Programming Languages (Project 1)

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Abstract

The goal of this project is simulate the game of kalaha using haskell.

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1 The Kalaha game with parameters (n, m)

```
module Kalaha where

type PitCount = Int
type StoneCount = Int
data Kalaha = Kalaha PitCount StoneCount deriving (Show, Read, Eq)

type KPos = Int
type KState = [Int]
type Player = Bool
```

1.1 The function startStateImpl

Very straightforward using replicate and concatenation

```
startStateImpl :: Kalaha -> KState
startStateImpl (Kalaha n m) = (replicate n m)++[0]++(replicate n m)++[0]
```

1.2 The function movesImpl

This function first calculates the lists of both players and depends on p calls positions who filters the elements that are equals to zero

1.3 The function valueImpl

This function first calculates the difference between two pits

```
valueImpl :: Kalaha -> KState -> Double
valueImpl g s = fromIntegral $ (s !! (extract g)) - (s !! ((*2) (extract g) + 1))
where extract (Kalaha n _) = n
```

1.4 The function moveImpl

Instead of iterating over the list as we would naively do we can compute how many times we would iterate over the entire list. Easy to note that this is equal to the number of stones divided by 2n + 1. The remainder of this division would be the number of stones left after all the "entire" rounds. Now this is easily done in O(n) by adding the number of entire rounds to all the elements (except the other's player kahala) and then iterating only once to add the last stones.

Instead of having two cases, one for each player, we used the fact that the board is kind of symmetric. We only implemented the function for player False and then reduced the case of player True to player False.

```
moveImpl :: Kalaha -> Player -> KState -> KPos -> (Player,KState)
  moveImpl g True s pos =
    let (npos, nst) = moveImpl g False (change_player s) (pos-(extract g+1))
    in (not npos, change_player nst)
    where change_player s = drop (extract g +1) s ++ take (extract g+1) s
          extract (Kalaha n _) = n
  moveImpl g False s pos =
        var = s!!pos
        divi = div var (2*n+1)
        modi = mod var (2*n+1)
        s1 = change pos 0 s
        s2 = map (+divi) (init s1) ++ [last s1]
17
        final = (pos+1) \ \ mod \ \ (2*n+1)
19
        initial = (pos+modi) `mod` (2*n+1)
20
        nKstate = if modi == 0 then s2
                     else map (func final initial) (zip s2 [0..])
        nKstate' = if nKstate!!initial == 1 && initial<n then takeInicial initial nKstate
24
                        else nKstate
25
      in (initial /= n, checkfinal nKstate')
      where
27
        n = extract g
        extract (Kalaha n _) = n
29
        change _{-} [] = []
        change pos val (a:as) = let na = if (pos == 0) then val
                                           else a
                                  in na:(change (pos-1) val as)
33
        func final initial (x, pos) = let r = final>initial
                                  in if (not r && final <= pos && pos <= initial)</pre>
                                        | | (r \&\& pos /=(2*n+1))|
36
                                             && (pos \leftarrow initial \mid \mid final \leftarrow pos)) then x+1
                                     else x
38
        takeInicial pos s = let var2 = s!!(2*n-pos) + s!!(n) + 1
39
                             in change n (var2) . change pos 0
40
                                    . change (2*n-pos) 0 $ s
        checkfinal s = if movesImpl g True s == [] || movesImpl g False s == [] then
42
                                let p1 = s!!n + (sum \$ take n s)
43
                                    p2 = s!!(2*n+1) + (sum \$ (take n . drop (n+1)) s)
44
                                in replicate n 0 ++ [p1] ++ replicate n 0 ++ [p2]
                        else s
46
```

1.5 The function showGameImpl

As stated, we compute maxLen = length(show(n * m * 2)), then for a number x we know we have to put maxLen - length(showx) spaces when printing. This can be done using replicate.

```
showGameImpl :: Kalaha -> KState -> String
showGameImpl g s =

prints ++ concatMap putsp b

++ "\n" ++ (putsp (s!!(2*n+1)) ++ concatMap (replicate n) prints ++ putsp (s!!n))

++ "\n" ++ prints ++ concatMap putsp a
where maxLen = length (show (n*m*2))

putsp x = replicate (maxLen - length (show x)) ' ' ++ show x

prints = replicate maxLen ' '

a = take n $ s

b = reverse . take n . drop (n+1) $ s

n = extractN g

extractN (Kalaha n _) = n

m = extractM g

extractM (Kalaha _ m) = m
```

