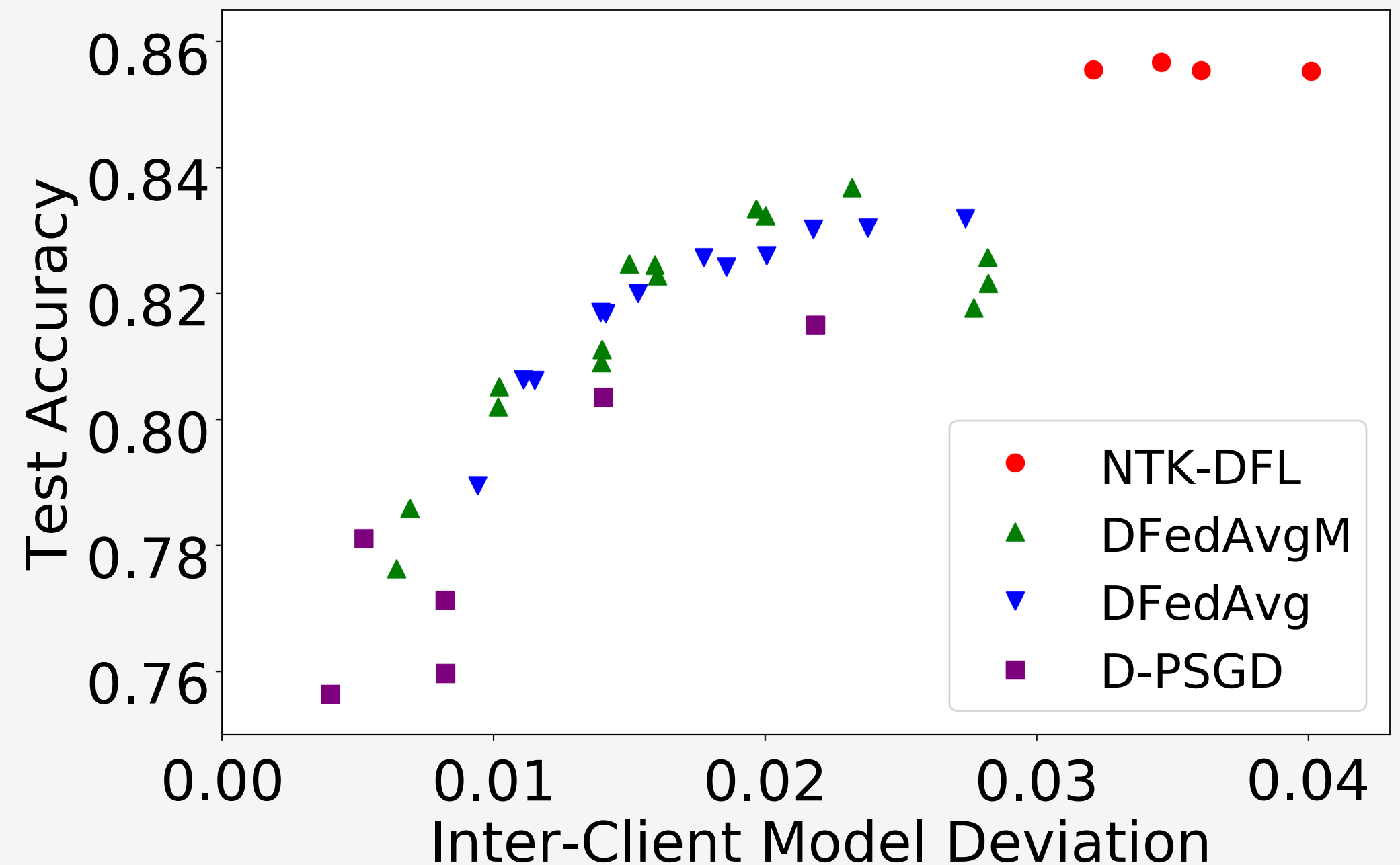
- NTK-DFL allows clients to communicate **more expressive updates**
- **Decreases** the number of communication rounds by **increasing** the communication volume per round

## Useful in scenarios with:

- Large per-round communication latency
- Limited device availability
- Synchronization delays

