

# ICS 365 - Concepts of Programming Languages. Problem Set 1

Due: 06/06/2017

Points: 30

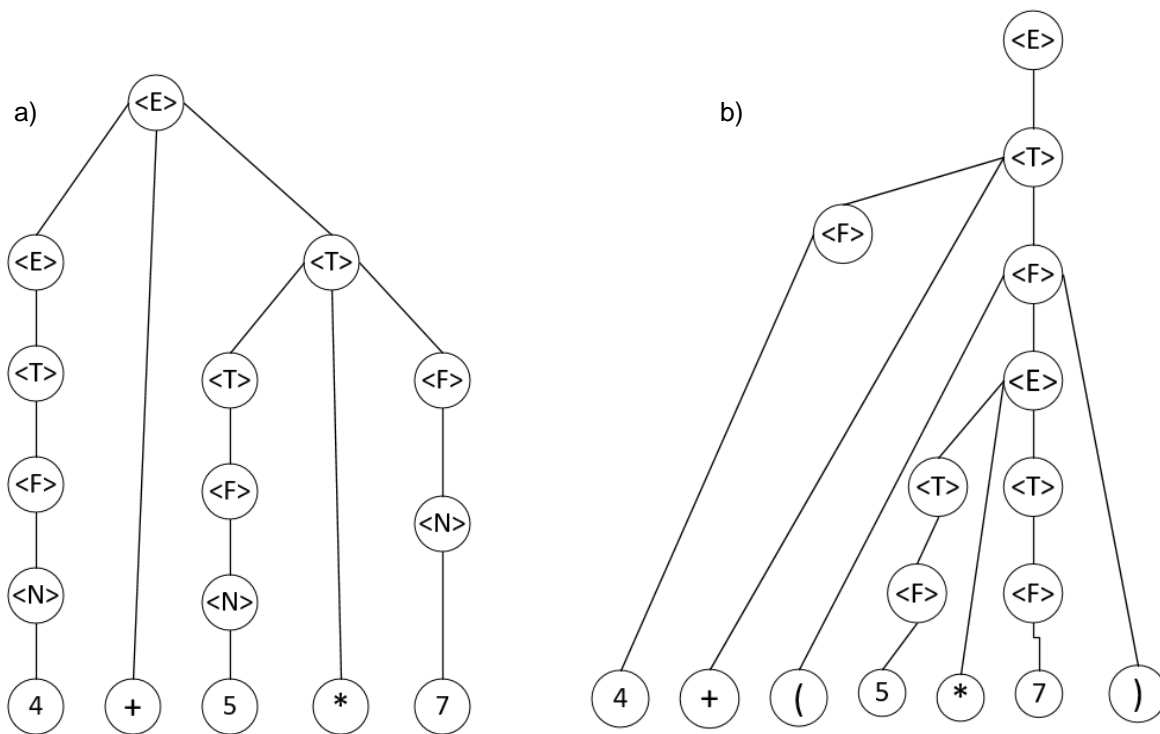
1. Derive and draw parse trees for the given expressions using the following grammar. 15 points

$\langle E \rangle \rightarrow \langle E \rangle + \langle T \rangle$   
 $\quad \quad \quad | \langle E \rangle - \langle T \rangle$   
 $\quad \quad \quad | \langle T \rangle$

$\langle T \rangle \rightarrow \langle T \rangle * \langle F \rangle$   
 $\quad \quad \quad | \langle T \rangle / \langle F \rangle$   
 $\quad \quad \quad | \langle F \rangle$

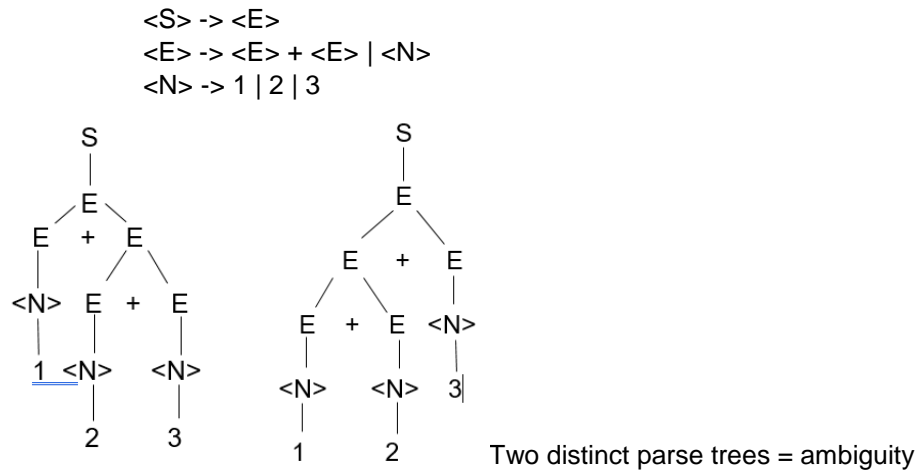
$\langle F \rangle \rightarrow \langle N \rangle | ( \langle E \rangle )$   
 $\langle N \rangle \rightarrow 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9$

a)  $4 + 5 * 7$                       b)  $4 + (5 * 7)$



2. Prove that the following grammar is ambiguous.

3 points



3. Compute the weakest precondition for each of the following assignments  
statements and postconditions

12points

1.  $a = 2 * (b - 1) - 1$        $\{a > 0\}$
2.  $b = (c + 10) / 3$        $\{b > 6\}$
3.  $a = a + 2 * b - 1$        $\{a > 1\}$
4.  $x = 2 * y + x - 1$        $\{x > 11\}$

$$\begin{aligned}
 1. \quad &a = 2 * (b - 1) - 1 \{a > 0\} \\
 &2 * (b - 1) - 1 > 0 \\
 &2 * b - 2 - 1 > 0 \\
 &2 * b > 3 \\
 &b > 3 / 2
 \end{aligned}$$

$$\begin{aligned}
 2. \quad &b = (c + 10) / 3 \{b > 6\} \\
 &(c + 10) / 3 > 6 \\
 &c + 10 > 18 \\
 &c > 8
 \end{aligned}$$

$$\begin{aligned}
 3. \quad &a = a + 2 * b - 1 \{a > 1\} \\
 &a + 2 * b - 1 > 1 \\
 &2 * b > 2 - a \\
 &b > 1 - a / 2
 \end{aligned}$$

$$\begin{aligned}
 4. \quad &x = 2 * y + x - 1 \{x > 11\} \\
 &2 * y + x - 1 > 11 \\
 &2 * y + x > 12
 \end{aligned}$$