2 Trees

```
data Tree m v = Node v [(m,Tree m v)] deriving (Eq, Show)
```

2.1 The function takeTree

We recursively go down the tree and when we get to the height we want we cut all the children.

```
takeTree :: Int -> Tree m v -> Tree m v
takeTree 0 (Node v ls) = Node v []
takeTree h (Node v ls) = Node v (map (\((x,y) -> (x, takeTree (h-1) y)) ls)
```

3 The Minimax algorithm

```
data Game s m = Game {
      startState
                   :: s -> String,
      showGame
      move
                    :: Player -> s -> m -> (Player,s),
                    :: Player -> s -> [m],
      moves
                    :: Player -> s -> Double}
      value
8 kalahaGame :: Kalaha -> Game KState KPos
9 kalahaGame k = Game {
      startState = startStateImpl k,
      showGame = showGameImpl k,
                = moveImpl k,
      move
                = movesImpl k,
      moves
      value
                = const (valueImpl k)}
startTree :: Game s m -> Player -> Tree m (Player, Double)
17 startTree g p = tree g (p, startState g)
```

3.1 The function tree

Implemented as said on the statement. We create a node with the given player and the value of the state. And then recursively called the tree constructor function on its children.

3.2 The function minimax

We note that when the statement means the value it refers to the minimax value, not to the value function on the game data.

3.3 The function minimaxAlphaBeta

We simulate a for loop by using a foldl function. Everything else is just a translation of the provided code (and wikipedia's article code).

```
_{1} inf = 10000000000.0
type AlphaBeta = (Double, Double)
4 minimaxAlphaBeta :: (Ord m) => AlphaBeta -> Tree m (Player, Double) -> (Maybe m, Double
5 minimaxAlphaBeta ab (Node (b, val) []) = (Nothing, val)
  minimaxAlphaBeta (al, be) (Node (True, val) ls) =
      let (v, mov, al', be') = foldl fmax (-inf, fst.head $ ls, al, be) $ (map swap' ls)
      in (Just mov, v)
          where fmax (v, mov, al', be') (t, m2) =
                   if be' <= al' then (v, mov, al', be')</pre>
                   else let
                               nv = v `max` (snd $ minimaxAlphaBeta (al', be') t)
                               nmov = if nv > v then m2
12
                                       else mov
                               nal' = al' `max` nv
14
                        in (nv, nmov, nal', be')
                 swap'(a,b) = (b,a)
16
  minimaxAlphaBeta (al, be) (Node (False, val) ls) =
18
      let (v, mov, al', be') = foldl fmin (inf, fst.head $ ls, al, be) $ (map swap' ls)
      in (Just mov, v)
20
21
          where fmin (v, mov, al', be') (t, m2) =
                   if be' <= al' then (v, mov, al', be')</pre>
                               nv = v `min` (snd $ minimaxAlphaBeta (al', be') t)
                   else let
23
                               nmov = if nv < v then m2
                                       else mov
25
                               nbe' = be' `min` nv
26
                        in (nv, nmov, al', nbe')
27
                 swap'(a,b) = (b,a)
28
```

