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Matéria: Arquitetura de Computadores II - Exercício prático 07

RESPOSTAS

Lista 07 - IEEE 754
Respostas

1a) $5B(IEEE754 \text{ 4E3M}) = ? (10)$

4 expoente
Normalizado
3 mantissa

01011011
 01011011
 1.011011
Bias = 2 - 1 = 7
Exp real = Exp mag - Bias = 4
Exp real = 11 - 7
32 16 8 4 2 1 = 22(10)
1 0 1 1 0

$S = 0(+)$
 $M = 011$
 $E = 1011(11)$
 $10110(2)$

b) $9,25(10) = ?(IEEE754 \text{ 4E3M})$

4 expoente
3 mantissa

$1001,01 = 1,00101 \cdot 2^3$
Exp real = 9
 $M = 001$
Mantissa = $1,001 \cdot 2^3$
Exp real = Exp mag - Bias = 10
 $3 = \text{Exp mag} - 7$

$01010001(IEEE754 \text{ 4E3M})$

2a) Precisão simples: 8E 23M
 Precisão dupla: 11E 52M

803ACABA (IEEE 754 8E 23M)

1000 0000	0011 1010 1100 1010 1011 1010
S	E M

$B_{bias} = 127$ $S = 1 (-)$
N normalizada

$M = 0,01110101100101010111010$
 \times
 -126
 2

$Exp_{real} = 1 - 127 = -126$

$*11, 10101100101010111010 \cdot 2^{-129}$

$-5.399183e-39$

b) 803 ACABA (IEEE 754 - 11 E 52M)

1	0000 0000 011	10101100 1010 1011 1010
		+ 32 zeros

S	E	M
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$$S = 1(-)$$

$$Bias = 2^{10} - 1 = 1023$$

$$Exp_{real} = Exp_{mg} - bias$$

$$Exp_{real} = 3 - 1023 = -1020$$

$$M = 1, 1010 1100 1010 1011 1010 \cdot 2^{-1020}$$

1 / 1

3a) $14.125_{(10)} = ?_{(IEEE 754 - 8E 23M)}$

~~102222200101101~~ $S = 0 (+)$

Mantissa: ^{leading bit} 1, 1011100101101 • 2

Bias = 127

Exp_{real} = Exp_{mag} - bias Exp_{mag} = 140
 $13 = \text{Exp mag} - 127$

0 | 10001100 | 101110010110100000000000
 S E M

b) $-58.375_{(10)} = ?_{(IEEE 754 - 8E 23M)}$

~~111001011011011 • 2~~ = Mantissa
 $S = 1 (-)$

Bias = 127

Exp_{mag} = 15 + 127 = 142

1 | 10001110 | 110010110110111000000000
 S E Mantissa

40) 13E → decimal (Normal) 8E 23M

0 | 1000 0001 | 011000000000000000000000
S | E | M

Montissa = 1,011 ^{no leading}
× 2²

Bias = 127

Exp_{real} = Exp_{maxima} - Bias

Exp_{real} = 129 - 127 = 2

1,011 · 2² = 101,1 = (5,5₍₁₀₎)

b)

1 | 1000 0001 | 0001 + 19 zeros
S | E | M

S = 1 (-)

Normal

Montissa: 1,0001 · 2

Bias = 127

100,01 = -4,25₍₁₀₎

Exp_{real} = 129 - 127

Exp_{real} = 2

5a) 7F7FF800 (IEEE 754 8E 23M)

0111 1111 0111 1111 1111 1000 0000 0000

0 1111 1110 | 111111111111110000 0000 0000

5	E	M
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$$5 \div 0 (+)$$
$$B_{\text{res}} = 127$$

Mantissa = $1,11111111111111 \cdot 2^{127}$

$$\text{Exp}_{\text{real}} = \text{Exp}_{\text{magenta}} \oplus \text{Basis} \oplus \text{Exp}_{\text{real}} = 127$$
$$Exp_{real} = 254 - 127$$

b) D57F0000C1EE754 8E 23m)

