



## **FORMULARIO**

**S-192**

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Función $f(t)$	Transformada de Laplace $\mathcal{L}\{f(t)\} = F(s)$	Sustitución
1	$\mathcal{L}\{1\}$	$\frac{1}{s}$
$t$	$\mathcal{L}\{t\}$	$\frac{1}{s^2}$
$t^2$	$\mathcal{L}\{t^2\}$	$\frac{2}{s^3}$
$t^n$	$\mathcal{L}\{t^n\}$	$\frac{n!}{s^{n+1}}$
$e^{at}$	$\mathcal{L}\{e^{at}\}$	$\frac{1}{s-a}$
$\cos(bt)$	$\mathcal{L}\{\cos(bt)\}$	$\frac{s}{s^2+b^2}$
$\sin(bt)$	$\mathcal{L}\{\sin(bt)\}$	$\frac{b}{s^2+b^2}$
$\sinh(bt)$	$\mathcal{L}\{\sinh(bt)\}$	$\frac{b}{s^2-b^2}$
$\cosh(bt)$	$\mathcal{L}\{\cosh(bt)\}$	$\frac{s}{s^2-b^2}$
$e^{at} \cos(bt)$	$\mathcal{L}\{e^{at} \cos(bt)\}$	$\frac{s-a}{(s-a)^2+b^2}$
$e^{at} \sin(bt)$	$\mathcal{L}\{e^{at} \sin(bt)\}$	$\frac{b}{(s-a)^2+b^2}$
$\delta(t-a)$	$\mathcal{L}\{\delta(t-a)\}$	$e^{-as}$
$u(t-a)$	$\mathcal{L}\{u(t-a)\}$	$\frac{e^{-as}}{s}$
$\frac{1}{t}$	$\mathcal{L}\{\frac{1}{t}\}$	$\ln(s)$
$te^{at}$	$\mathcal{L}\{te^{at}\}$	$\frac{1}{(s-a)^2}$
$t^n e^{at}$	$\mathcal{L}\{t^n e^{at}\}$	$\frac{n!}{(s-a)^{n+1}}$
$\sinh(at) \cosh(bt)$	$\mathcal{L}\{\sinh(at) \cosh(bt)\}$	$\frac{a}{s^2-(a+b)^2} - \frac{a}{s^2-(a-b)^2}$
$\cosh(at) \sinh(bt)$	$\mathcal{L}\{\cosh(at) \sinh(bt)\}$	$\frac{s}{s^2-(a+b)^2} - \frac{s}{s^2-(a-b)^2}$
$\int_0^t f(\tau) d\tau$	$\mathcal{L}\{\int_0^t f(\tau) d\tau\}$	$\frac{F(s)}{s}$

$f'(t)$	$\mathcal{L}\{f'(t)\}$	$sF(s) - f(0)$
$f''(t)$	$\mathcal{L}\{f''(t)\}$	$s^2F(s) - sf(0) - f'(0)$
$e^{bt}t^n$	$\mathcal{L}\{e^{bt}t^n\}$	$\frac{n!}{(s-b)^{n+1}}$
$t \sin(at)$	$\mathcal{L}\{t \sin(at)\}$	$\frac{2as}{(s^2+a^2)^2}$
$t \cos(at)$	$\mathcal{L}\{t \cos(at)\}$	$\frac{s^2-a^2}{(s^2+a^2)^2}$
$\sin(at+b)$	$\mathcal{L}\{\sin(at+b)\}$	$\frac{a \cos(b) + s \sin(b)}{s^2+a^2}$
$\cos(at+b)$	$\mathcal{L}\{\cos(at+b)\}$	$\frac{s \cos(b) - a \sin(b)}{s^2+a^2}$
$\sinh(at)$	$\mathcal{L}\{\sinh(at)\}$	$\frac{a}{s^2-a^2}$
$\cosh(at)$	$\mathcal{L}\{\cosh(at)\}$	$\frac{s}{s^2-a^2}$
$u(t) \cos(at)$	$\mathcal{L}\{u(t) \cos(at)\}$	$\frac{s}{s^2+a^2}$
$u(t) \sin(at)$	$\mathcal{L}\{u(t) \sin(at)\}$	$\frac{a}{s^2+a^2}$
$u(t) \cosh(bt)$	$\mathcal{L}\{u(t) \cosh(bt)\}$	$\frac{s}{s^2-b^2}$
$u(t) \sinh(bt)$	$\mathcal{L}\{u(t) \sinh(bt)\}$	$\frac{b}{s^2-b^2}$
$u(t-a) \cos(b(t-a))$	$\mathcal{L}\{u(t-a) \cos(b(t-a))\}$	$\frac{e^{-as}(s \cos(b) + a \sin(b))}{s^2+b^2}$
$u(t-a) \sin(b(t-a))$	$\mathcal{L}\{u(t-a) \sin(b(t-a))\}$	$\frac{e^{-as}b}{s^2+b^2}$
$u(t-a) \cos(bt)$	$\mathcal{L}\{u(t-a) \cos(bt)\}$	$\frac{e^{-as}s}{s^2+b^2}$
$u(t-a) \sin(bt)$	$\mathcal{L}\{u(t-a) \sin(bt)\}$	$\frac{e^{-as}b}{s^2+b^2}$
$t^n e^{-at}$	$\mathcal{L}\{t^n e^{-at}\}$	$\frac{n!}{(s+a)^{n+1}}$
$e^{-at} \cosh(bt)$	$\mathcal{L}\{e^{-at} \cosh(bt)\}$	$\frac{s+a}{(s+a)^2-b^2}$
$e^{-at} \sinh(bt)$	$\mathcal{L}\{e^{-at} \sinh(bt)\}$	$\frac{b}{(s+a)^2-b^2}$