4 Testing and sample executions

```
runhaskell MainTestRun.hs "Kalaha 6 6" "(Minimax, 5)" "(AlphaBeta, 4)"
moveImpl g False [6,6,6,6,6,6,6,6,6,6,6,6,6,6] 0 == (\text{False},[0,7,7,7,7,1,6,6,6,6,6,6])
moveImpl g False [0,7,7,7,7,1,6,6,6,6,6,6,0] 2 == (True,[0,7,0,8,8,8,2,7,7,7,6,6,6,0])
moveImpl g True [0,7,0,8,8,8,2,7,7,7,6,6,6,0] 7 == (False,[1,7,0,8,8,8,2,0,8,8,7,7,7,1])
moveImpl g False [1,7,0,8,8,8,2,0,8,8,7,7,7,1] 0 == (\text{True},[0,8,0,8,8,8,2,0,8,8,7,7,7,1])
moveImpl g True [0.8,0.8,8.8,2.0.8,8.7,7.7,1] 8 == (False,[1.9,1.8,8.8,2.0.0,9.8,8.8,2])
moveImpl g False [1,9,1,8,8,8,2,0,0,9,8,8,8,2] 0 == (\text{True},[0,10,1,8,8,8,2,0,0,9,8,8,8,2])
moveImpl g True [0,10,1,8,8,8,2,0,0,9,8,8,8,2] 9 == (False,[1,11,2,9,9,8,2,0,0,0,9,9,9,3])
moveImpl g False [1,11,2,9,9,8,2,0,0,0,9,9,9,3] 0 == (\text{True},[0,12,2,9,9,8,2,0,0,0,9,9,9,3])
moveImpl g True [0,12,2,9,9,8,2,0,0,0,9,9,9,3] 11 == (False, [1,13,3,10,10,0,2,0,0,0,9,0,10,14])
moveImpl g False [1,13,3,10,10,0,2,0,0,0,9,0,10,14] 0 == (\text{True},[0,14,3,10,10,0,2,0,0,0,9,0,10,14])
moveImpl g True [0.14,3.10,10.0,2.0,0.0,9.0,10.14] 10 = (False,[1.15,4.11,11.1,2.0,0.0,0.1,11.15])
moveImpl g False [1,15,4,11,11,1,2,0,0,0,0,1,11,15] 0 == (\text{True},[0,16,4,11,11,1,2,0,0,0,0,1,11,15])
moveImpl g True [0,16,4,11,11,1,2,0,0,0,0,1,11,15] 12 == (False,[1,17,0,12,12,2,2,1,1,1,0,1,0,22])
moveImpl g False [1,17,0,12,12,2,2,1,1,1,0,1,0,22] 0 == (\text{True},[0,18,0,12,12,2,2,1,1,1,0,1,0,22])
moveImpl g True [0,18,0,12,12,2,2,1,1,1,0,1,0,22] 7 == (False,[0,18,0,12,12,2,2,0,2,1,0,1,0,22])
moveImpl g False [0.18, 0.12, 12, 2, 2, 0, 2, 1, 0, 1, 0, 22] 4 == (True, [1,19,1,13,0,3,3,1,3,2,1,2,1,22])
moveImpl g True [1,19,1,13,0,3,3,1,3,2,1,2,1,22] 7 == (False, [1,19,1,13,0,3,3,0,4,2,1,2,1,22])
moveImpl g False [1,19,1,13,0,3,3,0,4,2,1,2,1,22] 0 == (\text{True},[0,20,1,13,0,3,3,0,4,2,1,2,1,22])
moveImpl g True [0,20,1,13,0,3,3,0,4,2,1,2,1,22] 8 == (False, [0,20,1,13,0,3,3,0,0,3,2,3,2,22])
moveImpl g False [0,20,1,13,0,3,3,0,0,3,2,3,2,22] 2 == (\text{True},[0,20,0,14,0,3,3,0,0,3,2,3,2,22])
moveImpl g True [0,20,0,14,0,3,3,0,0,3,2,3,2,22] 9 == (False, [0,20,0,14,0,3,3,0,0,0,3,4,3,22])
moveImpl g False [0.20,0.14,0.3,3.0,0.0,3.4,3.22] 3 == (\text{True},[1.21,1.1,2.4,4.1,1.1,4.5,4.22])
moveImpl g True [1,21,1,1,2,4,4,1,1,1,4,5,4,22] 7 == (False,[1,21,1,1,2,4,4,0,2,1,4,5,4,22])