1101 0101 0111 1111 0000 0000 0000 0000

S E M S = 1 (-)

$$B_{bias} = 127$$

$$M = 1,1111111 \cdot 2^{43}$$

$$Exp_{real} = 170 - 127 = 43$$

c) 5F7FF800

0101 1111 0111 1111 1111 1000 0000 0000

S E M

$$B_{bias} = 127$$

$$S = 0 (+)$$

$$M = 1,111111111111 \cdot 2^{63}$$

$$Exp_{real} = 190 - 127$$

$$Exp_{real} = 63$$

ORDEM CRESCENTE: B < C < A

128 64 32 16 8 4 2 1
 1 1 1 0 0 0 0 0

G) MULT : $112 \cdot 0,224 = 25,088$

$1^2) 112 : 1110000$

S = 0 (+)

M = 110

M = $1,110 \cdot 2^6$

4E, 3M

Bias = $2 - 1 = 7$

Exp_{real} = Exp_{mag} - Bias

G = Exp_{mag} - 7

Exp_{mag} = 13

0 | 1101 | 110 =

S | E | M

S = 0 (+)

Normal

M = $1,110 \cdot 2^6 = 1110 \cdot 2^3 =$

$13 \cdot 8 =$

(10400)

Bias = 7

Exp_{real} = 13 - 7

$112 - 104 = 8$

Exp_{real} = 6

* Erro absoluto : 8

* Erro relativo : $\frac{8}{112} = 0,0714 = 7,14\%$

$2^{27} 0,224 : 0,001110 =$

$1,110 \cdot 2^{-3}$

$Bias = 7$

$Exp_{real} = Exp_{mag} - Bias$
 $-3 = Exp_{mag} - 7$
 $Exp_{mag} = 4$

Exp +
 → aumento
 ← aumento
 $S = 0 (+)$
 $M = 110$
 $E = 0100$

0	0100	110
S	E	M

Exp -
 → aumento
 ← aumento
 $S = (+)$
 Normalizado
 $Bias = 7$

$1,110 \cdot 2^{-3} = 1,110 \cdot 2^{-6}$

$Exp_{real} = 4 - 7$
 $Exp_{real} = -3$

$14 \cdot 1 = 0,21875 (10)$
 64

*Erro absoluto: $0,224 - 0,21875 = 0,00525$

*Erro relativo: $\frac{0,00525}{0,224} = 2,34\%$

1 / 1

$$3^{\circ}) \text{ ORIGINAL} = 112 \cdot 0,224 = 25,088$$

$$\text{ALTERADO} = 104 \cdot 0,21875 = 22,75$$

$$22,75_{(10)} = 10110,11 \quad 4E,3M$$

$$1,011011 \cdot 2^4$$

$$S = 0(+)$$

$$M = 011$$

$$E = 1011$$

$$\text{Bias} = 7$$

$$\text{Exp}_{\text{real}} = \text{Exp}_{\text{mag}} - \text{Bias}$$

$$4 = \text{Exp}_{\text{mag}} - 7$$

$$\text{Exp}_{\text{mag}} = 11$$

$$\begin{array}{c|c|c} 0 & 1011 & 011 \\ \hline S & E & M \end{array}$$

$$S = 0(+)$$

$$\text{Normalizada}$$

$$\text{Bias} = 7$$

$$1,011 \cdot 2^4 = 1011 \cdot 2^1 = 11 \cdot 2 = 22_{(10)}$$

$$\text{Exp}_{\text{real}} = 11 - 7 = 4$$

$$\text{*Erro absoluto: } 22,75 - 22 = 0,75$$

$$\text{*Erro relativo: } \frac{0,75}{22,75} = 3,29\%$$

$$\text{ERRO ABSOLUTO TOTAL} \rightarrow 25,088 - 22 = 3,088$$

$$\text{ERRO REL. TOTAL} \rightarrow \frac{3,088}{25,088} = 12,30\%$$

→ Somando: ORIGINAL = $112 + 0,224 = 112,224$
 ALTERADO = $104 + 0,21875$

$104,21875_{(10)} = 1,101002,00111_{(2)}$

$1,101 \cdot 2^6$

4E

3M

Bias = 7

S = 0(+)

M = 101

E = 1101

G = EXP mag - 7

EXP mag = 13

O | 1101 | 101

S = 0(+)