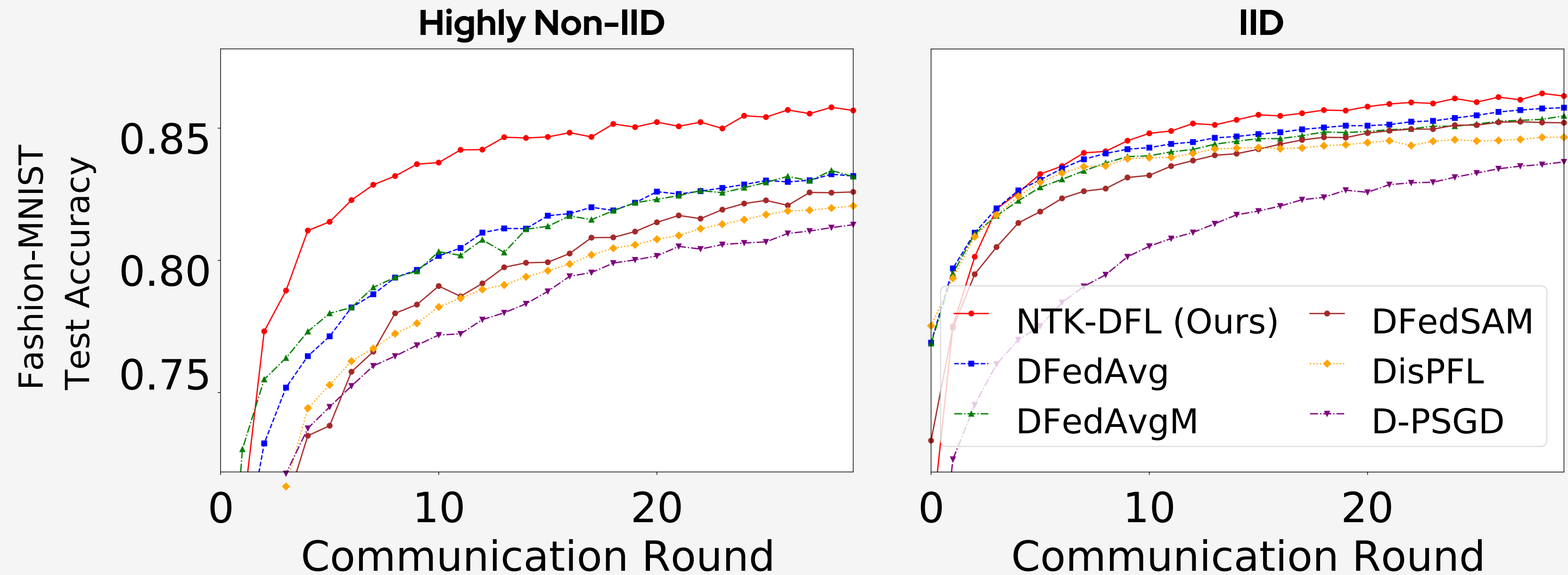
*NTK weight evolution is **synergetic** with model averaging in DFL*

- NTK updates encourage a useful **inter-client model deviation**, improving generalization in the decentralized setting