moveImpl g False [1,21,1,1,2,4,4,0,2,1,4,5,4,22] 0 == (\text{True},[0,22,1,1,2,4,4,0,2,1,4,5,4,22])
moveImpl g True [0,22,1,1,2,4,4,0,2,1,4,5,4,22] 8 == (False,[0,22,1,1,2,4,4,0,0,2,5,5,4,22])
moveImpl g False [0.22,1,1,2,4,4,0,0,2,5,5,4,22] 2 == (\text{True},[0.22,0,2,2,4,4,0,0,2,5,5,4,22])
moveImpl g True [0,22,0,2,2,4,4,0,0,2,5,5,4,22] 9 == (False, [0,22,0,2,2,4,4,0,0,6,6,4,22])
moveImpl g False [0,22,0,2,2,4,4,0,0,0,6,6,4,22] 3 == (\text{True},[0,22,0,0,3,5,4,0,0,0,6,6,4,22])
moveImpl g True [0,22,0,0,3,5,4,0,0,0,6,6,4,22] 10 == (False,[1,23,1,0,3,5,4,0,0,0,0,7,5,23])
moveImpl g False [1,23,1,0,3,5,4,0,0,0,7,5,23] 4 == (\text{True},[1,23,1,0,0,6,5,1,0,0,0,7,5,23])
moveImpl g True [1,23,1,0,0,6,5,1,0,0,0,7,5,23] 7 == (False,[1,23,1,0,0,6,5,0,0,0,0,7,5,24])
moveImpl g False [1,23,1,0,0,6,5,0,0,0,0,7,5,24] 0 == (\text{True},[0,24,1,0,0,6,5,0,0,0,0,7,5,24])
moveImpl g True [0.24, 1.0, 0.6, 5.0, 0.0, 0.7, 5.24] 11 = (False, [1.25, 2.1, 1.6, 5.0, 0.0, 0.0, 6.25])
moveImpl g False [1,25,2,1,1,6,5,0,0,0,0,0,6,25] 5 == (\text{True},[1,25,2,1,1,0,6,1,1,1,1,1,6,25])
```

```
moveImpl g True [1,25,2,1,1,0,6,1,1,1,1,1,6,25] 7 == (False,[1,25,2,1,1,0,6,0,2,1,1,1,6,25])
moveImpl g False [1,25,2,1,1,0,6,0,2,1,1,1,6,25] 0 == (\text{True},[0,26,2,1,1,0,6,0,2,1,1,1,6,25])
moveImpl g True [0.26, 2.1, 1.0, 6.0, 2.1, 1.1, 6.25] 8 == (False, [0.26, 2.1, 1.0, 6.0, 0.2, 2.1, 6.25])
moveImpl g False [0.26, 2.1, 1.0, 6.0, 0.2, 2.1, 6.25] 3 == (True, [0.26, 2.0, 2.0, 6.0, 0.2, 2.1, 6.25])
moveImpl g True [0.26, 2.0, 2.0, 6.0, 0.2, 2.1, 6.25] 10 == (False, [0.26, 2.0, 2.0, 6.0, 0.2, 0.2, 7.25])
moveImpl g False [0.26, 2.0, 2.0, 6.0, 0.2, 0.2, 7.25] 2 == (True, [0.26, 0.1, 3.0, 6.0, 0.2, 0.2, 7.25])
moveImpl g True [0.26,0.1,3.0,6.0,0.2,0.2,7.25] 9 == (False, [0.26,0.1,3.0,6.0,0.0,1.3,7.25])
moveImpl g False [0.26,0.1,3.0,6.0,0.0,1.3,7.25] 1 == (True,[2.2,2.3,5.2,8.2,2.2,3.5,9.25])
moveImpl g True [2,2,2,3,5,2,8,2,2,2,3,5,9,25] 7 == (False,[2,2,2,3,5,2,8,0,3,3,3,5,9,25])
moveImpl g False [2,2,2,3,5,2,8,0,3,3,3,5,9,25] 0 == (\text{True},[0,3,3,3,5,2,8,0,3,3,3,5,9,25])
moveImpl g True [0,3,3,3,5,2,8,0,3,3,3,5,9,25] 9 == (False,[0,3,3,3,5,2,8,0,3,0,4,6,10,25])
moveImpl g False [0,3,3,3,5,2,8,0,3,0,4,6,10,25] 2 == (\text{True},[0,3,0,4,6,3,8,0,3,0,4,6,10,25])
moveImpl g True [0,3,0,4,6,3,8,0,3,0,4,6,10,25] 8 == (False, [0,3,0,4,6,3,8,0,0,1,5,7,10,25])
moveImpl g False [0,3,0,4,6,3,8,0,0,1,5,7,10,25] 1 == (True,[0,0,1,5,7,3,8,0,0,1,5,7,10,25])