S | E | M

Normalizada

Bias = 7

$13 - 7 = 6$

$1,101 \cdot 2^6$

$1,101 \cdot 2^6 = 1101 \cdot 2^3 = 13 \cdot 8 = 104_{(10)}$

* Erro absoluto: $104,21875 - 104 = 0,21875$

* Erro relativo: $\frac{0,21875}{104,21875} = 2,09\%$

ERRO ABS. TOTAL → 8,224

ERRO REL. TOTAL → $\frac{8,224}{112,224} = 7,32\%$

1 1

3E 4M

$$7) \text{MULT: } 112 \cdot 0,224 = 25,088$$

$$1^{\circ}) 112: 1110000$$

$$1,1100 \cdot 2^3$$

$$S = 0(+)$$

$$M = 1100$$

$$E = 100$$

$$Bias = 2 \quad -1 = 4 - 1 = 3$$

3 bits de expoente, ou seja, valor negativo $\checkmark 111(2)$

$$Bias = 3$$

$$G = E \times P_{\text{orig}} - 3$$

$$E \times P_{\text{orig}} = 9 \quad \checkmark 1001(2)$$

$$0 \mid 100 \mid 1100$$

$$S = 0(+)$$

Normalizada

$$Bias = 3$$

$$S \mid E \mid M$$

$$1,1100 \cdot 2^1 = 11,1 \approx 3,5(10)$$

$$Bias = 3$$

$$E \times P_{\text{real}} = 4 - 3 \approx 1$$

$$\times \text{Erro absoluto: } 112 - 3,5 = 108,5(10)$$

$$\times \text{Erro relativo: } \frac{108,5}{112} = 96,8\%$$

$$2^2) 0,224 : 0,001110 = 1,1100 \cdot 2^{-3}$$

$$\text{Bias} = 3$$

$$S = 0(+)$$

$$M = 1100$$

$$E = 000$$

$$-3 = \text{Exp}_{\text{max}} - 3$$

$$\text{Exp}_{\text{max}} = 0$$

$$\begin{array}{c|c|c} 0 & 000 & 1100 \\ \hline S & E & M \end{array}$$

$$\sim S = 0(+)$$

Normalizado

$$\text{Bias} = 3$$

$$E = 000$$

$$M = 000$$

$$\text{Exp}_{\text{real}} = 1 - \text{Bias} = -2$$

no leading bit -2

$$0,1100 \cdot 2 \rightarrow 1100 \cdot 2^{-6} =$$

$$\frac{12 \cdot 1}{64} = 0,1875_{(10)}$$

$$\text{*Error absolute: } 0,224 - 0,1875 = 0,0365$$

$$\text{*Error relative: } \frac{0,0365}{0,224} = 16,29\%$$

1/1

3F 4M

32) ORIGINAL: 25,088

ALTERADO: $3,5 \cdot 0,1875 = 0,65625$

0,65625: 0,10101

-1

S = 0(+)

1,0101 · 2

M = 0101

E = 010

B₁₀₂ = 3

-1 = E & P_{max} - 3

E & P_{max} = 2 ≈ 010101

0 | 010 | 0101

S | E | M

S = 0(+)

-1

Normalizado

1,0101 · 2

B₁₀₂ = 3

E_{real} = 2 - 3 = -1 → 10101 · 1 = 21

32 32

0,65625

* Erro absoluto: 0

* Erro relativo: 0

ERRO ABS. TOTAL → $25,088 - 0,65625 =$

24,43175

ERRO REL. TOTAL → $24,43175 = 97,38\%$

25,088

Somando: ORIGINAL = 112,224 3E
ALTERADO = 3,6875 4M

$$3,6875 = 11,1011_{(2)}$$

$$1,11011 \cdot 2^{-1}$$

$$S = 0(+)$$

$$M = 1101$$

$$E = 010$$

$$Bias = 3$$

$$-1 = Exp_{magnitud} - 3$$

$$Exp_{paralelo} = 2$$

0	010	1101
S	E	M

$$S = 0(+)$$

$$1,1101 \cdot 2^{-1} =$$

Normalizado

$$Bias = 3$$

$$11101 \cdot 2^{-5} = 29 \cdot \frac{1}{32} =$$

$$Exp_{real} = 2 - 3$$

$$0,90625_{(10)}$$

$$* Erro absoluto: 3,6875 - 0,90625 = 2,78125$$

$$* Erro relativo = 75,42\%$$

$$ERRO ABS. TOTAL \rightarrow 112,224 - 0,90625 =$$

$$111,31775$$

$$ERRO REL. TOTAL \rightarrow \frac{111,31775}{112,224}$$

$$99,19\%$$