$te^{-at} \cos(bt)$	$\mathcal{L}\{te^{-at} \cos(bt)\}$	$\frac{s+a}{(s+a)^2+b^2}$
$te^{-at} \sin(bt)$	$\mathcal{L}\{te^{-at} \sin(bt)\}$	$\frac{b}{(s+a)^2+b^2}$
$e^{bt} \cos(at)$	$\mathcal{L}\{e^{bt} \cos(at)\}$	$\frac{s-b}{(s-b)^2+a^2}$
$e^{bt} \sin(at)$	$\mathcal{L}\{e^{bt} \sin(at)\}$	$\frac{a}{(s-b)^2+a^2}$
$t^m e^{bt}$	$\mathcal{L}\{t^m e^{bt}\}$	$\frac{m!}{(s-b)^{m+1}}$
$t^m e^{-bt}$	$\mathcal{L}\{t^m e^{-bt}\}$	$\frac{m!}{(s+b)^{m+1}}$
$e^{-bt} \cos(at)$	$\mathcal{L}\{e^{-bt} \cos(at)\}$	$\frac{s+b}{(s+b)^2+a^2}$
$e^{-bt} \sin(at)$	$\mathcal{L}\{e^{-bt} \sin(at)\}$	$\frac{a}{(s+b)^2+a^2}$
$e^{-bt} \cosh(at)$	$\mathcal{L}\{e^{-bt} \cosh(at)\}$	$\frac{s+b}{(s+b)^2-a^2}$
$e^{-bt} \sinh(at)$	$\mathcal{L}\{e^{-bt} \sinh(at)\}$	$\frac{a}{(s+b)^2-a^2}$
$\cos(at) \sin(bt)$	$\mathcal{L}\{\cos(at) \sin(bt)\}$	$\frac{s^2-a^2}{(s^2+a^2)^2} - \frac{a}{(s^2+b^2)^2}$
$\sin(at) \cos(bt)$	$\mathcal{L}\{\sin(at) \cos(bt)\}$	$\frac{ab}{(s^2+(a+b)^2)(s^2+(a-b)^2)}$
$\cos(at)$	$\mathcal{L}\{\cos(at)\}$	$\frac{s}{s^2+a^2}$
$\sin(at)$	$\mathcal{L}\{\sin(at)\}$	$\frac{a}{s^2+a^2}$
$\cosh(at)$	$\mathcal{L}\{\cosh(at)\}$	$\frac{s}{s^2-a^2}$
$\sinh(at)$	$\mathcal{L}\{\sinh(at)\}$	$\frac{a}{s^2-a^2}$
$u(t) \cos(at)$	$\mathcal{L}\{u(t) \cos(at)\}$	$\frac{s}{s^2+a^2}$
$u(t) \sin(at)$	$\mathcal{L}\{u(t) \sin(at)\}$	$\frac{a}{s^2+a^2}$
$u(t) \cosh(at)$	$\mathcal{L}\{u(t) \cosh(at)\}$	$\frac{s}{s^2-a^2}$
$u(t) \sinh(at)$	$\mathcal{L}\{u(t) \sinh(at)\}$	$\frac{a}{s^2-a^2}$
$u(t-a) \cosh(bt)$	$\mathcal{L}\{u(t-a) \cosh(bt)\}$	$\frac{e^{-as}s}{s^2-b^2}$
$u(t-a) \sinh(bt)$	$\mathcal{L}\{u(t-a) \sinh(bt)\}$	$\frac{e^{-as}b}{s^2-b^2}$