moveImpl g True [0,0,1,5,7,3,8,0,0,1,5,7,10,25] 9 == (False, [0,0,1,5,7,3,8,0,0,0,6,7,10,25])
moveImpl g False [0,0,1,5,7,3,8,0,0,0,6,7,10,25] 2 == (\text{True},[0,0,0,6,7,3,8,0,0,0,6,7,10,25])
moveImpl g True [0.0,0.6,7,3.8,0.0,0.6,7,10.25] 10 == (False,[1.1,1.6,7,3.8,0.0,0.0.8,11.26])
moveImpl g False [1,1,1,6,7,3,8,0,0,0,0,8,11,26] 0 == (\text{True},[0,2,1,6,7,3,8,0,0,0,0,8,11,26])
moveImpl g True [0,2,1,6,7,3,8,0,0,0,8,11,26] 12 == (False,[1,3,0,7,8,4,8,1,1,1,0,8,0,30])
moveImpl g False [1,3,0,7,8,4,8,1,1,1,0,8,0,30] 0 == (True,[0,4,0,7,8,4,8,1,1,1,0,8,0,30])
moveImpl g True [0.4,0.7,8.4,8.1,1.1,0.8,0.30] 8 == (False, [0.4,0.7,8.4,8.1,0.2,0.8,0.30])
moveImpl g False [0.4,0.7,8,4.8,1,0.2,0.8,0.30] 1 == (\text{True},[0.0,1,8.9,5.8,1,0.2,0.8,0.30])
moveImpl g True [0,0,1,8,9,5,8,1,0,2,0,8,0,30] 9 == (False,[0,0,1,8,9,5,8,1,0,0,1,9,0,30])
moveImpl g False [0,0,1,8,9,5,8,1,0,0,1,9,0,30] 2 == (True,[0,0,0,9,9,5,8,1,0,0,1,9,0,30])
moveImpl g True [0,0,0,9,9,5,8,1,0,0,1,9,0,30] 10 == (False, [0,0,0,9,9,5,8,1,0,0,0,10,0,30])
moveImpl g False [0,0,0,9,9,5,8,1,0,0,0,10,0,30] 5 == (\text{True},[0,0,0,9,9,0,9,2,1,1,1,10,0,30])
moveImpl g True [0,0,0,9,9,0,9,2,1,1,1,10,0,30] 7 == (False,[0,0,0,9,9,0,9,2,2,1,10,0,30])
moveImpl g False [0,0,0,9,9,0,9,0,2,2,1,10,0,30] 4 == (True,[0,0,0,9,0,1,12,1,3,3,2,11,0,30])
moveImpl g True [0,0,0,9,0,1,12,1,3,3,2,11,0,30] 7 == (False,[0,0,0,9,0,1,12,0,4,3,2,11,0,30])
moveImpl g False [0,0,0,9,0,1,12,0,4,3,2,11,0,30] 3 == (\text{True},[0,0,0,0,1,2,13,1,5,4,3,12,1,30])
moveImpl g True [0,0,0,0,1,2,13,1,5,4,3,12,1,30] 7 == (False,[0,0,0,0,1,2,13,0,6,4,3,12,1,30])
moveImpl g False [0.0,0.0,1,2,13,0,6,4,3,12,1,30] 4 == (True,[0.0,0,0,0,3,13,0,6,4,3,12,1,30])
moveImpl g True [0,0,0,0,0,3,13,0,6,4,3,12,1,30] 8 == (False, [1,0,0,0,0,3,13,0,0,5,4,13,2,31])
moveImpl\ g\ False\ [1,0,0,0,0,3,13,0,0,5,4,13,2,31]\ 5 == (True,[1,0,0,0,0,0,14,1,1,5,4,13,2,31])
moveImpl g True [1,0,0,0,0,0,14,1,1,5,4,13,2,31] 9 == (False,[2,0,0,0,0,0,14,1,1,0,5,14,3,32])
moveImpl g False [2,0,0,0,0,0,14,1,1,0,5,14,3,32] 0 == (\text{True},[0,1,0,0,0,0,20,1,1,0,0,14,3,32])
```

```
moveImpl g True [0,1,0,0,0,0,20,1,1,0,0,14,3,32] 12 == (False, [1,2,0,0,0,0,20,1,1,0,0,14,0,33])
moveImpl g False [1,2,0,0,0,0,20,1,1,0,0,14,0,33] 0 == (\text{True},[0,3,0,0,0,0,20,1,1,0,0,14,0,33])
