

**MACHINE** m3

**REFINES** m2

**SEES** c0

**VARIABLES**

wait  
process  
clk  
t1  
t2  
qsize  
queue  
dqueue  
t3  
index

**INVARIANTS**

**inv1:**  $dqueue \in PROCESS \leftrightarrow \mathbb{N}$   
**inv3:**  $\forall p. p \in dom(dqueue) \Rightarrow 0 \leq dqueue(p) \wedge dqueue(p) \leq clk$   
**inv4:**  $\forall p. (p \in wait \wedge p \in dom(dqueue) \wedge p = queue(1) \wedge process = \emptyset) \Rightarrow clk - dqueue(p) \leq ddl4$   
**inv5:**  $\forall p. (p \in dom(dqueue) \wedge p \in dom(t2) \wedge t2(p) \geq dqueue(p)) \Rightarrow t2(p) - dqueue(p) \leq ddl4$   
deadline(wish.empty/leave,enter,ddl4)  
**inv6:**  $t3 \in PROCESS \leftrightarrow \mathbb{N}$   
**inv7:**  $\forall p. (p \in process \wedge p \in dom(t2)) \Rightarrow clk - t2(p) \leq ddl2$   
**inv8:**  $\forall p. p \in dom(t3) \Rightarrow 0 \leq t3(p) \wedge t3(p) \leq clk$   
**inv9:**  $\forall p. (p \in dom(t2) \wedge p \in dom(t3) \wedge t3(p) \geq t2(p)) \Rightarrow t3(p) - t2(p) \leq ddl2$   
deadline(enter,leave,ddl2)  
**inv11:**  $index \in PROCESS \leftrightarrow \mathbb{N}$   
**inv10:**  $\forall p. (p \in dom(t2) \wedge p \in dom(t3) \wedge t3(p) \geq t2(p) \wedge t3(p) = dqueue(queue(1)) \wedge queue \neq \emptyset) \Rightarrow$   
 $dqueue(queue(1)) - t2(p) \leq ddl2$   
deadline(enter,leave,ddl2)

**EVENTS**

**Initialisation**  $\langle \text{extended} \rangle$

**begin**

**act1:**  $wait := \emptyset$   
**act2:**  $process := \emptyset$   
**act3:**  $clk := 0$   
**act4:**  $t1 := \emptyset$   
**act5:**  $t2 := \emptyset$   
**act7:**  $qsize := 0$   
**act8:**  $queue := \emptyset$   
**act9:**  $dqueue := \emptyset$   
**act10:**  $t3 := \emptyset$   
**act11:**  $index := \emptyset$

**end**

**Event** wish.empty  $\langle \text{ordinary} \rangle \hat{=}$

**extends** wish

**any**

pro

**where**

**grd1:**  $pro \in PROCESS \setminus wait$   
**grd2:**  $pro \in PROCESS \setminus process$   
**grd3:**  $wait = \emptyset \wedge process = \emptyset$

**then**

**act1:**  $wait := wait \cup \{pro\}$   
**act2:**  $t1(pro) := clk$   
**act3:**  $queue(qsize + 1) := pro$

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    act4: qsize := qsize + 1
    act5: dqueue(pro) := clk
    act6: index(pro) := qsize
end
Event wish_nonempty ⟨ordinary⟩ ≐
extends wish
  any
    pro
  where
    grd1: pro ∈ PROCESS \ wait
    grd2: pro ∈ PROCESS \ process
    grd3: wait ≠ ∅ ∨ process ≠ ∅
  then
    act1: wait := wait ∪ {pro}
    act2: t1(pro) := clk
    act3: queue(qsize + 1) := pro
    act4: qsize := qsize + 1
    act6: index(pro) := qsize
  end
Event enter ⟨ordinary⟩ ≐
extends enter
  any
    pro
  where
    grd1: pro ∈ wait
    grd2: card(process) = 0
    grd3: qsize > 0
    grd4: pro = queue(1)
  then
    act1: wait := wait \ {pro}
    act2: process := process ∪ {pro}
    act3: t2(pro) := clk
    act4: queue :| queue' ∈ 1 .. qsize - 1 ⇨ wait \ {queue(1)} ∧ (∀ i · i ∈ 1 .. qsize - 1 ⇒ queue'(i) = queue(i + 1))
    act5: qsize := qsize - 1
  end
Event leave ⟨ordinary⟩ ≐
extends leave
  any
    pro
  where
    grd1: pro ∈ process
    grd2: queue ≠ ∅
  then
    act1: process := process \ {pro}
    act3: dqueue(queue(1)) := clk
    act4: t3(pro) := clk
  end
Event leave_idle ⟨ordinary⟩ ≐
extends leave
  any
    pro
  where
    grd1: pro ∈ process
    grd2: queue = ∅
  then
    act1: process := process \ {pro}
    act2: t3(pro) := clk

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    end
Event tick ⟨ordinary⟩ ≐
refines tick
    when
        grd2:  $\forall p. (p \in process \wedge p \in dom(t2)) \Rightarrow clk + 1 - t2(p) \leq ddl2$ 
        grd3:  $\forall p. (p \in wait \wedge p \in dom(dqueue) \wedge p = queue(1) \wedge process = \emptyset) \Rightarrow clk + 1 - dqueue(p) \leq ddl4$ 
    then
        act1:  $clk := clk + 1$ 
    end
END

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