$u(t-a)\cos(bt)$	$\mathcal{L}\{u(t-a)\cos(bt)\}$	$\frac{e^{-as}s}{s^2+b^2}$
$u(t-a)\sin(bt)$	$\mathcal{L}\{u(t-a)\sin(bt)\}$	$\frac{e^{-as}b}{s^2+b^2}$
$t^n e^{-at}$	$\mathcal{L}\{t^n e^{-at}\}$	$\frac{n!}{(s+a)^{n+1}}$
$te^{-at}\cos(bt)$	$\mathcal{L}\{te^{-at}\cos(bt)\}$	$\frac{s+a}{(s+a)^2+b^2}$
$te^{-at}\sin(bt)$	$\mathcal{L}\{te^{-at}\sin(bt)\}$	$\frac{b}{(s+a)^2+b^2}$
$e^{bt}\cos(at)$	$\mathcal{L}\{e^{bt}\cos(at)\}$	$\frac{s-b}{(s-b)^2+a^2}$
$e^{bt}\sin(at)$	$\mathcal{L}\{e^{bt}\sin(at)\}$	$\frac{a}{(s-b)^2+a^2}$
$t^m e^{bt}$	$\mathcal{L}\{t^m e^{bt}\}$	$\frac{m!}{(s-b)^{m+1}}$
$t^m e^{-bt}$	$\mathcal{L}\{t^m e^{-bt}\}$	$\frac{m!}{(s+b)^{m+1}}$
$e^{-bt}\cos(at)$	$\mathcal{L}\{e^{-bt}\cos(at)\}$	$\frac{s+b}{(s+b)^2+a^2}$
$e^{-bt}\sin(at)$	$\mathcal{L}\{e^{-bt}\sin(at)\}$	$\frac{a}{(s+b)^2+a^2}$
$e^{-bt}\cosh(at)$	$\mathcal{L}\{e^{-bt}\cosh(at)\}$	$\frac{s+b}{(s+b)^2-a^2}$
$e^{-bt}\sinh(at)$	$\mathcal{L}\{e^{-bt}\sinh(at)\}$	$\frac{a}{(s+b)^2-a^2}$
$\cos(at)\sin(bt)$	$\mathcal{L}\{\cos(at)\sin(bt)\}$	$\frac{s^2-a^2}{(s^2+a^2)^2} - \frac{a}{(s^2+b^2)^2}$
$\sin(at)\cos(bt)$	$\mathcal{L}\{\sin(at)\cos(bt)\}$	$\frac{ab}{(s^2+(a+b)^2)(s^2+(a-b)^2)}$
$\cos(at)$	$\mathcal{L}\{\cos(at)\}$	$\frac{s}{s^2+a^2}$
$\sin(at)$	$\mathcal{L}\{\sin(at)\}$	$\frac{a}{s^2+a^2}$
$\cosh(at)$	$\mathcal{L}\{\cosh(at)\}$	$\frac{s}{s^2-a^2}$
$\sinh(at)$	$\mathcal{L}\{\sinh(at)\}$	$\frac{a}{s^2-a^2}$
$u(t)\cos(at)$	$\mathcal{L}\{u(t)\cos(at)\}$	$\frac{s}{s^2+a^2}$
$u(t)\sin(at)$	$\mathcal{L}\{u(t)\sin(at)\}$	$\frac{a}{s^2+a^2}$
$u(t)\cosh(at)$	$\mathcal{L}\{u(t)\cosh(at)\}$	$\frac{s}{s^2-a^2}$
$u(t)\sinh(at)$	$\mathcal{L}\{u(t)\sinh(at)\}$	$\frac{a}{s^2-a^2}$
$u(t-a)\cosh(bt)$	$\mathcal{L}\{u(t-a)\cosh(bt)\}$	$\frac{e^{-as}s}{s^2-b^2}$
$u(t-a)\sinh(bt)$	$\mathcal{L}\{u(t-a)\sinh(bt)\}$	$\frac{e^{-as}b}{s^2-b^2}$
$\cos(at)\sin(bt)$	$\mathcal{L}\{\cos(at)\sin(bt)\}$	$\frac{ab}{(s^2+(a+b)^2)-(s^2+(a-b)^2)}$
$\sin(at)\cos(bt)$	$\mathcal{L}\{\sin(at)\cos(bt)\}$	$\frac{s(a^2-b^2)}{(s^2+a^2)(s^2+b^2)}$