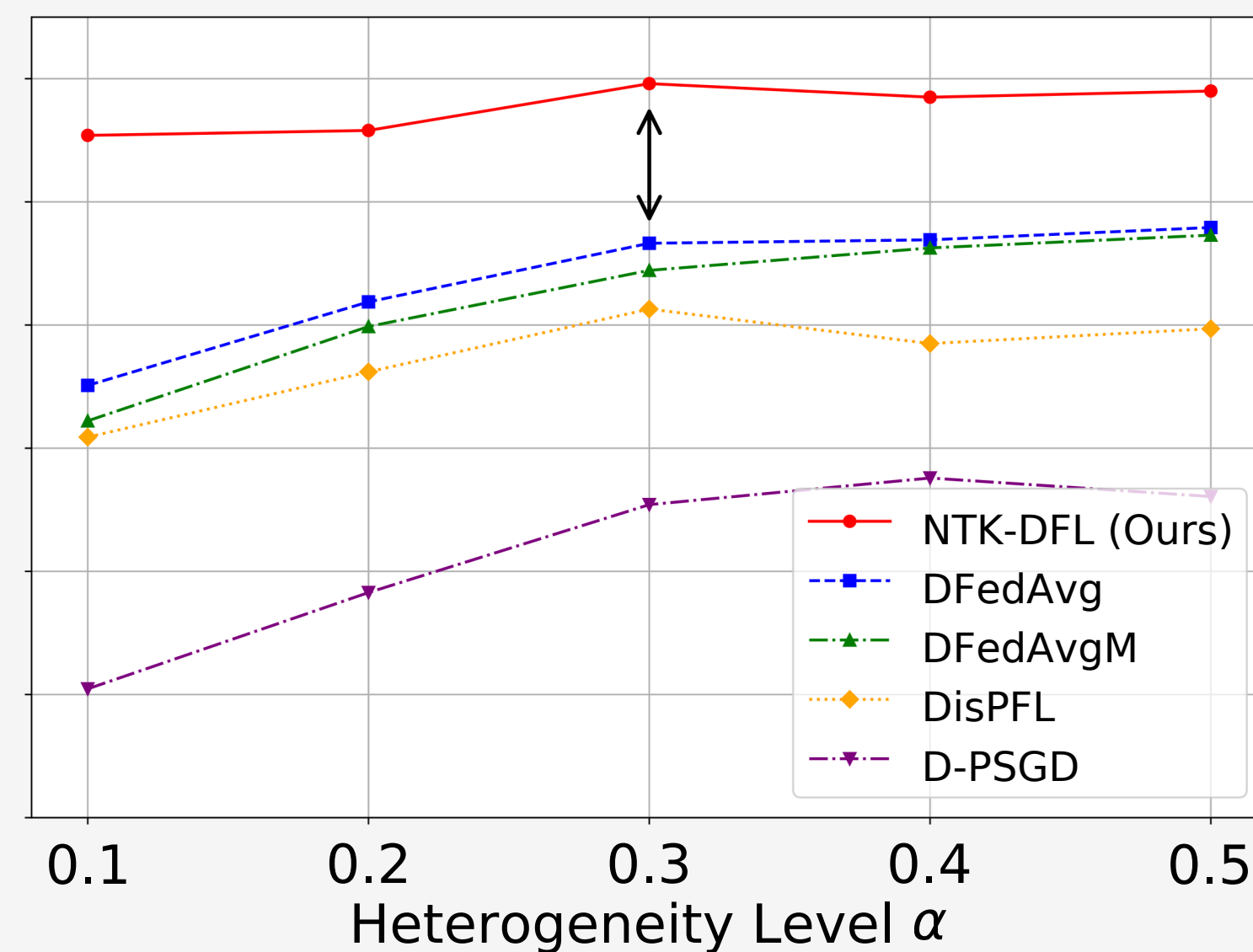
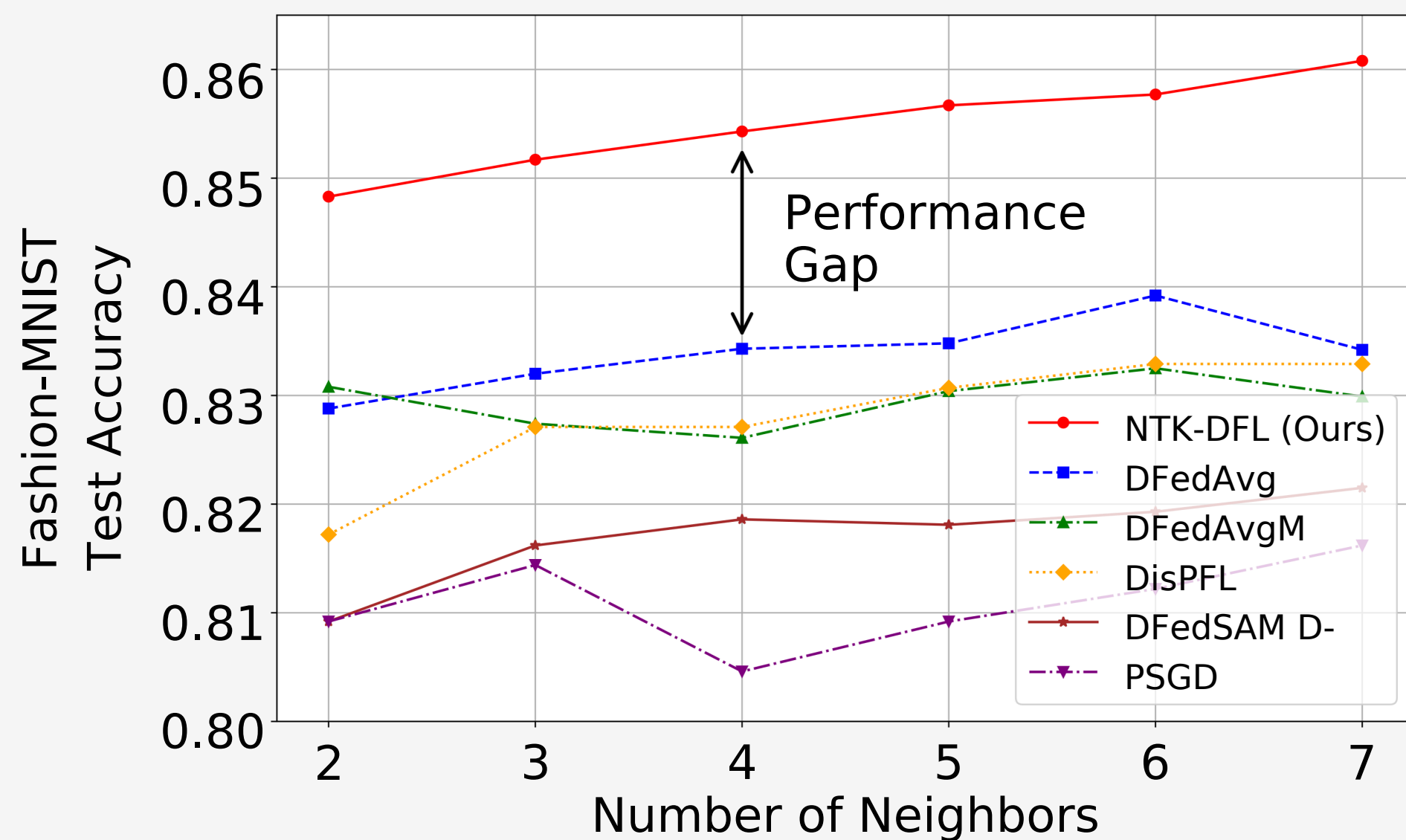