moveImpl g True [0,3,0,0,0,0,20,1,1,0,0,14,0,33] 7 == (False, [0,3,0,0,0,0,20,0,2,0,0,14,0,33])
moveImpl g False [0,3,0,0,0,0,20,0,2,0,0,14,0,33] 1 == (True,[0,0,1,1,0,0,23,0,0,0,0,14,0,33])
moveImpl g True [0,0,1,1,0,0,23,0,0,0,0,14,0,33] 11 == (False,[1,1,2,2,1,1,23,1,1,1,1,1,2,34])
moveImpl g False [1,1,2,2,1,1,23,1,1,1,1,1,2,34] 0 == (\text{True},[0,2,2,2,1,1,23,1,1,1,1,1,2,34])
moveImpl g True [0,2,2,2,1,1,23,1,1,1,1,1,2,34] 7 == (False, [0,2,2,2,1,1,23,0,2,1,1,1,2,34])
moveImpl g False [0,2,2,2,1,1,23,0,2,1,1,1,2,34] 1 == (\text{True},[0,0,3,3,1,1,23,0,2,1,1,1,2,34])
moveImpl g True [0,0,3,3,1,1,23,0,2,1,1,1,2,34] 8 == (False,[0,0,3,3,1,1,23,0,0,2,2,1,2,34])
moveImpl g False [0,0,3,3,1,1,23,0,0,2,2,1,2,34] 4 == (\text{True},[0,0,3,3,0,2,23,0,0,2,2,1,2,34])
moveImpl g True [0,0,3,3,0,2,23,0,0,2,2,1,2,34] 10 = (False,[0,0,3,3,0,2,23,0,0,2,0,2,3,34])
moveImpl g False [0,0,3,3,0,2,23,0,0,2,0,2,3,34] 2 == (\text{True},[0,0,0,4,1,3,23,0,0,2,0,2,3,34])
moveImpl g True [0,0,0,4,1,3,23,0,0,2,0,2,3,34] 9 == (False, [0,0,0,4,1,3,23,0,0,0,1,3,3,34])
moveImpl g False [0,0,0,4,1,3,23,0,0,0,1,3,3,34] 4 == (\text{True},[0,0,0,4,0,4,23,0,0,0,1,3,3,34])
moveImpl g True [0,0,0,4,0,4,23,0,0,0,1,3,3,34] 10 == (False, [0,0,0,4,0,4,23,0,0,0,0,4,3,34])
moveImpl g False [0,0,0,4,0,4,23,0,0,0,0,4,3,34] 3 == (\text{True},[0,0,0,0,1,5,24,1,0,0,0,4,3,34])
moveImpl g True [0.0,0.0,1.5,24,1.0,0.0,4,3.34] 11 = (False,[1.1,0.0,1.5,24,1.0,0.0,0.4,3.5])
moveImpl g False [1,1,0,0,1,5,24,1,0,0,0,0,4,35] 4 == (\text{True},[1,1,0,0,0,6,24,1,0,0,0,0,4,35])
moveImpl g True [1,1,0,0,0,6,24,1,0,0,0,0,4,35] 7 == (False, [1,1,0,0,0,6,24,0,0,0,0,4,36])
moveImpl g False [1,1,0,0,0,6,24,0,0,0,0,4,36] 5 == (\text{True},[1,1,0,0,0,0,25,1,1,1,1,1,4,36])
moveImpl g True [1,1,0,0,0,0,25,1,1,1,1,1,4,36] 7 == (False,[1,1,0,0,0,0,25,0,2,1,1,1,4,36])
moveImpl g False [1,1,0,0,0,0,25,0,2,1,1,1,4,36] 1 == (True,[1,0,0,0,0,0,27,0,2,1,0,1,4,36])
moveImpl g True [1,0,0,0,0,0,27,0,2,1,0,1,4,36] 12 = (False, [2,1,1,0,0,0,27,0,2,1,0,1,0,37])
moveImpl g False [2,1,1,0,0,0,27,0,2,1,0,1,0,37] 0 == (\text{True},[0,2,2,0,0,0,27,0,2,1,0,1,0,37])
moveImpl g True [0,2,2,0,0,0,27,0,2,1,0,1,0,37] 8 == (False,[0,2,0,0,0,0,27,0,0,2,0,1,0,40])
moveImpl g False [0,2,0,0,0,0,27,0,0,2,0,1,0,40] 1 == (\text{True},[0,0,1,0,0,3,0,0,0,0,0,1,0,40])
moveImpl g True [0,0,1,0,0,3,0,0,0,0,0,1,0,40] 11 == (False, [0,0,0,0,0,3,1,0,0,0,0,0,41])
No available moves!
```