- NTK-DFL **reduces communication rounds** needed for convergence
- Particularly effective with **non-IID** data





- NTK-DFL performs consistently better across various **heterogeneity levels** and **topological sparsity** compared to SOTA methods



# Results

*Theoretical analysis highlights possible source of improved convergence compared to DFedAvg*

**NTK-DFL**  
(Proposed)



$$\min_{1 \leq k \leq K} \left\| \nabla \mathcal{L} \left( \bar{w}^{(k)} \right) \right\|^2 \leq O \left( \frac{\mathcal{L}(\bar{w}^{(1)}) - \mathcal{L}^*}{\sqrt{KT}} + \dots \right)$$

**vs.**

**DFedAvg**  
(Sun et al., 2021)



$$\min_{1 \leq k \leq K} \left\| \nabla \mathcal{L} \left( \bar{w}^{(k)} \right) \right\|^2 \leq O \left( \frac{\mathcal{L}(\bar{w}^{(1)}) - \mathcal{L}^*}{\sqrt{K}} + \dots \right)$$

# Takeaway + Future Directions

## Takeaway

- NTK evolution enables more expressive model updates
  - Trades *communication volume* for *communication rounds*
- NTK-DFL is synergetic with DFL model averaging

## Future Directions

- Adopt to more modern ML architectures
- Apply NTK-DFL to suitable real-world applications (cross-silo DFL, healthcare)



# THANK YOU

Please refer to our paper for more experimental results, ablation studies, the theoretical analysis, and analysis of communication overhead.

***Gabriel Thompson, Kai Yue, Chau-Wai Wong, and Huaiyu Dai, “NTK-DFL: Enhancing decentralized federated learning in heterogeneous settings via neural tangent kernel,” ICML 2025.***